Evaluation

May 13, 2022

1 Lab 1 Evaluation

Names, Surnames, and Group: (to complete by 2 students)

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In the following, we consider the (binarized) Compas dataset that we studied in the Lab

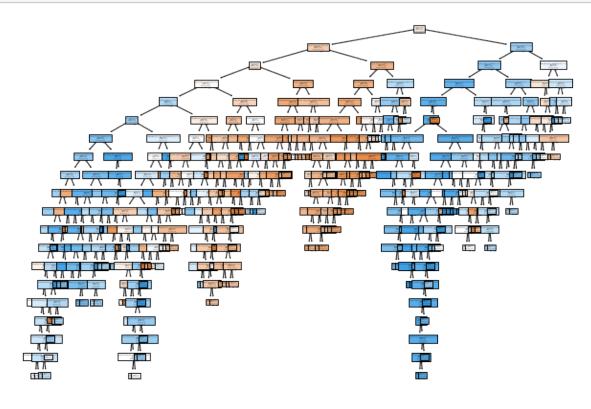
- 1) A decision tree configuration is a set of parameters that one can use to build decision trees. Propose 6 configurations that are likely to provide different topologies and caracteristics
- 2) Train a decision tree for each of the previous configurations on the full dataset

First we prepare the data set to build the decision tree and make all the import we need

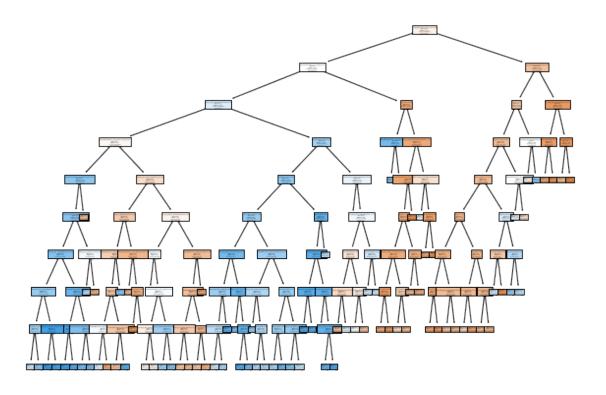
In order to have 6 different configurations, we decided to change some parameters of "decision tree Classifier" like the max depth of the tree, the minimum number of samples required to be at a leaf node, the strategy used to choose the split at each node, the function to measure the quality of a split and the number of features to consider when looking for the best split.

Configuration A: without specification

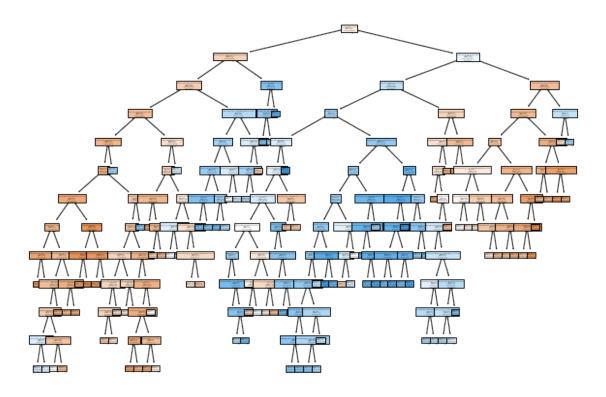
```
class_names= ("false (0)", "true (1)" ),
filled=True)
```



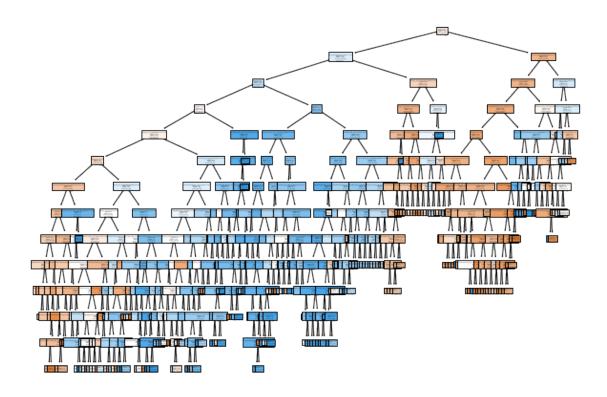
Configuration B:



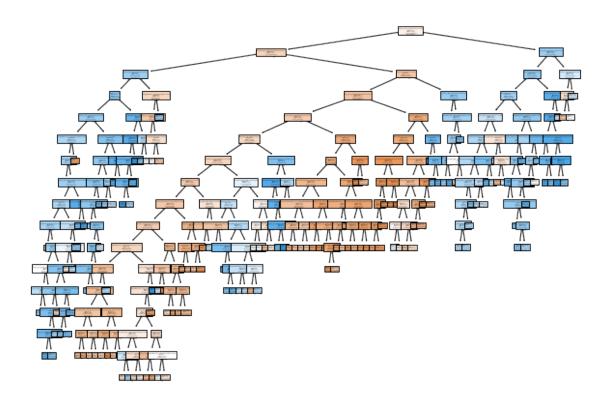
Configuration C:



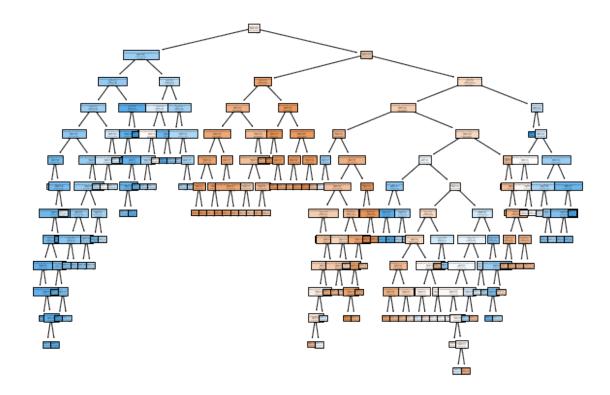
Configuration D:



Configuration E:



Configuration F:



3) Propose an evaluation in terms of training and testing accuracies using 5-cross validation on two decision trees that have different typologies

```
[8]: taille = len(train_examples)

def taill_en_poucentage(x):
    return x*taille/100

def moyen(L):
    return sum(L)/len(L)

tail_prct = int(taill_en_poucentage(80))

#DIFFERENT SPECIFICATIION TO BUILD DIFFERENT TREE DECISION
profondeur=[5,2,5,3,6,8]
min_feuille =[1,10,5,2,4,6]

kf = model_selection.KFold(n_splits=5) # Specify the split in K
kf.get_n_splits(train_examples)

score_tree1=[]
score_tree2=[]
```

```
# CROSS VALIDATION FOR FIRST TYPOLOGI
for train_index, test_index in kf.split(train_examples):
    #print("TRAIN:", train_index, "TEST:", test_index)
   X_train, X_test = train_examples[train_index], train_examples[test_index]
   y_train, y_test = train_labels[train_index], train_labels[test_index]
   clf = tree.DecisionTreeClassifier(max_depth=profondeur[0],min_samples_leaf_
→= min_feuille[0])
   clf = clf.fit(X_train, y_train)
    #print("SCORE : ",clf.score(X_train,y_train)*100 , "Profondeur :
 → ", profondeur[index], "Feuille Min : ", min_feuille[index])
    #print("----\n")
    #ADD THE SCORE TO AN LIST
    score_tree1.append(clf.score(X_train,y_train)*100)
# CROSS VALIDATION FOR THE SECOND TYPOLOGI
for train_index, test_index in kf.split(train_examples):
    #print("TRAIN:", train_index, "TEST:", test_index)
   X train, X test = train examples[train_index], train_examples[test_index]
   y_train, y_test = train_labels[train_index], train_labels[test_index]
   clf = tree.DecisionTreeClassifier(max_depth=profondeur[1],min_samples_leaf_
→= min_feuille[1])
   clf = clf.fit(X_train, y_train)
    \#print("SCORE : ",clf.score(X_train,y_train)*100 , "Profondeur :
→ ", profondeur[index], "Feuille Min : ", min_feuille[index])
    #print("----\n")
    #ADD THE SCORE TO AN LIST
   score_tree2.append(clf.score(X_train,y_train)*100)
print("SCORE TREE N°1 :",moyen(score tree1))
print("SCORE TREE N°2 :",moyen(score_tree2))
```

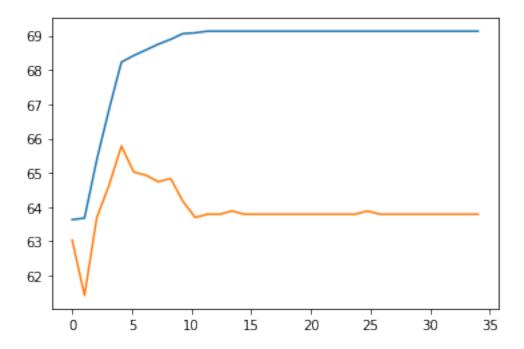
SCORE TREE N°1 : 67.82190256523161 SCORE TREE N°2 : 63.607068477391955

