

Multi-level evaluation of autonomous vehicle
using agent-based transport simulation for the
case of Singapore

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1 Introduction

- General introduction, MATSim is suitable for simulating autonomous vehicles (Boesch and Ciari, 2015) etc ...
- Solves last-mile problem (Litman, 2014)
- Interesting previous studies (Fagnant et al., 2014; International Transport Forum, 2014)
- Progress (Silberg et al., 2013; Schoettle and Sivak, 2014)
- Singapore (Kheong and Sheun, 2014)

TODO Introduction

2 Simulation Framework

The investigations of autonomous vehicles in this thesis will be based on the agent-based transport simulation MATSim (Horni et al., 2015). The following sections will outline how the framework works and where it can be extended to shape it towards a autonomous taxi simulation. An overview will be given on which components need to be modified and how the final transport situation will result from all the different parts that are playing together in MATSim.

2.1 Agent-based transport simulation

The approach that is used in MATSim is to simulate a population on an per-agent timestep-based level. At the beginning of a day each person in the synthetic population has an initial plan of what it is supposed to do during the day. Mainly those plans consist of two elements:

Activities have a start and an end time, as well as, depending on the respective scenario, certain constraints on when the earliest start or latest end time could be. Alternatively activities could be defined using a certain duration after which the agent needs leave the activity location. The “standard” activities are “home” (which usually is the first plan element of a day) and “work”. More elaborate simulations can additionally use an arbitrary number of secondary activities.

Legs are the second type of plan elements. These describe connections between two activity locations and contain information like which mode of transport the agent will use (e.g. “car”, “public transport”, or “walk”) and, depending on the selected mode, further data like the route that should be taken through the street network.

A typical day plan of a MATSim agent can be seen in fig. 1. The agent starts at home, then walks to his job, stays there for a certain time and then goes back home. Each agent in a poluation (which can range from several hundreds to hundeds of thousands) has it’s own individual plan that is executed when one day is simulated.



Figure 1: A typical agent plan in MATSim

The network, on which the simulation is taking place, is described through nodes and connecting links. These are described by a specific capacity which tells the simulation how many vehicles are able to pass the link within a certain time frame, while the length and an average link speed determine how fast vehicles will travel to the next node.

The whole MATSim simulation is done time-step by time-step. In a single simulation step (usually 1 second) the agents that are currently in an activity don't need to be taken into account unless their scheduled activity end is reached. The other agents, which are currently on a leg, are simulated in a dedicated traffic network simulation. This simulation moves the agents according to the capacity and current congestion from the start node to the end node of the respective links. Traffic is not simulated on a micro-level (i.e. the vehicles don't have distinct positions along the link) in order to increase the simulation speed.

The congestion on the traffic network is therefore emerging from the single travel plans of all the agents. If there are too many agents which try to use one route at the same time, the overall congestion will increase.

All steps described above, i.e. the simulation of activities and legs during a whole day, are summarized as the "Mobility Simulation" or, in short, Mobsim of the MATSim framework.

In order to simulate dynamic agents, which are not statically residing in a fixed-timed activity or a predefined leg route, quite significant changes need to be made and some of the computational advantages of the simulation approach need to be partly circumvented. This, however, mainly addresses implementational details and will be discussed later throughout the thesis in section 4.

2.2 Utility-based scoring

As pointed out in the last section, individual travel decisions might lead to waiting times on the network, which then can also lead to late arrivals at the designated activity locations, which usually would be disadvantageous in the real world. Therefore, it might be beneficial for an agent to reconsider the time and route choices that had been made for the current day, just as a real person would do.

In order to “know” whether a plan worked out well or was disadvantageous, the single elements need to be weighed and quantified. This is done using the Charypar-Nagel scoring function (Horni et al., 2015):

$$S_{plan} = \sum_{q=0}^{N-1} S_{act,q} + \sum_{q=0}^{N-1} S_{trav,mode(q)} \quad (1)$$

Basically, it combines the marginal utilities of all activities ($S_{act,q}$) ranging over the N activities in a plan and the marginal utilities for all the legs in between.

The marginal utility for the activities, among other factors, depends on how long the activity has been performed, whether the agent needed to wait to start it (due to an early arrival) or whether it was forced to leave early. For more details the complete computation is shown in (Horni et al., 2015).

For the scope of this thesis the travel utility is more interesting. A basic version for a single leg q can look as follows:

$$S_{trav,mode(q)} = C_{mode(q)} + \beta_{trav,mode(q)} \cdot t_{trav,q} + \gamma_{d,mode(q)} \cdot \beta_m \cdot d_{trav,q} \quad (2)$$

Mode Choice The first term, $C_{mode(q)}$, describes a constant (dis)utility for the choosing a certain mode for the leg. It can be interpreted as how “favorable” a certain mode is and is generally negative.

Travel Time The parameter $\beta_{trav,mode(q)}$ is the marginal utility of traveling, which is multiplied by the time spent on the leg $t_{trav,q}$. It signifies how favorable it is to spend time on such a leg, i.e. the longest one needs to stay in a car or in the public transport, the larger the disutility gets (and therefore the parameter is usually negative). Values which are absolutely bigger therefore stand for travel modes where time is spent less useful or comfortably.

Travel Cost The third element involves the (positive) marginal utility of money β_m , which is an universal simulation parameter and describes how the utility of money can be weighed against e.g. time. It is multiplied with the (negative) monetary distance rate $\gamma_{d,mode(q)}$, which states, to how much disutility per spanned distance the leg will lead. This parameter is useful for imposing distance-based fares in a certain transport mode and thus making it monetarily attractive or unattractive compared to other ways of traveling.

Beyond these parameters, which are usually used by all travel modes, there are a number of additions, e.g. for public transport, or yet generally unused options, such as a direct marginal utility of distance travelled.

For the purpose of simulation autonomous taxi services, two additions are made:

$$S_{av} = C + \beta_{trav} \cdot t_{trav} + \gamma_d \cdot \beta_m \cdot d_{trav} + \beta_{wait} \cdot t_{wait} + f_m(d_{trav}, t_{trav}) \quad (3)$$

Waiting Time Here, β_{wait} is the marginal utility of waiting time, quantifying how disadvantageous it is to wait for a taxi to arrive.

Service Cost Furthermore the function $f_m(\cdot)$ is a placeholder for any pricing strategy that might be tested (on top or as a replacement for the beforementioned travel cost). The implementation will allow for an easy modification of this function.

TODO Explain double penalty for waiting time due to less time to do activities

All these utility computations are done after all agents have been simulated for a whole day (in fact, usually 30h are used). This step in the MATSim framework is simply called the “scoring” phase.

TODO It would be better to explain the additional parameters further down in the chapter about the AV fleet model. Here, further explanations on how those parameters are usually measured and estimated would be more adequate.

2.3 Evolutionary replanning

The last step in order to make all the agents “learn” more optimal plans which make sure that they arrive on time at the activity locations and avoid congestion is to make them replan their day. This is done using an evolutionary algorithm in the following way:

Usually an agent will start out with one quite random plan, go through it during one whole day and then get a score for it. Afterwards, in some iterations, this plan is copied and modified slightly. Those modifications can happen with respect to start and end times of activities, mode choices for certain legs, etc. So after one iteration the agent might already have two plans to choose from.

Before the next day starts, one of the available plans is selected due to a certain strategy. The standard approach is to do a multinomial selection with respect to the previously obtained plan scores. So one after another plans, will be created, scored, modified, rescored and so on. Because of the selection process, which favors high scores, better and better choices will be made.

However, this is done for each and every agent, so while improving the performance of one agent’s plans, this might effect the performance of other agents negatively, which is especially true if one thinks about the example of highly congested roads due to too many agents choosing the same route. Finally though, the algorithm reach at a quasi-equilibrium, which in MATSim is usually refered to as the “relaxed state”, in which the average score of the used plans stabilizes within a reasonable variance.

Each “day” that is simulated in this manner is usually called an “iteration” of the simulation. It is common to divide these iterations into two parts. The first one is the “innovation phase”, where plans have a certain probability to be modified, while in the second phase innovation is turned off. This means that the agent will only choose among the present plans in his repertoire (usually around 5) and rescore them again and again, until the most favorable is selected.

All of the above is known as the “replanning” in MATSim. Putting everything together, a whole cycle in a MATSim simulation can be seen in fig. 2. Since the final traffic situation evolves from the evolutionary choice in the replanning and selection, as well as from the emergent congestion in the Mobsim, this whole cycle

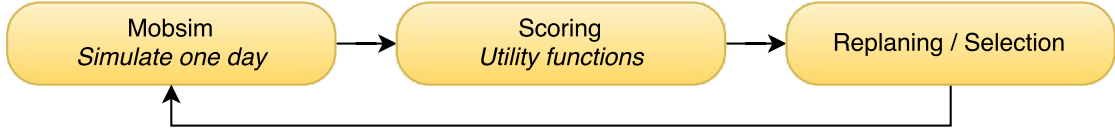


Figure 2: The basic co-evolutionary algorithm of MATSim, showing the three main stages: Mobsim, Scoring and Replanning/Selection

is usually referred to as a “co-evolutionary” algorithm.

Figure 3 shows a typical progression of the population-wide score in a MATSim simulation. What one can see there is an average over the worstor best plans of each agent, additionally the averaged average score of all the plans that the agents own is displayed. Finally one can see the average of all the plans that have been executed by the agents in a particular iteration.

The first phase until iteration 100 is the innovation phase, where time and mode choices can be done, while at iteration 100 it is turned off. There, because now the best plans must adapt to the overall situation, they are loosing in value, while the worst scored plans are dropped are likely to be discarded. Finally, a quite stable population-wide relaxed state is reached.

2.4 Queue-based simulation

The heart of the simulation in MATSim is the queue simulation, or more briefly, the QSim. This part of the framework is iterating through all the agents that need to take action in the current simulation step.

Itself the QSim is split into the handling of agents which are currently performing an activity (i.e. are in an idle state in terms of the traffic simulation) and another part, the Netsim, which is simulating the traffic network.

When running the Netsim, the agents are moved on the network according to their current route and dependent on congestion. After moving an agent, the Netsim checks whether the agent should end its trip at the current link he has been moved to. If this is the case, the agent is removed from the Netsim and the next agent state is computed.

