## **QPM Model**

```
2: % Basic Quarterly Projection Model (QPM)
4:
5: !transition_variables
6: 'Real GDP (100*log)'
                                                                    L_GDP
7: 'Trend in Real GDP (100*log)'
                                                                    L_GDP_BAR
8: 'Output Gap (in %)'
                                                                    L_GDP_GAP
9: 'Quarterly Growth in Real GDP(in % pa)'
                                                                    DLA_GDP
10: 'Real GDP Growth YoY (in % pa)'
                                                                    D4L_GDP
11: 'Real GDP Trend Growth QoQ annualized (in % pa)'
                                                                    DLA_GDP_BAR
12: 'Growth trend'
                    GROWTH_BAR
13:
14: 'Real Monetary Condition Index (in % pa)'
                                                                    MCI
15:
16: 'CPI (level, 100*log)'
                                                                    L_CPI
17: 'CPI Inflation QoQ annualized (in % pa)'
                                                                    DLA_CPI
18: 'Expected CPI Inflation QoQ annualized (in % pa)'
                                                                    E_DLA_CPI
19: 'Expected CPI Inflation YoQ (in % pa)'
                                                           E_D4L_CPI
20: 'CPI Inflation YoY (in % pa)'
                                                                    D4L_CPI
21: 'Inflation Target (in % pa)'
                                                                    D4L_CPI_TAR
22:
23: 'Real Marginal Cost (in %)'
                                                                    RMC
24:
                                                                    L_S
25: 'Nominal Exchange Rate (LCY/FCY, 100*log)'
                                                                    DLA_S
26: 'Nominal Exch. Rate Depreciation QoQ annualized (in % pa)'
27: 'Nominal Exch. Rate Depreciation YoY (in % pa)'
                                                                    D4L_S
                                                                    PREM
28: 'Country Risk Premium (in % pa)'
29:
                                                                    RS
30: 'Nominal Policy Interest Rate (in % pa)'
31: 'Real Interest Rate (in % pa)'
                                                                    RR
32: 'Trend Real Interest Rate (in % pa)'
                                                                    RR_BAR
33: 'Real Interest Rate Gap (in %)'
                                                                    RR_GAP
34: 'Nominal Policy Neutral Interest Rate (in % pa)'
                                                                    RSNEUTRAL
35:
36: 'Real Exchange Rate (level, 100*log)'
                                                                    L_Z
37: 'Trend Real Exchange Rate (level, 100*log)'
                                                                    L_Z_BAR
                                                                    L_Z_GAP
38: 'Real Exchange Rate Gap (in %)'
```

```
39: 'Real Exchange Rate Depreciation QoQ annualized (in % pa)'
                                                                                 DLA_Z
