

Variational Methods for Discrete Surface Parameterization. Applications and Implementation.

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Chapter 1

Discrete Differential Geometry - Software Packages

1.1 Introduction

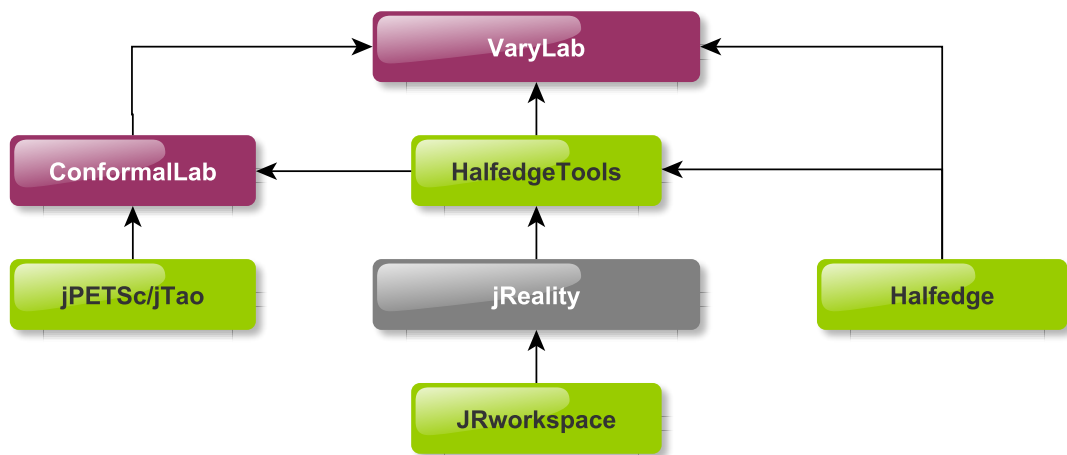


Figure 1.1: Software architecture and dependencies of the DDG Framework. JTEM library packages (green), mathematical software packages (red).

In the field of Discrete Differential Geometry (DDG) there is a special need for experiments conducted with the help of computer software. Especially if the methods of DDG are applied to problems in computer graphics, geometry processing, or architecture, algorithms have to be implemented and convincing examples have to be presented. Additionally a suitable visualization of the results has to be included in a state-of-the-art publication.

There is a growing knowledge of software development in the mathematical community. This is due to the curricula of universities which started to include programming courses for undergraduate students with a visualization emphasis, e.g., [4, 3]. It enables students to extend

their abilities of creating visualizations and mathematical software, where former generations of students solely used the visualization abilities of standard computer algebra packages like Mathematica or MatLab.

The audience of this chapter is two-fold. On the one hand it is students creating their visualizations of surfaces and develop algorithms. On the other hand it is researchers in the field of discrete differential geometry who need a stable data structure and programming infrastructure to get the job done.

This Chapter is the description and getting-started manual of a set of software packages (Berlin DDG Framework) written in the programming language `JAVA`. They are specifically designed for the creation of custom interactive software for experiments with algorithms and geometries treated within DDG. It is currently being used for teaching a mathematical visualization course at TU-Berlin [4] and for research projects within the geometry group.

Section 1.2 gives an overview of existing software packages that have a focus similar to the DDG Framework. Section 1.3 introduces the `JRWORKSPACE` library of the `JTEM` project [8]. It is the foundation of any application created with the DDG Framework. It is also the user interface basis of `JREALITY`, a mathematical visualization library that uses `JRWORKSPACE` as plug-in and user interface tool [7]. Section 1.4 introduces the `HALFEDGE` and `HALFEDGETOOLS` package. They implement half-edge data structure and various user interface tools and algorithms for interaction and editing. In Section 1.5 we describe the software `CONFORMALLAB`. This package implements the methods of the publications [1, 9, 11, 2]. Section 1.6 introduces `VARYLAB`, the software implementation of the methods described in the publications [5, 6, 11]. This package is also released to partners of the development group as `VARYLAB[GRIDSHELLS]`, `VARYLAB[ULTIMATE]`, or even online as `VARYLAB[SERVICE]`[10].

