



Norwegian University  
of Life Sciences

Master's Thesis 2018 60 ECTS

Norwegian University of Life Sciences  
Faculty of Chemistry, Biotechnology and Food Science

# **On the Application of Machine Learning Techniques for Phenotypic Clustering and Classification of Heart Failure Patients**

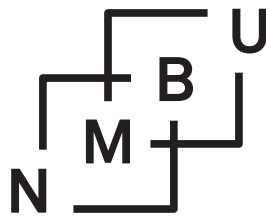
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Master of Science in Bioinformatics and Applied Statistics



# **On the Application of Machine Learning Techniques for Phenotypic Clustering and Classification of Heart Failure Patients**

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**Thesis submitted for the degree of**  
*Master of Science in Bioinformatics  
and Applied Statistics*

**Norwegian University of Life Sciences**

**November 13, 2018**



# Abstract

In this thesis, we attempt to investigate how well various clustering algorithms (hierarchical clustering, k-means and expectation–maximization) perform in producing phenotypically distinct clinical patient groups (i.e. phenomapping) with heart failure with preserved ejection fraction (HFpEF) and mid-range ejection fraction (HFmrEF). Furthermore, we evaluate the performance of various classification algorithms (k-nearest neighbours, logistic regression, naive Bayes, linear discriminant analysis, support vector machines and random forest) in predicting patient mortality and readmission. All the algorithms were applied on a data set consisting of 375 patients with symptomatic heart failure (HF) identified at a tertiary hospital in the United Kingdom.

In the cluster analysis, we found that the hierarchical and k-means algorithms show signs of clustering more mutually exclusive patient groups with HF compared to the physicians. Overall the patient groups produced by these algorithms had 62 significantly different baseline characteristics compared to 59 produced by the physicians.

In the classification of mortality and readmission, we found that the random forest and logistic regression show promising potential. That is, the level of accuracy for which the algorithms predicted mortality and readmission rank high compared to the other algorithms evaluated. The random forest predicted mortality with 72% accuracy and readmission with 99.7%. The logistic regression had similar results with approximately 67% accuracy for mortality and 97.5% for readmission. Similar results are reported in the literature. Our findings lend support to the idea that the application of such algorithms may help in better understanding the complex nature of a clinical syndrome such as HF.



# Acknowledgments

Firstly, I would like to thank my supervisors, Ulf Geir Indahl and Kristin Tøndel, for helpful guidance throughout the process of writing my thesis. They have always been available to answer my questions and their many comments and suggestions have certainly been of great help. They have shown great patience and for that I am truly thankful.

I would also like to thank my family for the support which they have shown over the years. I would especially like to thank my sister for proofreading and much good advice.

Lastly, I would like to thank all my friends from the university for making studying for this degree a memorable experience.

All errors or ambiguities are solely my responsibility.

**Samir Adrik**

Ås, November 13, 2018





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# Chapter 1

## Introduction

Heart failure (HF) is a clinical syndrome typically associated with high prevalence, high mortality, frequent hospitalization and overall reduced quality of life (QoL). Approximately 65 million people are effected by HF globally ([Hay et al., 2017](#)). With an aging population, it is expected that the prevalence of HF is to increase. In developed countries, about 3-5% of hospital admissions are linked with HF, accounting for about 2% of the total health cost ([Tripoliti et al., 2017](#)). It is not unusual for HF to be characterized as a global pandemic with prognosis being worse than that of most cancers, see e.g. [Braunwald \(2015\)](#) and [Savarese and Lund \(2017\)](#).

In terms of clinical classification, there is no single "universally agreed upon" system for classifying the causes of HF. Typically HF manifests itself as at least two major subtypes ([Alonso-Betanzos et al., 2015](#)). All being commonly distinguished based on measures of the left ventricle ejection fraction (LVEF)<sup>1</sup>. The first subtype encompasses patients with LVEF values larger or equal to 50%. These patients are characterized as having HF with preserved ejection fraction (HEpEF). The second subtype includes patients with LVEF values less than 40%, and are characterized as having HF with reduced ejection fraction (HErEF). However, the European Society of Cardiology (ESC) recently defined a third subtype with patients belong to the "gray zone" or the "the middle child", namely when the LVEF values

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<sup>1</sup>Fraction of blood ejected from the left ventricle of the heart with each contraction. Calculated as the left ventricle stroke volume (LVSV) divided by the left ventricle end-diastolic volume (LVEDV), i.e.  $LVEF = LVSV / LVEDV$  ([Cikes and Solomon, 2015](#))

lies between 40% and 49%<sup>2</sup>. These patients are defined as having HF with mid-range ejection fraction (HFmrEF), see e.g. [Lam and Solomon \(2014\)](#) and [Ponikowski et al. \(2016\)](#). Clinically clustering patients according to HF subtypes and identifying HF patients most at risk of mortality and readmission is something that remains challenging. Especially considering that the 1-year mortality rates for acute HF across different regions in Europa ranges from 21.6% to 36.5% (35.1% - 37.5% in the US), see e.g. [Cheng et al. \(2014\)](#), [Inamdar and Inamdar \(2016\)](#) and [Crespo-Leiro et al. \(2016\)](#). Patients with HFmrEF have also a clinical profile and prognosis that is close to those of HFpEF who have LVEF values considered to be normal. Current therapies have also shown to be unable to reduce *both* morbidity and mortality in patients with HFmrEF and HFpEF, see e.g. [Ponikowski et al. \(2016\)](#) and [Hsu et al. \(2017\)](#). All of which makes the overall job of identifying and distinguishing these patients challenging. It is also unknown if improving phenotypic classification is clinically useful or even possible ([Shah et al., 2014](#)).

Nonetheless, the rapid increase in available medical data on patients has led to machine learning (ML) techniques gaining widespread attention by researchers. The application of such techniques is one that *may* offer an opportunity to build better management strategies, as well as early detection and better prediction of adverse effects associated with HF. Of the ML techniques gaining most attention, one typically finds *clustering* and *classification* methods being intensely studied. Accordingly, the use of these ML techniques to identify distinct patient groups with *post-diagnosed* HFmrEF and HFpEF most at risk of mortality and readmission, is one we will try to examine to its full potential.

## 1.1 Problem statement

In this thesis, we investigate how well various clustering algorithms (hierarchical clustering, k-means and expectation-maximization) perform in producing phenotypically distinct clinical patient groups (i.e. phenomapping) with HFpEF and HFmrEF. Furthermore, we evaluate the performance of various classification algorithms (k-nearest neighbours, logistic regression,

<sup>2</sup>The American College of Cardiology Foundation/American Heart Association (ACC/AHA) were the first to define HF with borderline ejection fraction as being patients with LVEF values between 41% to 49% ([Yancy et al., 2013](#)).

naive Bayes, linear discriminant analysis, support vector machines and random forest) in predicting the clinical outcomes mortality and readmission among the patients studied. When evaluating the results, we compare the clusters according to their level homogeneity, i.e. the number of significantly different baseline characteristics between each patient group and rank methods accordingly. For the classification of the clinical outcomes, we evaluate the estimations based on the classification accuracy and Cohen's Kappa. The algorithms are validated with 10-fold cross-validation in order to rank methods accordingly. All the models and techniques are applied on a data set consisting of 375 patients with symptomatic HF identified at a tertiary hospital in the United Kingdom.

## 1.2 Thesis structure

The thesis is divided into five chapters and proceeds as follows: The next chapter (2) reviews the literature related to the application of ML techniques for the assessment of heart failure. This is done to put the proposed research in a relevant context. Chapter (3) details the methodology, including presenting the data and the quality of the data. Preliminary analysis of the data will also be done in this chapter. This includes evaluating and treating the data set based on methods of imputation and dimensional reduction. Next, chapter (4) presents the results of the clustering comparisons and the prediction accuracy of the clinical outcomes classification, with conclusive remarks found in chapter (5). The source code and relevant statistical output can be found in the appendix.



# Chapter 2

## Background

The following chapter presents a thorough treatment of the literature on the application of ML techniques for the assessment of heart failure<sup>1</sup>. Important topics such as HF detection, subtype estimation and prediction of clinical outcomes in the context of ML will be presented and explained.

### 2.1 HF detection

The ESC defines HF as a clinical syndrome caused by structural and/or functional cardiac abnormality, resulting in a reduced cardiac output (CO) and/or elevated intracardiac pressures at rest or during stress. It is typically characterized by symptoms, such as breathlessness, ankle swelling and fatigue that may be accompanied by signs, such as elevated jugular venous pressure (JVP), pulmonary crackles and peripheral oedema (swelling in lower limbs) ([Ponikowski et al., 2016](#)). HF prevents the heart from fulfilling the circulatory demands from the body, due to its impairing abilities on the ventricles to maintain the bodies hemodynamics (blood flow). As there is no broad definitive industry accepted diagnostic test for HF, one finds in clinical practice that medical diagnosis is done with a combination of careful examinations (physical and historical) with assisting tests, such as blood tests, chest radiography (chest X-ray, CXR), electrocardiography (EKG) and echocardiography (cardiac echo), see e.g. [Henein \(2010\)](#) and [Son et al. \(2012\)](#). As a result of this, several criteria for determining the presence of HF have

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<sup>1</sup>We highly recommend reading [Tripoliti et al. \(2017\)](#) for a broader overview of the literature on the state-of-the-art ML techniques applied for the assessment of heart failure.

been proposed, including the Framingham criteria (McKee et al., 1971), the Boston criteria (Carlson et al., 1985), the Gothenburg criteria (Eriksson et al., 1987) and the ESC criteria (Swedberg et al., 2005) (Roger, 2010). All of which are much used in clinical practise.

In a non-acute onset, the ESC has also defined an algorithm for diagnosing HF (Ponikowski et al., 2016). The algorithm is structured in the following way: First, the probability of HF ( $\hat{p}_{HF}$ ) is evaluated along three dimensions:

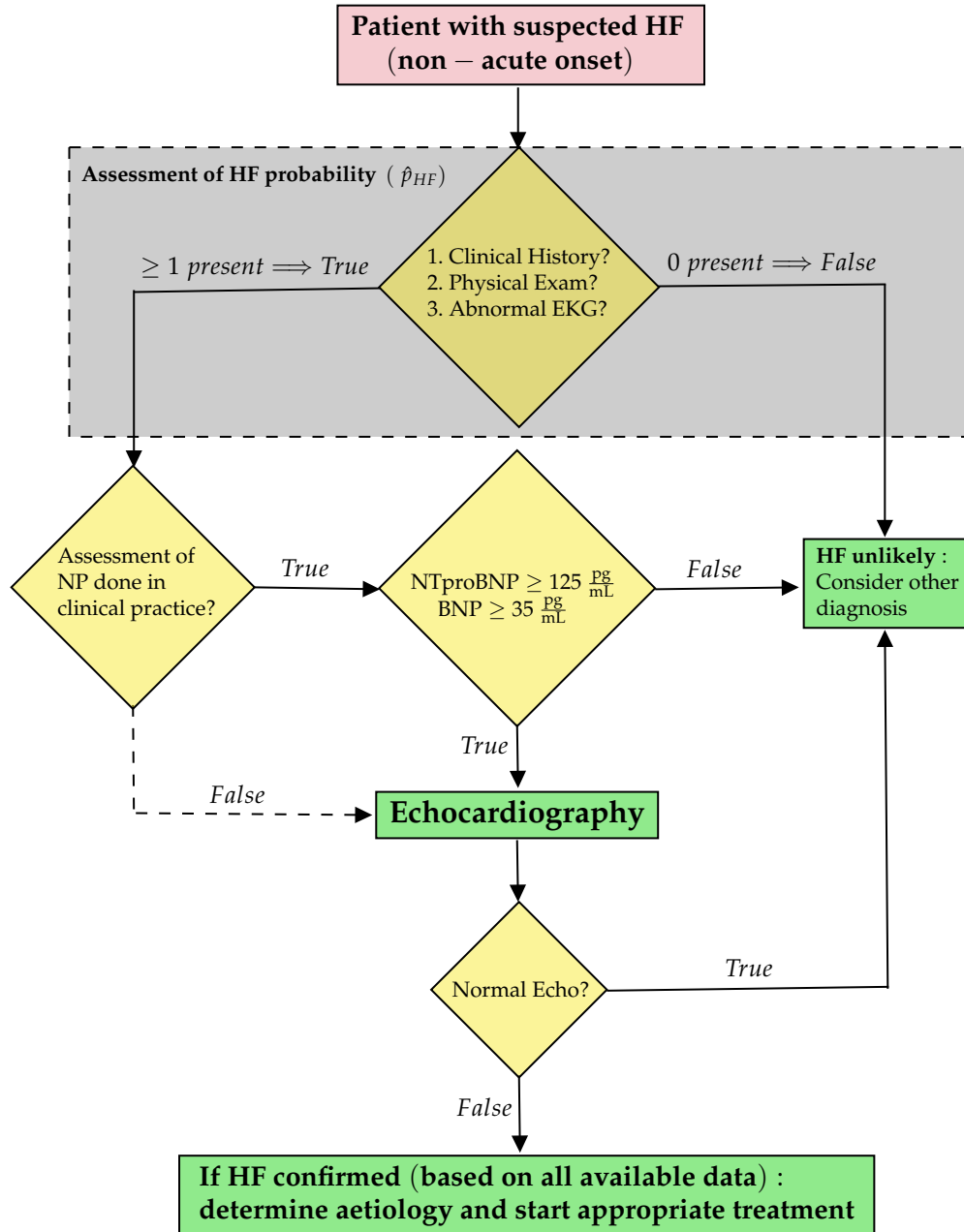
- (i) **Prior clinical history:** History of coronary artery disease (CAD) or arterial hypertension, exposition to cardiotoxic drugs/ radiation, diuretic use (any substance that promotes the production of urine) or orthopnea (shortness of breath when lying down)
- (ii) **Physical examination:** Crackles/rales, bilateral ankle oedema (swelling in both ankles), abnormal heart sounds/murmur, jugular venous dilatation, laterally displaced/broadened apical beat (pulse felt at the point of maximum impulse (PMI))
- (iii) **Abnormalities in electrocardiography (EKG)**

If all elements along the three dimensions are normal/absent,  $\hat{p}_{HF}$  is estimated to be highly unlikely. If at least one element is abnormal, then plasma Natriuretic Peptides (NP)<sup>2</sup> should be measured in order to identify patients who need echocardiography. Specifically, if the NP values are above the exclusion threshold<sup>3</sup> or should the assessment of NPs not be routinely done in clinical practice then patients need to be forwarded for an echocardiography. With the help of the cardiac echo, specialist can detect abnormalities in the heart rhythm. Should the results of the plasma NP or the echocardiography be normal<sup>4</sup>, then HF is also considered unlikely. Should the results of the echo yield any abnormal results, appropriate HF treatment should be initiated. The structure of the ESC algorithm is

<sup>2</sup>A hormone, mainly secreted from the heart, that has important natriuretic and kaliuretic properties (excretion of sodium and potassium in the urine) (Pandit et al., 2011). In clinical practice it is found that brain NP (also called BNP) levels can be used to predict the risk of death and cardiovascular events (Wang et al., 2004).

<sup>3</sup>The recommended threshold levels are BNP levels  $\geq 35pg/mL$  or NTproBNP levels  $\geq 125pg/mL$ , see e.g. Cowie et al. (1997), Yamamoto et al. (2000), Krishnaswamy et al. (2001), Zaphiriou et al. (2005), Fuat et al. (2006) and Maisel et al. (2008).

<sup>4</sup>Normal ventricular and atrial volumes and function (Aune et al., 2009).



**Figure 2.1:** ESC diagnostic algorithm for the diagnosis of heart failure of non-acute onset (Ponikowski *et al.*, 2016, page. 2141).

illustrated in the flow chart in Figure (2.1). Being that the ESC algorithm is much used in clinical practice throughout the world, there is research that suggest that the medical and economic benefits of applying ML in the detection of HF should not be ignored. In the context of diagnosing patients with HF, the benefits typically include: (i) less time consumption, (ii) more support (large global community of ML practitioners in business and academia) and (iii) same level of accuracy as conventional tools when applied on available data. Many ML methods used to detect HF as a statistical learning problem, fall in the category of *supervised* statistical learning (see section 2.2.1). The relevant ones include expressing the detection of HF as a two class classification problem, where the presence of HF is the output of the classifiers. Methods including logistic regression, linear discriminant analysis (LDA), Bayesian classifier, k-nearest neighbours (k-NN), random forests (RF), boosting, support vector machines (SVM) and neural networks (NN) are all very popular. As the response variable of the classification problem is categorical, most ML studies tend to use measures of heart rate variability (HRV)<sup>5</sup> as the main predictors for distinguishing patients as normal or with HF (Tripoliti et al., 2017). Other predictors include parameters from clinical tests (i.e. blood test, echo, EKG, chest radiography), clinical variables (e.g. gender, age, blood pressure, smoking habit) and other lab-

**Table 2.1:** Literature review of HF detection

Author	HRV?	Method	Data	Features	Evaluation
Masetic and Subasi (2016)	False	SVM, k-NN, NN, RF	$N = 28$ (13 normal and 15 HF)	Response: Normal & HF. Predictor: Features extracted by EKG.	SVM: Accuracy: 99.53% k-NN: Accuracy: 99.93% NN: Accuracy: 99.20% RF: Accuracy: 100.00%  Validation: 10-fold cross validation

<sup>5</sup>HRV is the amount of heart rate fluctuations around the mean heart rate (van Ravenswaaij-Arts et al., 1993). The HRV can be assessed using R-waves produced by an EKG and reduced HRV is typically an established sign of HF (Ernst, 2016).

**Table 2.1:** Literature review of HF detection (*continued*)

Author	HRV?	Method	Data	Features	Evaluation
<a href="#">Liu et al. (2014)</a>	True	SVM, k-NN	$N = 47$ (30 normal and 17 HF)	Response: Normal & HF. Predictor: Short term HRV measure (ST-HRV)	SVM: Accuracy: 100.00% Validation: Cross-validation
<a href="#">Narin et al. (2014)</a>	True	SVM, k-NN, LDA, NN	$N = 83$ (54 normal and 29 HF)	Response: Normal & HF. Predictor: ST-HRV	SVM: Accuracy: 91.56% k-NN: Accuracy: 85.54% LDA: Accuracy: 85.54% NN: Accuracy: 89.15%  Validation: Leave-one-out cross validation.
<a href="#">Gharehchopogh and Khalifelu (2011)</a>	False	NN	$N = 40$ (26 normal and 14 HF)	Response: Normal & HF. Predictor: Gender, age, blood pressure, smoking habits.	NN: Accuracy: 95.00% Validation: Testing set.
<a href="#">Yang et al. (2010)</a>	False	Naive-Bayes, SVM, NNC	$N = 153$ (58 Normal, 30 HF-prone, 65 HF)	Response: Non-HF group (Health or HF-prone) & HF. Predictor: clinical test results	SVM: Accuracy: 74.40% Validation: Test set of $N = 90$ subjects

oratory findings. Relevant articles where one applies ML techniques to address the statistical learning problem of detecting patients with HF is shown in table (2.1). Some common evaluation measures used in such research include: sensitivity (true positive rate), specificity (true negative rate), accuracy<sup>6</sup> and Cohen's kappa  $\kappa$  (Cohen, 1960). The accuracy is the only evaluation measure reported in Table (2.1). We also need to emphasize that as this particular statistical learning problem (i.e. detection of HF) is outside of the scope of the problem statement mentioned in chapter (1), we will not be pursuing a further literature review of this problem. However, we highly recommend reading the likes of Tripoliti et al. (2017), Acharya et al. (2017) or Awan et al. (2018), for a more up-to-date overview of the literature on ML used for HF detection.

## 2.2 Subtype estimation

According to the ESC algorithm (Figure 2.1), once HF is confirmed and the probability of HF is assessed and estimated to be likely, the next step is to estimate the causes (aetiology) and the subtype of HF. The main definition of HF subtypes is based on historical research. Most of the research done after the 1990s emphasize estimating the subtype of HF patients based on the measure of the left ventricle ejection fraction (LVEF). The two usual ways of obtaining the LVEF values are through an echocardiography or cardiac magnetic resonance imaging (CMR or cardiac MR) (Ponikowski et al., 2016). In prior guidelines presented by the ESC, HF<sub>r</sub>EF and HF<sub>p</sub>EF were the two main subtypes of HF (McMurray et al., 2012). The ESC did however acknowledge that a gray zone existed between the two. As a result of this a new subtype was introduced, namely HF<sub>mr</sub>EF. The ESC did so in hopes of stimulating research into the underlying characteristics, pathophysiology and treatment of this group of patients (Ponikowski et al., 2016). Details about the criteria for the various HF subtypes are shown in Table (2.2). The differences between HF<sub>mr</sub>EF and HF<sub>p</sub>EF are difficult to distinguish. As mentioned, these two groups were previously classified as HF<sub>p</sub>EF. Diagnosing HF<sub>p</sub>EF is a very complex process with the diagnosis of chronic HF<sub>p</sub>EF being especially cumbersome in elderly patients with one or more additional diseases (comorbidity). With the exception of the LVEF

<sup>6</sup>The fraction/proportion of true positives (*sensitivity*) or true negatives (*specificity*) correctly identified (James et al., 2013).

**Table 2.2:** HF subtypes based on LVEF (Ponikowski et al., 2016, page. 2137)

Criteria	HFrEF	HFmrEF	HFpEF
1	Symptoms $\pm$ Signs	Symptoms $\pm$ Signs	Symptoms $\pm$ Signs
2	LVEF $< 40\%$	$40 \leq \text{LVEF} < 50$	$50 \leq \text{LVEF}$
3	–	1. Elevated NP levels (fig 2.1) 2. At least one additional criteria: a) Relevant structural heart disease <sup>7</sup> b) Diastolic dysfunction <sup>8</sup>	1. Elevated NP levels (fig 2.1) 2. At least one additional criteria: a) Relevant structural heart disease b) Diastolic dysfunction

values, signs and symptoms between HFmrEF and HFpEF are often non-specific and do not discriminate well between other clinical conditions. LVEF  $\geq 50\%$  is also considered to be normal. The ECS has also underlined the difficulties with an emphasis on the LVEF as the main discriminant between HFmrEF and HFpEF. The cut-off at 50% is set arbitrary and in clinical trials patients with LVEF between 40% and 49% are often classified as HFpEF, see e.g. Kelly et al. (2015) and Ponikowski et al. (2016). The ESC places an emphasis on additional objective measures of cardiac dysfunction in order to sufficiently discriminate the two subtypes, but currently no gold standard exists. The hope of stimulating more research into the characteristics of the patient group HFmrEF has fuelled much research into the application of ML, to further advance the literature. The appeal from the ESC into further research has also served as a motivation for much of the research done. We have organized the literature review of the “state-of-the-art” research into two parts and have structured the literature based on the statistical learning problem category, i.e. supervised or unsupervised.