40: 'Trend Real Exchange Rate Depreciation QoQ annualized(in % pa)'
                                                                                 DLA_Z_BAR
41:
42: 'Foreign Output Gap (in %)'
                                                                                 L_GDP_RW_GAP
43: 'Foreign Nominal Interest Rate (in % pa)'
                                                                                 RS_RW
44: 'Foreign Real Interest Rate (in % pa)'
                                                                                 RR_RW
45: 'Foreign Real Interest Rate Trend (in % pa)'
                                                                                 RR_RW_BAR
46: 'Foreign Real Interest Rate Gap (in %)'
                                                                                 RR_RW_GAP
47: 'Foreign CPI (level, 100*log)'
                                                                                 L_CPI_RW
48: 'Foreign Inflation QoQ annualized (in % pa)'
                                                                                 DLA_CPI_RW
49:
50: 'Unemployment rate'
                                                                                 UNEM
51: 'equilibrium value of the unemployment (NAIRU)'
                                                                                 UNEM_BAR
52: 'Unemployment Gap'
                                                                                 UNEM GAP
53: 'Temporaty Variation in the trend'
                                                                                 DLA_UNEM_BAR
54:
55:
56: % ------ %
57: !transition_shocks
58: 'Shock: Output gap (demand)'
                                                                                 SHK_L_GDP_GAP \langle \sigma = 0.3345 \rangle
59: 'Shock: CPI inflation (cost-push)'
                                                                                 SHK_DLA_CPI\langle \sigma = 0.464 \rangle
60: 'Shock: Exchange rate (UIP)'
                                                                                 SHK_LS\langle \sigma = 0.5047 \rangle
61: 'Shock: Interest rate (monetary policy)'
                                                                                 SHK_RS\langle \sigma = 0.0432 \rangle
62: 'Shock: Inflation target'
                                                                                 SHK_D4L_CPI_TAR\langle \sigma = 0.0933 \rangle
63:
64: 'Shock: Real interest rate'
                                                                                  SHK_RR_BAR\langle \sigma = 0.4097 \rangle
65: 'Shock: Real exchange rate depreciation'
                                                                                 SHK_DLA_Z_BAR\langle \sigma = 3.6468 \rangle
66: 'Shock: Potential GDP growth'
                                                                                  SHK_DLA_GDP_BAR\langle \sigma = 0.1191 \rangle
67:
68: 'Shock: Foreign output gap'
                                                                                 SHK_L_GDP_RW_GAP\langle \sigma = 0.4366 \rangle
69: 'Shock: Foreign nominal interest rate'
                                                                                 SHK_RS_RW\langle \sigma = 0.1153 \rangle
70: 'Shock: Foreign inflation'