The result of this computation is either that the agents wants to start a leg, in which case he is reinserted into the Netsim, or that he wants to start an activity,

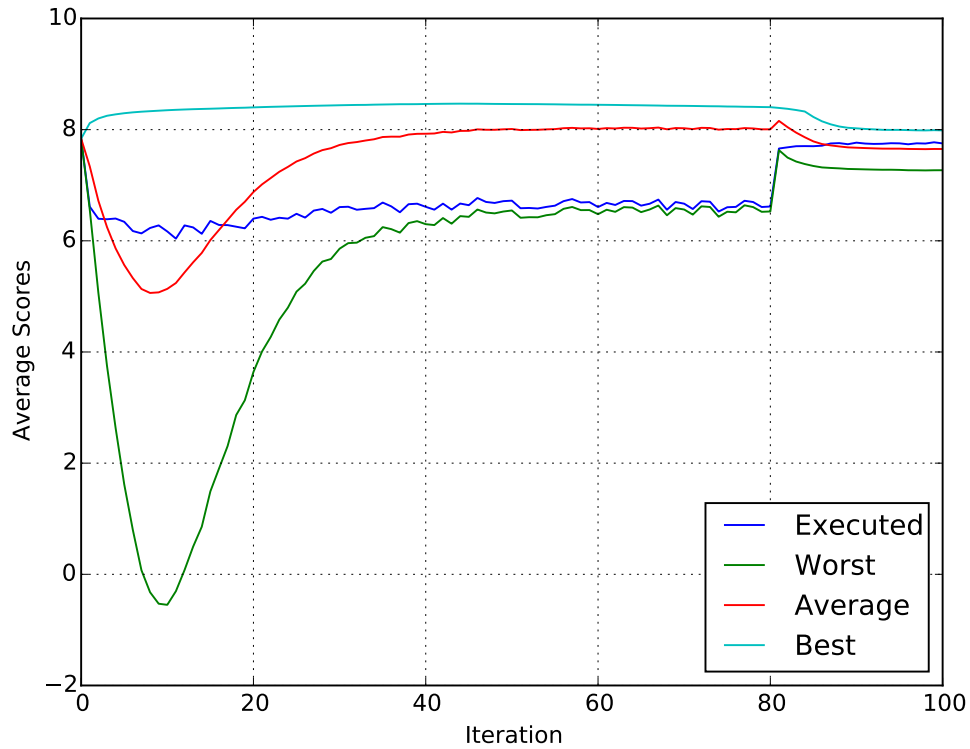


Figure 3: Typical progression of the agent scores throughout a MAT-Sim simulation. “Worst” means that the plans with the worst scores from all the agents are taken and averaged, the same applies for the other graphs. **TODO** make a better graphic with a more clearer relaxation (simple corridor should be okay)

which will make the agent to be added to the activity queue.

This activity queue is the other main component of the QSim. In fact it is a priority queue, where all agents are sorted according to the time at which they want to end the next activity. So when adding an agent to the activity queue it first is checked when the activity should be ended and then the agent is inserted at the corresponding position in the queue.

The processing of this queue in the QSim for each simulation step then works as follows: The first element of the queue is looked at and it is checked, whether the agent should already end the activity. If this is not the case, the simulation step is already finished. On the other hand, if the activity should be ended now (or previously if the time resolution of the simulation is quite high), the agent is removed from the top of the queue and the next state is computed as described above. Then the new top element of the queue is examined, until the simulation step is finished. The whole QSim simulation is schematically rendered in fig. 4.

The big advantage of this simulation architecture is as follows: When an agent is in an activity, no computation needs to be performed. So instead of polling all the agents in every simulation step to check if they want to end an activity, the computational demand is much lower when using the queue, since a lot of agents can be skipped. The sequential processing of the priority queue is very fast in terms of computational complexity ($\mathcal{O}(1)$ for checking the top element and $\mathcal{O}(\log n)$ for fetching it, Java API (2016))

Furthermore the same concept is used within the Netsim to speed up the computation of the traffic situation. In both cases, for the QSim and Netsim, those savings in computation time naturally decrease the versatility of the simulation environment.

One major drawback is that if an agent, which is already queued should abort its current activity, it needs to be removed from the queue and added at a new position. Both operations are quite costly for the priority queue (Java API, 2016), so if more and more reschedulings are needed, the computational overhead can become quite large.

However, for truly dynamic agents, like autonomous vehicles, it is necessary to adopt their plans frequently and thus some thought needs to be put into how to achieve this freedom while still keeping as many advantages from the existing

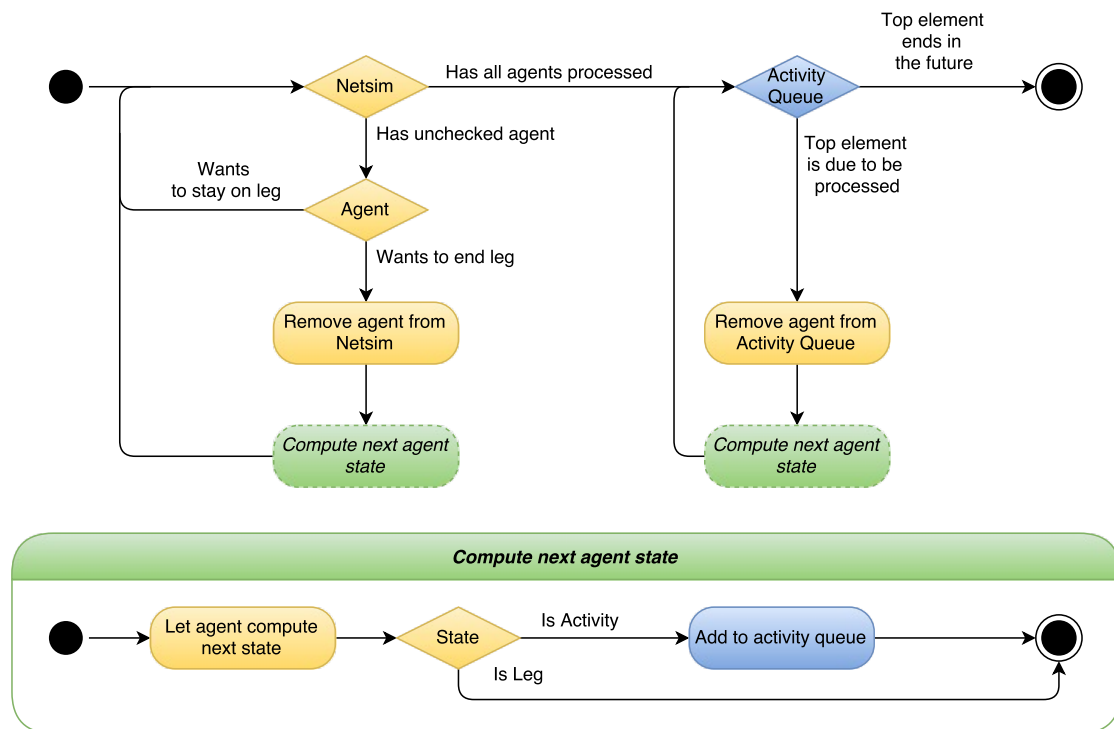


Figure 4: Simplified structure of the QSim in MATSim.

simulation architecture.

3 The Sioux Falls Scenario

The City of Sioux Falls in South Dakota has been a classical test case in transport research for more than four decades, being first mentioned in this context in Morlok et al. (1973). While none of the numerous implementations of the network are intended to be accurate and realistic with respect to the actual City of Sioux Falls, they are merely aiming towards providing downscaled, computationally tractable test cases for transport planning and simulation problems.

In Chakirov and Fourie (2014) the scenario (“Sioux-14”, fig. 5) has been adapted to the MATSim framework. A sparse street network, which is computationally easy to handle by the simulation, was introduced. It consists of 27 nodes and 76 links, representing the main arterial roads of the city, split further down into 282 nodes and 334 links in order to arrive at partial link sizes of less than 500m. This is necessary, because MATSim agents start their travels at the start node of a link and thus a high resolution is needed to avoid unrealistic clustering. (TODO Is it the start node? Or end?)

On the supply side there is furthermore a public transport network, which consists of 5 lines with bus stops along the arterial roads in a distance of 600m. The stops are placed in a distance of 5m perpendicular to the road and departures from the lines’ respective start links take place every 5 minutes.

A lot of effort has been put into the modelling of the demand side, covering the realistic generation of home locations, work places, secondary activity locations, as well as the distribution of socio-economic factors such as age, car ownership and gender across a synthetic population, as it is needed for the agent-based simulation.

In this regard the scenario provides a lightweight example of a complete MATSim simulation, where it is easy to test different parameters and extensions to the framework on a near-realistic baseline scenario. However, while working with the original Sioux-14 network during the course of this thesis, it became clear that the simplified structure of the underlying traffic network does not provide enough resolution for the simulation of autonomous vehicles.

The main reason is, that agents, who choose to take a car in the Sioux-14 network, probably living in the middle of the squared regions of the network,

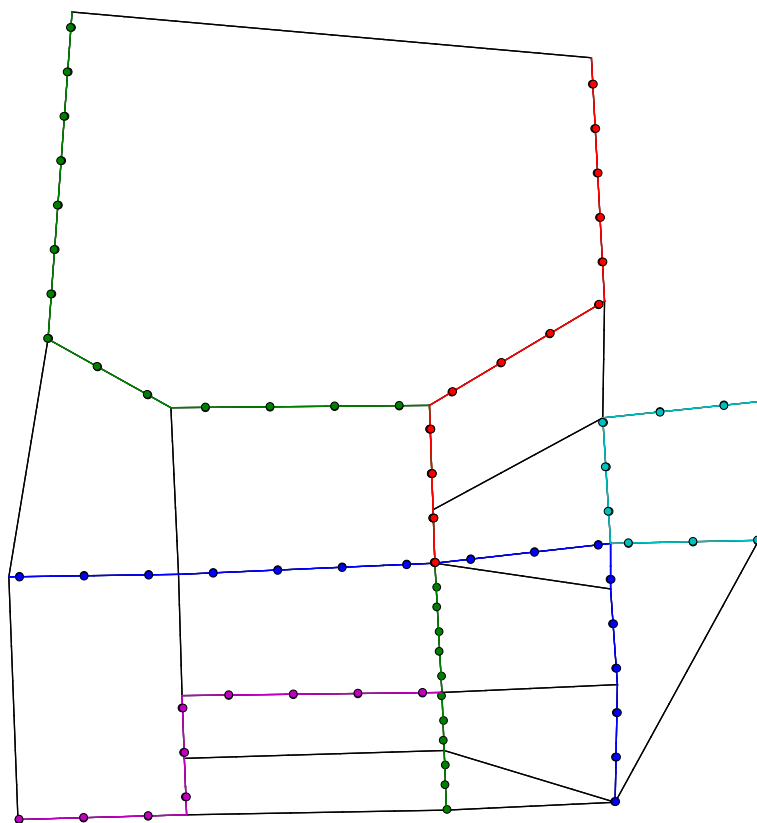


Figure 5: **TODO** todo

would be teleported to the nearest link to start their travels. This would be also true for autonomous vehicles, which is not a realistic assumption in both cases, especially when comparing it with public transport, where agents in MATSim are explicitly penalized for covering the distance between home and bus stop by foot. Furthermore effects like people being more inclined to opt for a autonomous taxi when living far from public transport can only be convincingly simulated on a finer network.