<sup>7</sup>Left ventricular hypertrophy (LVH): Thickening of the heart muscle of the left ventricle of the heart and/or Left atrial enlargement (LAE): Enlargement of the left atrium (LA) of the heart (Nagueh et al., 2009)

<sup>8</sup>Increased resistance to diastolic filling of one or both cardiac ventricles. In addition to structural abnormalities, physiological derangement of myocardial inactivation and relaxation (Grossman, 1990).

### 2.2.1 Supervised learning

In this thesis we use the terms *machine learning* (ML) and *statistical learning* (SL) interchangeably. Even though the two are very closely linked, they do differ in terms of emphasis and terminology. ML is defined as “a set of methods that can automatically detect patterns in data, and then use the uncovered patterns to predict future data, or to perform other kinds of decision making under uncertainty” (Murphy, 2012). SL on the other hand is often considered to be the statistical framework of ML, and emphasize the importance of building *probabilistic* models for the analysis and prediction of data in order to draw inference, see e.g. Friedman et al. (2009), Murphy (2012), James et al. (2013) and Wasserman (2013). Individuals of both camps (i.e. computer scientists and statisticians) often use different language for the same thing. In this thesis we refer to the underlying learning problem to be solved by a given algorithm as a statistical learning problem. The actual algorithms used to solve the SL problem are referred to as ML methods/algorithms<sup>9</sup>. This is done in an effort to reduce confusion among the readers.

Most SL problems fall into one of two main categories, i.e. *supervised* and *unsupervised* learning, see e.g. Friedman et al. (2009) and James et al. (2013)<sup>10</sup>. The example of detecting HF we discussed in section (2.1) is typically a learning problem that falls into the supervised learning domain. For each predictor(s) (input(s) or independent variable(s))  $x_i, i = 1, \dots, n$  there is an associated response (output or dependent variable),  $y_i$ . The objective of supervised learning is to fit a model that relates the response ( $y_i$ ) to the predictors ( $x_i$ ) (James et al., 2013). Supervised learning is the most common category of SL problem in practice. Of the ML methods most used to solve supervised SL problems, one typically mentions *classification*. The goal of classification is to learn a mapping from the predictors ( $x_i$ ) to the response ( $y_i$ ), where  $y \in \{1, \dots, C\}$ , with  $C$  being the number of classes. We can formalize classification as a SL problem by referring to it as a functional approximation problem. We assume that a functional form  $y = f(\mathbf{x})$  exists for some unknown function  $f$ , and the goal of the learning process is to estimate  $f$  given a training set with labeled and known values. We can then use the estimated function  $\hat{y} = \hat{f}(\mathbf{x})$  to make predictions on a testing / validation set (Murphy, 2012).

<sup>9</sup>We need to emphasize that the methods can also be called statistical learning methods/algorithms as they are often done so in the literature.

<sup>10</sup>The categories are also referred to as the two main types of ML, see e.g. Murphy (2012)



The application of classification to estimate HF subtypes is a relatively new approach. HF subtype estimation using ML in earlier research have similarities with HF detection. Both subjects reduce the classification problem to a two class classification problem with the assumption that the predicted responses are mutually exclusive. As  $C = 2$ , one often calls this a *binary classification* problem. In which case one often assumes that  $y \in \{0, 1\}$  (Murphy, 2012). Prior to the ESC introduction of HFmrEF as a third subtype of HF, most ML research focused on classifying HF patients according to the two common subtypes, i.e. HFrEF and HFpEF. A list of some relevant literature can be found in Table (2.3). Most predictors are features including measures of demographic characteristics, HRV, signs and symptoms, vital signs, results of laboratory investigations and previous medical history. Methods include bagging, boosting, random forest, supp-

**Table 2.3:** Literature review of HF subtype classification

Author	Method	Data	Features	Evaluation
<a href="#">Austin et al. (2013)</a>	Bagging, Boosting, RF, SVM	$N = 8212$ (3697 for training, 4515 for testing)	Response: HFrEF & HFpEF. Predictor: Demographics, vital signs, symptoms, lab investigation and prev. history.	Bagging: Sensitivity: 45.1% Specificity: 84.9% Boosting: Sensitivity: 87.6% Specificity: 45.3% Random Forest: Sensitivity: 37.8% Specificity: 89.7% SVM: Sensitivity: 40.1% Specificity: 88.7%  Validation: Testing set of 8339 subjects

**Table 2.3:** Literature review of HF subtype classification (*continued*)

Author	Method	Data	Features	Evaluation
<a href="#">Alonso-Betanzos et al. (2015)</a>	Naive-Bayes, SVM, NNC	$N = 111$ (48 for training, 63 Monte Carlo simulated instances for testing)	Response: HFrEF & HFpEF. Predictor: End-systolic Volume Index.	Naive-Bayes: Train error: 4.14% Test error: 9.52% SVM: Train error: 2.08% Test error: 4.76% NNC (ib1, see <a href="#">Aha et al. (1991)</a> ): Train error: 2.08% Test error: 4.76%  Validation: Testing set of 63 instances. 10-fold cross validation.
<a href="#">Isler (2016)</a>	k-NN, NN	$N = 30$ (18 with HFrEF & 12 with HFpEF)	Response: HFrEF & HFpEF. Predictor: Short term HRV measures	k-NN: Sensitivity: 87.5% Specificity: 91.07% Accuracy: 89.29% NN: Sensitivity: 93.75% Specificity: 100.00% Accuracy: 96.43%  Validation: Leave-one-out cross-validation.

ort vector machines (SVM), naive-Bayes, nearest neighbour classifiers (NNC), k-nearest neighbours (k-NN) and neural networks (NN). As classification methods are much used in the literature for HF subtype estimation, we reserve the use of these methods in a later section dealing with the prediction of clinical outcomes (see section 2.3). Supervised learning methods also assume a priori that there exists a response  $y_i$  with a predefined number of classes ( $C$ ). Because of this we feel that such an application to the problem of HF subtype estimation would fall outside the scope of the problem statement mentioned in chapter (1). One of the main motivations of this thesis is to investigate how well it is possible to produce pheno-

typically distinct clinical patient groups using dense phenotypic data (i.e. phenomapping). Given the motivation, we seek to better understand the possible relationship between patient groups by placing an assumption of no response variable to supervise our analysis. To answer this question, we turn to the second main category of SL problems, namely unsupervised learning.

### 2.2.2 Unsupervised learning

The main goal of unsupervised learning is to discover hidden structures in the data that are not predefined. Sometimes it's also referred to as *knowledge discovery* and is widely used, as it is arguably more typical for animal and human learning. The formalization of unsupervised learning is often done in the setting of *unconditional density estimation*, i.e. we want to build models of the form  $p(\mathbf{x}_i|\theta)$ . Instead of a conditional setting as done with supervised learning, i.e.  $p(y_i|\mathbf{x}_i, \theta)$ , the use of unsupervised learning is often considered to be more "convenient" than supervised learning, as it does not require an expert to manually label all the data (Murphy, 2012). This convenience is often stated as a major reason for the relevance of unsupervised learning done for distinguishing phenotypical characteristics between HF patient groups. Not to mention that there is no agree-upon measure of what distinguishes HF subtypes (see section 2.2). Furthermore, because of the complex nature and high degree of heterogeneity of HF subtypes such as HFpEF, the sole use of genetic information for helping to *precisely* classify HF subtypes has often been seen as unlikely. Uncertain behavior by weak genetic factors is very probable in eliciting disease phenotypes (Deo, 2015). This additional complexity is avoided by framing the SL problem in the setting of unsupervised learning.

A lot of research has been conducted using unsupervised learning to group HF patients into subtypes with phenotypically distinct characteristics. Of the ML methods most used here, one typically finds *clustering* methods. These methods are designed to find subgroups or *clusters* within a data set. The goal of clustering is to partition the data set into distinct groups with high degree of homogeneity and arranging the clusters into a natural hierarchy (Friedman et al., 2009). A list of the newest literature on the application of clustering methods for phenomapping of HF patients is shown in Table (2.4). Of the clustering methods found here, one can men-

**Table 2.4:** Literature review of HF subtype clustering

Author	Method	Data	Features	Results
<a href="#">Shah et al. (2014)</a>	Hierarchical, model-based clustering	$N = 397$ with HFpEF	67 continuous clinical variables	The analysis revealed 3 distinct pheno-groups.
<a href="#">Ahmad et al. (2014)</a>	Hierarchical clustering (Ward's minimum variance method)	$N = 2331$ (1619 incl., 712 excl.)	45 baseline clinical variables	Four clusters were identified whose patients varied considerably along measures of age, sex, race, symptoms, comorbidities, HF etiology, socio-economic status, quality of life, cardiopulmonary exercise testing parameters, and biomarker levels.
<a href="#">Alonso-Betanzos et al. (2015)</a>	k-Means clustering, EM, SIBA.	3 Data sets: D1: $N = 48$ (13 HFrEF, 35 HFpEF) D2: $n = 63$ (29 HFrEF, 34 HFpEF) D3: $N = 403$ (137 HFrEF, 150 HFpEF)	End-systolic Volume Index, End-diastolic volume index	Algorithms generated dividing patterns
<a href="#">Kao et al. (2015)</a>	Latent class analysis (LCA)	$N = 4113$ with HFpEF	11 prospectively selected clinical features	Identified 6 subgroups of HFpEF patients with significant differences in event-free survival.

**Table 2.4:** Literature review of HF subtype classification (*continued*)

Author	Method	Data	Features	Results
<a href="#">Ahmad et al. (2016)</a>	Hierarchical clustering (Ward's minimum variance method)	$N = 433$ (172 incl.)	29 baseline clinical variables	Four advanced HF clusters were identified.  The analysis was done on patients diagnosed with acute decompensated heart failure (ADHF).
<a href="#">Katz et al. (2017)</a>	Hierarchical clustering, model-based clustering	$N = 1273$	47 continuous clinical variables	Identified 2 distinct groups that differed markedly in clinical characteristics, cardiac structure /function, and indices of cardiac mechanics.

tion hierarchical, k-means and model-based clustering, such as expectation maximization (EM), sequential information bottleneck algorithm (SIBA) and latent class analysis (LCA). Addressing phenomapping within an unsupervised setting started with [Ahmad et al. \(2014\)](#) and [Shah et al. \(2014\)](#). The latter employed the use of hierarchical and penalizing model-based clustering to distinguish HFpEF patients. The analysis was done on 67 continuous variables including clinical, laboratory, electrocardiographic and echocardiographic features. The results suggest that HFpEF patients can be clustered into three distinct pheno-groups with meaningful, clinically relevant categories.

[Ahmad et al. \(2014\)](#) did a similar analysis using 45 baseline clinical variables on a much larger data set consisting of 1619 patients with chronic HF (i.e. both HFrEF and HFpEF). The study identified four clusters of patients which varied considerably along measures of demographics, symptoms and comorbidities. The study underscored the high degree of disease heterogeneity that exists within chronic HF patients and the need for improved phenotyping of the syndrome. [Alonso-Betanzos et al. \(2015\)](#) used a

somewhat different approach for phenomapping HF patient groups. Their objective was to use ML techniques to discriminate between patients with preserved EF and those with reduced EF using the concept of the Volume Regulation Graph (VRG)<sup>11</sup>. The authors evaluated three clustering methods (i.e. k-means, EM and SIBA) and found that the algorithms generated dividing patterns. [Kao et al. \(2015\)](#) used latent class analysis (LCA) on a data set of 4113 HFpEF patients along 11 prospectively selected clinical features. The use of LCA is in many ways different than other clustering algorithms as it does not require continuous variables. It is optimized for analyzing categorical variables and identifies clusters based on several traits rather than a single trait. With the use of LCA the authors identified 6 subgroups of HFpEF patients with significant differences in event-free survival. Other authors like [Katz et al. \(2017\)](#) and [Ahmad et al. \(2016\)](#) have organized their research along different phenomapping objectives. The latter addressed phenomapping on patients diagnosed with acute decompensated heart failure (ADHF), and [Katz et al. \(2017\)](#) on the systemic hypertensive patients with myocardial substrate (i.e. abnormal cardiac mechanics). As the two studies have a different phenomapping objective than the ones mentioned earlier, they still managed to identify four and two respective patient groups with acute ADHF and systemic hypertension with myocardial substrate.

