

## **Primary Examination**

## !! PRACTICE EXAM !!

## MATHS 7107 Data Taming

Course Coordinator: Anthony Mays

Writing time: 120 mins

Number of questions: 7 Written, 16 Multiple Choice

Total marks: ??

### Instructions for Candidates

- This examination is **closed book**.
- Examination materials must not be removed from the examination room.
- Answer all written questions in the answer book provided.
- Answer all multiple choice questions on the provided multiple choice sheet.

#### **Permitted Materials**

- Multiple Choice Question (MCQ) Sheet
- Paper translation dictionary
- Scientific calculator.
- One double-sided A4 page of handwritten or typed notes.

# DO NOT COMMENCE WRITING UNTIL INSTRUCTED TO DO SO. STOP WRITING IMMEDIATELY WHEN INSTRUCTED

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## **Written Questions**

1. A committee has been established to organise 200-year anniversary celebrations in each Australian capital city. A large statue has been built and needs to be moved to each city for the celebration. The following tibble contains some of the information that the committee has gathered

#	A tibble: $8 \times 5$				
	Name	population	urban_pop	`Capital city`	Year
	<chr></chr>	<db1></db1>	<db1></db1>	<fct></fct>	<db 7=""></db>
1	New South Wales	7 <u>759</u> 274	64.8	Sydney	<u>1</u> 788
2	Victoria	6 <u>179</u> 249	76.5	Melbourne	<u>1</u> 851
3	Queensland	4 <u>848</u> 877	48.7	Brisbane	<u>1</u> 860
4	Western Australia	2 <u>558</u> 951	79.0	Perth	<u>1</u> 829
5	South Australia	1 <u>713</u> 054	77.3	Adelaide	<u>1</u> 836
6	Tasmania	<u>517</u> 588	43.4	Hobart	<u>1</u> 826
7	Australian Capital Territory	<u>403</u> 468	100	Canberra	<u>1</u> 913
8	Northern Territory	<u>245</u> 740	59.4	Darwin	<u>1</u> 911

The variables in the table are:

- Name: the name of the state or territory
- population: the number of people residing in the state
- urban\_pop: the percentage of the state's population who lives in the state's capital city
- Capital city: the name of the state's capital city
- Year: the year the city became the state's capital city, which is used for planning where the statue needs to be.
- (a) For each of the variables in the dataset identify the type of variable, ie. is it quantitative continuous, quantitative discrete, categorical nominal or categorical ordinal. Make sure you write a short description justifying your choice.
- (b) For each variable state whether the corresponding column in the tibble is the correct data type. If it is incorrect, say what the correct data type should be.

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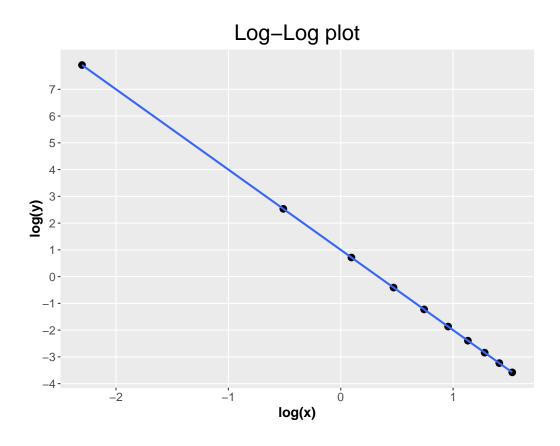


Figure 1: Log-Log plot of data for Question 2.

2. (a) Assume that a data set consists of continuous variables x and y, which are related by the formula

$$y = \alpha x^k$$
.

Using the logarithm laws, show that the Log-Log plot of this data will be a straight line.

- (b) Using the straight line in part (a), write down the:
  - i). gradient of the line,
  - ii). the value at which the line cuts the vertical axis.
- (c) Using the Log-Log plot in Figure 1 determine the explicit relationship between x and y. (Make sure you show your working.)

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Table 1: Dataset for Questions 3 and 4.

- 3. For this question, use the dataset in Table 1.
  - (a) Transform the dataset in Table 1 to  $x^*$  by applying Min-Max scaling. Calculate your answers to 2 decimal places. (Make sure you show your working.)
  - (b) What are the minimum and maximum values of the transformed dataset  $x^*$ ? Give exact values for your answers. (Make sure you show your working.)

