



Hands-on Density Functional Perturbation Theory: calculation of phonons

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Outline

- 1. Introduction
- 2. Exercise 1: Phonons at Gamma in non-polar materials
- 3. Exercise 2: Phonon dispersion in non-polar materials
- 4. Exercise 3: Phonons at Gamma in polar materials
- 5. Exercise 4: Phonon dispersion in polar materials

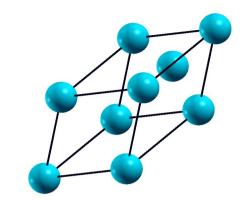
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Let us consider a unit cell with N_{at} atoms.

 $s = 1...N_{at}$ index of an atom in the unit cell $\alpha = x, y, z$ is the Cartesian index

R is the point in the Bravais-lattice, identifying the position of a given unit cell



 $N_{\mathbf{R}}$ is the number of unit cells in the crystal

 $\mathbf{u}_{s\alpha}(\mathbf{R})$ is the α -component of the displacement of \mathbf{s} -th atom $3 \times N_{at}$ variables

Interatomic Force Constants:

$$C_{s\alpha,s'\beta}(\mathsf{R},\mathsf{R}') = C_{s\alpha,s'\beta}(\mathsf{R}-\mathsf{R}') = \frac{\partial^2 E_{tot}}{\partial \mathsf{u}_{s\alpha}(\mathsf{R})\partial \mathsf{u}_{s'\beta}(\mathsf{R}')} \longrightarrow \mathsf{N}_{\mathsf{R}}^2$$

Fourier transformation:

$$\tilde{\mathsf{u}}_{slpha}(\mathsf{q}) = \sum_{\mathsf{R}} \mathsf{u}_{slpha}(\mathsf{R}) \, e^{-i\mathsf{q}\cdot\mathsf{R}}$$

Essence of the Bloch theorem:

$$\frac{\partial^2 E_{tot}}{\partial \tilde{\mathbf{u}}_{s\alpha}^*(\mathbf{q})\partial \tilde{\mathbf{u}}_{s'\beta}(\mathbf{q}')} = \delta_{\mathbf{q},\mathbf{q}'} \frac{\partial^2 E_{tot}}{\partial \tilde{\mathbf{u}}_{s\alpha}^*(\mathbf{q})\partial \tilde{\mathbf{u}}_{s'\beta}(\mathbf{q})}$$



Important concept: We can perform calculations of Interatomic Force Constants for each **q** independently !!!

Important concept: Instead of $N_{\mathbf{R}}^2$ Interatomic Force Constants we need only $N_{\mathbf{R}}$!!!

Sampling theorem

The number of \mathbf{q} points is equal to the number of \mathbf{R} points at which Interatomic Force Constants are computed.

Normal mode frequencies, ω , and eigenvectors, $\mathbf{U}_{s\alpha}$ are determined by the secular equation:

$$\sum_{s',\beta} \tilde{D}_{s\alpha,s'\beta}(\mathbf{q}) \, \tilde{\mathbf{u}}_{s'\beta}(\mathbf{q}) = \omega_{\mathbf{q}}^2 \, \tilde{\mathbf{u}}_{s\alpha}(\mathbf{q})$$

where

$$\tilde{D}_{s\alpha,s'\beta}(\mathbf{q}) = \frac{1}{\sqrt{M_s M_{s'}}} \sum_{\mathbf{R},\mathbf{R}'} \frac{\partial^2 E_{tot}}{\partial \mathbf{u}_{s\alpha}(\mathbf{R}) \partial \mathbf{u}_{s'\beta}(\mathbf{R}')} e^{i\mathbf{q}(\mathbf{R}'-\mathbf{R})}$$

is the *dynamical matrix*.

Diagonalization of the dynamical matrix gives phonon modes at q.

Interatomic Force

Constants (IFC)

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Go to the directory with the input files:

```
cd Hands-on_DFPT/exercise1
```

In this directory you will find:

- README File describing how to do the exercise
- Si.scf.in Input file for the SCF ground-state calculation
- Si.ph.in Input file for the phonon calculation at Γ
- Si.dynmat.in Input file to impose the acoustic sum rule
- Si.vbc.UPF Pseudopotential of silicon
- reference Directory with the reference results
- out Directory for temporary files

Step 1. Perform a Self-Consistent Field ground-state calculation for silicon at the equilibrium structure using the pw.x program.

