UFME7K-15-M Intelligent and Adaptive Systems

Introduction to Artificial Neural Networks

Charlie Sullivan

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Intelligent Adaptive Systems Lecture 3

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- Each processor has very low processing "power"
- ANNs can learn or be trained

Some real Neurons

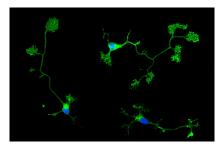


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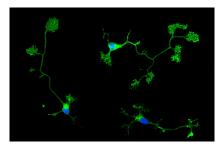


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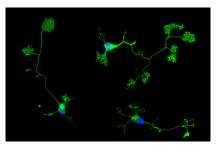


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 - The first step towards this was made by IBM research laboratories.

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 - an adaptive filter that eliminates echoes on phone lines.
 - while the system is as ancient as air traffic control systems, it is still in commercial use

The Perceptron

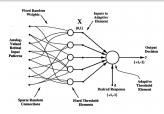


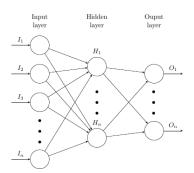
Figure 2: Perceptron



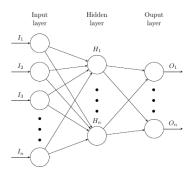
Figure 3: Early prototype

• Rosenblatt's Perceptron (1962)

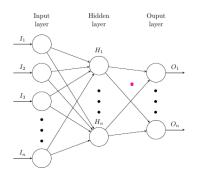
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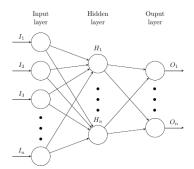
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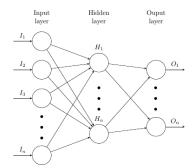
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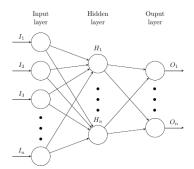
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- comprise a layer of input units,
- a layer of output units
- and one or more hidden layers which connect them together.



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 - ntstool for Dynamic Time Series problems

Using the nftool

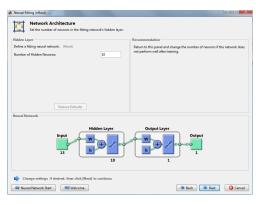


Figure 5: Network architecture

MLP Neuron

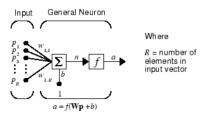


Figure 6: Single MLP Neuron

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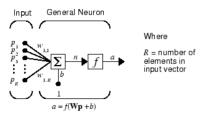


Figure 6: Single MLP Neuron

- Each input is multiplied by an appropriate weight $w_{i,j}$
- ullet The sum of the weighted inputs and the bias forms the input to the activation (threshold) function f

Activation Functions

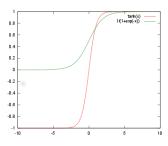


Figure 7: Typical Activation Functions

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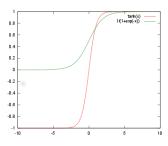


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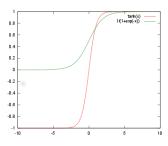


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- Multilayer networks often use the logistic sigmoid transfer function logsig(x) = 1/(1 + exp(-x))
- generates outputs between 0 and 1 as the neuron's input goes from negative to positive infinity
- Sigmoid output neurons are often used for pattern recognition problems, while linear output neurons are used for function fitting problems

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- A feedforward network with one hidden layer and enough neurons in the hidden layers, can fit any finite input-output mapping problem.

Function approximation

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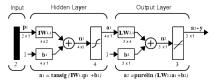


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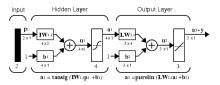


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Function approximation

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 - can approximate any function with a finite number of discontinuities arbitrarily well,
 - given sufficient neurons in the hidden layer

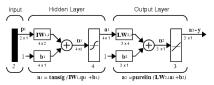


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 - It is also useful to plot the test set error during the training process
 - If the error on the test set reaches a minimum at a significantly different iteration number than the validation set error, this might indicate a poor division of the data set.

Using Data Subsets in nftool

A simple example of partitioning data

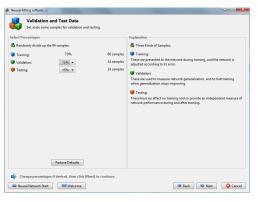


Figure 9: Simplefit Example

Training algorithms in the Matlab Toolbox

Function	Algorithm
trainlm	Levenberg-Marquardt (default)
trainbr	Bayesian Regularization
trainbfg	BFGS Quasi-Newton
trainrp	Resilient Backpropagation
trainscg	Scaled Conjugate Gradient
traincgb	Conjugate Gradient with Powell/Beale Restarts
traincgf	Fletcher-Powell Conjugate Gradient
traincgp	Polak-Ribiére Conjugate Gradient
trainoss	One Step Secant
traingdx	Variable Learning Rate Gradient Descent
traingdm	Gradient Descent with Momentum
traingd	Gradient Descent (backpropagation)

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- Bayesian Regularization is also a good option in many cases
- Although widely known, the back-propagation algorithm is usually slower than the others and is not often used these days.
- All of these methods are gradient-based and can be prone to converging on local minima.

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- differences between the resulting output signal and the predetermined desired output signal in each output unit represent an error that is back-propagated through the network in order to adjust the weights.
- The process continues until the the sum of root-mean-square errors from the desired output signals is less than a preset value.

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- This is known as generalisation and it can be quantified using the test set.
- The key to achieving this is in the design of the network, particularly in the number of hidden layer neurons
- A good practice is to start with a small number (the default in the feedforwardnet is 10) and try increasing to see if the fit improves or gets worse.

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- If the number of hidden neurons is increased too much, the error at the training points can go to zero but large errors can occur between the training points
- This is known as over-fitting and is one of the biggest problems in ANN design

Failure to converge

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- Sometimes, gradient-based learning algorithms converge on local minima or simply diverge if the function is complicated and there are too few training points
- There are alternative training methods such as using Evolutionary Algorithms but that is beyond the scope of this introduction

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 - trainFcn
 - Training function (default = 'trainlm')
- and returns a fitting neural network.

Example MATLAB code

 Here a fitting neural network is used to solve a simple regression problem.

```
[x,t] = simplefit_dataset;
% Create and display the network
net = fitnet(10);
% Train the network using the data in x and t
net = train(net,x,t);
view(net)
% Predict the response using the trained network
y = net(x);
% Measure the performance
perf = perform(net,y,t)
```

Plot of trained network

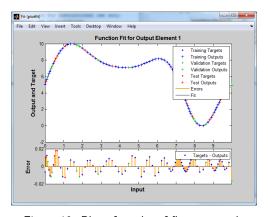


Figure 10: Plot of results of fitnet example

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 - good introductory textbook which covers all of the ANN types which we will look at