4) Propose an experimental study that shows the transition phase from underfitting to overfitting

```
[9]: taille = 0
#print("TRUC GENERAL")
#CONFIGURATION
```

```
profendeur = 5
split = 'best'
feuille = 5
print("PREDICTION :",prediction)
taille = len(train_examples)
def taill_en_poucentage(x):
    return x*taille/100
def difference (liste1,liste2):
    somme = 0
    for i in range(len(liste1)):
        if (liste1[i] != liste2[i]):
            somme = somme + 1
    return somme
tail_prct = int(taill_en_poucentage(80))
y1=[]
y2=[]
for i in range (1,35):
    profendeur = i
    train = train_examples[:tail_prct]
    labels = train_labels[:tail_prct]
    test = train_examples[tail_prct:]
    waitedResult = train_labels[tail_prct:]
    clf = tree.DecisionTreeClassifier(max_depth = profendeur, splitter = split_
→, min_samples_leaf = feuille)
    clf = clf.fit(train, labels)
    y1.append(clf.score(test,waitedResult)*100)
    y2.append(clf.score(train,labels)*100)
x1=np.linspace(0,34,34)
plt.plot(x1,y2)
plt.plot(x1,y1)
train = train_examples[:tail_prct]
labels = train_labels[:tail_prct]
test = train_examples[tail_prct:]
```

PREDICTION: two_year_recid SCORE FOR THE PREDICTION: 63.791469194312796



We can see above two lines, the orange one represents the predection score of the decision tree after the training and the blue one represents the predection score of the decision tree during the training. With a depth going from 0 to 3, we can see an underfitting because the model is not efficient enough to predict an acceptable value. With depth equal 4, we have a good fitting and the prediction score is the highest. With a depth equal to 5 or higher, we can see an overfitting because the prediction score of the decision tree is decreasing.

- 5) Construct the confusion matrix on a particular good configuration (after explaining your choice)
 - To construct our confusion matrix we decided to compare two parameters: the predicted value and the expected value. This confusion will display the number of correspondance between them.

```
[14]: confusionMatrix = metrics.confusion_matrix(predicted, waitedResult) print("Confusion Matrix : \n", confusionMatrix)
```

Confusion Matrix : [[406 229] [153 267]]

- 6) Provide an evaluation of the fairness of the model based on the False Positive Rate
 - The confusion Matrix can be read as the number of : -True positif at confusion Matrix [0][0] -True negatif at confusion Matrix [0][1] -False positif at confusion Matrix [1][0] -False negatif at confusion Matrix [1][1]

True negatif rate 36.06299212598425 False positif rate 36.42857142857142

perceptron

May 13, 2022

0.1 Objectives of the practical work

The objective is to get hands on experience on the fundamental elements of neural networks:

- perceptron architecture (linear regression)
- loss function
- empirical loss
- gradient descent

For this we will implement from scratch the data-structure and algorithms to train a perceptron. Note that slides related to the perceptron and neural networks in general are available on moodle.

0.2 Dataset

The objective of the regression is the prediction of the hydrodynamic performance of sailing yachts from dimensions and velocity. The **inputs** are linked to dimension and hydrodynamics characteristics: 1. Longitudinal position of the center of buoyancy (*flottabilité*), adimensional. 2. Prismatic coefficient, adimensional. 3. Length-displacement ratio, adimensional. 4. Beam -draught ratio ((*tiran d'eau*), adimensional. 5. Length-beam ratio, adimensional. 6. Froude number, adimensional

Target value/predicted value (Output) = Residuary resistance per unit weight of displacement, adimensional

```
[1]: # Import some useful libraries and functions
from matplotlib import pyplot as plt
import numpy as np
import pandas

def print_stats(dataset):
    """Print statistics of a dataset"""
    print(pandas.DataFrame(dataset).describe())
```

```
[2]: # Download the data set and place in the current folder (works on linux only)
filename = 'yacht_hydrodynamics.data'

import os.path
import requests

if not os.path.exists(filename):
```

Dataset available

f([0.

0.2.1 Explore the dataset

- how many examples are there in the dataset? There are 308 examples in the data set.
- how many features for each example? There are 6 features in each example.
- what is the ground truth of the 10th example? The ground truth of the 10th example is 1.83.

```
[3]: # loads the dataset and slip between inputs (X) and ground truth (Y)
     dataset = np.genfromtxt("yacht_hydrodynamics.data", delimiter='')
     X = dataset[:, :-1] # examples features
     Y = dataset[:, -1] # ground truth
     # Print the first 5 examples
     for i in range (0,5):
         print(f''f(\{X[i]\}) = \{Y[i]\}'')
    f([-5.
               0.6
                     4.78 \quad 4.24 \quad 3.15 \quad 0.35) = 8.62
    f([-5.
                0.565 4.77
                               3.99
                                       3.15
                                              0.15]) = 0.18
    f([-2.3
                               5.35
                0.565
                       4.78
                                       2.76
                                              0.15 ]) = 0.29
    f([-5.
                0.6
                        4.78
                               4.24
                                       3.15
                                              0.325]) = 6.2
```

The following command adds a column to the inputs.

