

1) Lets, X be the random variable denoting the total number of duplications for an array of n random numbers. So the solution to the problem is $E[X]$ and X is equal to the sum of all the $X_{i,j}$'s.

For $1 \leq i < j \leq n$,

$$X_{i,j} = I\{A[i] = A[j]\}.$$

$X_{i,j}$ be the indicator random variable for the event that the pair (i, j) is duplicated.

$$E[X] = E[\sum X_{i,j}]$$

$$= \sum E[X_{i,j}], \text{ by property of } E$$

$$= \sum_{i=1}^{n-1} \sum_{j=i+1}^n \Pr\{A[i] = A[j]\}$$

$$= (n-1)/2$$

$$E[X_{i,j}] = \Pr\{A[i] = A[j]\}$$

$$\Pr\{A[i] = A[j]\} = \frac{1}{n} \cdot \frac{1}{n} \cdot n = \frac{1}{n}$$

2) I wrote `exp_num` function for calculating the expected number of duplications. I did error handling if the user enters a number or char other than a positive number. I created a dynamic array based on the number. Then I filled the array with values from 1 to n using uniform random number generator.

I printed the array elements up to 10 array elements per line. I used the `exp_num` function for calculated the expected number of duplications. Then, I found all the duplications of the array and printed them out. And there are two for loops and it will take $O(n^2)$ time. And running time of the algorithm is $O(n^2)$.