- 4. For this question, use the dataset in Table 1.
  - (a) Find the mean  $\overline{x}$  and (sample) standard deviation  $\sigma_x$  of the dataset. Calculate your answers to 2 decimal places. (Make sure you show your working.)
  - (b) Standardise the dataset by calculating the z-scores  $x_j^*$  for each  $x_j$ . Calculate your answers to 2 decimal places. (Make sure you show your working.)
  - (c) What is the mean  $\overline{x^*}$  and standard deviation  $\sigma_{x^*}$  of the transformed data set. Give exact values for your answers. (Make sure you show your working.)

5. Show that when  $x \neq 0$  the Box-Cox transformation is continuous at  $\lambda = 0$ , by showing that

$$\lim_{\lambda \to 0} \frac{x^{\lambda} - 1}{\lambda} = \log(x) \qquad \text{(for } x \neq 0\text{)}.$$

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6. We are looking to measure the amount of pollen in the air. We have built 31 cubic boxes, each one with a pollen counter in it. The side lengths of each box is recorded in the list  $(s_1, \ldots, s_{31})$ , where the side lengths are measured in metres. We collect pollen counts from the air samples inside each box, and record the pollen counts in box j as  $p_j$ .

We expect to find a good linear fit with the model

$$p_j = \beta_0 + \beta_1 z_j + \epsilon_j, \qquad N(0, \sigma) \tag{1}$$

where  $z_j = s_i^3$ .

We use R to fit our linear model to the data and we obtain the following output:

```
> pollen_lm <- lm(p ~ z, pollen)
> summary(pollen_lm)
```

#### Call:

lm(formula = p ~ z, data = pollen)