The number of studies done on phenomapping HF patients is eminent and as evident from Table (2.4), the results vary considerably with respect to the optimal number of clusters. This is something that this thesis will try to address by re-evaluating a number of the clustering methods used in the literature, but along a single phenomapping objective. Before that time, we move on to reviewing the literature associated with the second objective of the problem statement, namely predicting clinical outcomes due to HF.

## 2.3 Prediction of clinical outcomes

As we mentioned in chapter (1), HF is a syndrome that globally affects approximately 65 million people ([Hay et al., 2017](#)). In addition to the high prevalence and overall reduced quality of life (QoL), one cannot but

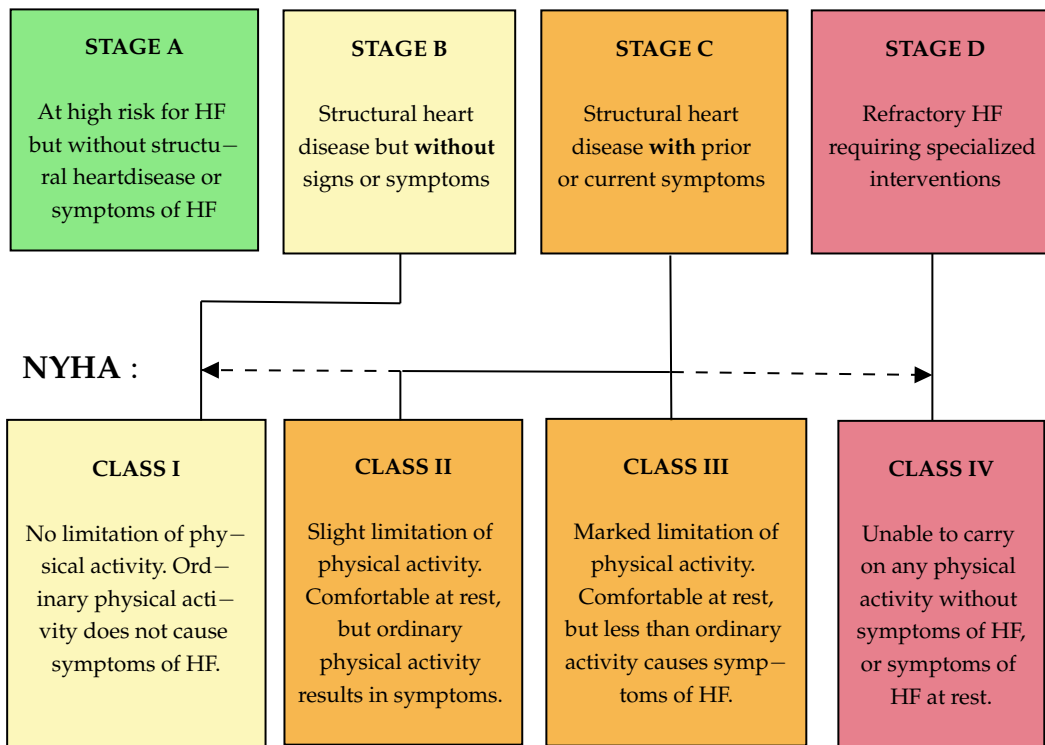
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<sup>11</sup>A graph of ESV versus EDV, which has the clear advantage of yielding (nearly perfect) linear relationships ([Berlinger and Kerkhof, 1998](#)).

mention the many serious clinical outcomes. This includes, but is not limited to mortality, morbidity, destabilization and readmission. These outcomes effect not only the patients and their families, but also the society. The patients and their families are effected by the many constraints that HF places on family life and an overall reduction in QoL. With the emotional dimensions often being more important than the physical dimensions ([Dunderdale et al., 2005](#)), the society is effected by the many economic constraints, such as an increase in the burden and cost of national health care expenditures. The main economic driver of costs related to HF being that of hospitalization, where about 60-70% of HF costs are related to inpatient care and almost 20% to primary care ([Braunwald, 2015](#)). The use of prognostics can assist in the monitoring and treatment of HF patients, with the goal of improving the quality of care and the outcomes of patients hospitalized with HF ([Tripoliti et al., 2017](#)).

Conducting good prognostics is often conditional on estimating the severity of HF for a given patient. Accordingly, the two most used classification systems for the severity estimation, is the New York Heart Association (NYHA) Functional Classification ([NYHA, 1994](#)) and the American College of Cardiology/American Heart Association (ACC/AHA) stages of HF ([Hunt et al., 2001](#)). The NYHA system places the patients in one of four categories based on how much they are limited during physical activity and is based on symptoms as well as physical activity. The ACC/AHA system on the other hand structures HF stages based on structural changes to the heart and symptoms. Both systems provide complementary information about the presence and severity of HF. The various stages and classes of the two systems are shown in Figure (2.2). Being that the NYHA classification system is based on subjective evaluation, it has been criticized because of a lack of taking into account the variability that can occur within patient groups. Furthermore, with the ACC/AHA system there is no moving backwards to prior stages, i.e. ones a patient is assigned a HF stage. The patient can never again achieve a different prior stage. With the NYHA it's different as patients can move between classes relatively quickly, as these are all based on symptoms alone, see [Fleg et al. \(2000\)](#) and [Yancy et al. \(2013\)](#). Most studies address HF severity estimation by expressing the statistical learning problem as a two or three class classification problem. The use of ML to address this particular SL problem will not be pursued, as the focus will be on the second objective of the problem statement, namely the prediction of clinical outcomes. However, the use of severity estimation

ACC/AHA :



**Figure 2.2:** Comparison of ACCF/AHA Stages of HF and NYHA Functional Classifications (Yancy *et al.*, 2013, page. 1502).

is very important as it serves as complementary information for medical practitioners to give objective prognostics about HF patients. A lot of studies have been conducted on the use ML to estimate HF severity, and again we recommend reading Tripoliti *et al.* (2017) for a further overview of the literature. As for the prediction of clinical outcomes it's especially readmission and mortality that has gained a lot of interest by researchers. Readmission is important because of the negative impact on healthcare systems' budgets. Mortality is obviously important as HF is one of the leading causes of death worldwide. The use of prediction models for mortality can benefit both physicians and patients. The literature is full of models taking into account various factors in producing statistics that have the objective of predicting mortality. Some of the most used statistical methods include



the Kaplan-Meier estimator ([Kaplan and Meier, 1958](#)) and multiple variable Cox proportional hazard models ([Cox, 1972](#)). All of which have lead to the formation of multiple scores that estimate the risk of mortality that are much used in clinical practice. Examples include: The enhanced feedback for effective cardiac treatment (EFFECT) score ([Lee et al., 2003](#)), the Seattle heart failure model ([Levy et al., 2006](#)), the get with the guidelines (GWTG) score ([Peterson et al., 2010](#)) and the heart failure survival score ([Ketchum and Levy, 2011](#)). A small list of the relevant literature related to the applica-

**Table 2.5:** Literature review of prediction of HF outcomes

Author	Outcome	Method	Data	Features	Evaluation
<a href="#">Austin et al. (2012)</a>	Mortality	Logistic regression Logistic, Bagged and Boosted trees. Random Forrest	Baseline: $N = 9945$ (8240 incl.) Followup: $N = 8339$ (7608 incl.)	Response: Whether 30-day death in hospital Predictors: 34 clinical variables	Logistic regression: (Splines) AUC: 0.786 $R^2$ : 0.203 Brier's score: 0.119 Boosted regression: (depth four) AUC: 0.777 $R^2$ : 0.180 Brier's score: 0.107  Validation: Follow-up sample used as validation.
<a href="#">Zolfaghar et al. (2013)</a>	Re-hospitalization	Logistic regression Random Forrest	No. of data: 1681562.	Response: 30-day risk of re- admission. Yes or No Predictor: more than 100 features	Logistic regression: Accuracy: 78.03% Random Forest: Accuracy: 87.12%  Validation: 70% training 30% testing
<a href="#">Shah et al. (2014)</a>	Mortality & Re-hospitalization	SVM	$N = 397$ with HFpEF	Response: mortality and re- admission: Yes or No. Predictor: 67 features	Mortality: Precision: 60.90% Re-hospitalization: Precision: 63.60%

**Table 2.5:** Literature review of prediction of HF outcomes (*continued*)

Author	Outcome	Method	Data	Features	Evaluation
<a href="#">Panahiazar et al. (2015)</a>	Mortality	Logistic Regression Random Forest	$N = 5044$	Response: 1, 2 and 5 yr survival Predictor: 45 clinical variables	1-year: Log Regression: AUC: 81.00% Random Forest: AUC: 80.00% 2-year: Log Regression: AUC: 74.00% Random Forrest: AUC: 72.00% 5-year: Log Regression: AUC: 73.00% Random Forrest: AUC: 72.00%  Validation: Testing set of 3484 patients.
<a href="#">Koulaouzidis et al. (2016)</a>	Re-hospitalization	Naive Bayes classifier	$N = 308$	Response: High or Low Risk of HF hospital-ization Predictor: 25 clinical variables	Naive Bayes classifier: AUC: 82.00%  Validation: 10-fold-cross-validation

tion of ML for predicting readmission and mortality is shown in Table (2.5). One of the first to use ML methods for this particular SL problem was [Austin et al. \(2012\)](#). They investigated predicting the 30-day mortality using a binary variable to denote whether a patient died within 30 days of hospital admission. Methods used include: Logistic regression, boosted regression and Random forest. The researchers used the methods on a total of 8240 baseline patients and 7608 follow-ups. The results seem to suggest that logistic regression and boosted regression trees are the most accurate with an area under the curve (AUC) of 0.786 and 0.777 respectively. [Zolfaghar et al. \(2013\)](#) applied logistic regression and random forest to

predict 30 day risk of readmission. This was done on a data set consisting of 1 681 562 patients. The predictors of the analysis contained more than 100 features. The accuracy was 78.03% and 87.12%, with 70% of the data set being reserved for training and 30% for testing. [Shah et al. \(2014\)](#) analyzed the prediction of both readmission and mortality on 397 patients and 67 clinical variables using support vector machines (SVM). The precision of mortality and readmission were 60.90% and 63.60%. As is evident from Table (2.5), the accuracy and precision of the prediction models using ML methods varies throughout the various studies. Along with the variability in the number of optimal clusters mentioned in section (2.2.2), we'll also try to address this point by again re-evaluating the performance of a number of classification algorithm related to the SL problem of predicting clinical outcomes.

# Chapter 3

## Methodology

In this chapter, we present the methodology and research structure used in this thesis. Some pre-processing of data, including imputation and dimensional reduction, will also be presented and explained. A high level description of the implementation details of the ML algorithms that produces the results are also presented in this chapter.