The following sections will describe how, starting from the initial Sioux-14 scenario, a new more fine-grained versatile test scenario for MATSim has been developed, which in turn has been used as the basis of the following investigations in this thesis.

The new Sioux-16 network, which has been developed for this thesis, is based on the demand model of Sioux-14, which means that all locations for homes, work places and secondary activities are kept equal, while it differs on the supply side, aiming to resemble the original scenario as closely as possible. The following sections will describe, how the Sioux Falls network from OpenStreetMap (with the state as of 18 Apr 2016) has been converted and adjusted to be compatible with MATSim and closely match the prior version of the test scenario. Furthermore it will be explained, how the public transport network has been adapted to the fine-grained Sioux-16 scenario.

3.1 Network generation and adjustment

For the creation of the new scenario, an area covering Sioux Falls has been captured from OpenStreetMap, which can be seen in fig. 6. Using the MATSim exporter in the JOSM tool ¹, a simplified, MATSim-compatible network of the selected region has been created. In this process all primary, secondary and tertiary streets have been selected, while road types further down the hierarchy (for instance residential streets) have been omitted.

However, some adjustment was needed in order for the network to play nicely with the given facilities from the Sioux-14 scenario. Most importantly, the network from OSM was defined in the EPSG:3857 coordinate system, while Sioux-14 uses

¹<https://josm.openstreetmap.de/>

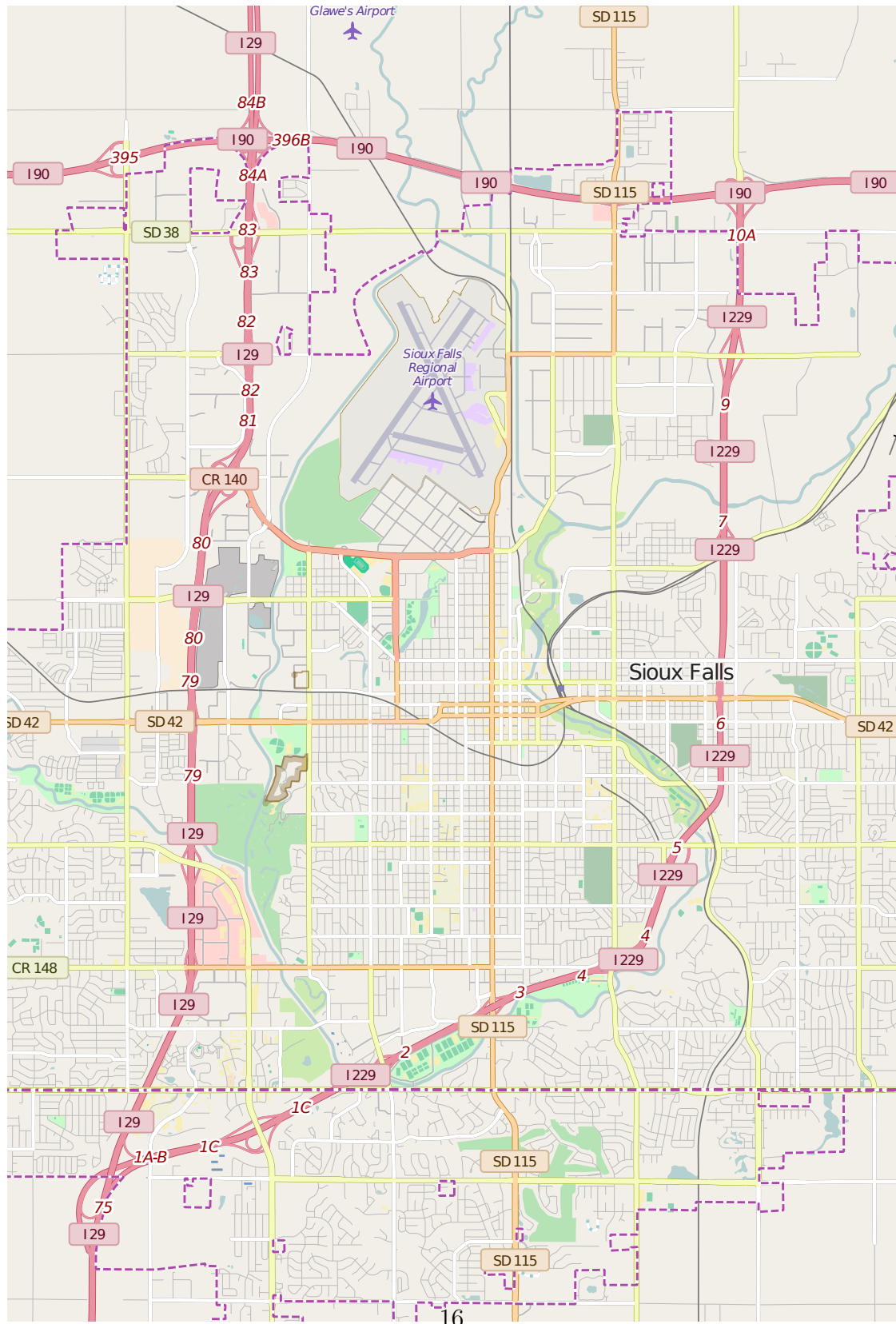


Figure 6: Map of Sioux Falls from OpenStreetMap. Longitude from -96.8105° to -96.6653° and latitude from 43.4729° to 43.6286° .

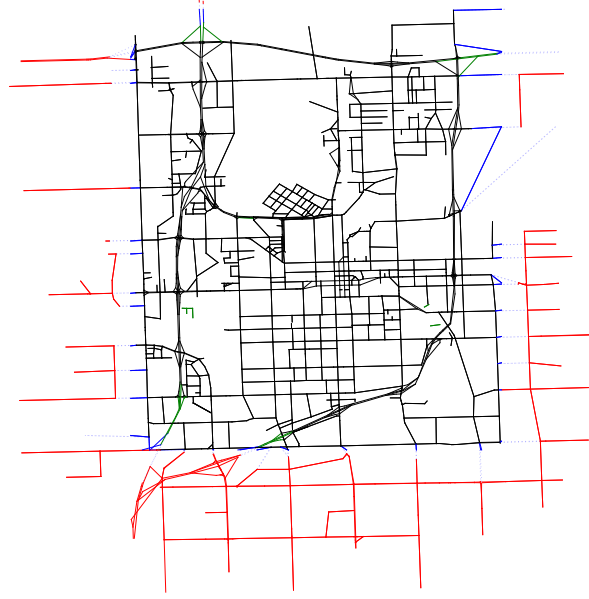


Figure 7: **TODO** todo

EPSG:26914. Therefore, in a first step, the coordinates of all the generated nodes needed to be converted to the old system.

In a second step, the positions of all facilities in Sioux-14 have been obtained and a bounding box with a margin of 500m around them has been computed. Subsequently, all links, which were located out of the bounding box, were removed from the network, while those who were crossing the borders have been cut to fit into the area. The initial network with all removed (red) and cut (blue) roads can be seen in fig. 7. In total 352 outside links have been removed and 83 links have been adjusted.

After that, a cleanup up the network needed to be done, partly because of artifacts due to the filtering of road types, partly because of the removal of the external sections. This removal was done in a couple of steps:

1. The lengths of all the links have been updated to the L^2 distance of their respective start and end nodes in the new coordinate system.

2. The network has been searched for sources (nodes that only have outgoing links) and sinks (nodes that only have incoming links). Those have been removed, because they make no practical sense. This procedure lead to 53 removed links in total.
3. One seed node has been defined, which definitely belongs to the street network and then by traversing the all paths from that node, it has been determined, which streets belong to the main network. All remaining nodes and links, which have become detached from this main network have been removed (11 nodes and 14 links).
4. Finally, the network has been searched for duplicate links with the exact same start and end node. Only the first of those links have been kept, which lead to the removal of 3 duplicates.
5. In Sioux-14, the links have been split such that there are no connections longer than $500m$. This procedure has also been applied to the network at hand, leading to 389 splitted links, which have been cut into a number of equal parts with less than $500m$ length depending on their overall length.

In terms of nodes, these procedures in total lead to an increase of nodes from 1392 to 1806 (ratio 0.77) and in an increase of links from 2957 to 3335 (ratio 0.89). The links that have been removed during the cleanup are colored in green in fig. 7.

3.2 Public Transport Adaptation

The adaptation of the public transport network to the new (“Sioux-16”) scenario posed some challenges that needed to be solved:

- The links of the original network did not exist anymore, obviously the routes for the different public transport needed to be mapped to the new network.
- The stops from the original network could not be mapped easily to the new roads, partly because some streets in Sioux-14 were “invented”, only approximating connections in the finer network on a very coarse level, but also because roads that consisted of two overlapped links for both directions

were now split up into two spatially distinct lanes (as can be seen in the upper left part of fig. 8).