 $0.53 \quad 4.78 \quad 3.75 \quad 3.15 \quad 0.175]) = 0.59$

- what is in the value added this column? The column added contains only ones.
- why are we doing this? So we can simulate the weight.

```
[4]: X = np.insert(X, 0, np.ones((len(X))), axis= 1)
print_stats(X)
```

```
0
                                     2
                                                  3
                                                               4
                                                                            5
                                                                               \
                        1
       308.0
              308.000000
                            308.000000
                                        308.000000
                                                     308.000000
                                                                  308.000000
count
mean
         1.0
                -2.381818
                              0.564136
                                           4.788636
                                                        3.936818
                                                                     3.206818
         0.0
                 1.513219
                              0.023290
                                           0.253057
                                                        0.548193
                                                                     0.247998
std
min
         1.0
                -5.000000
                              0.530000
                                           4.340000
                                                        2.810000
                                                                     2.730000
25%
         1.0
                -2.400000
                              0.546000
                                           4.770000
                                                        3.750000
                                                                     3.150000
50%
         1.0
                -2.300000
                              0.565000
                                           4.780000
                                                        3.955000
                                                                     3.150000
75%
         1.0
               -2.300000
                              0.574000
                                           5.100000
                                                       4.170000
                                                                     3.510000
```

1.0 0.000000 0.600000 5.140000 5.350000 3.640000 max6 308.000000 count mean 0.287500 0.100942 std min 0.125000 25% 0.200000 50% 0.287500 75% 0.375000 0.450000 max

0.3 Creating the perceptron

We now want to define a perceptron, that is, a function of the form:

```
h_w(x) = w_0 + w_1 \times x_1 + \dots + w_n \times x_n
```

- Complete the code snippet below to:
 - create the vector of weight ${\tt w}$
 - implement the h function that evaluate an example based on the vector of weights
 - check if this works on a few examples

```
[5]: w = None # TODO
index = 0

w = [row[0] for row in X]
ligne = X[index,1:]
def h(w, x):
    h = np.multiply(w, x)
    return sum(h)
h(w[index], ligne)

# print the ground truth and the evaluation of h_w on the first example
```

[5]: 8.12

0.4 Loss function

Complete the definition of the loss function below such that, for a **single** example x with ground truth y, it returns the L_2 loss of h_w on x.

```
[16]: def loss(w, x, y):
    return (y - h(w, x))**2

print(loss(w[index], ligne, Y[index]))
print(len(X))
```

0.25 308

0.5 Empirical loss

Complete the function below to compute the empirical loss of h_w on a **set** of examples X with associated ground truths Y.

```
[17]: def emp_loss(w, X, Y):
    somme = 0
    for index in range (0,len(X)):
        ligne = X[index,1:]
        somme = somme + (loss(w[index], ligne, Y[index]) / len(X))
    return somme

print("Empirical loss:",emp_loss(w,X,Y))
```

Empirical loss: 228.81521738311693

0.6 Gradient update

A gradient update is of the form: $w \leftarrow w + dw$

• Complete the function below so that it computes the dw term (the 'update') based on a set of examples (X, Y) the step (alpha)

If you are not sure about the gradient computation, check out the perceptron slides on Moodle (in particular, slide 26). Make sure this computation is clear to you!

```
[13]: def compute_update(w, X, Y, alpha):
    dw = np.zeros_like(w)
    for index in range(0,len(w)):
        ligne = X[index,1:]
        dw[index] = w[index] + alpha*loss(w[index], ligne, Y[index])*ligne[0]
    return dw
#print(w,X,Y)
#compute_update(w, X, Y, alpha = 2)
#print(w,X,Y)
```

0.7 Gradient descent

Now implement the gradient descent algorithm that will:

- repeatedly apply an update the weights
- stops when a max number of iterations is reached (do not consider early stopping for now)
- returns the final vector of weights

```
[14]: def descent(w_init, X, Y, alpha, max_iter):
    index = 0
    wzero = 0
```

```
dw = w_init
while(index < max_iter ):
    dw += compute_update(w_init, X, Y, alpha)
    index+=1
return dw

test = descent( w ,X, Y, 2, 50)
#print(test)</pre>
```

