

Sympy Tutorial

- `sp.init_printing()` is specifically for SymPy mathematical expressions and sets a global display format used to print/display expressions in nice math like format
- `display()` is similar but more versatile and can handle multiple types of objects, but needs to be called explicitly each time (called as *from IPython.display import display*)
- `sympy.symbols()`: core way to create symbolic objects . accepts string containing the names of the symbols you want, separated by spaces or commas. returns the Symbol objects, which you typically assign to Python variables.
- `sympy.var()` :Shortcut for symbols() with automatic assignment, It automatically creates the Symbol objects and assigns them to Python variables with the same names.

```
In [1]: import sympy as sp
import numpy as np
```

```
In [2]: # Define symbolic variables x and y
x,y = sp.symbols('x y')
# printed as y+4 and not any value as its treated a symbolic variable
y+4
# to enable symbolic printing similar to latex ,
# use sympy.init_printing() with display() function
sp.init_printing()
y+4
```

Out[2]: $y + 4$

```
In [3]: print(x**y)
```

x^y

```
In [4]: from IPython.display import display
display(x**y)
display(np.sqrt(2))
display(sp.sqrt(2))
```

x^y

1.4142135623731

$\sqrt{2}$

```
In [5]: x,y = sp.symbols('x y')
display(y*x**2)
```

```
# symbols also works with greek letters
mu, sigma = sp.symbols('mu sigma')
y_guass = 1/(sigma*sp.sqrt(2*sp.pi))*sp.exp(-(x-mu)**2/(2*sigma**2))
display(y_guass)
```

$$x^2y$$

$$\frac{\sqrt{2}e^{-\frac{(-\mu+x)^2}{2\sigma^2}}}{2\sqrt{\pi}\sigma}$$

- using ***sym.subs()***

subs() is a method used to substitute values or expressions into symbolic expressions, thus evaluating symbolic expression at that value

subs(x,2) -> replace x with 2

expr.subs(old, new) - replaces old with new

expr.subs({old1: new1, old2: new2}) - multiple substitutions

```
In [6]: # Define symbolic variables
x, y = sp.symbols('x y')

# Create an expression
expr = x**2 + 2*x + y
display(expr)

# Basic substitution - replace x with 2
# # Returns: 4 + 2*2 + y = 8 + y
display(expr.subs(x, 2) )

# Multiple substitutions using a dictionary
# this is 3^2 + 2*3 + 1 = 9 + 6 + 1 = 16
display(expr.subs({x: 3, y: 1}))

# Substitute expressions
display(expr.subs(x,y))
```

$$x^2 + 2x + y$$

$$y + 8$$

$$16$$

$$y^2 + 3y$$

Why Latex

`display(sp.sqrt(4)*x) # gives 2x and not desired $ \sqrt{4} x`

without using `sp.init_printing`

`display(sp.sqrt(x)*sp.sqrt(x)) # gives x and not desired`

`\sqrt{x} * \sqrt{x}` \$

So, we can use latex for this using `sympy.latex` for printing and evaluating. The `sympy.latex` function in SymPy is used to convert symbolic expressions into LaTeX strings, which can be rendered nicely in Jupyter Notebooks or other environments that support LaTeX rendering.

```
In [7]: # Define symbolic variables
x, y = sp.symbols('x y')
# Create an expression
expr = x**2 + 2*x + y
display(expr) # prints x^{2} + 2 x + y
# display(sp.latex()) dont give correct view
display(sp.latex(expr)) # prints string 'x^{2} + 2 x + y'
#method 2
from IPython.display import display, Math
# Display the LaTeX string using Math and display : display(Math(sp.latex()))
display(Math(sp.latex(expr)))

# suppose want to print latex string 3/4

print('3/4') # prints 3/4
display('3/4') # prints '3/4'
display(sp.latex('3/4')) # prints \\mathtt{\\text{3/4}}
display(Math(sp.latex('3/4'))) # prints 3/4
# use sp.simplify(expr) to convert the string to a sympy expression

display(Math(sp.latex(sp.simplify('3/4')))) # prints correctly
```

$$x^2 + 2x + y$$

`'x^{2} + 2 x + y'`

$$x^2 + 2x + y$$

`3/4`

`'3/4'`

`'\\mathtt{\\text{3/4}}'`

`3/4`

$$\frac{3}{4}$$

Latex tutorial

`*display(Math())*` is used to display a mathematical expression formatted using LaTeX syntax within a notebook cell, allowing you to present complex equations with proper formatting