#### Residuals:

```
Min 1Q Median 3Q Max -22.195 -6.719 -0.049 6.826 20.877
```

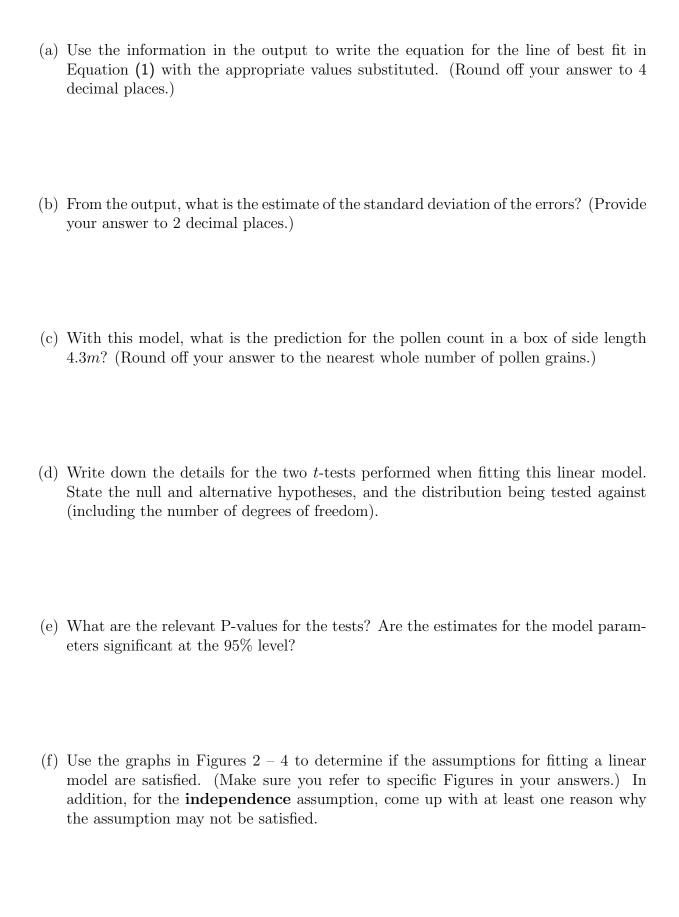
#### Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 6.23517 3.59069 1.736 0.0931 .
z 1.31177 0.05785 22.675 <2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 11.27 on ##### degrees of freedom Multiple R-squared: 0.9466, Adjusted R-squared: 0.9448 F-statistic: 514.1 on 1 and ##### DF, p-value: < 2.2e-16
```

• Note that we have replaced the number degrees of freedom with ####, and so you need to calculate this number.

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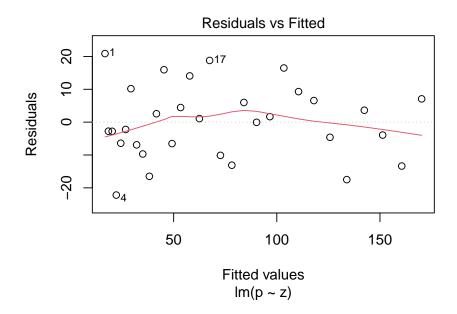


Figure 2: A residuals vs fitted graph for the linear model in Question 6.

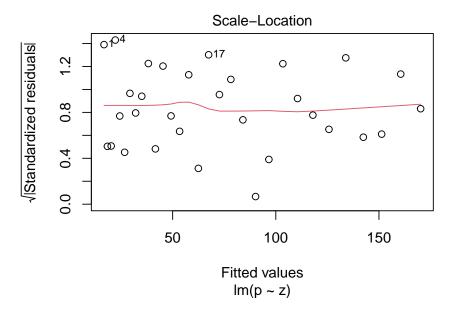


Figure 3: A scale-location graph for the linear model in Question 6.

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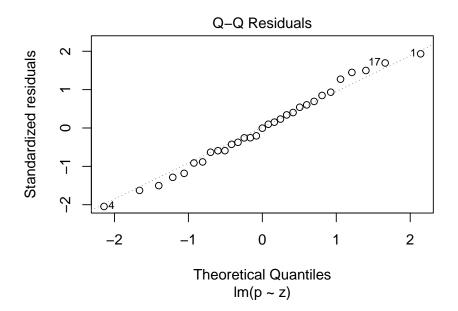


Figure 4: A Q-Q plot of residuals for the linear model in Question 6.

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7. A medical test for a certain disease has the following confusion matrix:

	No disease	Has disease
Test negative	100	20
Test positive	50	180

A true positive is where a patient has the disease and the test is positive.

- (a) Calculate the sensitivity of the test. Provide an exact answer or 3 significant figures of precision. (Make sure you show your working.)
- (b) Calculate the specificity of the test. Provide an exact answer or 3 significant figures of precision. (Make sure you show your working.)
- (c) Calculate the accuracy of the test. Provide an exact answer or 3 significant figures of precision. (Make sure you show your working.)
- (d) Based on your results from parts (a)–(c), would you estimate that the AUC (area under the curve) for the ROC curve is closest to:
  - $\bullet$  between 0.65 and 0.90
  - between 0.45 and 0.55
  - $\bullet$  between 0.1 and 0.35
  - between -0.35 and -0.1
  - between -0.9 and -0.65

Justify your reasoning.

(e) What does an AUC value close to 0 tell you about your prediction model? If this was the case, how could we improve the model?

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## **Multiple Choice Questions**

Use the multiple choice answer sheet to record your answers.

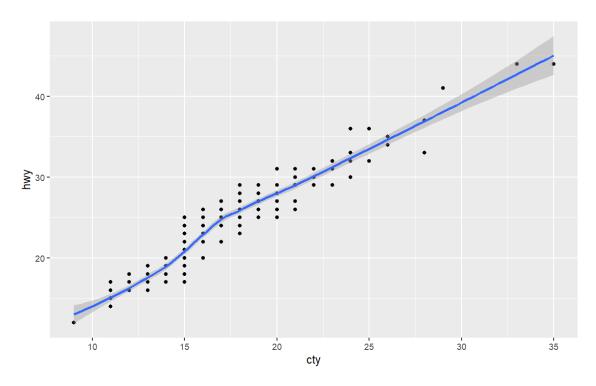


Figure 5: Plot of city fuel efficiency (cty) against highyway field efficiency (hwy) for Multiple Choice Questions 1 and 2.

- 1. From the data in Figure 5 what is the relationship between city and highway fuel efficiency?