Si.scf.in

Input file for the SCF calculation

```
&control
    calculation='scf'
    restart mode='from scratch',
    pseudo dir='./'
    outdir='./out'
    prefix='Si',
 &svstem
    ibrav = 2,
    celldm(1) = 10.20.
    nat = 2.
    ntyp = 1,
    ecutwfc = 16
&electrons
    diagonalization = 'davidson'
    mixing mode = 'plain',
    conv thr = 1.0d-8
    mixing beta = 0.7
ATOMIC SPECIES
 Si 28.0855 Si.vbc.UPF
ATOMIC POSITIONS
 Si 0.00 0.00 0.00
 Si 0.25 0.25 0.25
K POINTS
   10
 0.1250000
            0.1250000 0.1250000
                                   1.00
                                   3.00
 0.1250000
            0.1250000 0.3750000
            0.1250000 0.6250000
                                   3.00
 0.1250000
 0.1250000
            0.1250000 0.8750000
                                   3.00
 0.1250000
            0.3750000 0.3750000
                                   3.00
 0.1250000
            0.3750000 0.6250000
                                   6.00
 0.1250000
            0.3750000 0.8750000
                                   6.00
                                   3.00
 0.1250000
            0.6250000 0.6250000
 0.3750000
            0.3750000 0.3750000
                                   1.00
 0.3750000
            0.3750000 0.6250000
                                   3.00
```

Step 2. Perform a phonon calculation at Γ using the **ph.x** program.

Si.ph.in

Input file for the phonon calculation

```
Phonons at Gamma &inputph prefix = 'Si', tr2_ph = 1.0d-14, amass(1) = 28.0855, outdir = './out' fildyn = 'Si.dyn', /

0.0 0.0 0.0 0.0 The same prefix as in the SCF calculation Threshold for self-consistency Atomic mass Directory for temporary files File containing the dynamical matrix Coordinates of the q point in units of 2*pi/a in Cartesian framework
```

ph.x < Si.ph.in > Si.ph.out

Step 2. Perform a phonon calculation at Γ using the ph.x program.

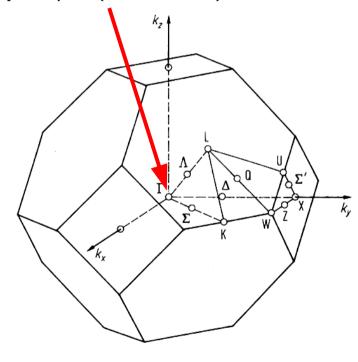
Si.ph.in

Input file for the phonon calculation

```
Phonons at Gamma
&inputph
   prefix = 'Si',
   tr2_ph = 1.0d-14,
   amass(1) = 28.0855,
   outdir = './out'
   fildyn = 'Si.dyn',
   /
   0.0   0.0   0.0
```

We consider only the Γ point:

 $\mathbf{q} = 2*pi/a (0.0, 0.0, 0.0)$



Brillouin zone

Dynamical matrix file Si.dyn:

```
(0.074375) [THz] =
 freq (
           1) =
                                            2.480880 [cm-1]
          0.000000 - 0.476699
                              0.000000 -0.116409
0.509124
                                                 0.000000
0.509124
          0.000000
                   -0.4<del>76699</del> 0.000000 -0.116409
                                                 0.000000
 freq (
           2) =
                      (0.074375)[THz] =
                                            2.480880 [cm-1]
0.047843
                             0.000000
          0.000000
                   -0.11<del>8723</del>
                                       0.695425
                                                 0.000000
0.047843
                   -0.1<del>18723</del> 0.000000
          0.000000
                                       0.695425
                                                 0.000000
                      (0.074375)[THz] =
 freq (
           3) =
                                            2.480880 [cm-1]
0.488369
          0.000000
                    0.508589 0.000000
                                       0.053228
                                                 0.000000
0.488369
          0.000000 0.508589
                              0.000000
                                       0.053228
                                                 0.000000
 freq (
                                          516.174002 [cm-1]
           4) =
                     15.474507
                               [THz] =
-0.366708
          0.000000
                   -0.101088
                              0.000000
                                       0.596076
                                                 0.000000
0.366708
          0.000000
                   0.101088
                              0.000000 -0.596076
                                                 0.000000
           5) =
 freq (
                     15.474507 [THz] =
                                          516.174002 [cm-1]
0.264492
          0.000000 -0.653724
                              0.000000
                                       0.051853
                                                 0.000000
-0.264492
          0.000000
                    0.653724
                              0.000000 - 0.051853
                                                 0.000000
 freq (
           6) =
                   15.474507 [THz] =
                                          516.174002 [cm-1]
0.543663
          0.000000
                    0.249852
                              0.000000
                                       0.376835
                                                 0.000000
-0.543663
                              0.000000 -0.376835
          0.000000 -0.249852
                                                 0.000000
```

Acoustic modes



Optical modes



Acoustic sum rule at Γ

Because of the numerical inaccuracies the interatomic force constants do not strictly satisfy the acoustic sum rule (ASR) => acoustic frequencies are not exactly zero.

However, the ASR can be imposed using the **dynmat.x** program.