### 3.1 Overview

As stated in chapter (1), the aim of the thesis is split into two parts. The first part is seeing how well various clustering methods perform in producing phenotypically distinct clinical patient groups with HFpEF and HFmrEF. We frame the SL problem in the setting of unsupervised learning and accordingly use the following clustering methods: hierarchical clustering, k-means and expectation-maximization to evaluate which produce the most mutually exclusive patient groups. The use of these clustering methods are common in the literature (see section 2.2.2) and serves as the main motivation for including them in our analysis. The second part of the problem statement looks at evaluating the accuracy of various classification algorithms in predicting the mortality and readmission of patients with post-diagnosed HF. In accordance with the literature as presented in section (2.3), we reduce the SL problem of predicting the mortality and readmission into a two class classification problem where both classes of outcomes are whether or not mortality/readmission occurred. The classification algorithms that will be evaluated are k-nearest neighbours (k-NN),

logistic regression, naive-bayes, support vector machines (SVM), linear discriminant analysis (LDA) and random forest (RF). All the algorithms are much used in the literature. The motivation behind the use of the chosen algorithms, has always been to confirm the practices done in the literature. We do, however, need to emphasize that many additional algorithms exist that can be used to further broaden the analysis done in this thesis. We have not done this due to limitations.

The machine learning procedure adopted in this thesis is illustrated in Figure (3.1). The procedure starts by pre-processing the data. This pre-processing step consists of three sub processes: consolidation, imputation and dimension reduction. The consolidation process merges the HFpEF and HFmrEF datasets into one data set with the same types of variables. In addition to having one data set with all the observations, the process also leaves the data separate (but with equal variables), so that an analysis on each separate data set can be done. Furthermore, the clinical outcomes of the patients in the data set are extracted by this process and stored for later use in the classification part of the thesis. The imputation process imputes missing data to ensure that the data is balanced, and the dimensional reduction process addresses eventual problems with higher dimensional multi-correlated variables. The pre-processing step is explained in further detail later in this chapter (see section 3.2). After the pre-processing is done, the procedure continues by first addressing the cluster analysis. We use the principal components derived from the dimension reduction process as input into the clustering algorithms evaluated. The cluster analysis runs the produced components through the three cluster algorithms (hierarchical clustering, k-means and expectation maximization). After the procedure is done, three sets of clusters are produced. The next step is to evaluate the clusters by assessing their level homogeneity. This is done by comparing the number of significantly different baseline characteristics.

The supervised classification track is structured in a somewhat different way. The imputed data is run through the six classification algorithms (k-NN, LR, NB, LDA, SVM and RF). The data is trained and validated to produce approximately unbiased estimates of the test errors/accuracy. The accuracy are also adjusted by means of the Cohens' Kappa  $\kappa$ . After the data is run through the classification process and the accuracy are produced, the algorithms are ranked and evaluated accordingly. The outputs of the whole ML procedure are i) clinical clusters that *may* have distinct phenotypical properties and ii) the accuracy of the various classification

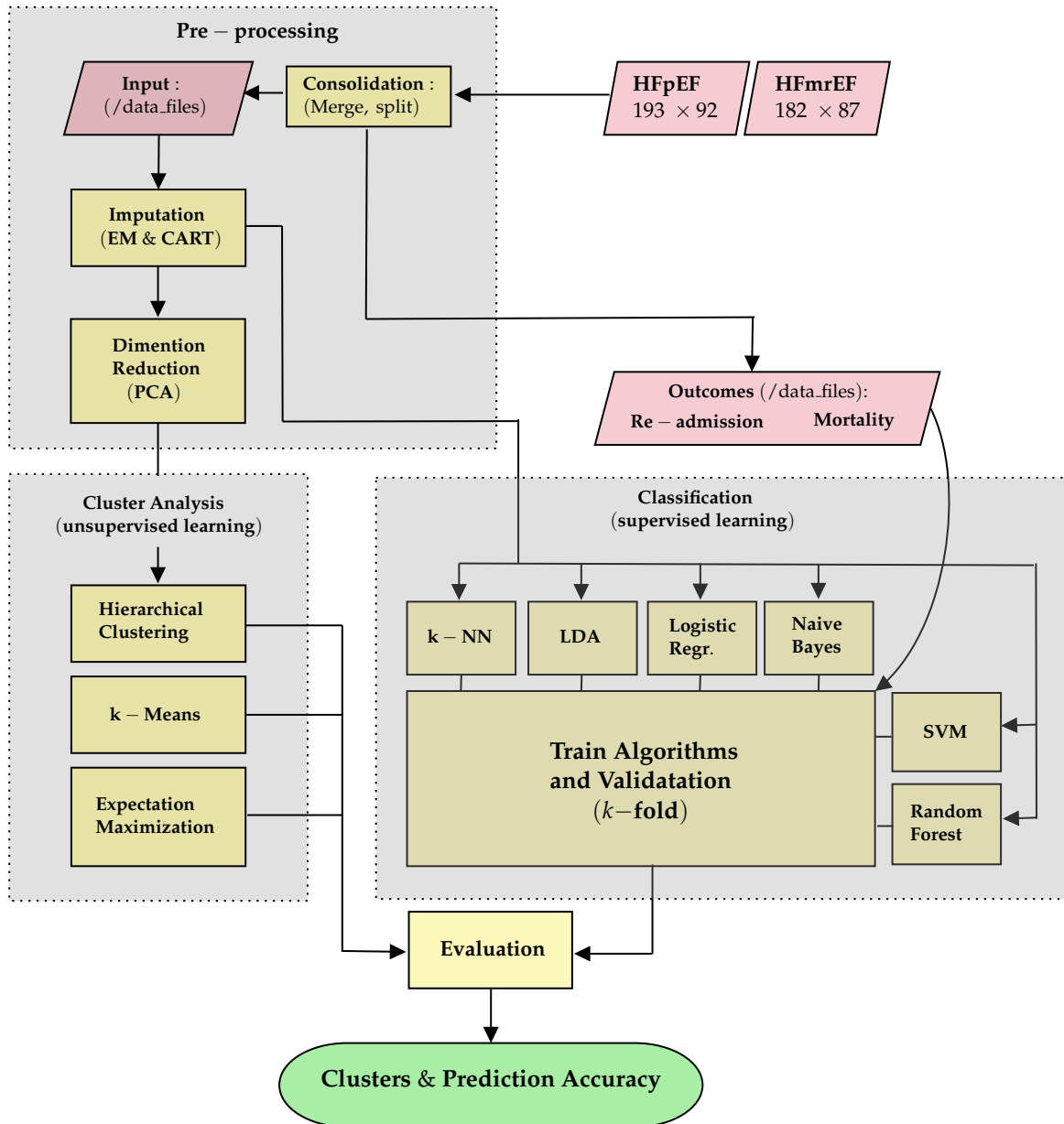


Figure 3.1: Machine learning procedure adopted in the thesis

algorithms in predicting readmission and mortality in the data sets. All the processes mentioned in the ML procedure in Figure (3.1) are developed using the R statistical programming language (version 3.4.4 - *Someone to Lean On*) (R Core Team, 2018a) with RStudio as the integrated development environment (IDE), version 1.1.423 (RStudio Team, 2018). We use a number of external libraries and self-made algorithms in order to make the whole research process more efficient. Data description with variable explanations, descriptive statistics and some relevant plots can be found in appendix (A). The source code used to produce all the results in this thesis, can also be found in appendix (B). As we now have given an overview of the ML procedure used in this thesis, we move on to presenting the data.

## 3.2 Data

The data used is comprised of two data sets (`data_use_HFpEF.mat`, dim:  $193 \times 92$  and `data_use_HFmrEF.mat`, dim:  $182 \times 87$ ). Being that both data sets have different types of clinical variables, we consolidated the data into three main data set with the same number and types of variables:

- (i) Full sample (`HFfullDataSet.Rdat`, dim:  $374 \times 55$ )
- (ii) HFpEF sample (`HFpEFdataSet.Rdat`, dim:  $193 \times 55$ )
- (iii) HFmrEF sample (`HFmrEFdataSet.Rdat`, dim:  $182 \times 55$ )

The data was collected by the medical staff at a tertiary hospital in the United Kingdom. At this particular hospital NT-proBNP led heart failure service were run on all patients with suspected heart failure. All patients with suspected HF based on an assessment of the HF probability and raised NT-proBNP/BNP levels (see Figure 2.1) were included and forwarded for an echocardiography. An expert HF physician reviewed all the patients after the echocardiography was performed. The patients were diagnosed with HF according to the 2016 ESC guidelines (Ponikowski et al., 2016). Accordingly, signs and symptoms of HF, raised NP values, echocardiographic results including left ventricular ejection fraction (LVEF) and evidence of structural or functional heart abnormalities were the primary basis for the assessment done by the hospitals cardiac physicians. After the diagnosis, patients were categorized based on LVEF following the ESC guidelines,

i.e. patients with  $LVEF > 50\%$  were classified as HFpEF and those with  $40 \leq LVEF < 50$  as HFmrEF. The patients with  $LVEF < 40\%$ , greater than moderate valvular heart disease and prior cardiac transplantation were excluded. The data was collected over a one-year period from October 10th 2014 to October 9th 2015. In total 375 patients were analyzed over this one-year period with data from almost 100 clinical features being recorded. The outcomes were evaluated through the hospital databases and mortality was confirmed with the Office for National Statistics. All the data was collected as part of the hospitals approved Clinical Audit. As mentioned in the previous section, we reduced the SL problem in the supervised learning part of the ML procedure to a two-class classification problem. The way this was done was with respect to the various patient groups in the data. The patients were grouped based on various outcomes. In total six outcome categories were defined in the data sets. The outcome categories are as follows: IN - inhospital mortality, Z mortality within 30 days, Y - mortality within 1 year, X - mortality by Fluorouracil (medication), V - cardiac readmission within 30 days, U - readmission and R - the rest. The various combinations of the outcome classes found in the data sets, and the way in which they were classified, are listed in Table (3.1). From this table, we can

**Table 3.1:** Clinical outcome classes

PANEL I: Full Sample (HFfullDataSet.Rdat)				
Group	Mort?	Readm?	<i>n</i>	% Tot
R	no	no	186	0.496
U	no	yes	59	0.157
X, R	yes	no	29	0.077
Y	yes	no	16	0.043
IN	yes	no	15	0.040
V	no	yes	15	0.040
Y, U	yes	yes	13	0.035
X, U	yes	yes	11	0.029
Y, V	yes	yes	11	0.029
X	yes	no	9	0.024
Z	yes	no	7	0.019
X, V	yes	yes	3	0.008
Z, V	yes	yes	1	0.003



PANEL II: Outcome Classes by Clinical Syndrome									
HFpEF (HFpEFdataSet.Rdat)					HFmrEF (HFmrEFdataSet.Rdat)				
Group	Mort?	Readm?	<i>n</i>	% Tot	Group	Mort?	Readm?	<i>n</i>	% Tot
R	no	no	85	0.440	R	no	no	101	0.555
U	no	yes	40	0.207	U	no	yes	19	0.104
X, R	yes	no	29	0.150	Y	yes	no	15	0.082
V	no	yes	10	0.052	IN	yes	no	8	0.044
IN	yes	no	7	0.036	X	yes	no	8	0.044
Y, U	yes	yes	7	0.036	Z	yes	no	7	0.038
Y, V	yes	yes	7	0.036	Y, U	yes	yes	6	0.033
X, U	yes	yes	6	0.031	V	no	yes	5	0.027
X	yes	no	1	0.005	X, U	yes	yes	5	0.027
Y	yes	no	1	0.005	Y, V	yes	yes	4	0.022
					X, V	yes	yes	3	0.016
					Z, V	yes	yes	1	0.005

see that approximately 36.8% of all the patients in the HFpEF data set were readmitted in some form, i.e either within 30 days or more. In the HFmrEF data set, this number was somewhat smaller being approximately 23.4%. In the full sample, approximately 29.1% of the patients were readmitted. The number also differed with respect to whether the patients were confirmed deceased or not. In the HFpEF data set, approximately 29.9% of the patients had confirmed mortality and in the HFmrEF data set this number was 31.1%. For the full sample, the number is approximately 30.7%. Further descriptive statistics on the data can be found in appendix (A.3). The source code for the two-class outcome classification shown in Table (3.1), can be found in appendix (B.3). As the data used in this thesis is cross-sectional, we need to emphasize that it is not ideal. Limitations to the data sets are many and one of the most relevant one is that of missing data.