                                                                                 SHK_DLA_CPI_RW\langle \sigma = 0.9828 \rangle
71: 'Shock: Foreign real interest rate'
                                                                                 SHK_RR_RW_BAR\langle \sigma = 0.5563 \rangle
72:
73: 'Shock: Unemployment'
                                                                                  SHK_UNEM_BAR\langle \sigma = 0.3265 \rangle
74: 'Shock: Variation in its trend unemployment'
                                                                                 SHK_DLA_UNEM_BAR\langle \sigma = 0.152 \rangle
75: 'Shock: Unemployment Gap'
                                                                                 SHK_UNEM_GAP \langle \sigma = 0.0405 \rangle
76: 'Shock: GDP trend'
                                                                                 SHK_L_GDP_BAR\langle \sigma = 0.5262 \rangle
77: % ------ %
78: !parameters
79: b1\langle 0.6072 \rangle b2\langle 0.1425 \rangle b3\langle 0.4751 \rangle b4\langle 0.5276 \rangle
```

```
80: a1\langle 0.2899 \rangle a2\langle 0.1758 \rangle a3\langle 0.6779 \rangle
 81: e1(0.5)
 82: g1\langle 0.7 \rangle g2\langle 1.5 \rangle g3\langle 0.375 \rangle
 83: u1\langle 0.4434 \rangle \ u2\langle 0.4585 \rangle \ n1\langle 0.9 \rangle
 84:
 85: rho_D4L_CPI_TAR(0.9069)
 86: rho_DLA_Z_BAR\langle 0.5304 \rangle
 87: rho_RR_BAR\langle 0.853 \rangle
 88: rho_DLA_GDP_BAR\langle 0.7425 \rangle
 89:
 90: rho_L_GDP_RW_GAP\langle 0.675 \rangle
 91: rho_RS_RW(0.94)
 92: rho_DLA_CPI_RW\langle 0.2632 \rangle
 93: rho_RR_RW_BAR(0.7948)
 94:
 95: rho_UNEM_BAR\langle 0.4483 \rangle
 96: rho_DLA_UNEM_BAR\langle 0.8251 \rangle
 97: rho_UNEM_GAP\langle 0.1783 \rangle
 98:
 99: ss_D4L_CPI_TAR(3)
100: ss_DLA_Z_BAR\langle 0 \rangle
101: ss_RR_BAR\langle 3 \rangle
102: ss_DLA_GDP_BAR\langle 3.3 \rangle
103:
104: ss_DLA_CPI_RW\langle 2 \rangle
105: ss_RR_RW_BAR(0.5)
106:
107: ss_UNEM_BAR\langle 11.1 \rangle
108:
109: %% ------ %
110: !transition_equations
111: %% === Aggregate demand (the IS curve) ===
112: L_GDP_GAP = b1\langle 0.6072 \rangle *L_GDP_GAP \{-1\} - b2\langle 0.1425 \rangle *MCI + b3\langle 0.4751 \rangle *L_GDP_RW_GAP + SHK_L_GDP_GAP \langle \sigma = 0.3345 \rangle;
113:
114: %-- Real monetary conditions index
115: MCI = b4\langle 0.5276\rangle *RR_GAP + (1-b4\langle 0.5276\rangle) *(-L_Z_GAP);
116:
117: %% === Inflation (the Phillips curve) ===
118: DLA_CPI = a1\langle 0.2899\rangle *DLA_CPI\{-1\} + (1-a1\langle 0.2899\rangle) *DLA_CPI\{+1\} + a2\langle 0.1758\rangle *RMC + SHK_DLA_CPI\{\sigma = 0.464\};
119:
120: %-- Real marginal cost
```

```
121: RMC = a3(0.6779)*L_GDP_GAP + (1-a3(0.6779))*L_Z_GAP;
122:
123: %- expected inflation
124: E_DLA_CPI = DLA_CPI{+1};
125: E_D4L_CPI = D4L_CPI{+4};
126:
127: %% === Monetary policy reaction function (a forward-looking Taylor-type Rule) ===
128: RS = g1\langle 0.7 \rangle *RS\{-1\} + (1-g1\langle 0.7 \rangle) *(RSNEUTRAL + g2\langle 1.5 \rangle *(D4L_CPI\{+4\} - D4L_CPI_TAR\{+4\}) + g3\langle 0.375 \rangle *L_GDP_GAP) + SHK_RS\langle \sigma = 0.0432 \rangle;
129:
130: %- Neutral nominal policy interest rate
131: RSNEUTRAL = RR_BAR + D4L_CPI{+1};
132:
133: %% === Modified Uncovered Interest Rate Parity (UIP) condition ===
134: L_S = (1-e^{(0.5)})*L_S\{+1\} + e^{(0.5)}*(L_S\{-1\} + 2/4*(D4L_CPI_TAR - ss_DLA_CPI_RW(2) + DLA_Z_BAR)) + (- RS + RS_RW + PREM)/4 + SHK_L_S(\sigma - RS_RW + RS