Figure 1.1 shows the dependencies of the packages. Every application depends on `JRWORKSPACE` which implements plug-in functionality. It is the basis of the `JREALITY` plug-in system. `HALFEDGETOOLS` is using `JREALITY` for visualization and is build on top of the `JTEM` project `HALFEDGE`. `CONFORMALLAB` and `VARYLAB` use `JPETSC/JTAO` to perform numerical optimization. Their algorithms are implemented as `JRWORKSPACE` plug-ins.

The development of the described software is joint work with Thilo Rörig (`HALFEDGETOOLS`, `VARYLAB`), the `JREALITY` members [7], Hannes Sommer (`JPETSC/JTAO`) [12], Ulrich Pinkall and Paul Peters (`JRWORKSPACE`), and Boris Springborn (`HALFEDGE`).

1.2 Related Work

JavaView, CGAL, ...

1.3 JRWORKSPACE - Java API for modular applications

`JRWORKSPACE` is part of the `JTEM` family of software projects [8]. It defines a simple API to create modular Java applications. This API consists of three basic classes (Listings 1.2, 1.3, and 1.4). The project contains a reference implementation that supports the creation of Java Swing applications using the `JRWORKSPACE` API. This implementation is used in all applications described in this work.

1.3.1 Plug-ins and the controller

In a JRWORKSPACE application a feature is implemented as plug-in and the corresponding Java class extends the abstract class `Plugin` (Listing 1.2). The idea is that a plug-in can be installed by the controller calling its `install` method or uninstalled via the `uninstall` method. You can think of it as a feature added to your program. In particular there is no more than one instance of a plug-in class in a JRWORKSPACE application.

A plug-in has a life-cycle during the runtime of the program which includes these basic steps:

instantiation	1	set default plug-in state
restoreStates	2	load plug-in state from Controller
install	3	calls <code>getPlugin</code> to obtain dependent plug-ins
-	4	program execution
storeStates	5	stores state values to the Controller
(uninstall)	6	clean up)

Step 1 instantiates a plugin and initializes its default properties. In step 2 the controller calls the `restoreStates` method. Step 3 is the actual installation of the plug-in. During runtime of the application the plug-in can interact with possible user interface it created during installation or offer services to other plug-ins. Before program termination or before uninstall the `storeStates` method is called. The plug-in is supposed to store its state values by calling the `storeProperty` method of the controller. Inter-plugin-communication is done via the `getPlugin` method of the controller. A plug-in should call `getPlugin` from within the `install` method to obtain the unique instance of a dependent plug-in. The `getPlugin` method always returns the same instance of a plug-in so its result can be stored by the `install` method for later reference, see for example Listing 1.1. Step 6 `uninstall` is only used with dynamic plug-ins that support this operation. An implementation of Controller may not support uninstallation of plug-ins.

We describe the basic API usage from a programmers point of view by giving an example plug-in in Listing 1.1 and the source code of the three basic API classes `Plugin`, `Controller`, and `PluginInfo` in Listings 1.2, 1.3, and 1.4.

```

1 public class MyPlugin extends Plugin {
2     private DependentPlugin dependency = null;
3     private double doubleState = 0.0;

4
5     public void helloPlugin() {
6         String depName = dependency.getPluginInfo().name;
7         System.out.println("I am a plug-in. I depend on " + depName);
8     }
9     @Override
10    public void storeStates(Controller c) throws Exception {
11        c.storeProperty(MyPlugin.class, "doubleState", doubleState);
12    }
13    @Override
14    public void restoreStates(Controller c) throws Exception {
15        doubleState = c.getProperty(MyPlugin.class, "doubleState", 1.0);
16    }
17    @Override
18    public void install(Controller c) throws Exception {
19        dependency = c.getPlugin(DependentPlugin.class);
20    }
21 }

```

Listing 1.1: A simple plug-in class. It depends on a plug-in called `DependentPlugin` and has the property `doubleState`. It provides the method `helloPlugin()` that prints some message. In the

