Mustererkennung WiSe 12/13 Übung 8

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1 Aufgabe 1: Online vs. Batch

1.1 Code

1.1.1 a1.m

Durchführung der Algorithmen und abspeichern der Resultate.

```
penTrainingData = load("-ascii", "pendigits-training.txt");
ionTrainingData = load("-ascii", "ionosphere.data");
3
   penFeaturesTraining = penTrainingData(:,1:end - 1);
   penLabelsTraining = penTrainingData(:, end);
   ionFeaturesTraining = ionTrainingData(:,1:end - 1);
   ionLabelsTraining = ionTrainingData(:, end);
10
11
   [penTrainingPCA, penMove, penCov, penU] = normalize(penFeaturesTraining);
12
   [ionTrainingPCA, ionMove, ionCov, ionU] = normalize(ionFeaturesTraining);
13
14
   % die labelmatrix zum Trainieren so aufbauen, dass an der entsprechenden ...
        Stelle eine 1 steht
   penLabels = [];
15
   for label = penLabelsTraining '
16
17
        row = zeros(1,10);
18
        row(label + 1) = 1;
19
        penLabels = [penLabels; row];
20
21
   penLabelsTraining = penLabels;
22
23
24 % die unwichtigsten Hauptkomponenten wegwerfen
25
   penTrainingPCAn = penTrainingPCA(:, 1:14);
26
27
   % die unwichtigsten Hauptkomponenten wegwerfen
   ionTrainingPCAn = ionTrainingPCA %(:, 1:14);
29
30 % arguments for online()/batch(): input, outputs, #hidden, maxError, ...
       gamma, subsetSize
    [ionDigitsWeightsOnline, ionDigitsErrorsOnline] = ...
       online (ionTrainingPCAn, ionLabelsTraining, 35, 0.5, 0.05, 100)
32
   save ionOnline.mat ionDigitsWeightsOnline ionDigitsErrorsOnline
33
34
   [ionDigitsWeightsBatch, ionDigitsErrorsBatch] = batch(ionTrainingPCAn, ...
       ionLabelsTraining, 35, 0.5, 0.05, 100)
35
   {\bf save} \ \ {\bf ionBatch.mat} \ \ {\bf ionDigitsWeightsBatch} \ \ {\bf ionDigitsErrorsBatch}
   [\, penDigitsWeightsOnline \, , \ penDigitsErrorsOnline \, ] \, = \, \dots
       online (penTrainingPCAn, penLabelsTraining, 35, 0.8, 0.05, 100)
38
   save penOnline.mat penDigitsWeightsOnline penDigitsErrorsOnline
39
```

```
40 [penDigitsWeightsBatch, penDigitsErrorsBatch] = batch(penTrainingPCAn, ... penLabelsTraining, 35, 0.8, 0.05, 100)
41 save penBatch.mat penDigitsWeightsBatch penDigitsErrorsBatch
```

1.1.2 aldisp.m

Plotten der Resultate.

```
2 load penOnline.mat
3 load penBatch.mat
5 load ionOnline.mat
6 load ionBatch.mat
8 hold on
9 figure
10
11
   subplot(2, 2, 1)
   semilogy(penDigitsErrorsOnline);
12
   grid on
13
14
   title ("pendigits errors online");
15
16
   subplot (2, 2, 2)
17
   semilogy(penDigitsErrorsBatch);
18
19
   grid on
   title("pendigits errors batch");
20
21
22
23 \quad \mathbf{subplot}(2, 2, 3)
24 semilogy (ionDigitsErrorsOnline);
25 grid on
26 title ("ionosphere errors online");
27
28
29 subplot (2, 2, 4)
30 semilogy(ionDigitsErrorsBatch);
31 grid on
32 title ("ionosphere errors batch");
33
34 hold off
35
36 print("a1.png");
37
38 pause
```