135:
136: %% === Definitions ===
137:
138: %- Fisher equation (RIR)
139: RR = RS - D4L_CPI\{+1\};
140:
141: %- Real exchange rate (RER)
142: L_Z = L_S + L_{CPI_RW} - L_{CPI};
143:
144: %- Long-term version of UIP (consistency of trends)
145: DLA_Z_BAR{+1} = RR_BAR - RR_RW_BAR - PREM;
146:
147: %% === Identities ===
148: GROWTH_BAR = 4*(L_GDP_BAR - L_GDP_BAR\{-1\});
149: L_GDP_BAR = L_GDP_BAR\{-1\} + DLA_GDP_BAR\{-1\} + \{-1\} + \{-1\} + DLA_GDP_BAR\{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} + \{-1\} +
150: DLA_Z_BAR
                                                             = 4*(L_Z_BAR - L_Z_BAR\{-1\});
151: DLA_Z
                                                             = 4*(L_Z - L_Z\{-1\});
152: DLA_GDP
                                                             = 4*(L_GDP - L_GDP\{-1\});
153: DLA_CPI
                                                             = 4*(L_CPI - L_CPI\{-1\});
154: DLA_S
                                                             = 4*(L_S - L_S\{-1\});
155:
156: D4L_GDP
                                                             = L_GDP - L_GDP\{-4\};
157: D4L_CPI
                                                             = L_CPI - L_CPI\{-4\};
158: D4L_S
                                                             = L_S - L_S{-4};
159:
160: %% === Gaps ===
161: RR_GAP
                                                     = RR - RR_BAR;
```

```
162: L_Z_{GAP} = L_Z - L_Z_{BAR};
163: L_GDP_GAP = L_GDP - L_GDP_BAR;
164:
165: %% === Trends ===
166: D4L_CPI_TAR = rho_D4L_CPI_TAR\langle 0.9069 \rangle*D4L_CPI_TAR\langle -1 \rangle + \langle 1-rho_D4L_CPI_TAR \langle 0.9069 \rangle)*ss_D4L_CPI_TAR\langle 3 \rangle + SHK_D4L_CPI_TAR\langle \sigma=0.0933 \rangle;
167: DLA_Z_BAR = rho_DLA_Z_BAR\langle 0.5304 \rangle*DLA_Z_BAR\langle -1 \rangle + \langle 1-rho_DLA_Z_BAR \langle 0.5304 \rangle*ss_DLA_Z_BAR\langle 0 \rangle + SHK_DLA_Z_BAR\langle \sigma = 3.6468 \rangle;
168: RR_BAR
                     = rho_RR_BAR\langle 0.853 \rangle*RR_BAR\{-1\} + (1-rho_RR_BAR\langle 0.853 \rangle)*ss_RR_BAR\langle 3 \rangle + SHK_RR_BAR\langle \sigma = 0.4097 \rangle;
169: DLA_GDP_BAR = rho_DLA_GDP_BAR\langle 0.7425\rangle*DLA_GDP_BAR\langle -1 \rangle + \langle 1-rho_DLA_GDP_BAR\langle 0.7425\rangle*ss_DLA_GDP_BAR\langle 3.3\rangle + SHK_DLA_GDP_BAR\langle 0.7425\rangle;
170:
171: %% === Foreign Sector Equations ===
172: L_GDP_RW_GAP = rho_L_GDP_RW_GAP\langle 0.675 \rangle*L_GDP_RW_GAP\langle -1 \rangle + SHK_L_GDP_RW_GAP\langle \sigma = 0.4366 \rangle;
173: DLA_CPI_RW = rho_DLA_CPI_RW\langle 0.2632 \rangle*DLA_CPI_RW\langle -1 \rangle + \langle 1-rho_DLA_CPI_RW\langle 0.2632 \rangle)*ss_DLA_CPI_RW\langle 2 \rangle + SHK_DLA_CPI_RW\langle \sigma = 0.9828 \rangle;
                       = rho_RS_RW\langle 0.94 \rangle*RS_RW\{-1\} + \langle 1-rho_RS_RW\langle 0.94 \rangle)*\langle RR_RW_BAR + DLA_CPI_RW \rangle + SHK_RS_RW\langle \sigma = 0.1153 \rangle;
174: RS_RW
175: RR_RW_BAR
                       = rho_RR_RW_BAR\langle 0.7948 \rangle*RR_RW_BAR\{-1\} + \langle 1-rho_RR_RW_BAR\langle 0.7948 \rangle)*ss_RR_RW_BAR\langle 0.5 \rangle + SHK_RR_RW_BAR\langle \sigma = 0.5563 \rangle;
176: RR_RW
                       = RS_RW - DLA_CPI_RW;
177: RR_RW_GAP
                       = RR_RW - RR_RW_BAR;