The input file is **Si.dynmat.in**:

```
&input
fildyn = 'Si.dyn',
asr = 'simple'
/ A way to impose the acoustic sum rule
(simple, crystal, one-dim, zero-dim)
```

dynmat.x < Si.dynmat.in > Si.dynmat.out

The program **dynmat.x** produces the file **dynmat.out** which contains the new acoustic frequencies, which are *exactly* equal to zero.

diagonalizing the dynamical matrix ...

```
0.0000
                     0.0000
                                  0.0000
            1) =
                        0.000000)[THz] =
  freq (
                                                0.000000 [cm-1]
                         <del>-0.707</del>107
 0.000000
            0.000000
                                      0.000000
                                                   0.000000
                                                               0.000000
 0.000000
            0.000000
                          0.707107
                                      0.000000
                                                   0.000000
                                                               0.000000
                        0.000000)[THz] =
  freq (
            2) =
                                                0.000000 [cm-1]
-0.707107
            0.000000
                          0.000000
                                      0.000000
                                                   0.000000
                                                               0.000000
-0.707107
            0.000000
                          0.000000
                                      0.000000
                                                   0.000000
                                                               0.000000
  freq (
            3) =
                        0.000000)[THz] =
                                                0.000000 [cm-1]
 0.000000
            0.000000
                          0.000000
                                      0.000000
                                                   -0.707107
                                                               0.000000
 0.000000
            0.000000
                          0.000000
                                      0.000000
                                                   -0.707107
                                                               0.000000
  freq (
            4) =
                       15.474329 [THz]
                                              516.168042 [cm-1]
 0.000000
            0.000000
                          0.707107
                                      0.000000
                                                   0.000000
                                                               0.000000
 0.000000
            0.000000
                         -0.707107
                                      0.000000
                                                   0.000000
                                                               0.000000
                       15.474329 [THz] =
                                              516.168042 [cm-1]
  freq (
            5) =
 0.000000
                                                   -0.707107
            0.000000
                          0.000000
                                      0.000000
                                                               0.000000
 0.000000
            0.000000
                          0.000000
                                      0.000000
                                                   0.707107
                                                               0.000000
  freq (
            6) =
                       15.474329 [THz] =
                                              516.168042 [cm-1]
-0.707107
            0.000000
                          0.000000
                                      0.000000
                                                   0.000000
                                                               0.000000
 0.707107
            0.000000
                          0.000000
                                      0.000000
                                                    0.000000
                                                               0.000000
```

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Go to the directory with the input files:

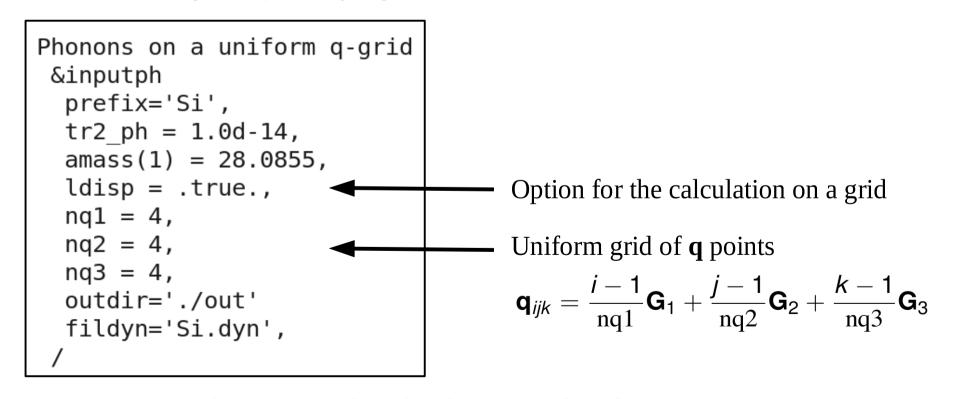
```
cd Hands-on_DFPT/exercise2
```

In this directory you will find:

- README File describing how to do the exercise
- Si.scf.in Input file for the SCF ground-state calculation
- Si.ph.in Input file for the phonon calculation on a uniform q-grid
- Si.q2r.in Input file for calculation of Interatomic Force Constants
- Si.matdyn.in Input file for Fourier Interpolation for various q points
- Si.plotband.in Input file for plotting a phonon dispersion
- Si.vbc.UPF Pseudopotential of silicon
- reference Directory with the reference results
- out Directory for temporary files

Step 1. Perform a SCF calculation for silicon at the equilibrium structure using the pw.x program.

Step 2. Perform a phonon calculation on a uniform grid of **q** points using the **ph.x** program.



ph.x < Si.ph.in > Si.ph.out

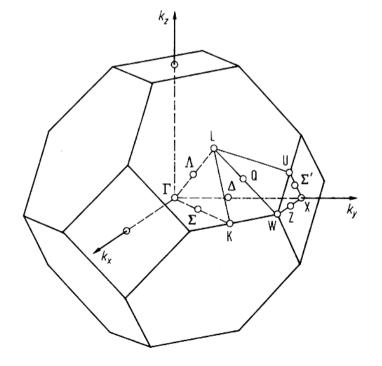
Step 1. Perform a SCF calculation for silicon at the equilibrium structure using the pw.x program.

```
pw.x < Si.scf.in > Si.scf.out
```

Step 2. Perform a phonon calculation.

```
Phonons on a uniform q-grid &inputph prefix='Si', tr2_ph = 1.0d-14, amass(1) = 28.0855, ldisp = .true., nq1 = 4, nq2 = 4, nq3 = 4, outdir='./out' fildyn='Si.dyn', /
```

We sample the Brillouin zone with a uniform grid 4x4x4 of **q** points.