1.2 Plots

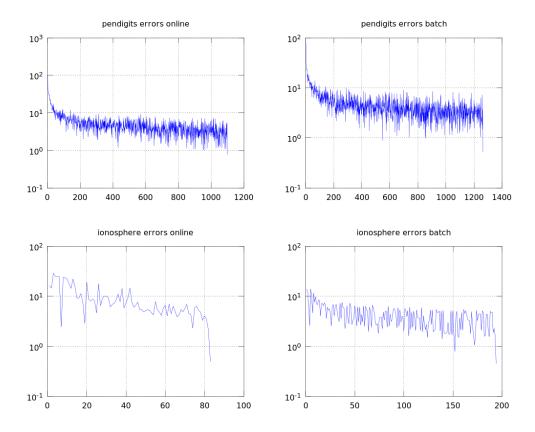


Figure 1: Iterationen vs. Fehler

1.3 Weiterer Code

1.3.1 online.m

```
function [weights, errors] = online(inputData, outputs, hiddenCnt, ...
       maxError, gamma, subsetSize)
2
       inputWidth = size(inputData, 2)
       outputWidth = size(outputs, 2)
3
4
       W1 = rand(inputWidth + 1, hiddenCnt) .- 0.5;
5
       W2 = rand(hiddenCnt + 1, outputWidth) .- 0.5;
6
7
        errors = [];
8
9
        error = inf
10
        while (error > maxError)
11
            error = 0;
12
            correction1 = zeros(size(W1));
13
            correction2 = zeros(size(W2));
14
15
           % generate a subset of inputs to fasten up the computation
16
            r = ceil((size(inputData, 1) - subsetSize) * rand());
17
            subsetInputs = inputData(r:(r + subsetSize),:);
18
            subsetOutputs = outputs(r:(r + subsetSize) ,:);
19
20
            subset = [subsetInputs, subsetOutputs];
21
22
            for input = subset '
23
                \% seperate the input from expected output
                output = input(end - (outputWidth - 1): end);
24
25
                input = augmentWithOnes(input(1:end - outputWidth)')';
26
27
                % forward propagation
28
                o1 = sigmoid(input ' * W1);
29
                o2 = sigmoid(augmentWithOnes(o1) * W2)';
30
31
                err = (o2 .- output);
32
                error += sum(0.5 .* err .^2);
33
34
                D1 = diag((o1 .* (1 .- o1)));
35
                D2 = diag((o2 .* (1 .- o2)));
36
37
                % the small W2 matrix
38
                W2s = W2(2:end,:);
39
40
                delta2 = D2 * err;
41
                delta1 = D1 * W2s * delta2;
42
43
                correction1 -= (gamma * delta1 * input') ';
44
                correction2 -= (gamma * delta2 * augmentWithOnes(o1)) ';
45
            end
46
47
           W1 += correction1;
48
           W2 += correction 2;
49
50
            error
51
            errors = [errors, error];
52
       end
53
54
        weights = \{W1, W2\};
55 end
```

1.3.2 batch.m

```
function [weights, errors] = batch(inputData, outputs, hiddenCnt, ...
       maxError, gamma, subsetSize)
       inputWidth = size(inputData, 2)
3
       outputWidth = size(outputs, 2)
4
       W1 = rand(inputWidth + 1, hiddenCnt) .- 0.5;
5
       W2 = rand(hiddenCnt + 1, outputWidth) .- 0.5;
6
7
        errors = [];
8
9
        error = inf
10
        while (error > maxError)
11
            error = 0;
12
13
           % generate a subset of inputs to fasten up the computation
            r = ceil((size(inputData, 1) - subsetSize) * rand());
14
15
            subsetInputs = inputData(r:(r + subsetSize),:);
16
            subsetOutputs = outputs(r:(r + subsetSize),:);
17
18
            subset = [subsetInputs, subsetOutputs];
19
20
            for input = subset '
21
                \% seperate the input from expected output
22
                output = input(end - (outputWidth - 1): end);
23
                input = augmentWithOnes(input(1:end - outputWidth)')';
24
25
                % forward propagation
26
                o1 = sigmoid(input ' * W1);
27
                o2 = sigmoid(augmentWithOnes(o1) * W2);
28
29
                err = (o2 .- output);
30
                error += sum(0.5 \cdot * err \cdot ^2);
31
32
                D1 = diag((o1 .* (1 .- o1)));
33
                D2 = diag((o2 .* (1 .- o2)));
34
35
                \% the small W2 matrix
36
                W2s = W2(2:end,:);
37
38
                delta2 = D2 * err;
39
                delta1 = D1 * W2s * delta2;
40
41
                W1 -= (gamma * delta1 * input') ';
                W2 = (gamma * delta2 * augmentWithOnes(o1))';
42
43
44
            end
45
46
            error '
47
            errors = [errors, error];
48
49
       end
50
51
        weights = \{W1, W2\};
52 end
```