### 3.2.1 Missing data

Missing values in data is a very important concept in data management and a highly prevalent problem in any data analysis. If one does not handle missing values properly, this may lead to inaccurate or invalid inference being drawn from the data. Results where improper treatment of missing data is present may differ significantly from those where missing data is

**Table 3.2:** Summary of missing values

PANEL I: Full Sample (HFfullDataSet.Rdat)									
Variable (V)	#Na	%n			%Na			%V	
grand.tot	3081	0.149			1.000				
irondef	254	0.012			0.082			0.677	
ferritin	250	0.012			0.081			0.667	
bmiadmission	223	0.011			0.072			0.595	
ironlevels	210	0.010			0.068			0.560	
tsat	210	0.010			0.068			0.560	
timetohfadm	184	0.009			0.060			0.491	
pasp	181	0.009			0.059			0.483	
admissionwgt	164	0.008			0.053			0.437	
ecgqrsduration	141	0.007			0.046			0.376	
obesity	137	0.007			0.044			0.365	
HFpEF (HFpEFdataSet.Rdat)					HFmrEF (HFmrEFdataSet.Rdat)				
Variable (V)	#Na	%n	%Na	%V	Variable (V)	#Na	%n	%Na	%V
grand.tot	973	0.092	1		grand.tot	2108	0.211	1	
irondef	124	0.012	0.127	0.642	bmiadmission	178	0.018	0.084	0.978
timetohfadm	124	0.012	0.127	0.642	admissionwgt	131	0.013	0.062	0.720
ferritin	122	0.011	0.125	0.632	irondef	130	0.013	0.062	0.714
tsat	99	0.009	0.102	0.513	obesity	129	0.013	0.061	0.709
ironlevels	98	0.009	0.101	0.508	ferritin	128	0.013	0.061	0.703
pasp	71	0.007	0.073	0.368	breathless	127	0.013	0.060	0.698
bmiadmission	45	0.004	0.046	0.233	ironlevels	112	0.011	0.053	0.615
ee	41	0.004	0.042	0.212	tsat	111	0.011	0.053	0.610
ecgqrsduration	36	0.003	0.037	0.187	pasp	110	0.011	0.052	0.604
ecgrate	34	0.003	0.035	0.176	ecgqrsduration	105	0.010	0.050	0.577

not present. In medical research, it is not uncommon for patient data to be missing. Missing data from patients clinical variables are typically defined as the values that are not directly observed ([Ibrahim et al., 2012](#)). Data can be missing due to a number of reasons. In clinical research some reasons may include: poor communication with study subject, difficulties assessing the clinical outcomes, lack of consolidation from test, duration of trial etc. The latter is often a reason for missing data, as longer trials tend to produce more risk of missing data. Especially considering that patients often run the risk of being dropped from the studies before completion

(Myers, 2000). In our data sets, the problem with missing values is very much present. In the full data set, a total of 3081 observations are missing accounting for about 14.9% of the total data set. The main non-indicator variables accounting for the highest amount of this number is the lack of registering ferritin levels (`ferritin`, 8.1% of missing), BMI at admission (`bmiadmission`, 7.2%), iron levels (`ironlevels`, 6.8%), transferrin saturation (`tsat`, 6.8%), time of HF admission (`timetohfadm`, 6%), pulmonary artery systolic pressure (`pasp`, 5.9%), weight at admission (`admissionwgt`, 5.3%) and ECQ QRS duration (`ecgqrsduration`, 4.6%). We can also look at the missing values in both sub data sets. In the HFpEF data set a total of 973 observations, i.e. approximately 9.2% of the data set is missing. Of the non-indicator variables, the largest contributors can be attributed to the failure of registering time to HF admission (`timetohfadm`, 12.7% of missing), ferritin levels (`ferritin`, 12.5%), transferrin saturation (`tsat`, 10.2%), iron levels (`ironlevels`, 10.1%), pulmonary artery systolic pressure (`pasp`, 7.3%), registering body-mass-index (BMI) at admission (`bmiadmission`, 4.6%), E/e' ratio (`ee`, 4.2%), ECQ QRS duration (`ecgqrsduration`, 3.7%) and ECG rate (`ecgrate`, 3.5%). These variables contribute to approximately 68.8% of the missing values in the HFpEF data. In the HFmrEF data set, the picture is very much different. In general, we can say that this data set has a much larger presence of missing values even though the clinical variables used in both sets are the same. In total 2108 observations, i.e. approximately 21.1% of the data is missing. The largest non-indicator contributors are: inability to record the body mass index (BMI) at admission (`bmiadmission`, 8.4%), the weight of patients at admission (`admissionwgt`, 6.2%), ferritin levels (`ferritin`, 6.1%), iron levels (`ironlevels`, 5.3%), transferrin saturation (`tsat`, 5.3%), pulmonary artery systolic pressure (`pasp`, 5.2%) and ECQ QRS duration (`ecgqrsduration`, 5%). These variables account for 41.1% of the missing values in the HFmrEF data. An overview of the variables with the most missing values in each data set can be found in Table (3.2).

### 3.2.2 Little's test for MCAR

The presence of missing values has to be addressed by any individual conducting data analysis. Missing values may make the data corrupted and introduce statistical bias that may lead to invalid results and inferences. This is vital for us as many of the statistical methods used later in this thesis

cannot be conducted in the presence of missing values. When talking about missing values one typically mention three distinct types of missing values, see e.g. [Sterne et al. \(2009\)](#) and [Kaushal \(2014\)](#) for further explanation. These are as follows:

- (i) Missing completely at random (MCAR): This type assumes that there is no systematic difference between the missing values and the observed values. An example can be if blood pressure values are missing due to breakdown in automatic sphygmomanometer, or if blood sugar values are missing due to a non working glucometer.
- (ii) Missing at random (MAR): The second type of missing values assumes that any difference between the missing values and the observed values can be explained by differences in the observed values. Again, an example can be that missing blood pressure values or blood sugar values may be lower than the measured values, but only because younger people may be more likely to have missing blood pressure and blood sugar as missing.
- (iii) Missing not at random (MNAR): The last and final type assumes that even after the observed data are taken into account, the systematic differences between the observed and missing values are still present. An example can be that people with high values of blood pressure or blood sugar may be less likely to attend an appointment due to headache.

MNAR can only be speculated and thus never determined, see e.g. [Rubin \(1976\)](#), [Schafer and Graham \(2002\)](#) and [Moons et al. \(2006\)](#). In our data, we assume that the missing data is at least missing at random (MAR). This is an assumption that many in the literature place on their data without any attempt at supplying some arguments to support such an assumption. To this we have carried out Little's MCAR test ([Little, 1988](#)) on our data (separately on indicator and continuous variables). The test is structured with the following three steps :

- (i) The test starts by using the expectation-maximization (EM) algorithm ([Dempster et al., 1977](#)) to estimate the maximum likelihood of the population mean  $\tilde{\mu}_{obs,j}$  and variance-covariance matrix  $\tilde{\Sigma}_{obs,j}$ . Here one enters the  $Y : N \times p$  matrix of data into the EM algorithm.

- (ii) Next step is to create a set of matrices  $S_j$  for  $j = 1, \dots, J$  where each matrix of the data set consists of all cases that are identified with particular missing patterns (0 = not-missing and 1 = missing). Define  $m_j$  to be the number of cases that belong to a given missing response pattern in  $S_j$ . From these  $J - 1$  cases, calculate the *observed* vector of means  $\hat{\mathbf{y}}_{obs,j}$  for each random response pattern.
- (iii) The final step comprises of calculating the difference between the observed means in step 2 with the estimated EM-means from step 1 weighted by  $m_j$  and the inverse variance-covariance matrix to obtain the following test statistics:

$$d^2 = \sum_{j=1}^J m_j (\hat{\mathbf{y}}_{obs,j} - \tilde{\boldsymbol{\mu}}_{obs,j}) \tilde{\boldsymbol{\Sigma}}_{obs,j}^{-1} (\hat{\mathbf{y}}_{obs,j} - \tilde{\boldsymbol{\mu}}_{obs,j})^T \quad (3.1)$$

Little (1988) showed that  $d^2$  is asymptotically  $\chi^2$ -distributed with  $f = \sum_{j=1}^J p_j - p$  degrees of freedom, where  $p_j$  is the number of observed variables for cases in  $S_j$ . Thus, with the use of  $d^2$ , a large-sample test of the MCAR assumption compares  $d^2$  with a chi-squared distribution with  $f$  df can be done, and rejecting the null hypothesis when  $d^2$  is large. Following this procedure, we have carried out Little's MCAR test and the results are presented in Table (3.3). The results were produced using the function `LittleMCAR()` in the `r` package `BaylorEdPsych` (Beaujean, 2012). We removed the variables that had more than 15% missing values from the

**Table 3.3:** Little's MCAR test

	num col	missing.patterns	Chi.squared ( $\chi^2$ )	df	p-value
Panel I: Full Sample					
indicator	24	27	273.7770	242	0.07844
continuous	14	15	96.3276	96	0.47141
Panel II: HFpEF					
indicator.1	26	16	103.7992	109	0.62273
continuous.1	17	14	101.7398	103	0.51661
Panel III: HFmrEF					
indicator.2	24	19	141.8979	135	0.32518
continuous.2	14	11	53.9340	51	0.36284

HFpEF data set, 25% from the HFmrEF data set and 20% from the full data set (see table 3.2 for top 10 missing variables). Next, we split the variables into two data sets, one for the continuous variables and one for the indicator variables. We also removed the variables that had near zero variance using the `nearZeroVar()` function in the `caret` package (Kuhn et al., 2018). As remarked by [Beaujean \(2012\)](#), the `LittleMCAR()` function can be very time inefficient for data sets with more than 50 variables. This time inefficiency is why we split the data sets into the two subsets, i.e. continuous and indicator and thus conducted separate tests on both subsets. The test assumes that the data is MCAR, and this is accordingly the null-hypothesis. From Table (3.3), we can see that all the  $p$ -values are insignificant at 5% significance level. This suggests that we cannot reject the null hypothesis of the missing data being MCAR. However, as argued by [Allison \(1999\)](#), just because the data passes this test, does not mean that the MCAR assumption is satisfied. The assumptions for MCAR are strong, and a simple test such as the one suggested by [Little \(1988\)](#) does not in and of itself satisfy those assumptions. It merely lends evidence in its support, and given the test results presented in Table (3.3), we consider this assumption to be intact. When it comes to the question regarding missing values, there exists many ways of dealing with this problem. Each of these ways have different advantages as well as disadvantages. One of the most common way of dealing with missing values is through the use of imputation techniques. This is something we will present in the next section.