  - (a) A strong positive relationship.
  - (b) A weak negative relationship.
  - (c) No relationship.
  - (d) Impossible to tell from this plot.
- 2. What R code could have generated the plot in Figure 5? (Select all the correct answers, and only the correct answers.)
  - (a) mpg %>% ggplot(aes(x=cty, y=hwy))+geom\_point()+geom\_smooth(method="lm")
  - (b) mpg %>% ggplot(aes(x=cty, y=hwy))+geom\_point()+geom\_smooth()
  - (c) ggplot(mpg, aes(x=cty, y=hwy))+geom\_smooth()
  - (d) ggplot(mpg, aes(x=cty, y=hwy))+geom\_point()+geom\_smooth()

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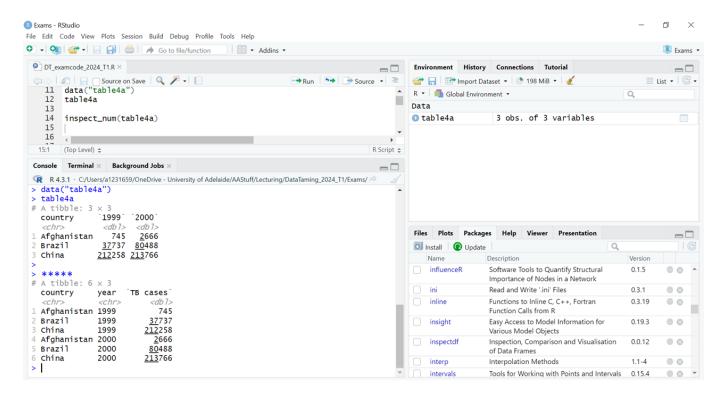


Figure 6: RStudio screenshot for Multiple Choice Questions 3-5.

- 3. Using the RStudio screenshot in Figure 6, what is the name of the Project?
  - (a) table4a
  - (b) Console
  - (c) DT\_examcode\_2024\_T1
  - (d) Exams
- 4. Look at the RStudio screenshot in Figure 6. If we name the tidy tibble table4a\_tidy, which command will convert it back into wide form?
  - (a) gather(table4a\_tidy, key = "year", value = "TB cases", '1999':'2000')
  - (b) inspect\_df(table4a\_tidy)
  - (c) wide\_form(table4a\_tidy, year, 'TB cases')
  - (d) spread(table4a\_tidy, key = year, value = 'TB cases')

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5. We would like to obtain summary statistics for the numerical variables in table4a. Based on the information in the RStudio screenshot in Figure 6, will the command inspect\_num(table4a) work for this purpose?

- (a) Yes, inspect\_num is the correct command.
- (b) No, inspect\_num does not calculate summary statistics.
- (c) No, we must first run the command library(inspectdf).
- (d) No, we must first run the two commands install.packages("inspectdf") and library(inspectdf).

- 6. Using the RStudio screenshot in Figure 6, what command will return a  $1 \times 1$  tibble containing just the value 745? (Select all the correct answers, and only the correct answers.)
  - (a) table4a %>% filter(country=="Afghanistan") %>% select("1999")
  - (b) filter(table4a, country=="Afghanistan")
  - (c) table4a %>% select("country"=="Afghanistan") %>% filter("1999")
  - (d) table4a[1,2]

- 7. If we run the command test\_string <- "abc (15) xyz", what is the command to extract just the number 15? (Select all the correct answers, and only the correct answers.)
  - (a) str\_match(test\_string, "abc  $\setminus ((\setminus d*)")[,2]$
  - (b) str match(test string, "abc \\((\\d)")[,2]
  - (c) str\_match(test\_string, "abc ( $\(\\d*)$ ")[,2]
