

Finite-Time Lyapunov exponents

Definition

Local: $\sigma = \frac{1}{|T|} \ln \frac{\Delta}{\delta}$

Global: $\sigma(\mathbf{x}) = \frac{1}{|T|} \ln \|\nabla \varphi(\mathbf{x})\|_2$

whereas $\|A\|_2 = \sqrt{\lambda_{\max}(A^T A)}$ is the spectral norm of matrix A

- measure for separation abilities of LTV (time-variant) systems concerning massless tracer particles
- Lagrangian view in vector fields: placing two close-by particles into and moving with the flow

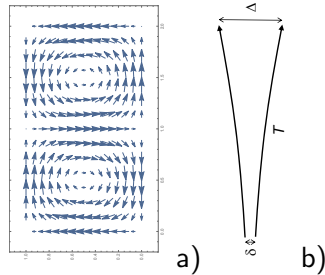


Fig.: a) Vector field, b) diverging pathlines

Finite-Time Lyapunov exponents

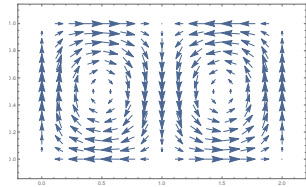
Definition

Local: $\sigma = \frac{1}{|T|} \ln \frac{\Delta}{\delta}$

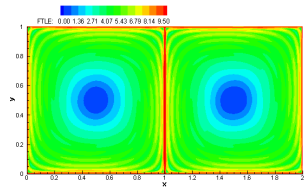
Global: $\sigma(\mathbf{x}) = \frac{1}{|T|} \ln \|\nabla \varphi(\mathbf{x})\|_2$

whereas $\|A\|_2 = \sqrt{\lambda_{\max}(A^T A)}$ is the spectral norm of matrix A

- measure for separation abilities of LTV (time-variant) systems concerning massless tracer particles
- Lagrangian view in vector fields: placing two close-by particles into and moving with the flow



a)



b)

Fig.: a) Vector field, b) FTLE field