### 3.2.3 Imputation

There exists a wide variety of methods that fall under the class of imputation. In general, all methods that attempt to replace each missing value in a data set with an estimate or a guess, are typically classified as being an imputation method ([Allison, 1999](#)). A very popular and conventional method of imputing missing values is through the use of mean imputation. This method implies swapping each missing value with the mean of the observed values in the given variable column. The method is very easy to use and maintains the sample size, but it has a problem with underestimating both the variance and standard deviation estimates. This implies that the estimates that produce the imputed values are unbiased see e.g. [Scheffer \(2002\)](#), [Enders \(2010\)](#) and [Eekhout et al. \(2012\)](#). Another class of imputation method that have proven to handle missing values in

a wide variety of cases, is the maximum likelihood methods. The use of set methods requires that the assumption of MCAR is intact and if this is done, can produce estimates that have the desirable properties normally associated with maximum likelihood. These properties are consistency (estimates will be approximately unbiased in large samples), asymptotic efficiency (estimates are close to being fully efficient i.e., having minimal standard errors) and asymptotic normality (allows the use of normal approximation to calculate confidence intervals and  $p$ -values). Additionally, the use of maximum likelihood methods can produce standard errors that fully account for the fact that some data is missing (Allison, 1999). It is exactly based on these qualities that we have chosen maximum likelihood based imputation as one of the strategies to address the problem with the missing values in our data set presented in subsection (3.2.1). We have also shown that this is relevant as the assumption of MCAR is assumed intact, see subsection (3.2.2).

A maximum likelihood method typically starts out by expressing a likelihood function. This function expresses the probability of the data as a function of the unknown parameters. Assuming two discrete random variables:  $\mathbf{X}$  and  $\mathbf{Z}$  with a joint probability function defined by  $p(x, z|\boldsymbol{\theta})$ , where  $\boldsymbol{\theta}$  is a vector of parameters. The joint probability function gives us the probability that  $\mathbf{X} = x$  and  $\mathbf{Z} = z$ . If we assume no missing values and that the observations are independent, i.e.  $cov(\mathbf{X}, \mathbf{Z}) = 0$ , then the likelihood function is defined by:

$$L(\boldsymbol{\theta}) = \prod_{i=1}^n p(x_i, z_i|\boldsymbol{\theta}) \quad (3.2)$$

To find an estimate of the maximum likelihood, we need to find the value for  $\boldsymbol{\theta}$  that maximizes the likelihood function (eq. 3.2). This can be done using the log-likelihood function ( $\mathcal{L}(\boldsymbol{\theta}) = \log L(\boldsymbol{\theta})$ ) and should give us an estimate defined by:

$$\hat{\boldsymbol{\theta}} \in \left\{ \arg \max_{\boldsymbol{\theta} \in \Theta} \sum_{i=1}^n \log p(x_i, z_i|\boldsymbol{\theta}) \right\} \quad (3.3)$$

If we assume that the data is MAR on  $\mathbf{Z}$  for the first  $r$  cases, and MAR on  $\mathbf{X}$  for the next  $s$  cases, we can then split the likelihood function into parts that correspond to each missing value pattern and accordingly factor these

parts. This is in order to get a likelihood function that takes into account the missing data patterns. The likelihood function becomes as follows:

$$L(\theta) = \prod_{i=1}^r g(x_i|\theta) \prod_{i=r+1}^{r+s} h(z_i|\theta) \prod_{i=r+s+1}^n p(x_i, z_i|\theta) \quad (3.4)$$

where  $g(x|\theta)$  and  $h(z|\theta)$  are the marginal distributions of  $\mathbf{X}$  and  $\mathbf{Z}$ , so that:

$$\prod_{i=1}^r g(x_i|\theta) \prod_{i=r+1}^{r+s} h(z_i|\theta) = \prod_{i=1}^{r+s} p(x_i, z_i|\theta) \quad (3.5)$$

For each missing data pattern, the likelihood is found by summing the joint distribution over all possible values of the variables with missing data. The estimated maximum likelihood parameters in this particular example should therefore be defined by:

$$\hat{\theta} \in \left\{ \arg \max_{\theta \in \Theta} \left( \sum_{i=1}^{r+s} \log p(x_i, z_i|\theta) + \sum_{i=r+s+1}^n \log p(x_i, z_i|\theta) \right) \right\} \quad (3.6)$$

We assumed the variables were discrete in the begin, and as such if the variables were continuous, the summations would be replaced by integrals. The extension to multiple variables is also relatively straightforward ([Allison, 1999](#)). In order to implement a maximum likelihood method on data that contains missing values, it is important to have a model for the joint distribution for all variables in the data set, and accordingly have a numerical method for maximizing the likelihood of this distribution. Determining this model can vary with the type of data that one is dealing with.

In our data set, we have both continuous and indicator variables. When the data is continuous it is common to assume a multivariate-normal model, i.e. that all the variables are independently identically normally distributed (iid) and can be expressed as a linear function of all other variables (or subsets). There is also an assumption that the errors are homoscedastic, i.e. constant and have a mean of 0. In the case of the indicator variables, it is difficult to assume that these variables are normally distributed. However, according to [Schafer \(1997\)](#), [Schafer and Olsen \(1998\)](#) and [Allison \(1999\)](#) simulation evidence and practical experience have shown that maximum likelihood methods can do a good job in imputing missing values, even if the variables in question are indicator variables. Still, we opted to use



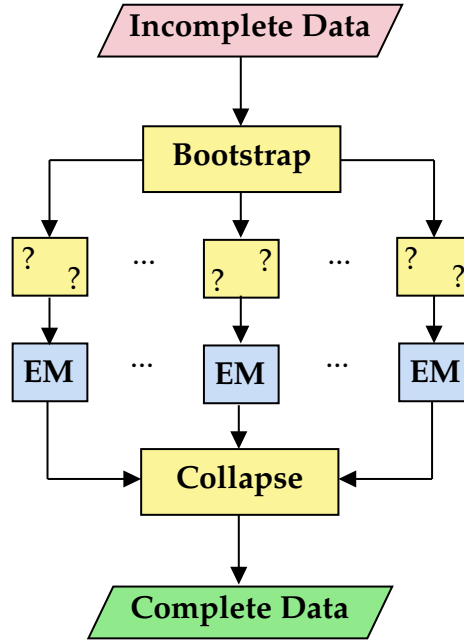
a different imputation method for each of the types of data, i.e. we use a bootstrapped expectation-maximization (EM) imputation method for the variables that are continuous and a classification- and regression tree (CART) based imputation method for the indicator variables.

As we mentioned, one needs to have a numerical method for maximizing the likelihood of the joint probability distribution. One of the most common numerical methods is the expectation-maximization (EM) algorithm ([Dempster et al., 1977](#)). We mentioned it slightly in subsection (3.2.2), but it is an iterative algorithm that is used to maximize the likelihood function (eq. 3.2) of a number of missing data models. It is comprised of two steps; the expectation step (often called the *E* step) and the maximization step (called the *M* step). In the expectation step, the expected values of the log-likelihood is taken over the variables with missing values using the current estimated parameters ([Allison, 1999](#)). Afterwards the maximization step involves maximizing the expected log-likelihood in order to get new estimates of the parameters. These two steps are continued until convergence is achieved, i.e. until the estimated parameters of the joint probability distribution doesn't change from one iteration to the next. Most standard software packages using an EM implementation have as a principal output a set of maximum likelihood parameters related to the joint probability distribution. The imputed values are often included in addition, but are not recommended for further analysis. The reason for this is that these imputed values are not designed for that purpose and as such will produce biased estimates of many parameters if used in further analysis ([Allison, 1999](#)).

A way to get around this problem is using multiple-imputation. [Honaker et al. \(2011\)](#) introduced a bootstrapped EM algorithm that combines the nice properties of the EM algorithm, i.e. consistency, asymptotic efficiency etc. with the accuracy property of the bootstrap re-sampling method, see [Efron \(1992\)](#) and [James et al. \(2013\)](#). [Honaker et al. \(2011\)](#) also argue that the EMB algorithm they developed is much faster and more reliable than alternative algorithms, in addition to making valid and much more accurate imputations for cross-sectional data. The algorithm is implemented in the *Amalie II* package in R. The assumptions of the algorithm are as follows: if we assume that the data set can be expressed as a matrix  $D$  consisting of dimensions  $(n \times k)$ . Let the matrix  $D$  be comprised of two parts, i.e.  $D^{mis}$  the missing part and  $D^{obs}$  the observed part. The matrix  $D$  is assumed to follow a multivariate distribution with mean vector  $\mu$  and

covariance matrix  $\Sigma$ . This assumption can be stated as  $D \sim N(\mu, \Sigma)$ . In addition to the multivariate normality assumption, the algorithm assumes that the data is MAR. The latter have we already shown to be intact, but the first assumption is somewhat difficult. As the data is by definition incomplete due to the missing data, we assume that this assumption is intact. Typically one would test if this assumption is intact by using a multivariate normality test similar to the ones mentioned by [Mardia \(1970\)](#), [Henze and Zirkler \(1990\)](#) or [Royston \(1982\)](#). Most of these tests assume that the data is complete, and should the data be incomplete then it is common to remove the missing observations and conduct the tests on the remaining data. The challenge for our part is that approximately 15% of our data set is missing which may cast doubt on the loss of statistical power that these tests may have. As a result of this, we have chosen to assume that the normality assumption is intact. The schematic approach of this algorithm and the way it used in this thesis is described in Figure (3.2). The procedure starts by producing  $n$  bootstrapped data sets for which the EM algorithm is run on each bootstrapped data sets. For all the data sets in the thesis, i.e. the full data (`HFfullDataSet.Rdat`), `HFmrEF` (`HFmrEFdataSet.Rdat`) and `HFpEF` (`HFpEFdataSet.Rdat`) we let the algorithm produce  $n = 100$  bootstrapped data set. After the imputed data sets are produced they are collapsed by averaging all the imputed values produced by the EM algorithm. All the data from the incomplete data set that the procedure started with should be the same, with the exception of the missing values, i.e. these have be replaced by the average of the imputed values.

For the indicator variables, the imputation technique is defined by a classification- and regression tree (CART) algorithm. This algorithm is implemented in the `mice` package in `r` ([Buuren and Groothuis-Oudshoorn, 2010](#)). The implementation proceeds as follows: for each variable  $k$  in the matrix  $D$ , the algorithm fits a classification or regression three by recursive partitioning. Then for each missing value in  $k$ , the algorithm finds the terminal nodes, i.e. the nodes the missing value can end up in according to the fitted tree. Lastly, the algorithm makes a random draw among the members in the nodes, and takes the observed value from that draw as the imputation. Rather than collapsing the multiple imputed data sets as with the BEM algorithm, we simply use the first imputed data sets for further analysis. Further description of the procedure of the algorithm can be found in [Burgette and Reiter \(2010\)](#). Our implementation of the algorithms with the source code can be found in appendix (B.2). This concludes



**Figure 3.2:** *Bootstrapped Expectation Maximization (BEM) procedure*

our treatment of the challenge with missing data in this thesis. Next, we present our treatment of the challenge with the higher dimensional data in the thesis.

### 3.2.4 Dimensional reduction

As we can see from Figure (3.1), the number of features in each HF data sets are 92 and 87. After the consolidation process, we reduce the number of features to 39 in each data sets. As the number of features are high, we need to have some process to address the challenge of higher dimensional data, i.e. when the number of features are more than the low-dimensional settings such as the three-dimensional physical space of everyday experience. The problem with such higher dimensional data is that some of these features may be noise features that are not truly associated with a given response. This may lead to a deterioration in a fitted model, and thus increase the uncertainty. Noise features may also exacerbate the risk of overfitting, i.e. having a statistical model that contains more parameters than can be justified by the data (Friedman et al., 2009), (James et al., 2013).