  - (d) str match(test string, "abc  $\backslash ((.*) \backslash)$ ")[,2]

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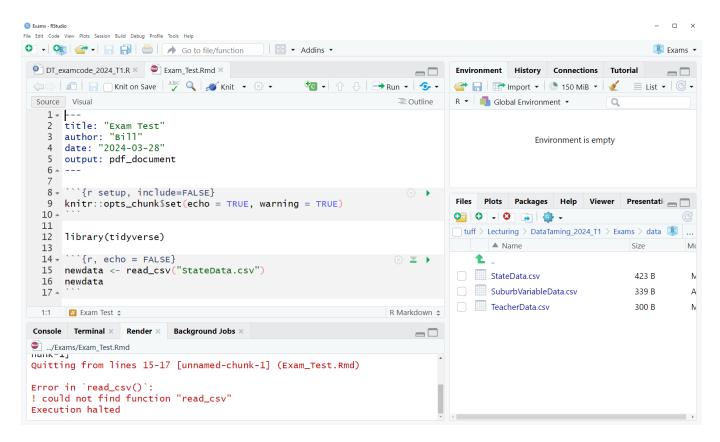


Figure 7: RStudio screenshot for Multiple Choice Questions 8-9.

- 8. We have hit an error when knitting the R Markdown file in Figure 7. We definitely have the tidyverse package installed, so what problems will prevent our file from knitting successfully?
  - (a) We have not specified the correct directory for the csv file and we need to click "Knit on Save".
  - (b) library(tidyverse) is not inside a code chunk, and we have not specified the correct directory for the csv file.
  - (c) We should have warning = FALSE and we need to click "Knit on Save".
  - (d) library(tidyverse) is not inside a code chunk and we should have warning = FALSE.

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9. Once we get the R Markdown file in Figure 7 to knit, we find that the output is being displayed in the PDF. However, the code newdata <- read\_csv("StateData.csv") runs successfully, but produces many warnings that we don't want to see. What changes could we make to prevent R Markdown from showing any warnings in the whole document?

- (a) Include the command print(!warnings) after line 16
- (b) Include the command print(read\_csv == FALSE) after line 9
- (c) Change warning = TRUE to warning = FALSE on line 9
- (d) Change echo = FALSE to echo = FALSE, warning = FALSE on line 14

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## See the attached page "mpg2 data set" for Questions 10 to 16.

For the remaining questions we are going to be working with the mpg2 data set, which is a simplified version of mpg.

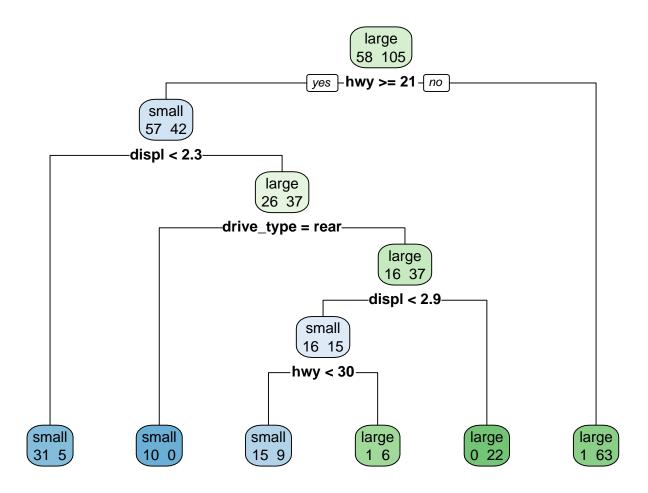


Figure 8: Decision tree diagram for Multiple Choice Questions 10–13.

- 10. In Figure 8 we have fit the model class ~ year + cyl + drive\_type + displ to a training subset of the mpg2 dataset for predicting the type of car, either small or large. What type of model have we fit?
  - (a) Logistic tree
  - (b) General linear model tree
  - (c) Regression tree
  - (d) Classification tree

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11. From the diagram in Figure 8, determine how decisions the model made.

	(a) 5
	(b) 6
	(c) 11
	(d) 21
12.	From the diagram in Figure 8, what proportion of the whole dataset was chosen for our training set?
	(a) $58\%$
	(b) 105%
	(c) 70%
	(d) 15%
13.	Using the model in Figure 8, what size do we predict for a car with an engine size of 3L, highway fuel efficiency of 23 miles per gallon, four wheel drive and built in 2008?