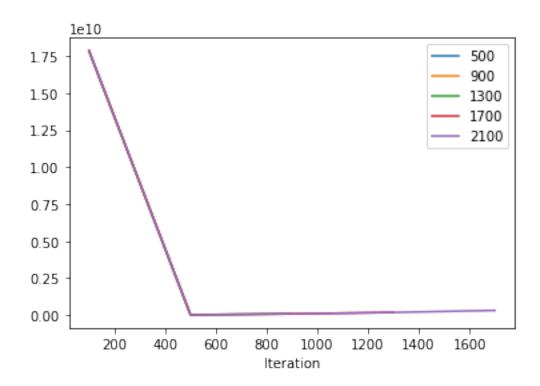
0.8 Exploitation

You gradient descent is now complete and you can exploit it to train your perceptron.

- Train your perceptron to get a model.
- Visualize the evolution of the loss on the training set. Has it converged? Yes it converged as we can see on the plot the loss decreases thanks to alpha and max_iter.
- Try training for several choices of alpha and max_iter. What seem like a reasonable choice?
 'alpha' = 10e-5 and max iter = 500
- Is the final model the optimal one for a perceptron? 'alpha' = 10e-5 and max iter = 500

```
[49]: # Code sample that can be used to visualize the difference between the ground
       \rightarrow truth and the prediction
      iteration = 100
      list_iter = []
      list_emp_loss = []
      list_alpha=[10e-2,10e-5,10e-7,10e-9,10e-10,10e-11]
      alpha = 10e-2
      for i in range (0,5):
          list_iter.append(iteration)
          temp_W = [row[0] for row in X]
          temp_W = descent(temp_W,X,Y,list_alpha[i],iteration)
          list_emp_loss.append(emp_loss(temp_W,X,Y))
          iteration+=400
          plt.plot(list_iter,list_emp_loss, label=str(iteration))
          plt.legend()
      plt.xlabel("Iteration")
```

```
[49]: Text(0.5, 0, 'Iteration')
```



1 Going further

The following are extensions of the work previously done. If attempting them **do not modify** the code you produced above so that it can be evaluated.

1.0.1 Improvements to gradient descent

Consider improving the gradient descent with:

- Stochastic Gradient Descent (SGD), which means selecting a subset of the examples for training
- Detection of convergence to halt the algorithm before the maximum number of iterations

1.0.2 Data normalization

Different input features can have different units, and very different ranges. Within the perceptron computation, these values will be summed together. While gradient descent is normally able to deal with this (by adapting the weights of the perceptron for each input feature), standardizing the input features usually eases the perceptron training, and can sometimes improve accuracy.

```
from sklearn.preprocessing import StandardScaler
sc = StandardScaler(copy=True)
X_normalized = sc.fit_transform(X)
```

mlp

May 13, 2022

1 Introduction

The objective of this lab is to dive into particular kind of neural network: the *Multi-Layer Perceptron* (MLP).

To start, let us take the dataset from the previous lab (hydrodynamics of sailing boats) and use scikit-learn to train a MLP instead of our hand-made single perceptron. The code below is already complete and is meant to give you an idea of how to construct an MLP with scikit-learn. You can execute it, taking the time to understand the idea behind each cell.

```
[1]: # Importing the dataset
import numpy as np
dataset = np.genfromtxt("yacht_hydrodynamics.data", delimiter='')
X = dataset[:, :-1]
Y = dataset[:, -1]
#to visualize the data you can uncomment the two following line
#print(X)
#print(Y)
```

```
[2]: # Preprocessing: scale input data
from sklearn.preprocessing import StandardScaler
sc = StandardScaler()
X = sc.fit_transform(X)
print(X)
```

```
[[-1.73302265 1.5423783 -0.03418367 0.55395671 -0.2294799 0.62017367]
[-1.73302265 0.03714219 -0.07376475 0.09717082 -0.2294799 -1.36438208]
[ 0.05415696 0.03714219 -0.03418367 2.58208609 -1.80462994 -1.36438208]
...
[ 0.05415696 -1.46809393 -0.11334584 -0.46924369 -0.18909144 -0.86824314]
[-1.73302265 1.5423783 -0.03418367 0.55395671 -0.2294799 -0.12403473]
[ 0.05415696 -1.46809393 1.27199221 -0.45097226 1.22450475 0.62017367]]
```

```
[4]: # Define a multi-layer perceptron (MLP) network for regression
from sklearn.neural_network import MLPRegressor
mlp = MLPRegressor(max_iter=3000, random_state=1) # define the model, with_
default params
mlp.fit(x_train, y_train) # train the MLP
```