- for using latex in python code , use `\` , first `\` is used to escape the second `\`

which specifies following latex code, as compared with `\` used in markdown which specifies latex code directly

```
In [ ]: # use sp.latex with display and Math
display(Math('\\sigma = \\mu \\times \\sqrt{5}' ))
```

- using `*sp.symbols, sp.eq*` and `*sp.latex*`

```
In [ ]: # method 2
# create symbols
sigma, mu = sp.symbols('sigma mu')
# Create the equation using sp.Eq
expr = sp.Eq(sigma, mu * sp.sqrt(5))
# use sp.latex with display and Math
display(Math(sp.latex(expr, order='old')))
# display sqrtx * sqrt x
display(Math('\\sqrt{x} \\times \\sqrt{x} {or} \\sqrt{x} \\sqrt{x}'))
# display fractions: \\frac{numerator}{denominator}
display(Math('\\frac{3}{4}'))
# markdown in latex: use \\text{markdown}
display(Math('\\text{The answer is } \\frac{1}{2} \\text{.}'))
```

- Note :In following expression, The symbols `*x, y, m, n, k, +, -*`,

subscripts (`*_`), and superscripts (`^*`) are all directly understood by LaTeX without needing a backslash., so there is no need of `\`

```
In [ ]: # display subscript: use _to beSubscripted
display(Math('x_{mm}'))
# display more chars in subscript: _{to beSubscripted}
display(Math('x_{mm}'))
# display superscript : ^{to beSuperscripted}
display(Math('x_{mm} + y^{n+2k-15}'))
```

- write text as is in latex:

The `*\text{*}` command tells LaTeX to treat the content inside the curly braces as normal text.

```
In [21]: display(Math(r'\text{The area of a circle is } A = \pi r^2'))
```

The area of a circle is $A = \pi r^2$

- Latex in markdown cell: here, we dont use \ for latex but single quote and dollar sign

so, we write

dollar \sigma = \mu \times \sqrt{5} dollar

$$\sigma = \mu \times \sqrt{5}$$

some common latex commands

Math	LaTeX	Example	Output
Fraction	<code>\frac{}{}</code>	<code>P(A)=\frac{n(A)}{n(U)}</code>	$P(A) = \frac{n(A)}{n(U)}$
Square root	<code>\sqrt{}</code>	<code>\sqrt{x+y}</code>	$\sqrt{x+y}$
Superscript	<code>u^n</code>	<code>u_n=u_1r^{n-1}</code>	$u_n = u_1 r^{n-1}$
Subscript	<code>u_n</code>	<code>u_n=u_1+(n-1)d</code>	$u_n = u_1 + (n-1)d$
Greek letters	<code>\alpha</code>	<code>\alpha \beta \pi \Gamma</code>	$\alpha \beta \pi \Gamma$
Text	<code>\text{}</code>	<code>A=\pi r^2\text{ ,where r is the radius}</code>	$A = \pi r^2$,where r is the radius
Sigma	<code>\sum</code>	<code>n=\sum \limits_{i=1}^{\infty} f_i</code>	$n = \sum_{i=1}^{\infty} f_i$
Limit	<code>\lim</code>	<code>\lim \limits_{x \rightarrow \infty}</code>	$\lim_{x \rightarrow \infty}$
Integration	<code>\int</code>	<code>\int \limits_a^b x^2 dx</code>	$\int_a^b x^2 dx$
Trig	<code>\sin</code>	<code>\sin()</code>	$\sin(x+y)$
Comparison	<code>\leq</code>	<code>\leq \geq \approx \neq</code>	$\leq \geq \approx \neq$
Overline	<code>\overline{}</code>	<code>\overline{x}</code>	\bar{x}
Tilde ~	<code>\sim</code>	<code>X\sim N(\mu, \sigma^2)</code>	$X \sim N(\mu, \sigma^2)$
Number sets	<code>\mathbb{}</code>	<code>\mathbb{I, R, Q, N, Z}</code>	$\mathbb{I, R, Q, N, Z}$

