

Portfolio assignment 2: Vectors and matrices

Experimental methods II - 2018; Mikkel Wallentin, Adam Finnemann

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Matrix exercise

In this exercise we are going to look at response time as a function of days of sleep deprivation (see details below).

Deadline

February 15, 2018.

Reporting:

Use `r_markdown` in RStudio for your report. Submit report as a single pdf-file. Include commented code and figures all the way from data import.

Mark the beginning of each answer to a question with its relevant number/letter.

Students who worked with their study group in class may submit the same assignment report. Make sure to note all the names of people who contributed to the assignment in the beginning of the report.

Submit report to Blackboard.

Tasks

1. Linear regression

Participant 372 from the sleepstudy has the following data:

```
Reaction372<-c(269.41, 273.47, 297.60, 310.63, 287.17, 329.61, 334.48, 343.22, 369.14, 364.12)
Days372<-c(0,1,2,3,4,5,6,7,8,9)
```

- 1.a: Make a constant vector of the same length as the data, consisting of ones.
- 1.b: Report the inner product (aka dot product) of the days vector and the constant vector.
- 1.c: What does the dot product say about the possibility of finding an optimal linear regression?
- 1.d: Create a 10x2 matrix called X with the days vector and constant vector and days vector as columns and use the least squares method manually to find the optimal coefficients (i.e. slope and intercept) to reaction time.
- 1.e: Check result using `lm()`. Use the formula `lm(Reaction372~0+X)` - the zero removes the default constant.
- 1.f: Subtract the mean of Days372 from the Days372 vector. Replace the days vector with the new vector in X and redo the linear regression. Did the coefficients change? (we will return to why this happened in a later class, but if you are curious, you can check this website out: <https://www.theanalysisfactor.com/center-on-the-mean/>)
- 1.g: Make a scatter plot with the mean-centered days covariate against response time and add the best fitted line.

2. Images and matrices

Load the data using something like:

```
#library(jpeg)
##Load data
#matrix<-readJPEG('portfolio_assignment2_matrices_data.jpg', native = FALSE)
```

2.a: report how many rows and how many columns the matrix has. What are the maximum, minimum and mean pixel values?

2.b: Make an image of the loaded matrix. Be sure to rotate the image into the correct orientation. The functions needed are found in the lecture slides. Furthermore, grey scale the picture with `gray(1:100/100)` - this will color values near 0 black/dark and values near 1 white/light.

2.c: Draw an image with the same dimensions as that from 2.b. But this image should be completely black (hint: use zeros).

2.d: Draw a white hat on the image from 2.b (hint: use ones).

2.e: Make an image which has the same dimensions as 2.b., and which only contains the parts which were hidden behind the hat in 2.d. The rest should be black.

3. Brains and matrices

Load the brain data using something like:

```
#library(jpeg)
##Load data
#brain<-readJPEG('portfolio_assignment2_matrices_data2.jpg', native = FALSE)
```

3.a: Make an image of the brain.

3.b: We will attempt to find the interesting areas of this brain image, e.g. only areas with gray matter. To do this we will create two masks, one that filters all darker areas away, and one that filters the white matter away. The masks will work by having zeros at the areas we want to filter away, and ones at the interesting areas. Thus, the mask will have the intended effect if we do element-wise multiplication with the brain matrix. Start by making an image which is white (have ones) where the pixel values of the brain image are larger than the mean value of the whole image. Let the image be black (have zeros) everywhere else. Call this matrix `mask1`.

3.c: Make an image which is white where the pixel values of the brain image are smaller than 2.5 times the mean value of the whole image. Call this matrix `mask2`.

3.d: Convert `mask1` and `mask2` into one mask with ones where the two masks overlap and zeros everywhere else. What type of mathematical procedure can be used to produce this?

3.e: Use the combined mask on the brain image to give you an image with only the image values where the mask has ones, and zeros everywhere else. Did we successfully limit our image to only contain gray matter?

3.f: Count the number of pixels in the combined mask.

4. Two equations with two unknowns

Two linear equations with two unknowns can be solved using matrix inversion. For example, see here: <https://www.mathsisfun.com/algebra/matrix-inverse.html>

4.a: In the Friday bar, men were three times as likely as women to buy beer. A total of 116 beers were sold. Women were twice as likely as men to buy wine. 92 glasses of wine were sold. How many men and women attended the Friday bar?