1.3.3 normalize.m

```
function \ [\, ret \; , \; mean , \; cov \; , \; u \, ] \; = \; normalize (\, inputData )
        % Mittelwert der Daten berechnden
3
        mean = [mean(inputData(:,1:end-1)) 0];
        inputData = inputData - repmat(mean, size(inputData, 1), 1);
4
5
6
        % compute mu and covanriance matrix
7
        [mu, cov] = gauss(inputData);
8
9
        [u, s, v] = svd(cov);
10
11
        ret = inputData * u;
12 end
```

2 Aufgabe 2: RPROP

2.1 Code

2.1.1 a2.m

Durchführung der Algorithmen und abspeichern der Resultate.

```
\begin{array}{lll} penTrainingData &=& load\left("-ascii"\,,\;\;"pendigits-training.txt"\right);\\ ionTrainingData &=& load\left("-ascii"\,,\;\;"ionosphere.data"\right); \end{array}
3
   penFeaturesTraining \ = \ penTrainingData \, (:\,,1:end \ - \ 1) \, ;
   penLabelsTraining = penTrainingData(:, end);
   ionFeaturesTraining = ionTrainingData(:,1:end - 1);
   ionLabelsTraining = ionTrainingData(:, end);
10
   [penTrainingPCA, penMove, penCov, penU] = normalize(penFeaturesTraining);
11
   [ionTrainingPCA, ionMove, ionCov, ionU] = normalize(ionFeaturesTraining);
13
14 % die labelmatrix zum Trainieren so aufbauen, dass an der entsprechenden ...
        Stelle eine 1 steht
15
   penLabels = [];
16
   for label = penLabelsTraining '
17
        row = zeros(1,10);
18
        row(label + 1) = 1;
19
        penLabels = [penLabels; row];
20
   penLabelsTraining = penLabels;
22
23
24~\% die unwichtigsten Hauptkomponenten wegwerfen
   penTrainingPCAn = penTrainingPCA(:, 1:14);
26
   % die unwichtigsten Hauptkomponenten wegwerfen
28
   ionTrainingPCAn = ionTrainingPCA %(:, 1:14);
29
30
   [ionWeightsRPROP, ionErrorsRPROP] = rprop(ionTrainingPCAn, ...
31
        ionLabelsTraining, 35, 0.05, 0.0001, 0.5, 1.2, 0.5, 100)
    [penWeightsRPROP, penErrorsRPROP] = rprop(penTrainingPCAn, ...
        penLabelsTraining, 35, 0.505, 0.0001, 0.5, 1.2, 0.5, 100)
33 save rprop.mat ionErrorsRPROP penErrorsRPROP
```

2.1.2 a2disp.m

Plotten der Resultate.

```
2 \quad {\color{red} \textbf{load}} \quad {\color{blue} \textbf{rprop.mat}}
 3
 4 hold on
 5 figure
 6
 7 \quad \mathbf{subplot}(2,1,1)
8 semilogy(ionErrorsRPROP);
 9 grid on
10 title ("ionospere errors rprop");
11
12 subplot(2,1,2)
13 semilogy (penErrorsRPROP);
14 grid on
15 title ("pendigits errors rprop");
16
17
18 hold off
20 print("a2.png");
21
22 pause
```