4x4x4 = 64 q-points => Use of symmetry => 8 non-equivalent q points
 The file Si.dyn0 contains a list of the non-equivalent q points (8, in this case).

```
(q-grid)
                   (number of non-equivalent q-points)
                             0.00000000000000E+00
      0.00000000000000E+00
                                                     0.00000000000000E+00
     -0.25000000000000E+00
                             0.25000000000000E+00
                                                    -0.25000000000000E+00
q3
      0.50000000000000E+00
                             -0.50000000000000E+00
                                                     0.50000000000000E+00
      0.00000000000000E+00
                             0.50000000000000E+00
                                                     0.00000000000000E+00
q5 =
     0.75000000000000E+00
                             -0.25000000000000E+00
                                                     0.75000000000000E+00
q6 =
      0.50000000000000E+00
                             0.00000000000000E+00
                                                     0.50000000000000E+00
      0.00000000000000E+00
                             -0.10000000000000E+01
                                                     0.00000000000000E+00
     -0.50000000000000E+00
                                                     0.00000000000000E+00
                             -0.10000000000000E+01
```

The phonon program ph.x generates files for every non-equivalent q point
 Si.dyn1, Si.dyn2, ..., Si.dyn8, which contain information about dynamical matrices, phonon frequencies and displacements.

Step 3. Calculation of the Interatomic Force Constants (IFC) using the q2r.x program.

Fourier transforms of IFC's:

$$\tilde{C}_{s\alpha,s'\beta}(\mathbf{q}_{ijk}) = rac{\partial^2 E_{tot}}{\partial \tilde{\mathbf{u}}_{s\alpha}^*(\mathbf{q}_{ijk})\partial \tilde{\mathbf{u}}_{s'\beta}(\mathbf{q}_{ijk})}$$

 α, β are Cartesian components, and \mathbf{S}, \mathbf{S}' are atomic indices.

$$\tilde{C}_{s\alpha,s'\beta}(\mathbf{R}_{lmn}) = \frac{1}{N_{\mathbf{q}}} \sum_{i,j,k} \tilde{C}_{s\alpha,s'\beta}(\mathbf{q}_{ijk}) e^{i\mathbf{q}_{ijk} \cdot \mathbf{R}_{lmn}} \\ \tilde{C}_{s\alpha,s'\beta}(\mathbf{q}_{ijk}) \xrightarrow{} C_{s\alpha,s'\beta}(\mathbf{R}_{lmn})$$

Fourier transforms of IFC's on a grid of **q** points nq1 x nq2 x nq3 in reciprocal space

IFC's in a supercell nq1 x nq2 x nq3 in real space

Input file Si.q2r.in:

```
&input
fildyn='Si.dyn',
zasr='simple',
flfrc='Si444.fc'

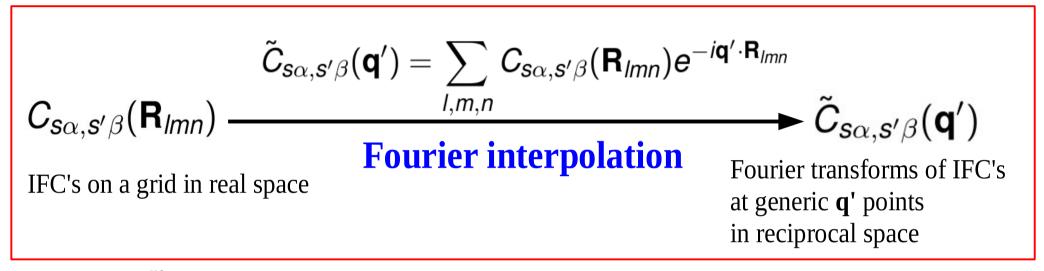
Output file of the interatomic force constants
```

The denser the grid of **q** points, the larger the vectors **R** for which the Interatomic Force Constants are calculated!

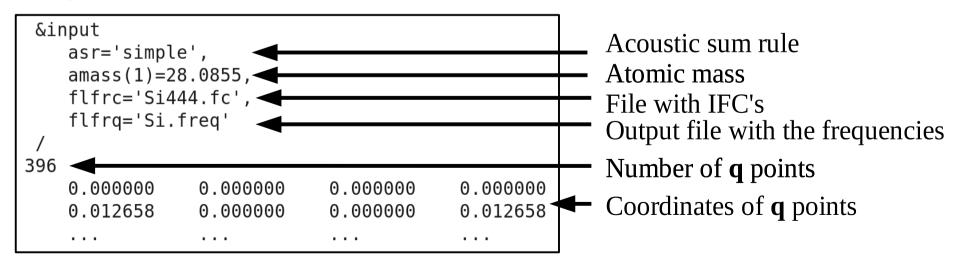
To perform the calculation:

```
q2r.x < Si.q2r.in > Si.q2r.out
```

Step 4. Calculate phonons at generic q' points using IFC by means of the code matdyn.x



