

DAY-12 TASK

Measurement and wave function collapse

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} + V\psi = i\hbar \frac{\partial \psi}{\partial t}$$

$$\psi_{jk} \longrightarrow \psi_{j,k+1}$$

When you measure...

1. You find an eigenvalue.
2. ψ becomes an eigenstate.

Collapse of wave function

eg: = speed

Position X

$|x_0\rangle$ = Position
eigenstate w/
eigenvalue x_0

$$X|x_0\rangle = x_0|x_0\rangle$$

$$|x_0\rangle = \delta(x - x_0)$$

Momentum P

$|p_0\rangle$ = Momentum eigenstate
w/
eigenvalue p_0

$$P|p_0\rangle = p_0|p_0\rangle$$

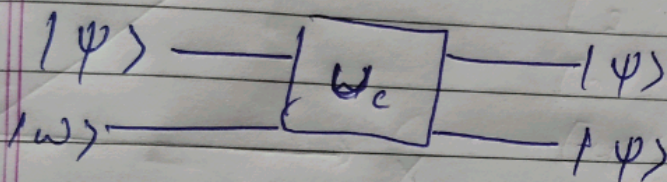
$$|p_0\rangle = e^{ip_0 x / \hbar}$$

$$P = \frac{\hbar}{i} \frac{\partial}{\partial x}$$

$$\frac{\hbar}{i} \frac{\partial}{\partial x} e^{ip_0 x / \hbar} = \frac{\hbar}{i} \frac{i p_0}{\hbar} e^{ip_0 x / \hbar}$$

No Cloning Theorem.

There is no unitary operator that clones arbitrary qubit.



$$|\omega\rangle = |0\rangle$$

$$U_c |\psi\rangle |0\rangle = |\psi\rangle |\psi\rangle$$

All unitary operators are linear.

$$U_c (a|\psi\rangle + b|\psi\rangle)$$

$$= a U_c |\psi\rangle + b U_c |\psi\rangle$$

$$\hookrightarrow |\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

$$|\psi\rangle|0\rangle = \alpha|00\rangle + \beta|11\rangle$$

$$U_c (\alpha|00\rangle + \beta|11\rangle) = \alpha U_c |00\rangle + \beta U_c |11\rangle$$