`storeStates` method the value of `doubleState` is written to the controller. The class `MyPlugin` is used as context class. The name of this class is used as name space to avoid property name ambiguities. The value of `doubleState` is read from the controller in the `restoreStates` method using the same context class and property name as in `storeStates`. If there is no value with the given context and name the default value `1.0` is returned by the `getProperty` method.

```

1 public abstract class Plugin {

3     public PluginInfo getPluginInfo() {
4         return PluginInfo.create(getClass());
5     }

7     public void install(Controller c) throws Exception{}
8     public void uninstall(Controller c) throws Exception {}
9     public void restoreStates(Controller c) throws Exception {}
10    public void storeStates(Controller c) throws Exception {}

12    @Override
13    public String toString() {
14        if (getPluginInfo().name == null) {
15            return "No Name";
16        } else {
17            return getPluginInfo().name;
18        }
19    }

21    @Override
22    public boolean equals(Object obj) {
23        if (obj == null) {
24            return false;
25        } else {
26            return getClass().equals(obj.getClass());
27        }
28    }

```

Listing 1.2: The Plugin base class (excerpt). Note that plug-ins are equal if their classes are. It is not supported to have multiple instances of the same plug-in class installed.

```

1 public interface Controller {

3     public <T extends Plugin> T getPlugin(Class<T> clazz);
4     public <T> List<T> getPlugins(Class<T> pClass);
5     public Object storeProperty(Class<?> context, String key, Object property);
6     public <T> T getProperty(Class<?> context, String key, T defaultValue);
7     public <T> T deleteProperty(Class<?> context, String key);
8     public boolean isActive(Plugin p);

10 }

```

Listing 1.3: The Controller interface. A plug-in can obtain other plug-in instances by calling `getPlugin` which returns a unique instance of the given plug-in class. The semantics of the `getPlugins` methods is different. It returns all plug-ins that are already known to the controller so no new dependencies are created by calling `getPlugins`. Property handling is done via the `xxProperty` methods. Note that any `Object` can be used as property value. This requires the controller to use generic serialization to store data. It is strongly discouraged to use other classes than official java API classes as stored values as deserialization may fail if class geometry changes.

```

1 public class PluginInfo {

3     public String name = "unnamed";
4     public String vendorName = "unknown";
5     public String email = "unknown";
6     public Icon icon = null;
7     public URL documentationURL = null;
8     public boolean isDynamic = true;

10    public PluginInfo() {
11    }

13    public PluginInfo(String name) {
14        this.name = name;
15    }

17    public PluginInfo(String name, String vendor) {
18        this(name);
19        this.vendorName = vendor;
20    }

22    public static PluginInfo create(Class<?> pluginClass) {
23        PluginInfo pi;
24        if (pluginClass == null) {
25            pi = new PluginInfo();
26        } else {
27            pi = new PluginInfo(pluginClass.getSimpleName());
28        }
29        if (pluginClass != null && pluginClass.getPackage() != null) {
30            pi.vendorName = pluginClass.getPackage().getImplementationVendor();
31        }
32        return pi;
33    }

35 }

```

Listing 1.4: The plug-in meta data class (excerpt). Instances are returned by the `getPluginInfo` method of any plug-in. The value of the `name` field is a plaintext name that could be shown in a user interface as well as the `vendorName` and `email` information. An optional icon and a `documentationURL` can be given. The flag `isDynamic` is evaluated by controller implementations that support deinstallation of plug-ins. A dynamic plug-in can be installed or uninstalled during application runtime. A non-dynamic plug-in must be installed at startup and remains installed until program termination. The static `create` method returns a default `PluginInfo` instance for the given plug-in class.

In the next section we describe an implementation of this API.

1.3.2 Reference implementation - SimpleController

This section describes a reference implementation of the JRWORKSPACE plug-in API. It was started as a user interface framework for JREALITY [7]. It implements the `Controller` interface in a class called `SimpleController`. This name is historic and did not change as the features evolved from simple into quite complex. `SimpleController` implements a JAVA SWING[®] framework for the creation of complex modular applications based on the JRWORKSPACE API. It defines various plug-in flavors that define user interface features. The implementation does not support dynamic plug-ins.

In the remainder of this section I describe the basic and most interesting features of this implementation. For a complete reference see the documentation on the JTEM website [8].