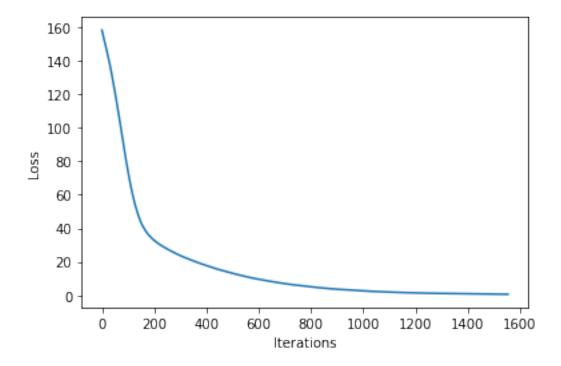
[4]: MLPRegressor(max_iter=3000, random_state=1)

```
[5]: # Evaluate the model
from matplotlib import pyplot as plt

print('Train score: ', mlp.score(x_train, y_train))
print('Test score: ', mlp.score(x_test, y_test))
plt.plot(mlp.loss_curve_)
plt.xlabel("Iterations")
plt.ylabel("Loss")
```

Train score: 0.9940765369322633 Test score: 0.9899773031580283

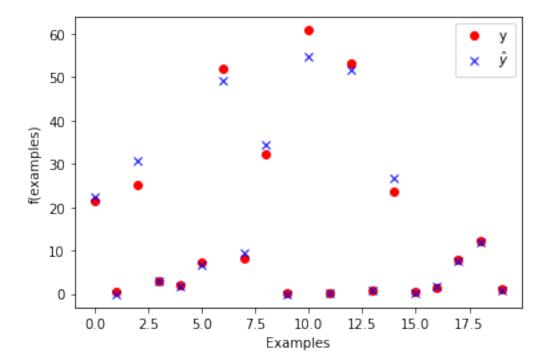
[5]: Text(0, 0.5, 'Loss')



```
[6]: # Plot the results
num_samples_to_plot = 20
plt.plot(y_test[0:num_samples_to_plot], 'ro', label='y')
```

```
yw = mlp.predict(x_test)
plt.plot(yw[0:num_samples_to_plot], 'bx', label='$\hat{y}$')
plt.legend()
plt.xlabel("Examples")
plt.ylabel("f(examples)")
```

[6]: Text(0, 0.5, 'f(examples)')



1.0.1 Analyzing the network

Many details of the network are currently hidden as default parameters.

Using the documentation of the MLPRegressor, answer the following questions.

- What is the structure of the network?
 - The network is composed of a multiLayer Perceptron regressor
- What it is the algorithm used for training? Is there algorithm available that we mentioned during the courses?
 - MLPRegressor propose different algorithms: 'LGBS' for quasi-Newton methods 'SGD' for stochastic gradient descent 'ADAM' for stochastic gradient-based optimizer proposed by Kingma, Diederik, and Jimmy Ba
 - We already seen quasi-Newton and Gradient descent during our courses.
- How does the training algorithm decides to stop the training? It decides to stop the training when the score is not improving.

2 Onto a more challenging dataset: house prices

For the rest of this lab, we will use the (more challenging) California Housing Prices dataset.

```
[7]: # clean all previously defined variables for the sailing boats %reset -f
```

```
[4.526 3.585 3.521 ... 0.526 0.469 0.939]
```

Note that each row of the dataset represents a **group of houses** (one district). The target variable denotes the average house value in units of 100.000 USD. Median Income is per 10.000 USD.

2.0.1 Extracting a subpart of the dataset for testing

• Split the dataset between a training set (75%) and a test set (25%)

Please use the conventional names X_train, X_test, y_train and y_test.

```
[9]: from sklearn.model_selection import train_test_split
x_train, x_test, y_train, y_test = train_test_split(X, Y,random_state=10, ___
→test_size = 0.25)
```

2.0.2 Scaling the input data

A step of **scaling** of the data is often useful to ensure that all input data centered on 0 and with a fixed variance.

Standardization of a dataset is a common requirement for many machine learning estimators: they might behave badly if the individual features do not more or less look like standard normally distributed data (e.g. Gaussian with 0 mean and unit variance). The function StandardScaler from sklearn.preprocessing computes the standard score of a sample as:

```
z = (x - u) / s
```

where u is the mean of the training samples, and s is the standard deviation of the training samples.

Centering and scaling happen independently on each feature by computing the relevant statistics on the samples in the training set. Mean and standard deviation are then stored to be used on later data using transform.

- Apply the standard scaler to both the training dataset (X_train) and the test dataset (X_test).
- Make sure that **exactly the same transformation** is applied to both datasets.