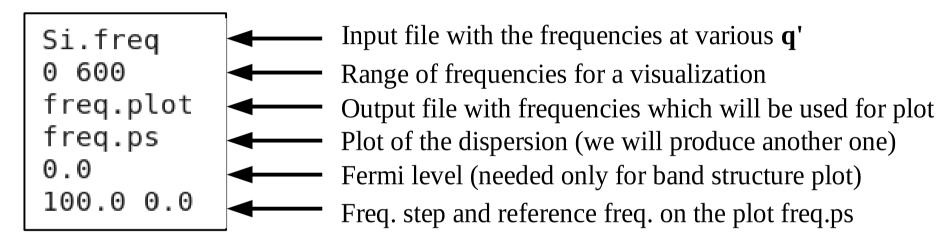
Input file Si.matdyn.in:



matdyn.x < Si.matdyn.in > Si.matdyn.out

Step 5. Plot the phonon dispersion using the plotband.x program and gnuplot.

Input file Si.plotband.in:

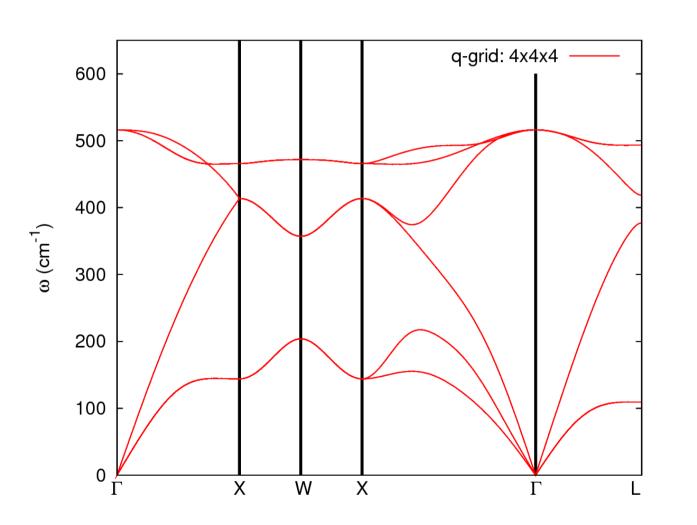


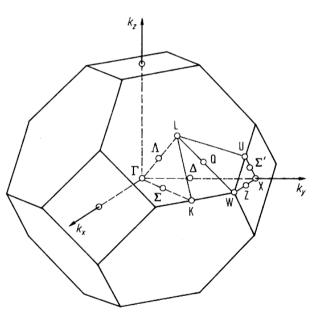
plotband.x < Si.plotband.in > Si.plotband.out

Use **gnuplot** and the file **plot_dispersion.gnu** in order to plot the phonon dispersion of silicon (**experimental_data.dat**).

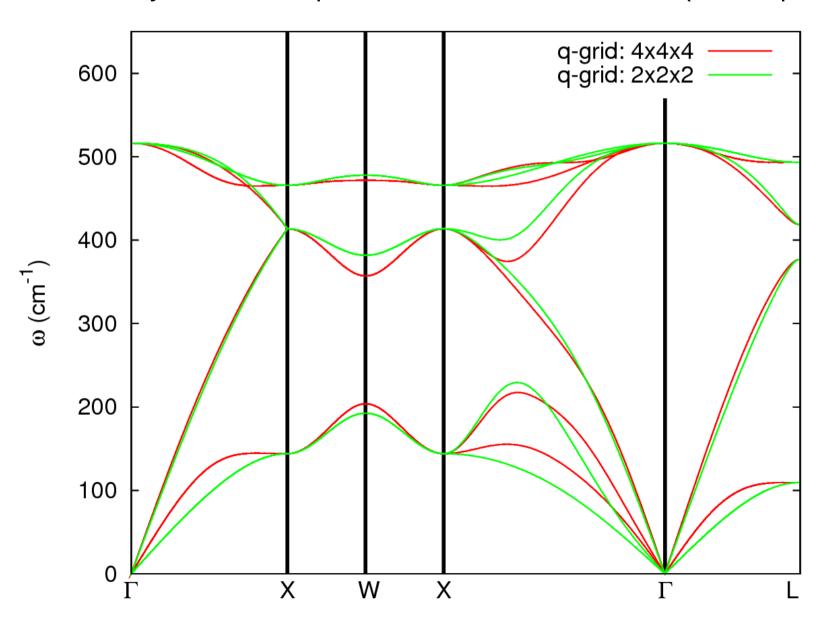
You will obtain a postscript file **phonon_dispersion.eps** which you can visualize.