Perspective Flavor

A plug-in implementing the interface `PerspectiveFlavor` provides the base for a program's user interface. It implements the method `getCenterComponent` that returns a `AWT Component` that is placed in the main frame of the application. The main program window itself is created and managed by the controller.

Menu Flavor

A plug-in implementing the `MenuFlavor` interface provides `JAVA SWING®` menu components that are placed at the top of the main window. A reference implementation of this flavor is the plug-in `MenuAggregator` that manages menu entries by contexts and menu paths.

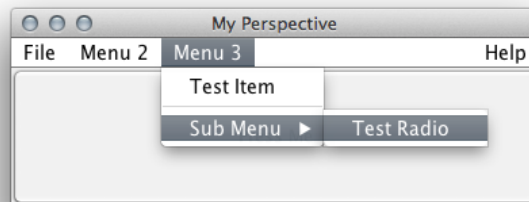


Figure 1.2: The menu created by Listing 1.5

```

2  @Override
3  public void install(Controller c) throws Exception {
4      super.install(c);
5      addMenu(MyMenuBar.class, 0.0, new JMenu("File"));
6      addMenu(MyMenuBar.class, 1.0, new JMenu("Menu 2"));
7      addMenuItem(MyMenuBar.class, 0.0, new QuitAction(), "File");
8      addMenuItem(MyMenuBar.class, 0.0, new JCheckBoxMenuItem("Test Checker"), "Menu 2");
9      addMenuItem(MyMenuBar.class, 0.0, new JRadioButtonMenuItem("Test Radio"), "Menu 3", "Sub Menu");
10     addMenuItem(MyMenuBar.class, 0.0, new JMenuItem("Test Item"), "Menu 3");
11     addMenuSeparator(MyMenuBar.class, 1.0, "Menu 3");
12 }

```

Listing 1.5: Usage of the `MenuFlavor` interface and the `MenuAggregator` implementation.

Tool Bar Flavor

This plug-in flavor creates a `JAVA SWING®` tool bar at the top of the main window. There can be more than one plug-in implementing this interface to create multiple tool bars.

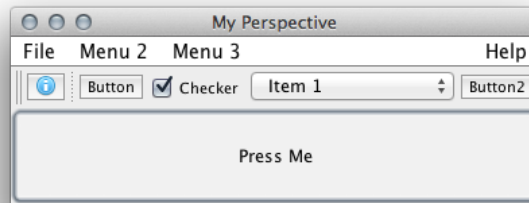


Figure 1.3: The menu bar created by Listing 1.6

```
2  @Override
3  public void install(Controller c) throws Exception {
4      addAction(MyToolBar.class, 0.0, new MyAction());
5      addTool(MyToolBar.class, 2.0, new JButton("Button"));
6      addSeparator(MyToolBar.class, 1.0);
7      addTool(MyToolBar.class, 3.0, new JCheckBox("Checker"));
8      addTool(MyToolBar.class, 4.0, new JComboBox(testItems));
9      addTool(MyToolBar.class, 5.0, new JButton("Button2"));
10     super.install(c);
11 }
```

Listing 1.6: Usage of the ToolFlavor interface and the ToolBarAggregator implementation.

1.3.3 Gui elements

1.3.4 JRWORKSPACE and JREALITY

1.3.5 Building a JRWORKSPACE application

1.4 The JTEM libraries HALFEDGE and HALFEDGETOOLS

1.4.1 The halfedge data structure and tools

1.4.2 Data model and algorithms

1.5 CONFORMALLAB - Conformal maps and uniformization

1.5.1 Embedded surfaces

1.5.2 Elliptic and hyperelliptic surfaces

1.5.3 Schottky data

1.5.4 Surfaces with boundary

1.6 VARYLAB - Variational methods for discrete surfaces

1.6.1 Functional plug-ins

1.6.2 Implemented functionals and options

1.6.3 Remeshing

1.7 Non-linear optimization with JPETSC/JTAO

1.7.1 A java wrapper for PETSc/TAO

1.8 U3D - 3D content in presentations and online publications

1.8.1 The JREALITY U3D export module

1.8.2 Discrete S-isothermic minimal surfaces

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