

THE DISCRETE NON LOCAL (DNL) RADIATION BOUNDARY CONDITION

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ABSTRACT

A general methodology for developing absorbing boundary conditions is presented [1,10,11]. In the plane case, it is based on a straightforward solution of the system of ODE's that arise from partial discretization in the directions transversal to the artificial boundary. This leads to an eigenvalue problem of the size of the number of degrees of freedom in the lateral discretization. The eigenvalues are classified as in-going or right-going and the absorbing boundary condition consists in imposing a null value for the in-going modes, leaving free the right-going ones. When the classification is straightforward for operators with definite sign, like the Laplace operator, a "virtual dissipative" mechanism has to be added in the mixed case, usually associated with wave propagation phenomena, like the Helmholtz equation, or potential flow with free-surface (the "wave resistance problem"). Numerical examples are presented in two companion papers at this same conference. [2,8].

1. INTRODUCTION

When solving PDE's on unbounded domains by "in volume" discretization methods using finite elements or finite differences, a fictitious boundary has to be introduced somewhere in order to get a bounded computational domain. For elliptic operators with definite sign, like the Laplace operator, enforcing a Dirichlet or Neumann boundary condition on this artificial boundary leads to a well posed problem that converges to the unbounded domain problem. For mixed operators, generally associated with wave phenomena, like the Helmholtz equation or potential flow with a free surface (the wave resistance problem), the limit process of pushing this artificial boundary to infinity may not converge, and some sort of absorbing boundary condition has to be imposed on the artificial boundary.

Artificial boundary conditions are usually devised by fitting the solution on the outer