In order to get a rough routing for the bus lines, the main nodes of the Sioux-14 network have manually been mapped by hand to nodes in the Sioux-16 network. This made it possible to obtain new public transport roads in terms of those guide points: For each of the lines it has been defined, which guide points should be traversed and in which order. Then, the Dijkstra algorithm (Dijkstra, 1959) with travel time as the objective has been used to find the shortest path from waypoint to waypoint. After fitting those partial paths together, the whole route in terms of the links of the Sioux-16 network have been obtained. As can be seen in the colored routes in fig. 8 this made it easy to obtain routes that take into account the specific map structure (for instance the highway on the upper left or the one way streets, which are traversed by the blue line in the center of the map).

The generation of bus stop facilities was a more challenging problem. Given the location from Sioux-14 one could roughly match the stops to links along the new routes, which worked in principle. However, using this approach, bus stops were cluttered all along the lines. With the intention of having a rather realistic network some conditions needed to be taken into account:

- The bus stops of one line should be on opposite sides of a street and not have a large longitudinal distance. While satisfying results could be obtained, for instance in the center with the blue line, the same approaches did not work well for the highway connectors on the left for the green line, and vice versa.
- The bus stops of parallel lines should be at the same locations, i.e. in the center where the green line uses the same roads as the red one, the same locations should be chosen. This constraint usually interfered with the approaches that took into account the first constraint (especially in the center for the blue line).
- Finally, some of the Sioux-14 locations were completely off the network in Sioux-16, for instance for the red line, where one can see a bend in the diagonal connection, which was modelled as a straight line in Sioux-14.

Given all those constraints the best approach seemed to put in manual work with some automated help. The final approach made use of a small program, written to manually choose the stop locations along all roads and then subsequently choose which stop locations should belong to which line. In this step one did not take into account the cases of two lanes, as just the general positions needed to be known (e.g. for the blue line in the center an approximate position between the two lanes would be chosen).

In another step, the locations that had been assigned for each line have been assigned to the respective links along the line. So for the blue one, the average points in between would have been assigned to a link underneath for one direction and another stop would be created for the link above. This resulted in a final set of stop locations.

Furthermore, some stop locations were actually located on one single link. This can happen if there is a link of roughly $500m$ and the stops are for instance located at $1m$ and $499m$ along the link. In those cases the network needed to be broken up at those positions. In the current scenario this leads to the splitting of only 4 links.

Finally, according to the setup of Sioux-14 the stop locations have been moved to a position normal to the link direction, with a distance of $5m$. Additionally a schedule with busses departing in $5min$ intervals has been created.

The final public transport network can be seen in fig. 8. It features 150 stops with an average distance of $520m$ and a median of $566m$. This is a result from not being able to put the stops as accurately in intervals of $600m$ as it is possible in Sioux-14. Moreover, the L^2 distance between two stops along the routes have been used instead of a measure along the actual path. The minimum and maximum distance between stops are $218m$ and $847m$, respectively.

All steps that have been described above have been implemented in a reusable and parametrized way. For instance, one could choose to allow a maximum link length of $5km$ and would still obtain a valid network at the end, probably just with a larger number of splitted links during the processing of the public transport.

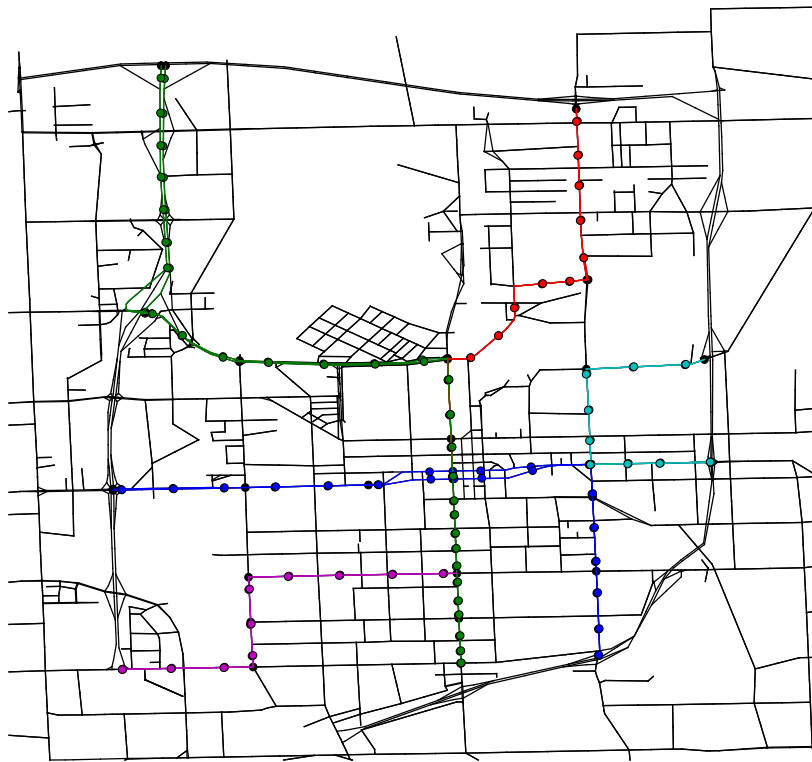


Figure 8: **TODO** todo

3.3 Scenario Calibration

The Sioux-14 network features artificially chosen link capacities, which are based on a minimum of two and a maximum of three lanes per link, where three have only be chosen for a fraction of highway links (Chakirov and Fourie, 2014). While the added minor streets in Sioux-16 should not make too much of an impact in overall capacity, the highways and main arterials of the real network usually feature greater capacity (for instance by providing *four* lanes on the western highway).

Looking at fig. 9, it can be seen that the travel time (of cars) in the new network is lower (red), compared to Sioux-16 (black). This effect can partly be explained by the increased capacity, but also by the multitude of new options to choose the most effective route for a trip through the fine-grained network. In fact, the route choice might be the major influence when comparing with the data from fig. 10. There the decrease in link speeds (relative to the freespeed) can be seen, which is quite similar, indicating a comparable amount of congestion in the network.

Depending on how important the comparability to Sioux-14 in a specific scenario is and what time of the day should be compared, it might be beneficial to adjust the flow capacity of the network²: In terms of travel times a scaling of 50% would resemble the afternoon peek way better than the 100% version, while the morning peek would best be recovered by a value in between (fig. 9). A similar situation arises for the link speeds in fig. 10, where a value of 50% is better suited for comparing the morning peak, while the 100% scaling creates more comparable results in the evening.

Furthermore, in terms of link speeds, it can be seen that the Sioux-16 scenario features less congestion during the off-peak hours due to the possibility of distributing trips all over the network.

A comparison of the scenarios in terms of average travel times, distances and more shares can be found in table 1. What can be seen is that averaged over the whole day, values stay roughly the same, with the biggest differences being present in car traffic. There, especially the decrease in travel distance is noticable,

²In MATSim, this can be easily done in the Mobsim configuration, e.g. `qsim.flowCapacityFactor` for QSim

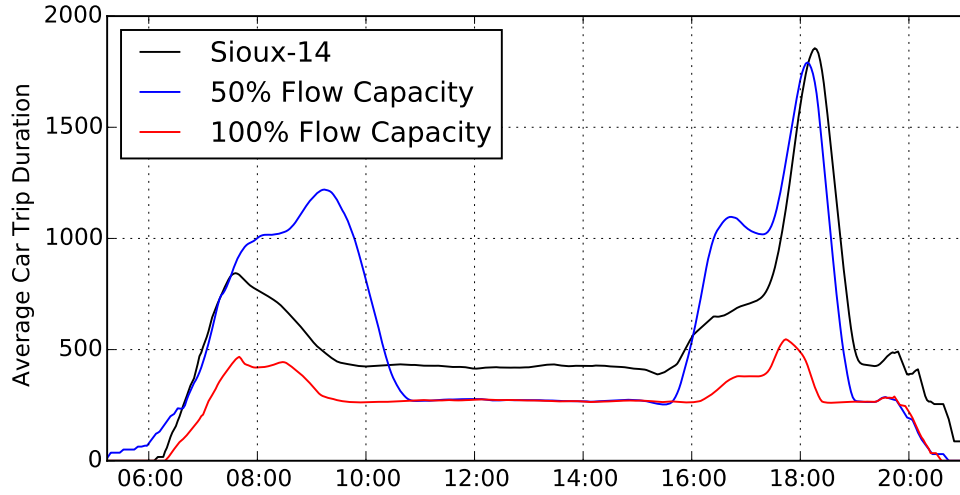


Figure 9: Comparison of the average duration of car trips by day time in Sioux-14 and Sioux-16 with 50% and 100% flow capacity.

but expected, since more direct routes can be taken. For public transport the result of Sioux-16 are similar to Sioux-14, which is an indicator that the network is strongly resembling the former version.

In terms of mode shares it is interesting to see that public transport does not see a big difference between Sioux-14 and Sioux-16 (100%), but that 3% of agents switch to using a car from walking. This effect can also be explained with the better car accessibility of destinations, where long detours would be needed in the sparse network.

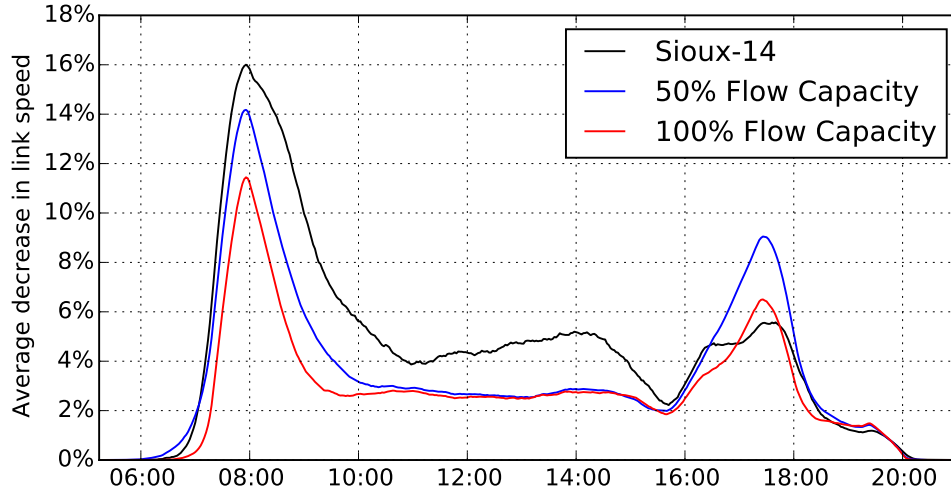


Figure 10: Comparison of the decrease of link speeds by day time in Sioux-14 and Sioux-16 with 50% and 100% flow capacity.