	(a) small
	(b) large
	(c) It can't be determined from this diagram
	(d) The model was inconclusive

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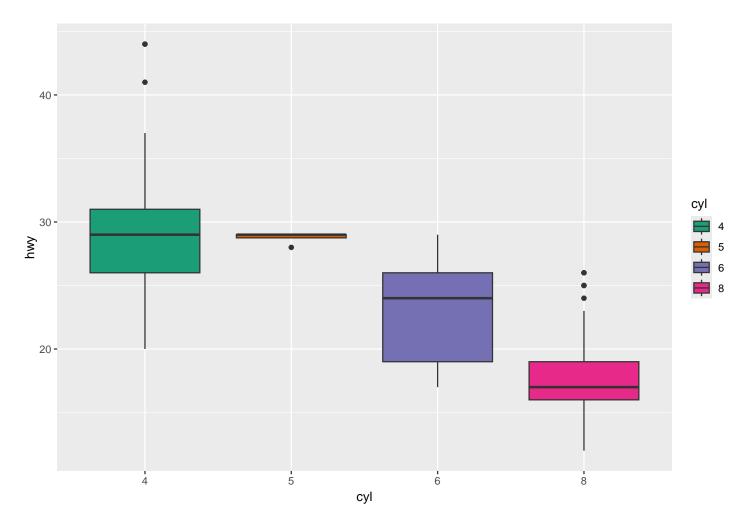


Figure 9: Boxplot of highway fuel efficiency hwy of a car against the number of cylinders in the car's engine cyl for Multiple Choice Questions 14–16.

- 14. According to the box plot in Figure 9, which number of cylinders has the smallest median highway fuel efficiency?
  - (a) 4
  - (b) 5
  - (c) 6
  - (d) 8

<b>n</b> .	_	•
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- 15. According to the box plot in Figure 9, which number of cylinders has the smallest interquartile range?
  - (a) 4
  - (b) 5
  - (c) 6
  - (d) 8

- 16. According to the box plot in Figure 9, which number of cylinders has the largest number of outliers?
  - (a) 4
  - (b) 5
  - (c) 6
  - (d) 8

#### > mpg2 # A tibble: 234 × 11 displ year cyl manufacturer model trans drive\_type cty hwy fl class <chr>> <chr> <dbl> <int> <ord> <chr> <fct> <dbl> <dbl> <chr> <fct> 1 audi a4 1.8 1999 4 auto(15) front 18 29 p small 2 audi a4 1.8 1999 4 manual(m5) front 21 29 p small 31 p 3 audi 2008 4 manual(m6) front 20 a4 small 2 2008 4 4 audi a4 auto(av) front 21 30 p small 5 audi a4 2.8 1999 6 auto(15) front 16 26 p small 6 audi 2.8 1999 6 a4 manual(m5) front 18 26 p small 7 audi a4 3.1 2008 6 auto(av) front 18 27 p small 1.8 1999 4 26 p small8 audi a4 quattro manual(m5) four 18 9 audi 1.8 1999 4 auto(15) four 16 a4 quattro 25 p small 10 audi a4 quattro 2 2008 4 manual(m6) four 20 28 p small # i 224 more rows > skim\_without\_charts(mpg2) -- Data Summary -----Values Name mpg2 Number of rows 234 Number of columns 11 Column type frequency: character 4 factor 3 numeric Group variables None -- Variable type: character ----skim\_variable n\_missing complete\_rate min max empty n\_unique whitespace 1 manufacturer 0 1 4 10 0 15 0 2 model 0 1 2 22 0 38 0 3 trans 0 10 0 10 0 4 fl 0 1 0 5 0

Variable type: factor									
skim_variable n_m	nissing	complete_rate	${\tt ordered}$	n_uni	ique top	counts	3		
1 cyl	0	1	TRUE		4 4:	81, 6:	79, 8:	70, 5:	4
2 drive_type	0	1	FALSE		3 fro	o: 106,	fou: 10	03, rea	: 25
3 class	0	1	FALSE		2 la:	r: 147,	sma: 8	7	
Variable type: numeric					_				
skim_variable n_m	nissing	complete_rate	mean	sd	p0	p25	p50	p75	p100
1 displ	0	1	3.47	1.29	1.6	2.4	3.3	4.6	7
2 year	0	1	2004.	4.51	1999	1999	2004.	2008	2008
3 cty	0	1	16.9	4.26	9	14	17	19	35
4 hwy	0	1	23.4	5.95	12	18	24	27	44