178:
179: DLA_CPI_RW
                     = 4*(L_CPI_RW - L_CPI_RW\{-1\});
180:
181: %% === Labour Market Equations ===
182: UNEM_GAP = UNEM_BAR - UNEM;
183: UNEM_BAR = rho_UNEM_BAR(0.4483)*UNEM_BAR\{-1\} + (1-rho_UNEM_BAR(0.4483))*ss_UNEM_BAR(11.1) + DLA_UNEM_BAR - u1(0.4434)*(L_GDP_GAP\{-8\}+L_G
184: %UNEM_BAR = rho_UNEM_BAR*UNEM_BAR{-1} + (1-rho_UNEM_BAR)*ss_UNEM_BAR + DLA_UNEM_BAR - u1*(L_GDP_GAP{-8}+L_GDP_GAP{+8})/2 + SHK_UNEM_BAR
185: DLA_UNEM_BAR = rho_DLA_UNEM_BAR\langle 0.8251 \rangle*DLA_UNEM_BAR\{-1\} + SHK_DLA_UNEM_BAR\langle \sigma = 0.152 \rangle;
186: UNEM_GAP = rho_UNEM_GAP(0.1783)*UNEM_GAP\{-1\} + u2(0.4585)*L_GDP_GAP + SHK_UNEM_GAP(\sigma = 0.0405);
187: %% ------ %
188: !measurement_variables
189: OBS_L_GDP
190: OBS_L_GDP_GAP
191: OBS_L_CPI
192: OBS_RS
193: OBS_L_S
194: OBS_D4L_CPI_TAR
195:
196: OBS_L_GDP_RW_GAP
197: OBS_DLA_CPI_RW
198: OBS_RS_RW
199: OBS_UNEM
200:
201: !measurement_equations
202: OBS_L_GDP = L_GDP;
```

```
203: OBS_L_GDP_GAP = L_GDP_GAP;
204: OBS_L_CPI = L_CPI;
205: OBS_RS
           = RS;
206: OBS_L_S = L_S;
207: OBS_D4L_CPI_TAR = D4L_CPI_TAR;
208:
209: OBS_L_GDP_RW_GAP = L_GDP_RW_GAP;
210: OBS_DLA_CPI_RW
                  = DLA_CPI_RW;
211: OBS_RS_RW
                   = RS_RW;
212: OBS_UNEM
                  = UNEM;
213:
214: %% ------ %
215: Legend
216: _GAP
              cyclical deviation from a trend
217: _BAR
              trend (equilibrium)
              steady-state value
218: ss_
219: DLA_
              q-o-q change
              y-o-y change
220: D4L_
              foreign variable
221: _RW
222: SHK_
              equation residual
```

## Steady state

Variable	Description	Value
$L_{GDP}_{GAP}$	Output Gap (in %)	0
$DLA\_GDP$	Quarterly Growth in Real GDP(in % pa)	3.3
$D4L\_GDP$	Real GDP Growth YoY (in % pa)	3.3
DLA_GDP_BAR	Real GDP Trend Growth QoQ annualized (in % pa)	3.3
$GROWTH\_BAR$	Growth trend	3.3
MCI	Real Monetary Condition Index (in % pa)	0
$DLA\_CPI$	CPI Inflation QoQ annualized (in % pa)	3
$E_DLA_CPI$	Expected CPI Inflation QoQ annualized (in % pa)	3
$E_D4L_CPI$	Expected CPI Inflation YoQ (in % pa)	3
D4L_CPI	CPI Inflation YoY (in % pa)	3
$D4L\_CPI\_TAR$	Inflation Target (in % pa)	3
RMC	Real Marginal Cost (in %)	0
$DLA\_S$	Nominal Exch. Rate Depreciation QoQ annualized (in $\%$ pa)	1
$D4L_S$	Nominal Exch. Rate Depreciation YoY (in % pa)	1
PREM	Country Risk Premium (in % pa)	2.5
RS	Nominal Policy Interest Rate (in % pa)	6
RR	Real Interest Rate (in % pa)	3
RR_BAR	Trend Real Interest Rate (in % pa)	3
$RR\_GAP$	Real Interest Rate Gap (in %)	0
RSNEUTRAL	Nominal Policy Neutral Interest Rate (in % pa)	6
$L_Z_GAP$	Real Exchange Rate Gap (in %)	0
$DLA_Z$	Real Exchange Rate Depreciation QoQ annualized (in $\%$ pa)	0
DLA_Z_BAR	Trend Real Exchange Rate Depreciation QoQ annualized (in $\%$ pa)	0
$L_{GDP}RW_{GAP}$	Foreign Output Gap (in %)	0
RS_RW	Foreign Nominal Interest Rate (in $\%$ pa)	2.5
$RR_RW$	Foreign Real Interest Rate (in $\%$ pa)	0.5
$RR_RW_BAR$	Foreign Real Interest Rate Trend (in $\%$ pa)	0.5
$RR_RW_GAP$	Foreign Real Interest Rate Gap (in $\%$ )	0
DLA_CPI_RW	For eign Inflation QoQ annualized (in $\%$ pa)	2
UNEM	Unemployment rate	11.1
UNEM_BAR	equilibrium value of the unemployment (NAIRU)	11.1
$UNEM\_GAP$	Unemployment Gap	0

Variable	Description	Value
${\rm DLA\_UNEM\_BAR}$	Temporaty Variation in the trend	0