Phonon dispersion of silicon along some high-symmetry directions in the Brillouin zone (file phonon_dispersion.eps):

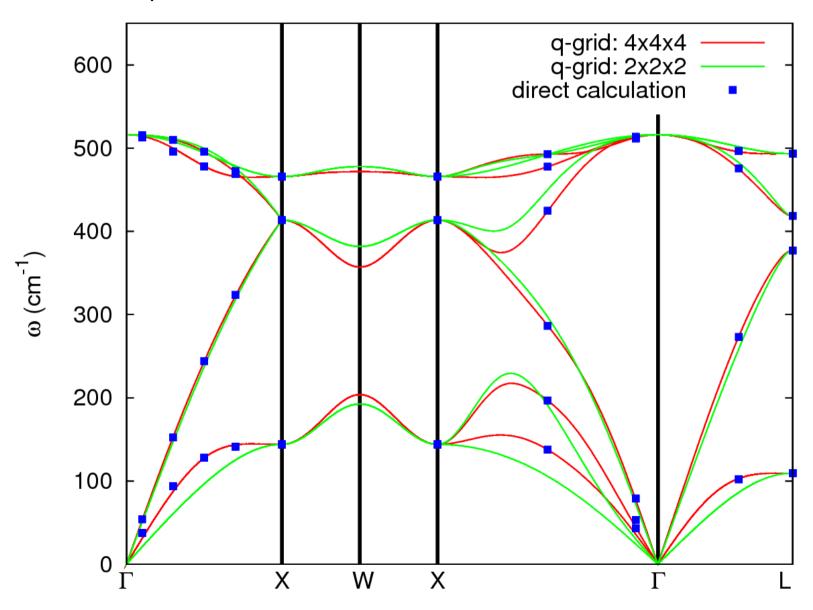




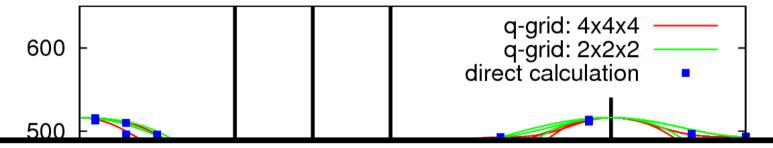
How to determine whether the quality of the Fourier interpolation is satisfactory? — Compare with the direct calculation (no interpolation)!



Comparison of the phonon dispersion computed using the Fourier interpolation with the direct calculation at several \mathbf{q} points. The \mathbf{q} -grid 4x4x4 is very satisfactory for the Fourier interpolation for silicon!

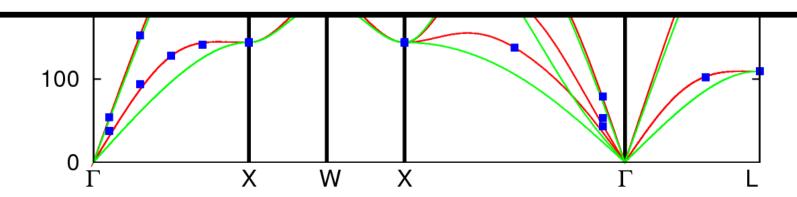


Comparison of the phonon dispersion computed using the Fourier interpolation with the direct calculation at several \mathbf{q} points. The \mathbf{q} -grid 4x4x4 is very satisfactory for the Fourier interpolation for silicon!

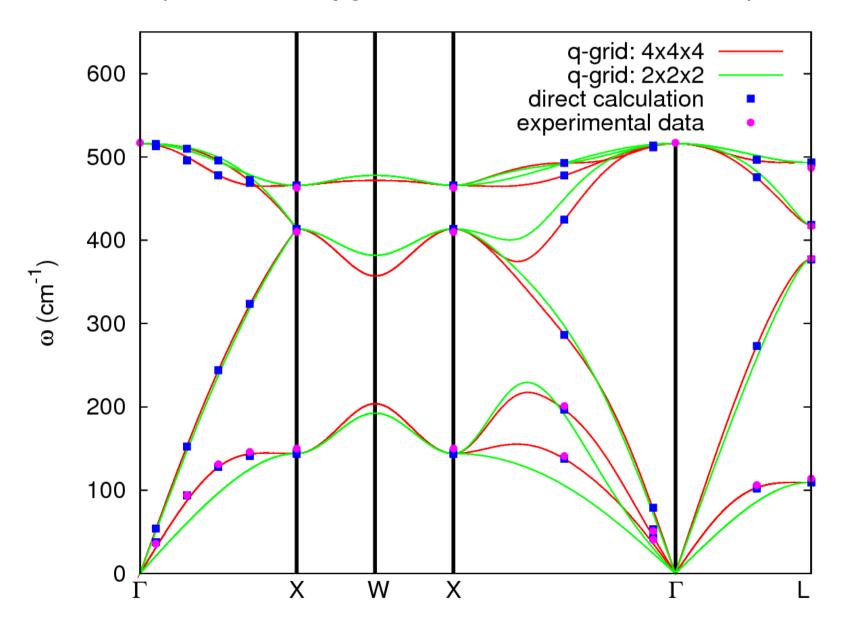


Perform a direct phonon calculation (no interpolation) at several **q'** points and make a comparison with the phonon frequencies obtained from the interpolation.

Use exercise1 as an example.



The agreement of *ab initio* calculation of the phonon dispersion using the Fourier interpolation on a **q**-grid 4x4x4 is excellent with the experimental data!