write command to display the following

$$\text{With } x = -2, \quad x^2 + 4 \Rightarrow -2^2 + 4 = 8$$

$$\text{With } x = -1, \quad x^2 + 4 \Rightarrow -1^2 + 4 = 5$$

$$\text{With } x = 0, \quad x^2 + 4 \Rightarrow 0^2 + 4 = 4$$

$$\text{With } x = 1, \quad x^2 + 4 \Rightarrow 1^2 + 4 = 5$$

$$\text{With } x = 2, \quad x^2 + 4 \Rightarrow 2^2 + 4 = 8$$

second way to display

$$\text{With } x = -2, \quad x^2 + 4 \Rightarrow -2^2 + 4 = 8$$

$$\text{With } x = -1, \quad x^2 + 4 \Rightarrow -1^2 + 4 = 5$$

$$\text{With } x = 0, \quad x^2 + 4 \Rightarrow 0^2 + 4 = 4$$

$$\text{With } x = 1, \quad x^2 + 4 \Rightarrow 1^2 + 4 = 5$$

$$\text{With } x = 2, \quad x^2 + 4 \Rightarrow 2^2 + 4 = 8$$

```
In [22]: expr = x**2 + 4
for i in range(-2, 3):
    display(Math('\text{With } x=%g, \quad x^2+4 \quad \Rightarrow \quad %g^2+4 = %g' % (i, i, expr.subs(x,i))))
    # breakdown

# Constructs a formatted string using
# # Math('\text{With } x=%g, \quad x^2+4 \quad \Rightarrow \quad %g^2+4 = %g' % (i, i, expr.subs(x,i)))
# # This string uses LaTeX notation to create a
# # nicely formatted mathematical expression. The %g placeholders are replaced with the result of the expression with x replaced by i.

# The \text{} command tells LaTeX to treat the content inside the curly braces
# x=%g, when combined with the first i in % (i, i, expr.subs(x,i)) part, gives
# %g^2+4, when combined with the second i in % (i, i, expr.subs(x,i)) part, gives
# %g, when combined with the expr.subs(x,i) in % (i, i, expr.subs(x,i)) part,
# with #expr.subs(x, i) calculating the result of the expression with x replaced by i.
print("second way to display")
for i in range(-2, 3):
    ans = (x**2 + 4).subs(x, i)
    display(Math('\text{With } x=%g, \quad x^2+4 \quad \Rightarrow \quad %g^2+4 = %g' % (i, i, ans)))
```

$$\text{With } x = -2, \quad x^2 + 4 \Rightarrow -2^2 + 4 = 8$$

With $x = -1$, $x^2 + 4 \Rightarrow -1^2 + 4 = 5$

With $x = 0$, $x^2 + 4 \Rightarrow 0^2 + 4 = 4$

With $x = 1$, $x^2 + 4 \Rightarrow 1^2 + 4 = 5$

With $x = 2$, $x^2 + 4 \Rightarrow 2^2 + 4 = 8$

second way to display

With $x = -2$, $x^2 + 4 \Rightarrow -2^2 + 4 = 8$

With $x = -1$, $x^2 + 4 \Rightarrow -1^2 + 4 = 5$

With $x = 0$, $x^2 + 4 \Rightarrow 0^2 + 4 = 4$

With $x = 1$, $x^2 + 4 \Rightarrow 1^2 + 4 = 5$

With $x = 2$, $x^2 + 4 \Rightarrow 2^2 + 4 = 8$

- solve these exercises

LaTeX exercises

1) $4x + 5y - 8z = 17$

2) $\sin(2\pi ft + \theta)$

3) $e = mc^2$

4) $\frac{4 + 5x^2}{(1 + x)(1 - x)}$

```
In [35]: display(Math('4*x + 5*y -8*z = 17'))  
display(Math('\\sin(2\\pi f t + \\theta)'))
```

```
display(Math('e=mc^2'))
display(Math('\\frac{4+5x^2}{(1+x)(1-x)}'))
```

$$4 * x + 5 * y - 8 * z = 17$$

$$\sin(2\pi ft + \theta)$$

$$e = mc^2$$

$$\frac{4 + 5x^2}{(1 + x)(1 - x)}$$