2.2 Plots

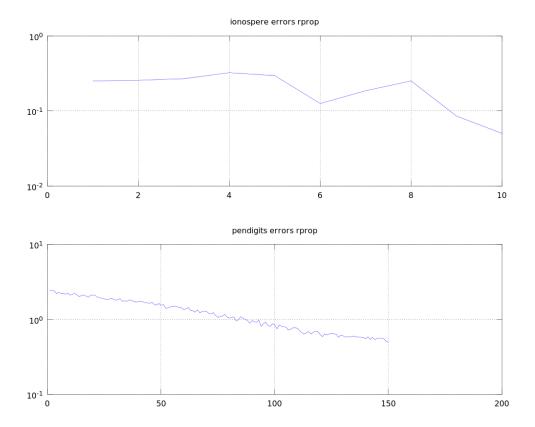


Figure 2: Iterationen vs. Fehler

2.3 Weiterer Code

2.3.1 rprop.m

```
function [weights, errors] = rprop(inputData, outputs, hiddenCnt, ...
       maxError, gammaMin, gammaMax, u, d, subsetSize)
2
       inputWidth = size(inputData, 2)
       outputWidth = size(outputs, 2)
3
 4
       W1 = (rand(inputWidth + 1, hiddenCnt) .- 0.5) .* 10;
       W2 = (rand(hiddenCnt + 1, outputWidth) .- 0.5) .* 10;
5
6
7
       gammaMax1 = repmat(gammaMax, size(W1));
8
       gammaMax2 = repmat(gammaMax, size(W2));
9
10
       gammaMin1 = repmat(gammaMin, size(W1));
       gammaMin2 = repmat(gammaMin, size(W2));
11
12
13
       gamma1 = gammaMin1;
14
       gamma2 = gammaMin2;
15
16
        errors = [];
17
18
        error = 999
19
        while (error > maxError)
20
            error = 0;
21
22
           \% generate a subset of inputs to fasten up the computation
23
            r = ceil((size(inputData, 1) - subsetSize) * rand());
24
            subsetInputs = inputData(r:(r + subsetSize),:);
25
            subsetOutputs = outputs(r:(r + subsetSize),:);
26
27
            subset = [subsetInputs, subsetOutputs];
28
29
            last\_correction11 = zeros(size(W1));
30
            last\_correction21 = zeros(size(W2));
31
32
            last\_correction12 = zeros(size(W1));
33
            last_correction 22 = zeros (size (W2));
34
35
            for input = subset '
36
                % seperate the input from expected output
37
                output = input (end - (outputWidth - 1): end);
38
                input = augmentWithOnes(input(1:end - outputWidth)')';
39
40
                % forward propagation
41
                o1 = sigmoid(input' * W1);
42
                o2 = sigmoid (augmentWithOnes(o1) * W2);
43
44
                err = (o2 .- output);
                error += (sum(0.5 .* err .^2) ./ subsetSize);
45
46
                D1 = diag((o1 .* (1 .- o1)));
47
48
                D2 = diag((o2 .* (1 .- o2)));
49
50
                W2s = W2(2:end,:);
51
52
                delta2 = D2 * err;
                delta1 = D1 * W2s * delta2;
53
54
55
                correction1 = (delta1 * input') ';
56
                correction2 = (delta2 * augmentWithOnes(o1))';
57
58
                            (min(gamma1 * u, gammaMax1) .* ...
                    ((last\_correction11 .* last\_correction12) < 0)) .+ ...
```

```
59
                               (max(gamma1 * d, gammaMin1) .* ...
                                    ((last\_correction11 .* last\_correction12) > ...
                                   0)) + \dots
60
                               (gamma1 .* ((last_correction11 .* ...
                                   last\_correction 12) == 0));
61
62
                 gamma2 =
                               (\min(\text{gamma2} * u, \text{gammaMax2}) .* ...
                      ((\,last\_correction21\ .*\ last\_correction22\,)\ <\ 0)\,)\ .+\ ...
63
                               (\max(\text{gamma2} * d, \text{gammaMin2}) .* ...
                                   ((last\_correction21 .* last\_correction22) > ...
                                   0)) .+ ...
64
                               (gamma2 .* ((last_correction21 .* ...
                                   last\_correction 22) == 0));
65
66
                 gamma1';
67
                 gamma2 \ ' \ ;
68
69
70
71
                 last_correction12 = last_correction11;
                 last_correction22 = last_correction21;
74
                  last_correction11 = correction1;
                 last_correction21 = correction2;
76
77
                 W1 -= gamma1 .* sign(correction1);
78
                 W2 = gamma2 .* sign(correction 2);
79
             end
80
81
             error '
82
             errors = [errors, error];
83
84
        end
85
86
        weights = \{W1, W2\};
87
    end
```