The Fourier interpolation works well if the Interatomic Force Constants (IFC's) are known on a sufficiently large supercell, i.e. on a large enough grid of **q** points in the phonon calculation.

There are cases when the IFC's are long range and the Fourier interpolation does not work properly:

- When there are Kohn anomalies in metals. In this case the dynamical matrices are not a smooth function of **q** and the IFC's are long range.
- In polar insulators where the atomic displacements generate long range electrostatic interactions and the dynamical matrix is not analitical for q→0. However, this case can be dealt with by calculating the Born effective charges and the dielectric tensor of the material.

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Polar materials in the $\mathbf{q} = \mathbf{0}$ limit: a macroscopic electric field appears as a consequence of the long-range character of the Coulomb interaction (incompatible with Periodic Boundary Conditions).

A non-analytic term must be added to Interatomic Force Constants at $\mathbf{q} = \mathbf{0}$:

$$ilde{C}_{slpha,s'eta}(\mathbf{q}) = ilde{C}_{slpha,s'eta}^{\mathrm{analytic}}(\mathbf{q}) + rac{4\pi}{\Omega} rac{(\mathbf{q}\cdotoldsymbol{Z}_s^{\star})_{lpha}(\mathbf{q}\cdotoldsymbol{Z}_{s'}^{\star})_{eta}}{\mathbf{q}\cdotoldsymbol{\epsilon}_{\infty}\cdot\mathbf{q}}$$

Effective charges Z_s^* are related to polarization **P** induced by a lattice distortion:

$$Z_{s,\alpha\beta}^{\star} = \Omega \frac{\partial \mathrm{P}_{lpha}}{\partial \mathit{u}_{seta}}$$

Dielectric tensor $\epsilon_{\infty}^{\alpha\beta}$ is related to polarization **P** induced by an electric field **E**:

$$\epsilon_{\infty}^{lphaeta} = \delta_{lphaeta} + 4\pi \left. rac{\partial \mathrm{P}_{lpha}}{\partial \mathrm{E}_{eta}} \right|_{u_{s}(q=0)=0}$$

All of the above can be calculated from (mixed) second order derivatives of the total energy.

Go to the directory with the input files:

```
cd Hands-on_DFPT/exercise3
```

Step 1. Perform a Self-Consistent Field ground-state calculation for a polar semiconductor AIAs.

Step 2. Perform a phonon calculation at Gamma for AlAs.

```
Phonons at Gamma &inputph prefix='AlAs', tr2_ph = 1.0d-14, amass(1) = 26.98, amass(2) = 74.92, outdir='./out' fildyn='AlAs.dyn', epsil = .true. /
0.0 0.0 0.0
```

If .true. will calculate and store the dielectric tensor and effective charges

In the file **Alas.ph.out** you will find an information about the dielectric tensor and effective charges:

```
Dielectric constant in cartesian axis
            13.744319556
                             -0.000000000
                                                -0.0000000000)
            -0.000000000
                             13.744319556
                                                 0.0000000000)
            -0.000000000
                              -0.000000000
                                                13.744319556 )
     Effective charges (d Force / dE) in cartesian axis
      atom
                1 Al
              1.88263
                                           -0.00000)
 Ex
                             0.00000
 Ey
              0.00000
                             1.88263
                                           0.00000)
                             0.00000
             -0.00000
                                            1.88263)
      atom
                2 As
 Ex
             -3.23388
                            -0.00000
                                           -0.00000)
                                           0.00000)
 Ev (
             -0.00000
                            -3.23388
                             0.00000
                                           -3.23388)
             -0.00000
Diagonalizing the dynamical matrix
                                     0.000000000)
         0.000000000
                       0.000000000
q = (
freq (
                                         4.538540 [cm-1]
                     0.136062 [THz] =
freq (
                                       4.538540 [cm-1]
                     0.136062 [THz] =
          2) =
freq (
         3) =
                     0.136062 [THz] =
                                         4.538540 [cm-1]
freq (
          4) =
                    11.258409 [THz] =
                                          375.540116 [cm-1]
freq (
                                          375.540116 [cm-1]
          5) =
                    11.258409 [THz] =
freq (
          6) =
                    11.258409
                                          375.540116 [cm-1]
```

No LO-TO splitting

Step 3. Impose Acoustic Sum Rule and add the non-analitic LO-TO splitting using the dynmat.x program.

