

quantile-improved

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11/02/2020

The line references are referring to this version:

<https://github.com/wch/r-source/blob/5a156a0865362bb8381dcd69ac335f5174a4f60c/src/library/stats/R/quantile.R#L24>

criticism:

- not enough subfunctions. Therefore the code becomes quite hard to read. Using more subfunctions also modularizes the code and makes it easier to modify

Solution: Modularize the code, i.e. split it up into the various subtasks.

- Keep it simple:
 - the main issue is the high cyclomatic complexity: especially stacked if/switch statements are hard to read (e.g. lines 50 - 102 and 29 - 35)
 - sometimes too much is done in one line: e.g. line 41: why not assign `p.ok <- !is.na(probs)` in the line before,
 - Line 57: `x[hi] != qs` implies `index > lo`

Solution: don't overload single lines, avoid high cyclomatic complexity also by creating more subfunctions and restructuring the code

- defensive programming:
 - no explicit input checks are done
 - no tailored warning messages
 - no warning messages if inputs are implicitly transformed by the functions that are called within `quantile.default`

Solution: Check inputs explicitly and give tailored warning messages

To illustrate the consequences of no input checking:

- if the type is negative, the function behaves quite unexpected: Because then it holds that `type <= 3` in (line 63) but afterwards `h` is assigned `NULL` (line 68ff) and at line 91 the quantiles are updated but nothing is done in the following lines because `h` is `NULL`...

In addition to that there are simply some inconsistencies and errors/ bugs:

- probabilities that are in $(0 - \text{eps}, 0)$ or $(1, 1 + \text{eps})$ are not corrected if `probs` does not contain any NAs (line 44 - 48).
- rounding errors are only addressed for the continuous quantiles: why?
- bug when `names == FALSE` and `probs` contains an NA (arises due to `'names(o.pr)[p.ok] <- names(qs)'`)
- whether or not character/ Date inputs for `x` work for types that are not 1 or 3 depends on the exact `probs` and `x`. Solution: only allow types 1 and 3 as is done for ordered factors

- some more comments: e.g. line 91 would be much easier to understand with a precise comment, line 98: explain why one needs the `if(any(other))`

Another major issue, that makes the code hard to read are the terrible names:

- notation is inconsistent with the help page
- abbreviations (e.g. `nppm`, `i`, `sml` ...) make it hard to know what the variable contains
- points are used in names which is reserved for S3/S4 (e.g. `o.pr`, `na.p`, `p.ok`)
- name ‘other’ (line 91) other is not really informative about what this variable means
- index (line 52): indices are usually whole numbers but not in this case

Summary of improvements:

- write more subfunctions/ modularize the code into the various subtasks.
- simplify the structure, specifically remove the nested if-conditionals
- Adhere to the styleguide and improve variable names
- Write explicit checks and exclude inputs that don’t make sense
- remove bugs and some major inconsistencies

Pseudocode

The `quantile_tidy` function is decomposed into three main components

1. The input checking: `check_inputs`
 - This function checks and modifies the inputs, as well as creates variables that are needed later
2. The actual quantile function: `quantile_main`
 - This function calculates the actual quantiles according to the type
 - It presupposes correct input that was already transformed by `check_inputs`
3. The formatting/ modification of outputs: `modify_quantiles`
 - formats the output depending on the value of names and whether the input was a factor

Only the middle part is described mathematically, the other parts will only be sketched informally.

1. check_inputs

Algorithm 1: check and modify inputs for the quantile function and create relevant variables

Result: check inputs

Input : x , $probs$, $na.rm$, $names$, $type$

Output: x , $probs$, $na.rm$, $names$, $type$, $probs_original$, $probs_NA$, x_levels

- 1 Check that **type** is an almost an integer in 1...9 and if yes round to that integer
 - 2 Check that **names** can be reasonably be interpreted as logical and extract the first element in case length > 1
 - 3 Check that **na.rm** can be reasonably be interpreted as logical and extract the first element in case length > 1
 - 4 Check that **probs** contains only values within $[0 - \epsilon, 1 + \epsilon]$ and round values in $[-\epsilon, 0)$ to 0 and values in $[1, 1 + \epsilon]$ to 1
 - 5 Remove NA values from **probs** and store the original **probs** vector in **probs_original** as well as a vector **probs_NA** that indicates which values in the original **probs** vector were NA
 - 6 Check that x is of type numeric, complex, logical, character, date, ordered factor or NULL; break otherwise
 - 7 Remove NAs from x if **na.rm** is TRUE, otherwise stop if NAs are contained
 - 8 Save the levels of x in x_levels
 - 9 **return** $list(x, probs, na.rm, names, type, probs_original, probs_NA, x_levels)$
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2. quantile_main

quantile_main only calls quantile_type_7 in case type is 7 and quantile_general otherwise. Both algorithms are described:

quantile_type_7

Algorithm 2: algorithm for quantile type 7

Result: quantiles according to type 7

Input : $p = (p_1, \dots, p_m)$, $x = (x_1, \dots, x_n)$

Output: $q = (q_1, \dots, q_m)$

- 1 $k \leftarrow 1 + (n - 1) \times p$
 - 2 $k^{(f)} \leftarrow \lfloor k \rfloor$
 - 3 $k^{(c)} \leftarrow \lceil k \rceil$
 - 4 $l \leftarrow \text{unique}(k_1^{(f)}, \dots, k_n^{(f)}, k_1^{(c)}, \dots, k_n^{(c)})$
 - 5 $x \leftarrow \text{partial_sort}(x, \text{partial} = l)$
 - 6 $w \leftarrow x_k - x_{k^{(f)}}$
 - 7 $q \leftarrow (1 - w) \times x_{k^{(f)}} + w \times x_{k^{(c)}}$
 - 8 **return** q
-

quantile_general

Algorithm 3: general quantile algorithm

Result: quantile for types 1 to 9

Input : $p = (p_1, \dots, p_m)$, $x = (x_1, \dots, x_n)$

Output: $q = (q_1, \dots, q_m)$

```
1  $a \leftarrow \text{get\_a}(\text{type})$ 
2  $b \leftarrow \text{get\_b}(\text{type})$ 
3  $k \leftarrow a + p \times (n + 1 - a - b)$ 
4  $k^{(f)} = \lfloor k \rfloor$ 
5  $k^{(c)} \leftarrow k^{(f)} + 1$ 
6  $l \leftarrow \text{unique}((1, x_{k^{(f)}}, x_{k^{(c)}}, n))$ 
7  $x \leftarrow \text{partial\_sort}(x, \text{partial} = l)$ 
8  $w \leftarrow \text{get\_weights}(\text{type}, k, k^{(f)})$ 
9 for  $i = 1 \dots m$  do
10 |   if  $k_i < 0$  then
11 |   |    $q_i \leftarrow x_1$ 
12 |   end
13 |   else if  $k_i > n - 1$  then
14 |   |    $q_i \leftarrow x_n$ 
15 |   end
16 |   else
17 |   |    $q_i \leftarrow (1 - w_i) \times k_i^{(f)} + w_i \times k_i^{(c)}$ 
18 |   end
19 end
20 return  $q$ 
```

3. modify_quantiles

Algorithm 4: modify quantiles

Result: modified quantiles

Input : **probs_NA**, **q**, **names**, **x_levels**, **p**

Output: $q = (q_1, \dots, q_m)$

```
1 Extend q with the NAs in the original probs vector
2 Assign x_levels to q
3 if names is TRUE then
4 |   Assign the corresponding probability values p as the names of q
5 end
6 return  $q$ 
```