Table 1: Comparison of Sioux-14 and Sioux-16 in terms of travel measures

Scenario	Sioux-14	Sioux-16	Sioux-16	Sioux-16
Flow Capacity		50%	70%	100%
Travel Distances [km]				
Car	2.60	1.83	1.80	1.79
Walking	1.33	1.29	1.27	1.26
Public Transport	3.70	3.82	3.86	3.89
Transit Walk	0.59	0.53	0.53	0.53
Travel Times [mm:ss]				
Car	09:00	08:39	07:01	05:12
Walking	26:35	25:48	25:19	25:08
Public Transport	31:20	29:05	28:32	28:14
Transit Walk	10:45	09:07	09:07	09:06
Mode Shares				
Car	63.52%	63.67%	65.26%	66.13%
Walking	9.44%	7.41%	6.72%	6.48%
Public Transport	27.04%	28.92%	28.01%	27.39%

4 Dynamic Agents in MATSim

In order to allow for dynamic behaviour in MATSim, several approaches have been proposed. Mainly the decision on which option is best usually depends on what a level of complexity in the behaviour is needed.

A simple version of dynamic behaviour is implemented in the public transport extension, where passenger agents are saved in a list, as soon as they reach the link in the network, where they should be picked up by a public transport agent. As soon as the pt agent (e.g. a bus) arrives at that link, persons from the link are deregistered from the list and “teleported” to the destination stop as soon as the vehicle arrives there. This setup fits very well into the queue based structure of MATSim.

An even more dynamic approach is used in the DVRP framework, which will be discussed in the first part of this section. At the time of this thesis and for the specific use case of autonomous vehicles some drawbacks will be shown and finally a new abstraction layer for dynamically acting agents will be presented, which has been part of the work for this thesis.

4.1 DVRP

The DVRP extension [TODO citation](#) is designed to provide a level of abstraction to the simulation of dynamic transport services, such as taxis. Its general structure is quite flexible, so that it is easy to implement for instance electric vehicles [TODO citation](#) (which need to recharge at some point during the simulation) or taxis, which are roaming randomly through the cities and serving concrete requests when they are made by passengers [TODO citation](#).

However, this flexibility comes with a cost. The architecture of DVRP basically circumvents the efficient queue simulation of MATSim for activities. While “normal” agents are simulated as described before, dynamic agents (DynAgents) have two modifications:

Legs are sent to the conventional Netsim. However, agents have the ability to change their paths dynamically, i.e. one can modify the route of the agent during the simulation steps and the next time the Netsim wants to move

the agent or checks whether the agent should arrive at the current link, its response is calculated from the updated path.

Activities are simulated separately from the non-dynamic agents. As soon as a DynAgent starts an activity it is added to a list of active agents. In each simulation step a specific callback for each of those agents is called and then it is checked whether the agent wants to end this activity or not. This polling approach, as depicted in fig. 11, makes sure that it is not necessary to know when an activity (for instance a taxi waiting for any requests) should end or how long it should take. On the other hand, this approach is much more computationally expensive than the efficient queue simulation. Given that the simulation is done on a second-by-second basis, an activity that would take one hour, would cost only one insert and one lookup on the activity queue. In the polling approach it costs 3600 calls to the simulation step callback (even if it does not actually compute anything, this adds a computational overhead) and 3600 checks whether the activity should be ended.

So far, DVRP has been successfully applied to a number of projects [TODO cite](#), though their overall usage of MATSim was different. For instance, in Bischoff and Maciejewski (2016) a study on autonomous vehicles has been done, where the demand in Berlin has been obtained using an ordinary MATSim simulation. Then the link speed of the underlying network have been modified, to resemble the traffic situation in a congested situation and then *only* autonomous vehicles have been simulated. This means that the simulation could be run once and the results were obtained, because only the QSim was used and not the evolutionary learning of MATSim.

However, in the project of this thesis, autonomous vehicles should be tested in an existing multi-modal scenario, where the evolutionary learning is necessary in order for the agents to arrive at their quasi-optimal mode choices. So if Bischoff and Maciejewski (2016) mentions computational times of 20h for a large number of agents, it is a measure for one iteration in the evolutionary algorithm. For the scenarios that will be tested here, a number of 100 iterations still does not reach a satisfactory equilibrium, though having a theoretical computational time of 2000h,

in the case of the given paper.

Measurements have been made to determine, how much the combination of executing an empty simulation step for an agent and the execution of an activity callback that always lets the agent stay in an activity would cost in terms of execution time on the platform that has been used throughout the thesis. The final results gave an average time of 25ns. So simulating for instance 8000 agents for a common time of 30h, would lead to an execution time of:

$$T_{30h} = \underbrace{25}_{\text{Nomial}} \cdot \underbrace{3600 \cdot 30}_{\text{One day in seconds}} \cdot \underbrace{8000}_{\text{Agents}} = 21.6s \quad (4)$$

For the whole MATSim simulation, this needs to be multiplied by at least 100 iterations, so that the overhead of a simulation of 8000 agents doing nothing would already reach a computational overhead of

$$T_{sim} = 21.6s \cdot 100 = 36min \quad (5)$$

Furthermore, while working with DVRP it has been found that the provided examples for DVRP were not fully compatible with parallelized computation in the Netsim, which would have lead to a neglect of a good way to improve the computational performance of the simulation. However, it seems like this problem has been fixed in the latest version of DVRP by the time of the writing of this thesis.

As a summary, one can say, that DVRP allows for a great freedom in simulating dynamic behaviour and its structure and signaling flows are very straightforward and easy to work with. However, for the purpose of simulating large nubmers of autonomous vehicles in the whole MATSim with large numbers of iterations, it would be beneficial to find more efficient ways for the simulation.

4.2 The AgentLock framework

As an alternative to the simulation of dynamic agents using DVRP, the AgentLock framework has been developed as part of this thesis. It tries to combine the advantages of a queue simulation while providing as much flexibility as possible to create rich dynamic agent behaviours in MATSim.

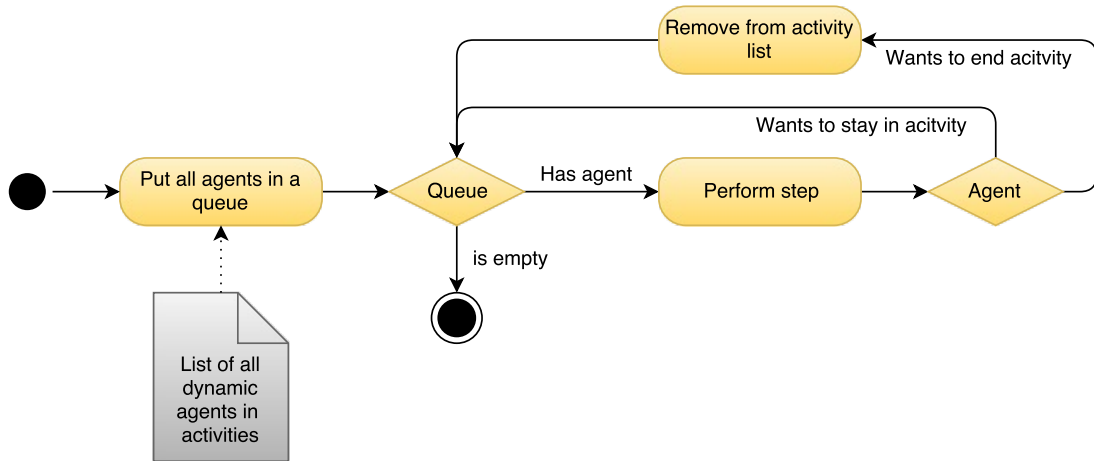


Figure 11: Polling approach of the DVRP framework

The basic idea is as follows: Usually agents in MATSim do not need a lot of processing power, i.e. the per-agent simulation step of DVRP is hardly ever used and can usually be replaced by some callbacks and event handlers outside of the actual agent simulation.

Furthermore, this means that an activity basically just means that an agent is residing at a certain position in the network and not taking part of the network. So an activity for an agent is just keeping the agent back from joining the traffic network again after a certain time or event.

With this idea in mind, three different types of ways to “lock” an agent into an activity have been proposed:

Blocking activities will just let the agent reside in this activity until it is released through a call from outside.

Time-based activities are the ones from the basic MATSim simulation: They have a certain duration and therefore a fixed end time.

Event-based activities let the agent reside in the activity until a certain event happens.

The heart of the AgentLock extension is the LockEngine. Whenever it encounters an agent that wants to start a blocking or event-based activity, it is removed from the simulation and only added back again as soon as this happens

manually or the event occurs. Then it either is passed to the ordinary Netsim or the next activity is starts, just as requested by the agent logic.

For time-based activities a similar approach to the activity queue for ordinary agents is taken. The first idea that would come to one's mind is to order the agents by the end of their activity and as soon as there is a change in plans, remove the element from the priority queue and add it back at a certain position.

Compared to DVRP, where a change of plans would cost nothing, here this would lead to an overhead of $\mathcal{O}(\log n)$ and $\mathcal{O}(n)$ for these operations (Java API, 2016). So it is necessary to weigh the overhead of the polling in DVRP against the overhead of the rescheduling, which mainly depends on how often such reschedulings appear. In the concrete example of autonomous taxis, this itself depends directly on the travel demand.

TODO cite sth here for the PQ? JavaDoc?

If one sacrifices increasing memory consumption for the sake of having a faster computational time, this setup can be improved further, as done for the AgentLock framework. Here, everytime a time-based activity is started, a handle to the corresponding agent is saved into the priority queue, ordered by the end time of that activity. Furthermore an indicator is saved, whether the handle is still valid. So if in the meantime (i.e. before the end of the activity has been processed) the plan is changed, this handle will be invalidated and it will simply be ignored when processing the priority queue.

So the whole process works as follows: In every simulation step the top element of the priority queue is checked. If it is scheduled for the current or a past time step, it is processed. This means if it is still valid, the agent is “woken up” from its current activity and the next state (activity or leg) is computed. Afterwards, or if the handle already had been invalidated, the processing continues with the updated top element of the priority queue. This process is also shown in figure ??.

TODO Create figure, or maybe not necessary?