Documentation of standard scaler in scikit learn

```
[10]: from sklearn.preprocessing import StandardScaler
sc = StandardScaler()
x_train = sc.fit_transform(x_train)
x_test = sc.fit_transform(x_test)
```

2.1 Overfitting

In this part, we are only interested in maximizing the **train score**, i.e., having the network memorize the training examples as well as possible.

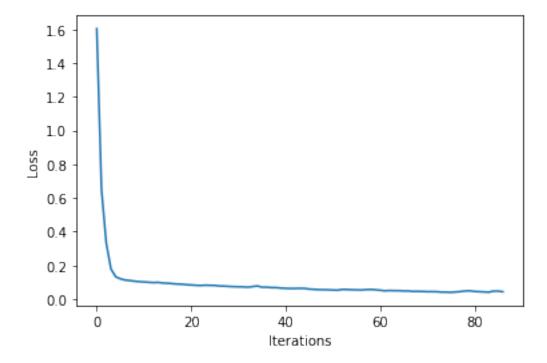
• Propose a parameterization of the network (shape and learning parameters) that will maximize the train score (without considering the test score).

While doing this, you should (1) remain within two minutes of training time, and (2) obtain a score that is greater than 0.90.

- Is the **test** score substantially smaller than the **train** score (indicator of overfitting)? The test score is way smaller than the train score.
- Explain how the parameters you chose allow the learned model to overfit. The parameters we choose allow the learned model to overfit. For example, when we add layers we allow the model to learn more but we allow also more noise that will disturb the model.

Train score: 0.9138260193968096 Test score: 0.734799767372307

[11]: Text(0, 0.5, 'Loss')



2.2 Hyperparameter tuning

In this section, we are now interested in maximizing the ability of the network to predict the value of unseen examples, i.e., maximizing the **test** score. You should experiment with the possible parameters of the network in order to obtain a good test score, ideally with a small learning time.

Parameters to vary:

- number and size of the hidden layers
- activation function
- stopping conditions
- maximum number of iterations
- initial learning rate value

Results to present for the tested configurations:

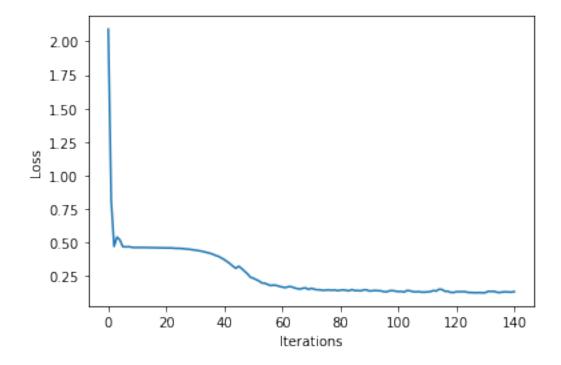
- Train/test score
- training time

Present in a table the various parameters tested and the associated results. You can find in the last cell of the notebook a code snippet that will allow you to plot tables from python structure. Be methodical in the way your run your experiments and collect data. For each run, you should record the parameters and results into an external data structure.

(Note that, while we encourage you to explore the solution space manually, there are existing methods in scikit-learn and other learning framework to automate this step as well, e.g., GridSearchCV)

Train score: 0.7355856630980302 Test score: 0.7009775458325185

[17]: Text(0, 0.5, 'Loss')



```
[18]: # Code snippet to display a nice table in jupyter notebooks (remove from import pandas as pd import numpy as np
```

```
[18]:
        activation max_iter early_stopping test_score
      1
              tanh
                         500
                                       False
                                                     0.91
      2
          logistic
                         500
                                       False
                                                     0.91
      3
          identity
                         500
                                       False
                                                     0.91
      0
              relu
                         500
                                       False
                                                     0.87
```

2.3 Evaluation

- From your experiments, what seems to be the best model (i.e. set of parameters) for predicting the value of a house?
 - Thanks to our experiments, we can say that the best model can be decided by : relu with a big number of layers and logistic with not so much layers.

Unless you used cross-validation, you have probably used the "test" set to select the best model among the ones you experimented with. Since your model is the one that worked best on the "test" set, your selection is *biased*.