Input file AlAs.dynmat.in:

```
&input
    fildyn = 'AlAs.dyn',
    asr='simple',
    amass(1)=26.98,
    amass(2)=74.92
    q(1) = 1.0,
    q(2) = 0.0,
    q(3) = 0.0
/
```



Direction for the LO-TO splitting

Output file dynmat.out:

```
freq (
                         -0.000000 [THz] =
  0.538473
              0.000000
                           -0.458309
                                       0.000000
  0.538473
              0.000000
                           -0.458309
                                       0.000000
   freq (
                        -0.000000 [THz] =
              2) =
  0.000000
              0.000000
                            0.000000
                                       0.000000
  0.000000
              0.000000
                           0.000000
                                       0.000000
   freq (
                         0.000000 [THz] =
              3) =
(-0.458309)
                           -0.538473
              0.000000
                                       0.000000
-0.458309
              0.000000
                           0.538473
                                       0.000000
                         1.257454 THz] =
   frea (
              4) =
  0.000000
                           0.940852
              0.000000
                                       0.000000
( -0.000000
              0.000000
                           -0.338817
                                       0.000000
   freq (
              5) =
                        11.257454 THzl =
              0.000000
                            0.000000
  0.000000
                                       0.000000
  0.000000
              0.000000
                           0.000000
                                       0.000000
   freq (
                        12.307908 THz]
              6) =
  0.940852
              0.000000
                           -0.000000
                                       0.000000
 -0.338817
              0.000000
                            0.000000
                                       0.000000
```

LO-TO splitting

Outline

- 1. Introduction
- 2. Exercise 1: Phonons at Gamma in non-polar materials
- 3. Exercise 2: Phonon dispersion in non-polar materials
- 4. Exercise 3: Phonons at Gamma in polar materials
- 5. Exercise 4: Phonon dispersion in polar materials

Go to the directory with the input files:

• Calculate phonon dispersion in AlAs following the same steps as in exercise2.

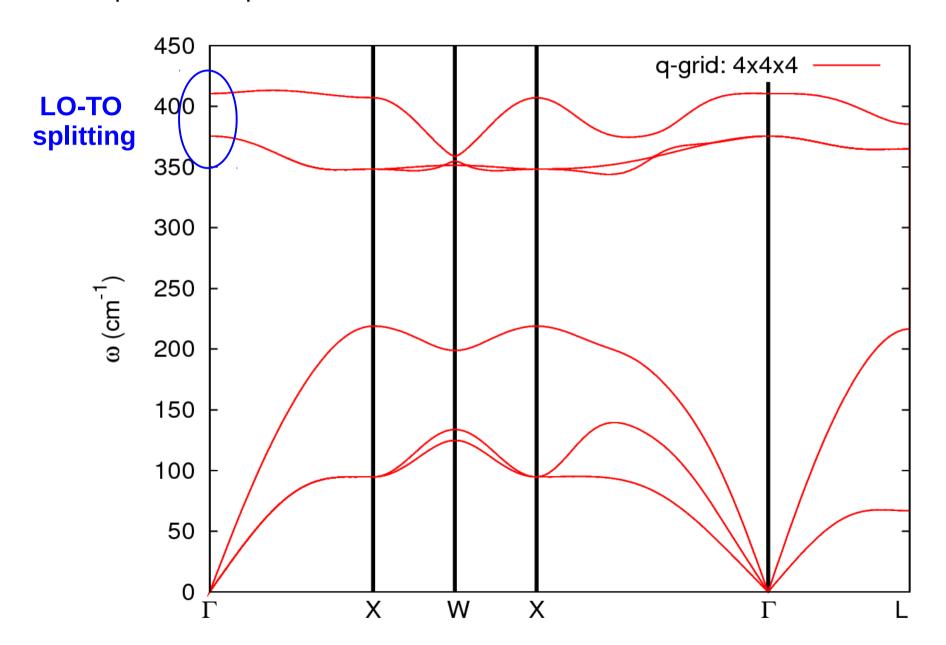
Where necessary put missing information in the input files.

- Step 1. Perform a SCF ground-state calculation for AlAs using pw.x
- Step 2. Perform a phonon calculation on a 4x4x4 **q**-grid using **ph.x** (dielectric tensor and effective charges will be calculated)
- Step 3. Perform Fourier Transformations (FT) of $\tilde{C}_{s\alpha,s'\beta}(\mathbf{q})$ in order to obtain Interatomic Force Constants in real space $C_{s\alpha,s'\beta}(\mathbf{R})$ using $\mathbf{q2r.x}$.

A term having the same behaviour for $\mathbf{q} \to \mathbf{0}$ as the non-analytic term is subtracted from $\tilde{C}_{s\alpha,s'\beta}(\mathbf{q})$ before the FT and re-added to $C_{s\alpha,s'\beta}(\mathbf{R})$, so that no problem related to non-analytic behaviour and related long-rangeness arises in the FT.

- Step 4. Calculate phonons at generic q' points using Interatomic Force Constants (including the non-analytic term) using the code matdyn.x
- Step 5. Plot the phonon dispersion of AlAs using plotband.x and gnuplot.

The phonon dispersion of AlAs:



Bibliography

1. S. Baroni, P. Giannozzi, and A. Testa, Green's-function approach to linear response in solids, Phys. Rev. Lett. **58**, 1861 (1987).

2. P. Giannozzi, S. de Gironcoli, P. Pavone, and S. Baroni, *Ab initio calculation of phonon dispersions in semiconductors*, Phys. Rev. B **43**, 7231 (1991).

3. S. Baroni, S. de Gironcoli, A. Dal Corso, and P. Giannozzi, *Phonons and related crystal properties from density-functional perturbation theory*, Rev. Mod. Phys. **73**, 515 (2001).