The main advantage of this setup is, that elements are only removed at the top of the queue, which is significantly less expensive than removing elements at arbitrary positions within the queue.

Furthermore the AgentLock framework provides methods for dynamically ending legs and it has been made sure that all the functionality has a high degree

of compatibility with the existing parts of MATSim, such as the multi-threaded Netsim.

4.3 AgentFSM

While the AgentLock extension mainly provides an abstraction layer for the dynamic rescheduling of activities and legs, another layer has been developed, which is loosely resembling a finite state machine [TODO cite](#), tailored towards agents in MATSim.

In this framework all the activities and legs are predefined states in a finite state machine and the transitions from one step to another can either be triggered manually (which is the *blocking* lock from above), by time (*time-base lock*) or by an event (*event-based lock*).

The main task of the AgentFSM framework is to encapsulate common programming steps when designing dynamic behaviour in MATSim. This means that one usually just has to define which states the behaviour is built of and how the transition from one to another works. All of this functionality is provided with a simple programming interface.

In more detail, each state is either an `LegState` or `ActivityState`. For each state an *enter* callback exists, which the programmer can use to execute arbitrary code. It needs to return how this state is locked from the three options above or either issue a direct switch to another state.

As soon as the state is ended due to the above conditions, the *leave* callback of a state is called, which must return to which next state the simulation should switch.

The concrete implementation for the autonomous vehicles will be discussed in section 5.

4.4 Comparison

An implementation of autonomous vehicles in DVRP has been compared to the implementation of the AV model developed in section 5. Basically, a specific number n of autonomous vehicles are created and put into a queue. As soon as an agent wants to start a leg using an AV, the top element of the queue will drive to

that position, pick up the passenger, bring him to the final destination and drop him off. Then the AV will be added back to the end of the queue. This dispatching algorithm is quite inefficient in most of the cases, but sufficient to do investigations in terms of computational time for the two implementations, since the behaviour is equal and easily understandable.

First, simulations with $n = 2000, 4000, 8000$ have been done on the Sioux Falls scenario, which will also be described in detail in section 5. What can be seen in fig. 12 is the share of AV legs of the total number of trips and the associated computation time. For a large range of shares the implementation using AgentLock and AgentFSM (solid) is much faster than the corresponding DVRP implementation (dashed). In fact, for $n = 8000$ only at a (quite unrealistically big) share of 70% DVRP starts to be more efficient.

Important to notice is that the performance of DVRP stays roughly the same over the whole range of shares. This is due to the fact that all 8000 AVs are simulated in every single time-step, no matter if they are active or not. In the AgentLock implementation, however, agents are only simulated if they are really in use. At 70% though, when the reschedulings of used AVs are getting to frequent, the repeated queue operations get more expensive than the polling and DVRP gets more efficient.

As a result, one can say that the FSM implementation is usually more efficient than the DVRP version. For increasing fleet sizes, this is even more true, since the roughly constant computation time for DVRP will increase linearly with n , moving the crossing in fig. 12 further towards 100%. On the contrary, if only small fleet sizes are used, the range of leg shares with FSM in favor will get smaller and smaller, because reschedulings get to frequent compared to the number of AVs.

In terms of a multithreaded Mobsim, only tests with the new AgentLock implementation could be done, as shown in figure fig. 13. Obviously, though the improvement is small, the simulation with two threads performed best. This shows that it is actually an advantage to be able to use the multithreaded Mobsim. Similar results have been found for other scenarios, for instance the optimal number of threads for the Singapore scenario has been found to be four (Erath et al., 2012).

TODO For the graphics, explain better what is shown: Time for whole Mobsim; also explain how the shares are computed?

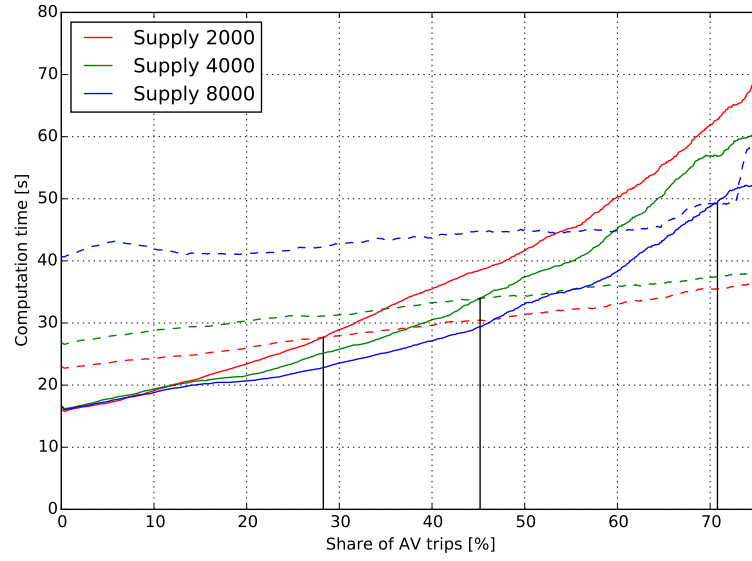


Figure 12: Comparison of Mobsim computational time between DVRP and Agent-Lock/AgentFSM implementation, dependent on share of AV legs. Scenario is Sioux Falls with a total number of legs of around 280.000. **TODO Measure again, at least for FSM-8000 for a better plot**

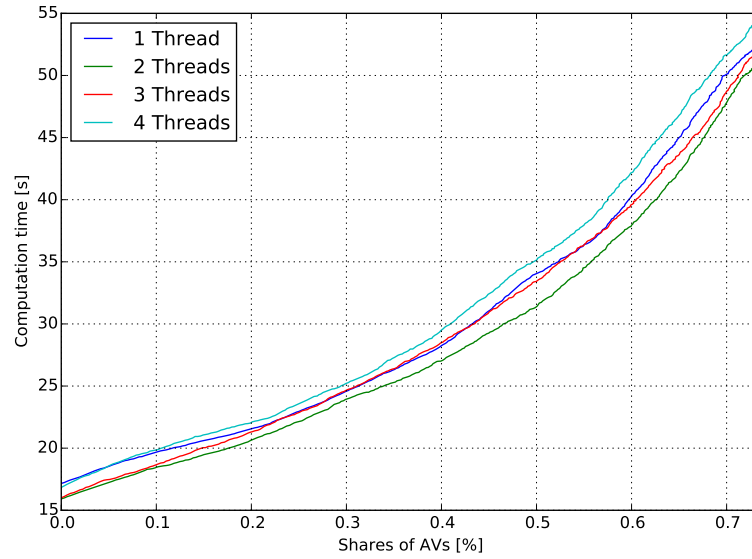


Figure 13: Comparison of different numbers of threads for the Mobsim with the AgentLock implementation

TODO add comments on how to design a dynamic agent framework in an adaptive way, using each strategy when it makes more sense

5 Autonomous Taxi Fleet Model

Simulating autonomous taxi services in MATSim requires the implementation, but even more so a concise planning and definition of how the exact behaviour of those agents should look like. This will be the first part of this section. Then, when it is known how those agents can be simulated the next question is how they should be dispatched for the requests of passengers and finally it has to be decided, where the autonomous taxis are placed on the network at the beginning of the simulation. These question will be answered in the second and third part of this section.

5.1 Agent Behaviour

The behaviour of an autonomous taxi is not a lot different from an ordinary one, except that there is no need to roam through the city to find new customers. Therefore, the AV behaviour presented here is mainly inspired by the model in [TODO cite](#), where ordinary taxi services have been simulated.

The behaviour of an autonomous taxi agent can be described in terms of a task life cycle. When the agent is not in a task, he is in idle mode, basically (for the basic model) meaning that he will just stay at the current position and wait for further instructions. The following steps in the life cycle are depicted in fig. 14.

1. **Pickup Drive** is the phase where the AV has got a task and is moving to the requested pick up location. If the AV is already at the right location, this point can be skipped, otherwise it represents a leg driving from the current position to the pickup location.
2. **Waiting** is the phase in which the AV has arrived at the pickup location, but the passenger is not there yet. This can only happen if passengers request cars in advance, prior to the time when they actually want to be picked up. If the passenger is already present at the time of the arrival at the pickup location, this state can be skipped.
3. **Pickup** is the state in which the passenger is picked up. It is modelled as a fixed time, e.g. one minute and started as soon as both the AV and the passengers are present at the pickup location.

4. **Dropoff Drive** represents the leg going from the pickup location to the dropoff point.
5. **Dropoff** is the point where the passenger leaves the vehicle. Again, this is modelled as a fixed time interaction.
6. **Idle** is the final (and initial) state of the AV life cycle. At this point the AV will just wait until it receives a new task to pick up another passenger.

The states described above fit very well to the distinction of Activities and Legs in MATSim as well as to the structure of the AgentFSM framework, which has been developed for this purpose. Resulting from this behavioural model, a couple of parameters end implementational questions arise, that can be configured accordingly:

The Idle behaviour for the basic model just means that the AV will stay at its last position. Future extensions could make use of parking facilities or do an intelligent repositioning to improve the overall performance of the service.

Pickup and Dropoff duration need to be specified. In accordance with [TODO cite](#), $t_{pickup} = 120s$ and $t_{dropoff} = 60s$ have been chosen. The time used for the pickup action will not be counted as waiting time (which, in turn, would be penalized through the marginal utility of waiting as described before).

5.2 Distribution Algorithm

At the beginning of a day simulation MATSim all the n available AVs must be placed somewhere in the network. Two simple distribution algorithms have been implemented for the purpose of testing in this thesis.

The first one is **Random Distribution**. Here n links are chosen randomly from all available network links. While this is an easy distribution strategy for testing, it create a quite unrealistic scenario. Obviously, in a real AV service, vehicles would be reloated over night, such that they can serve as many passengers as possible during the morning peek.