In all rigor the original dataset should be split in three:

- the training set, on which each model is trained
- the validation set, that is used to pick the best parameters of the model
- the test set, on which we evaluate the final model

Evaluate the score of your algorithm on a test set that was not used for training nor for model selection.

```
[62]: # the **training set**, on which each model is trained
# the **validation set**, that is used to pick the best parameters of the model
# the **test set**, on which we evaluate the final model

import time
from sklearn import metrics
from time import gmtime, strftime
```

```
x_train, x_test, y_train, y_test = train_test_split(X, Y,random_state=10,_u
 \rightarrowtest size = 0.25)
x_train, x_validation, y_train, y_validation = train_test_split(x_train,_u
 →y train,random state=10, test size = 0.45)
data =[]
nbr_layer_
 \Rightarrow [(100),(100,100),(100,100,100),(100,100,100,100),(100,100,100,100,100,100)]
stop = True
maxIter = 500
active = ["relu","identity","logistic","tanh"]
learnRate = 0.001
index = 0
for layer in nbr_layer:
    for actv in active:
        temps= time.time()
        x_train, x_test, y_train, y_test = train_test_split(X,__
 →Y,random_state=10, test_size = 0.25)
         x_train, x_validation, y_train, y_validation =
 -train_test_split(x_train, y_train,random_state=10, test_size = 0.15)
        mlp = MLPRegressor(learning_rate_init = learnRate,activation_
 →=actv,early_stopping=stop,max_iter=maxIter,random_state=5, alpha = 3e-7,
 →hidden_layer_sizes= layer)# define the model, with default params
        mlp.fit(x_train, y_train) # train the ML
        temps = time.time() - temps
         data.append({'index':index, 'activation':actv, 'layer':layer, 'max_iter':
 →maxIter, 'early_stopping':stop, 'train_score':mlp.score(x_train, __

    y_train), 'time':temps})
         index+=1
table = pd.DataFrame.from_dict(data)
table = table.replace(np.nan, '-')
table = table.sort_values(by='train_score', ascending=False)
table
/usr/local/insa/anaconda/lib/python3.8/site-
packages/sklearn/neural_network/_multilayer_perceptron.py:614:
ConvergenceWarning: Stochastic Optimizer: Maximum iterations (500) reached and
```

the optimization hasn't converged yet.

warnings.warn(

```
[62]:
           index activation
                                                           layer
                                                                  max_iter
      10
                                                (100, 100, 100)
              10
                    logistic
                                                                        500
      8
               8
                        relu
                                                (100, 100, 100)
                                                                        500
      14
              14
                    logistic
                                          (100, 100, 100, 100)
                                                                        500
      18
                               (100, 100, 100, 100, 100, 100)
              18
                    logistic
                                                                        500
      2
               2
                    logistic
                                                             100
                                                                        500
      0
               0
                        relu
                                                             100
                                                                        500
      1
               1
                    identity
                                                             100
                                                                        500
      4
               4
                                                     (100, 100)
                        relu
                                                                        500
      7
               7
                                                     (100, 100)
                        tanh
                                                                        500
      11
                                                (100, 100, 100)
                                                                        500
              11
                        tanh
      12
              12
                                          (100, 100, 100, 100)
                                                                        500
                        relu
                               (100, 100, 100, 100, 100, 100)
      19
              19
                                                                        500
                        tanh
                                          (100, 100, 100, 100)
      15
              15
                                                                        500
                        tanh
      17
                               (100, 100, 100, 100, 100, 100)
              17
                    identity
                                                                        500
                                          (100, 100, 100, 100)
      13
              13
                    identity
                                                                        500
      5
               5
                    identity
                                                     (100, 100)
                                                                        500
                                                (100, 100, 100)
      9
               9
                    identity
                                                                        500
      16
              16
                        relu
                               (100, 100, 100, 100, 100, 100)
                                                                        500
      3
               3
                        tanh
                                                             100
                                                                        500
      6
               6
                                                     (100, 100)
                    logistic
                                                                        500
           early_stopping
                            train_score
                                                time
      10
                      True
                                0.722274
                                            1.841020
      8
                      True
                                0.718311
                                            1.864872
      14
                      True
                                0.709680
                                            3.166287
      18
                      True
                                0.700325
                                            4.686566
      2
                      True
                                0.698407
                                            0.960957
      0
                      True
                                0.696545
                                            0.717048
      1
                      True
                                0.687407
                                            0.972398
      4
                      True
                                0.683163
                                            1.594779
      7
                      True
                                0.681408
                                            1.252844
      11
                      True
                                0.676987
                                            1.261975
      12
                      True
                                0.673400
                                            2.784359
      19
                      True
                                            3.622228
                                0.641668
      15
                      True
                                0.638442
                                            2.049415
      17
                      True
                                           10.380034
                                0.460923
      13
                      True
                                0.409403
                                            4.141897
      5
                      True
                                            0.842226
                                0.401997
      9
                      True
                                0.281989
                                            1.633010
      16
                      True
                                0.043660
                                            0.810340
      3
                      True
                                0.039858
                                            0.124614
      6
                      True
                                0.009941
                                            0.311909
```