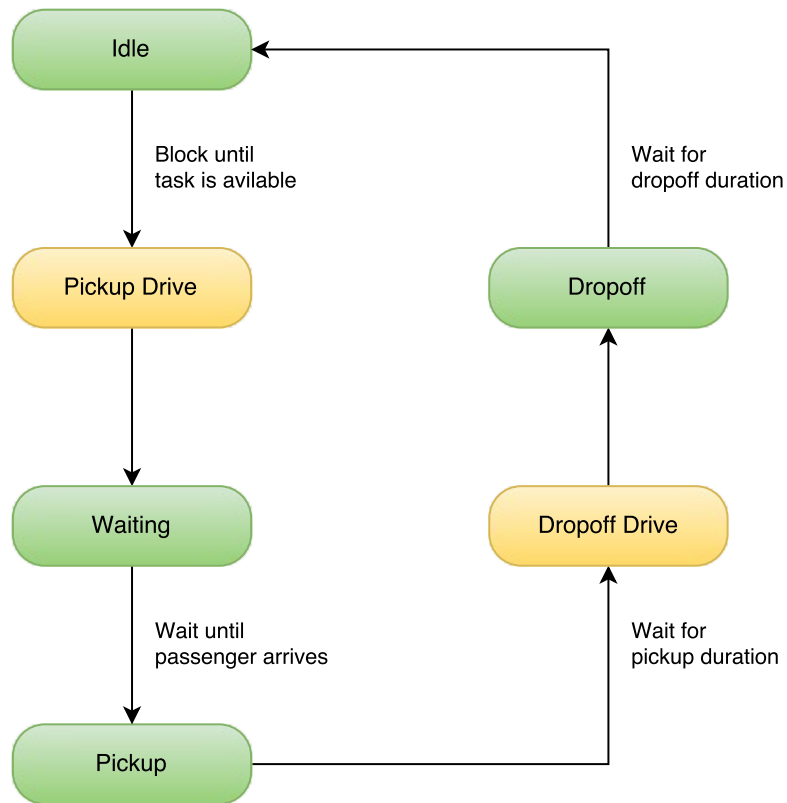


Figure 14: State chart of an AV agent. Activity states are displayed in green, while Leg states are yellow.

Therefore a more elaborate distribution strategy has been implemented, which should lead to more realistic results. Basically one can define a density over the network, such that every link has a certain probability to get an AV assigned. Then, in n steps, the n available AVs are added to a link dependent on the assignment probability.

This probability density can be based on many factors. The ones that are implemented for this thesis are:

Population density What is measured here is the population density in terms of how many people are having their “home” activity on a certain link.

AV commuter density Here for each link it is counted how many people will have chosen the AV mode for their first leg, i.e. the one that is starting from home.

While the prior one is static, the latter one is dynamic in the sense that for every iteration in the evolutionary learning, the density will change. So while the population-density based distribution is a fixed constraint, the latter one captures the factor of availability. For instance, if there are many agents using AVs in a certain area, the availability is very high, and thus more people might be inclined to use it. On the other hand, if availability is low in an area, it might lead to longer waiting times and people are less likely to use AVs.

While it might be interesting to observe different patterns of availability, for the first testing purposes the population density is better suited, since a detailed investigation would need to be done if any results from the AV leg density come from the mode choice of the agents or of feedback behaviour within the algorithm itself.

5.3 Dispatcher Algorithm

The dynamic dispatching of taxi vehicles is quite a complex scheduling problem, which is quite hard to solve or needs numerous assumptions to be feasible. In general, the problem will be a NP hard and heuristical solution strategies need to be applied if fast solutions are needed. An overview, as well as a proposed

heuristic algorithm can be found in Maciejewski and Bischoff (2015); Bischoff and Maciejewski (2016).

The algorithm can be described in two different states:

Oversupply occurs when there are more available autonomous vehicles than requests. This means that each request can be assigned without delay. In that case, as soon as a request arrives at the dispatcher, the closest vehicle to this request is searched and assigned to serve the customer.

Undersupply is the case when all autonomous vehicles are occupied. In that case requests will stack up, which cannot be handled immediately. In this case the algorithm works the other way round: As soon as an autonomous vehicle gets available, it is dispatched to the closest request.

According to the beforementioned papers this strategy gives a near-optimal solution, although providing fast computational times.

The implementation for this thesis is based on a spatial relaxation of the traffic network. This means that a grid with a specific resolution in x and y is fitted over the links. One of these grids saves the locations of all the available AVs, while another grid saves the locations of all open requests. Because the grids have a fixed structure, finding the closest AV or request is quite simple, since each position in x and y belongs to one specific cell of the grid. If no option is found in a certain cell, the search continues with all cells in its Moore neighborhood (all 8 surrounding cells). If this still gives no result, the radius is increased and so forth. When specifying “find at least K hits” as a stop criterion for a search this resembles an approximate K -nearest-neighbor search based on a L_1 norm due to the grid character. The procedure is depicted in fig. 15.

This search algorithm imposes new parameters to the implementation, which basically are the cell counts in horizontal and vertical direction. Depending on the topology of the network, different parameters might be more efficient. If the grid is chosen to be too dense, many iterations are needed in the algorithm, while a too sparse one in the extreme case can lead to finding most of the items in only single cell.

In fact, for some topologies it might probably be more efficient to use different data structures like a binary tree or quadtree to improve the search procedure. Also

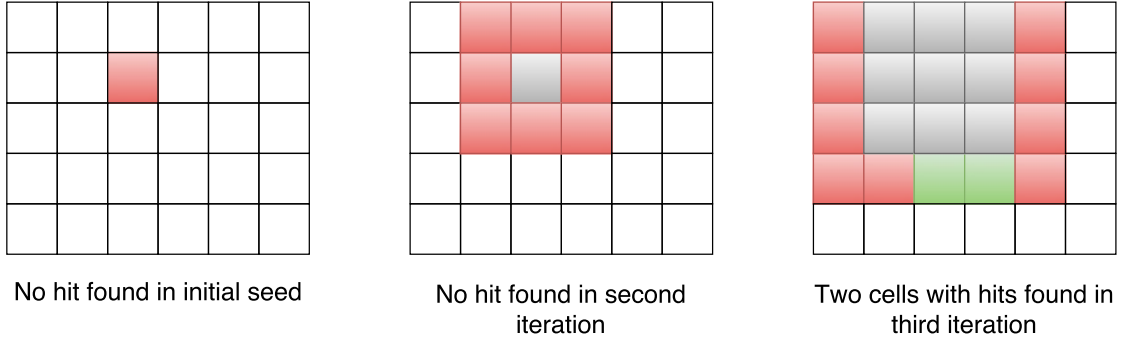


Figure 15: Schematic grid search algorithm for the dispatcher

more elaborate network search algorithms could be used, which make direct use of the topology. **TODO cite example maybe**

TODO Explain how this has been parallelized! Show speed improvement!

For the Sioux Falls scenario it has been tested which impact the choice of the grid size has on the results. In fig. 16 one can see that very high resolution grids ($n = 200$) lead to a great increase in computational time, due to the necessary “expansion” of unoccupied cells, as described above. On the contrary, very low grid sizes lead to very poor results in terms of the overall average travel time of the agents, because just selecting a random agent from one of a few cells is basically just random assignment. A good value for the Sioux Falls network has been found to be $n = 20$, which is computed fastest over the whole range of shares and furthermore does a good job in decreasing the overall travel time.

Further improving the dispatching process, the routing has been parallelized. When the dispatcher is called one per iteration, all the assignments between autonomous taxi agents and passengers are cached to be processed while the network simulation of the next iteration is running. Only then, so after one iteration, the dispatcher waits for all running routing jobs to finish and notifies the agents. This way all the expensive routing through the network can be done in parallel to the Netsim. Figure 17 shows the impact of adding this feature: While only applying one parallel router there is already a huge increase in computational performance compared to the serial processing of the routing tasks. As soon as more routers work concurrently, this performance is even improved. However, as usual there is the point where managing the parallelization adds more overhead to the simula-

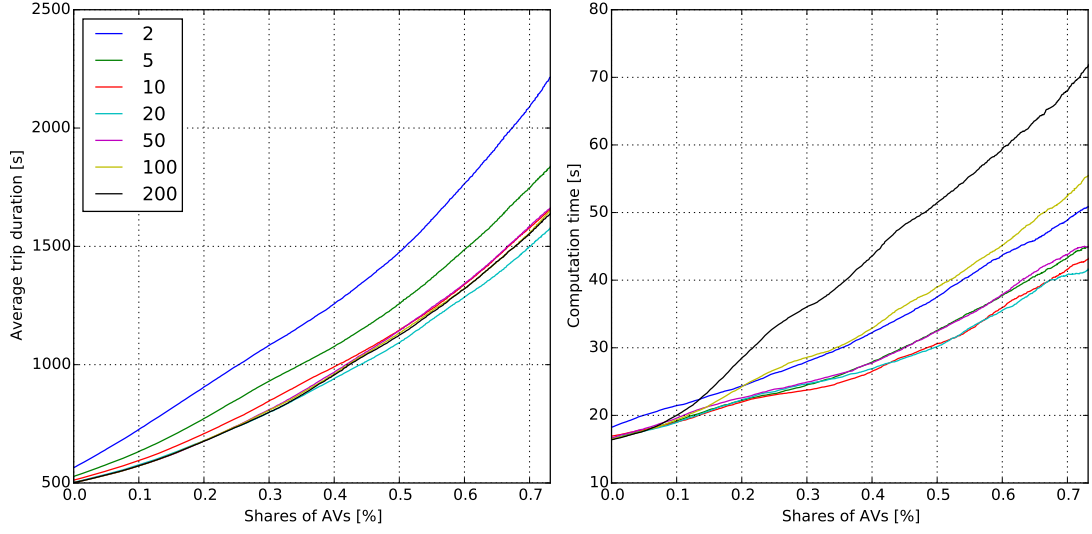


Figure 16: Performance of different grid sizes in the dispatching algorithm for Sioux Falls

tion. For the given scenario a number of routers of 2 seems to be a reasonable choice.

The parallelization of the dispatcher could be pushed even further. Next to the routing the actual assignment is the other expensive component in the algorithm. However, it would probably be hard to parallelize, because concurrent workers would need to access the same grid structures. The overhead of managing which worker has access is likely to very fast add more overhead than improvement to the simulation. One could, however, put the whole assignment process as a serial procedure in parallel to the Netsim, as done with the routers. This could be a promising approach of pushing the performance of the simulation even further.

5.4 Routing Algorithm

The easiest most simple option for routing autonomous vehicles in the model would be to solve a Dijkstra routing problem through the street network, while minimizing the expected travel time based on the freespeed values of the links. This strategy works well for small shares of AVs, because they have not a big impact on the overall traffic situation. However, when reaching high shares of AVs one (in

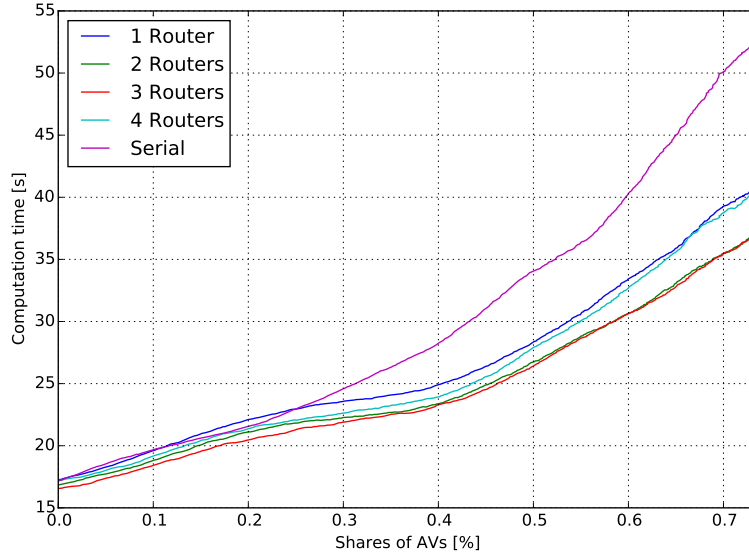


Figure 17: **TODO** todo

simulation as in reality) faces the problem that the routing cannot be done on the fastest route for most of the people, as this generates too much congestion. By finding the shortest path in terms of freespeed, one artificially creates bottlenecks, because all AVs are routed through the same arterials. This is already an interesting result that can be moved directly to reality: As soon as an AV operator gains such a high share that he directly impacts the traffic situation, he must also make sure to relax congestion in the network, otherwise the service is creating too much of a delay.

In the simulation this got apparent when, for certain shares, huge numbers of agents could not finish their plans, because all arterials were cluttered by queueing autonomous taxis. While finding an “intelligent” congestion redistribution strategy is a whole different topic **TODO** There are probably interesting publications, have a look for that, for the purpose of simulating AVs in this thesis a rather static approach is taken. The main idea is to add stochasticity to the Dijkstra process, thus creating slightly perturbed routes. What needs to be answered for using this approach is, which magnitude those perturbations should have. In order to solve this problem, the Sioux-16 baseline scenario has been examined. The 30h day has been divided into $N = 720$ bins ($2min$ each) and for

each find the relative decrease in speed for all link passages starting in each bin has been computed:

$$r_{i,j} = \sum_{j=1}^{n_i} \frac{v_{i,j,freespeed} - v_{i,j,simulated}}{v_{i,j,freespeed}} \quad (6)$$

Here n_i is the number of link passages (all agents and all links) that occurred in bin number i and $r_{i,j}$ is the relative decrease of speed in each bin for each passage.

As can be seen in fig. 18, the distribution of decreases in travel speeds of the network links can approximated using a Gamma distribution. The outliers, which can be seen on the right, are those cases where there is a lot congestion in peak hours. Because those are exactly the cases that one wants to avoid here, they are omitted in the following steps. The assumption of a Gamma-distribution is wholly motivated by the shape of the histogram, performing an educated derivation of the distribution shape would be an interesting investigation, which is out of the scope of this thesis though.

A Gamma distribution is defined by a shape parameter k and a scale parameter θ . For all bins in the baseline scenario, the respective parameters have been obtained using the MLE estimator for θ and a Newton approximation for k as described in **TODO add citation**. Figure 19 shows the parameter values for each bin on top, after they have been smoothed using a moving average filter of length 20. Also, for the times before roughly 5am and after 10pm, average parameter values over the off-peak hours in the middle of the day have been inserted due to a lack of sufficient data for fitting the speed decreases in these outer areas.

Also shown in fig. 19 (on the bottom) is the mean of the speed decrease at each time of the day, framed by the 10% and 90% quantiles, now instead of simulation results based on the statistical model. It can be seen that due to the Gamma model, the range of probable decreases is high in peak hours, up to 70%, while the mean still stays relatively constant over the whole day.

The final travel speed for the router can now be described as a random variable:

$$V_{i,j,routing} = v_{i,j,freespeed} \cdot (1 + R_i) \quad (7)$$

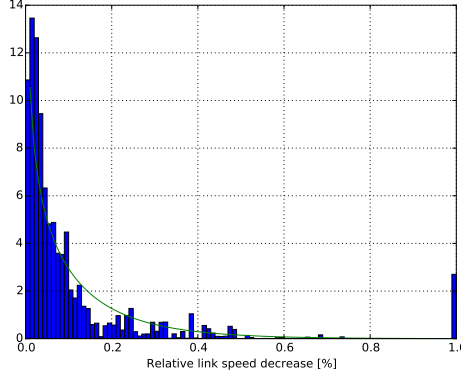


Figure 18: **TODO** todo

with $R_i \sim \Gamma(k_i, \theta_i)$ being Gamma-distributed for each bin.

The overall effect of this model is then as follows: There is a certain increase in travel time expected for each link, which depends on its freespeed and the time of the day. However, especially in peak hours, when the bottlenecks would be a critical problem, more variation is added to the expected increases in travel time and thus a better variation in the routing is reached. In each case, the expected increases are founded on the actual network characteristics of the Sioux-16 network.

What has to be kept in mind is, that this effectively puts a boundary on the possible number of AVs in the simulation. While the presented approach helps to avoid too much congestion for a wide range of AV shares, it doesn't perform an actual intelligent redistribution of congestion in the network. So because of too much congestion there will be a limit of AVs that can be used, since waiting times and travel times will get to expensive. This equilibrium generally should be lower than the actual "network congestion capacity" for the theoretical case of globally optimally routed AVs.

In the same sense it has to be acknowledged that no investigation has been done to find out how close the proposed model is operating to a theoretical optimum, so the following results in this thesis have to be understood under the assumption of this stochastic routing approach and might not represent the best possible solution.

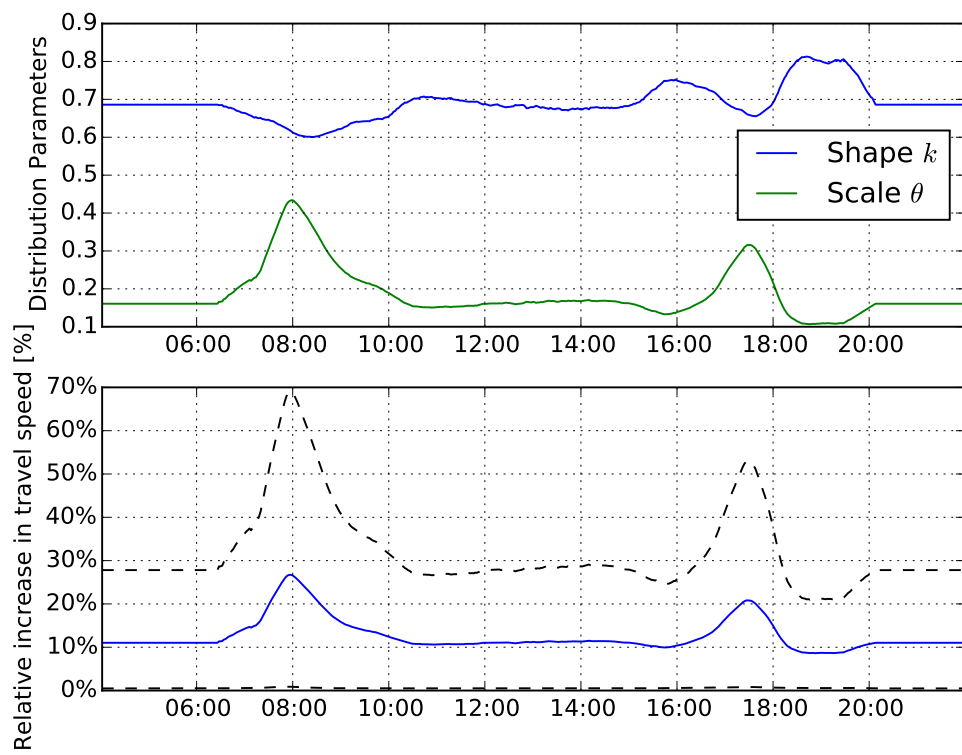


Figure 19: **TODO** todo

5.5 Sensitivity Analysis

three dominating factors: av supply, utility, network capacity

TODO Ongoing. The following are just notes.

Idea is to find the general properties how the demand depends on the parameters. The idea is that there should be two limiting factors: The utility (depending on the cost of the AV, the equilibrium will find a certain value) and the supply (if utility is such good that the AVs go into saturation, the supply level should dominate the equilibrium).

Some questions:

+ What are the utility values at which the system goes into saturation? +
How does the supply effect the share of AVs?

For the utility the effects should be quite clear. In some way, giving better utility to AVs should increase the AV share until it goes into saturation.

For the supply the situation is a bit different. If there are not enough AVs it will be quite unattractive to use AVs, because one has to wait really long. So it is likely that there is a threshold, which defines the minimum supply in the system.

Then again there should be an interplay between utility and supply, because if one has saturation at a certain utility and then increases the supply, again going into saturation there are less and less people who are *not* using AVs, so the increase should have a parabolic shape, while increasing the utility when the system is not in saturation should show a logistic growth.

In essence, what I'm trying to find out if there is a parametric bifurcation, that let's changes the equilibrium dynamics substantially...

The purpose of all the sensitivity analysis is to get a bit more insight for the following operator model, because there the variables will be the cost per km for the operator and the price for the customer, as well as a price per car which depends on the supply.

6 Operator Model

7 Outlook

- AV need to recharge! (Chen, 2015) (minimum idle time?)
- Try car sharing!
- Last-mile: Use AVs instead of transit_walk
- Adaptive Initial Distribution: start legs, end legs
- Repositioning when idle
- Prescheduled trips (5min before, or longer)
- Parking (where do AVs park?)
- Heterogeneity (which groups use AVs and why?)
- Adaptive pricing strategies (Chen, 2016)
- Interesting experiments: Creating a congestion zone within the highways for all / non-avs
- Where are customers coming from (spatially)?
- real-world scenario contrary to Sioux

8 References

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