One can also run the risk of drawing invalid inference, as many of the features may be correlated with each other and thus one may face the case of multicollinearity, i.e. risking inflated standard errors.

We have chosen to address this problem with the use of Principal Component Analysis (PCA). The purpose of PCA is to express the information in the data set  $\mathbf{D}$  by a less number of variables  $\mathbf{Z}$ , called principal components. These principal components act as lower dimensional representation of the data that contains as much as possible of the variation. As each of the principal components are computed from the linear combination of the  $p$  features, then this means that the components are orthogonal and linearly uncorrelated. This property is ideal for addressing the challenge with multicollinearity.

For a given  $n \times p$  data set  $\mathbf{D}$ , we assume that each of the variables has been centered to have mean zero. We then want the linear combination of the sample feature values of the form  $z_{i1} = \theta_{11}x_{i1} + \theta_{21}x_{i2} + \dots + \theta_{p1}x_{ip}$  that has the largest sample variance, subject to the constraint  $\sum_{j=1}^p \theta_{j1}^2 = 1$ . The optimization problem becomes (James et al., 2013):

$$\max_{\theta_{11}, \dots, \theta_{p1}} \left\{ \frac{1}{n} \sum_{i=1}^n \left( \sum_{j=1}^p \theta_{j1} x_{ij} \right)^2 \right\} \quad \text{subject to} \quad \sum_{j=1}^p \theta_{j1}^2 = 1 \quad (3.7)$$

In the optimization problem above, we want to maximize the sample variance of the  $n$  values of  $z_{i1}$ . The elements  $z_{11}, \dots, z_{n1}$  are referred to as the *scores* of the first component, and solving the optimization problem can be done using an eigen value decomposition. One can compute these principal components by using the estimated correlation or co-variance matrix of  $\mathbf{D}$ . We have chosen to use the correlation matrix and the implementation of this is done using the `princomp()` function in the `stats`-package in `r`, (R Core Team, 2018b). We run the imputed data sets produced in subsection (3.2.3) through the PCA function and select the first principal components that explain most of variance in the data set for further analysis. The number of components used for the full sample data set is 4. For the other data sets, i.e. the HFpEF and HFmrEF datasets, we use the first two principal components. In the succeeding analysis, we use these principal components as input to the cluster analysis. Much of the literature on the topic applies the same procedure to address the challenge of higher dimensional data, see e.g. Shah et al. (2014), Ahmad et al. (2014) and Katz et al. (2017).

### 3.3 Clustering patient groups

In this section, we present the unsupervised clustering algorithms used in this thesis. The clustering algorithms used are as mentioned: hierarchical, k-means and expectation-maximization (EM) clustering. As there exists many clustering algorithm, we follow the strategy defined in section (3.1) and try to keep to the ones most used in the literature. An overview of the implementation and the source code can be found in appendix (B.5).

#### 3.3.1 Hierarchical

The first clustering algorithm evaluated in the cluster analysis process is the hierarchical clustering algorithm, [Sibson \(1973\)](#), [Defays \(1977\)](#) and ([Rohlf, 1982](#)). This algorithm uses a simple algorithm that takes into account the dissimilarity between clusters and accordingly produces a graphical representation in the form of a dendrogram. The algorithm starts by calculating

---

**Algorithm 1:** Hierarchical clustering

---

```

1 initialization;
2    $n$  observations
3   Distance measure
4   Treat every observation  $n$  as its own cluster
5 for  $i = n, n - 1, \dots, 2$  do
6   |   Examine and fuse the most similar clusters
7   |   Compute the pairwise inter-cluster dissimilarities
8   |   among the  $i - 1$  remaining clusters
9 end
10 Cut dendrogram based on max relative loss of inertia criteria
11 return Clusters

```

---

the dissimilarity between each pairs of observations, i.e. the patients. A common measure of the dissimilarity is the euclidean distance between pairs of observations. For all clustering algorithms where the distance is required, we have assumed that the euclidean distance measure is the most optimal. However, there exists many other distance measures, e.g. squared, polynomial, Manhattan, maximum and Mahalanobis distance that may be equally optimal. After selecting the distance, the algorithm starts at

the bottom of the dendrogram, i.e. where the observations are the most similar, and treats each of the  $n$  observations as its own clusters. Next, the algorithm fuses the two clusters that are most similar and this continued iteratively for the remaining  $n - 1$  clusters. When the algorithm is finished and the dendrogram is complete, all the clusters are now part of the same cluster. It is then up to the user to choose where to cut the dendrogram. In our implementation, we cut the dendrogram based on the criteria of maximizing the relative loss of inertia. The pseudocode for this algorithm is presented above.

The advantage of the hierarchical clustering algorithm, is that one does not need to define the number of clusters a priori, and thus a user can cut the dendrogram at any given height based on a given index or heuristic. There are many implementations of this algorithm, but since we use the principal components as input to this and all the other clustering algorithm, we have chosen to use the Hierarchical Clustering on Principal Components function `HCPC()` in the `FactoMineR`-package in `r` (Lê et al., 2008). We have also created our own function (`pca.var.plot()`) that visually presents the clustering results from all the clustering algorithms chosen for evaluation in this thesis. This function is very useful as it can supply the user with a visual illustration of the clustering results for each clustering algorithm. The evaluation criteria used to evaluate the clustering methods is something that we will be addressing in later sections. The hierarchical clustering algorithm is, however, just one of the algorithms that we use and accordingly, we now move on to explaining the k-means algorithm.

### 3.3.2 k-means

The k-means clustering algorithm (Forgy, 1965) is a prototype-based technique for partitioning data into a pre-defined number of clusters ( $K$ ). The clusters are represented by the centroids of the clusters (Tan et al., 2007). The algorithm assumes that each observations  $x_i$  belong to at least one of the  $K$  clusters and that the clusters are non-overlapping, i.e. that no observations belong to more than one cluster. The idea behind the k-means clustering algorithm is that a good clustering is one that minimizes the within-cluster variation, i.e. a measure of how much the amount of observations within a cluster varies  $W(C_k)$ , where  $C_k$  is the set containing the indices of the observations in cluster  $K$ . Similar to the hierarchical clustering algorithm, this measure is often the euclidean distance between

each pair of observations. Accordingly, the algorithm seeks to solve the following optimization problem (James et al., 2013):

$$\min_{C_1, \dots, C_K} \left\{ \sum_{k=1}^K \frac{1}{|C_k|} \sum_{i, i^* \in C_k} \sum_{j=1}^P (x_{ij} - x_{i^*j})^2 \right\} \text{ where } i \neq i^* \quad (3.8)$$

The solution to this optimization problem is very difficult as there exists  $K^n$  possible ways of partitioning  $n$  observations into  $K$  clusters. The k-means algorithm solves this problem with the following steps represented with the following pseudocode:

---

**Algorithm 2:** k-means clustering

---

```

1  initialization;
2   $n$  observations
3  Distance measure
4  The number of clusters  $K$  to be produced
5  for  $i = 1, \dots, n$  do
6  |   Randomly assign a number in  $\{1, K\}$  to  $i$ 
7  end
8  while Cluster assignment continuous to change do
9  |   for Each cluster  $C_k$  do
10  |   |   Compute cluster centroid
11  |   |   for Each observation in  $C_k$  do
12  |   |   |   Assign each observation to the cluster
13  |   |   |   whose centroid is closest
14  |   |   end
15  |   end
16 end
17 return Clusters

```

---

The algorithm takes as input  $n$  observations, the defined distance measure and the number of clusters  $K$  to be produced. Then all the observations  $n$  are assigned a number in the set of the number corresponding to the clusters. This assignment is done at random and serves as the initial cluster assignment for the observations. Then the algorithm iterates until there is no change in cluster assignment between cluster assignment  $a_t$  and  $a_{t-1}$ .

The cluster assignments is done by computing the cluster centroid and assigning each observation in the cluster  $C$  to the cluster  $C_1, \dots, C_k$  whose centroid is closest, i.e. given the distance measure.

The disadvantage of the k-means algorithm is that it requires a user to define the number of clusters a priori, which in some cases may be seen as defeating the purpose of the cluster analysis, i.e. the results may vary with the number of clusters chosen. We have tried to address this problem by using the `r` function `NbClust()` (Charrad et al., 2014) that uses almost 25 indices for determining the number of clusters and proposes to the user the "optimal" number of clusters by the use of a majority-rule of all the indices. As for the actual implementation of the k-means clustering algorithm, we use the `kmeans()` function in the `stats`-package (R Core Team, 2018b). The implementation of this algorithm is wrapped in the `pca.cluster.plot()` function we mentioned in the preceding section.

### 3.3.3 Expectation-maximization

The k-means algorithm is closely related to the EM algorithm (Dempster et al., 1977) for estimating certain Gaussian mixture model(s). As we mentioned in section (3.2.3), the EM algorithm consists of estimating the maximum likelihood parameters of the given Gaussian(s) in question. This is done in the E-step of the algorithm and as such this is responsible for assigning the "responsibilities" for each data points based on its relative density under each mixture components. Whilst the M-step is responsible for recomputing the component density parameters based on the current responsibilities (Friedman et al., 2009). The aim of the EM clustering algorithm is to assign the data into  $K$  clusters according to the observations probability of belonging to each of the clusters. It is often stated that the EM algorithm is a "soft" version of the k-means algorithm, as the points are assigned based on a probabilistic (rather than a deterministic) approach (James et al., 2013). The pseudocode for the EM algorithm is given below. Accordingly, the algorithm starts by having the user input the data matrix  $\mathbf{D}$ , a parametric model  $f_{\theta}$ , an initial distribution  $\pi_0$  and a randomly selected parameter vector  $\theta$ . The algorithm then computes the expected responsibilities of each observations and updates the parameters  $\theta$  with the maximum likelihood estimates  $\theta_{max}$ . This is done iteratively until convergence. Being that the EM algorithm is similar to the k-means algorithm, it has also the same disadvantages, i.e. the user needs to define the number of



clusters to be produced a priori. In addition, it can sometimes be very time consuming or even impossible for the algorithm to achieve convergence, i.e. no changes in cluster assignment between iterations. In theory, as the exit criteria of the EM algorithm may be defined by convergence, this could mean that the algorithm may never stop as convergence is not guaranteed in all cases. One could however define an exit criteria as a set number of iterations  $i_{max}$  to terminate the algorithm, but this is something we have not done and accordingly the algorithm stops once convergence is reached. As for the implementation, we use the `Mclust()` function in the `mclust` package in `r` (Scrucca et al., 2017). All the default setting are used in the implementation and as with the previous clustering algorithms, the EM algorithm is also wrapped in the `pca.var.plot()` function.

---

**Algorithm 3:** EM clustering

---

```

1 initialization;
2   Data set  $\mathbf{D} = \{X_1, \dots, X_n\}$ 
3   Parametric model  $f_\theta$ 
4   Choose an initial distribution  $\pi_0$  and pick
5     a parameter vector  $\theta$  at random.
6 while No convergence do
7   | E step:
8   | Compute expected responsibilities on each observation
9   | M step:
10  | Update the parameters in  $\theta$  with the likelihood
11  | maximization parameters  $\theta_{max}$ .
12 end
13 return Clusters produced by EM process

```

---

### 3.4 Classifying clinical outcomes

In this section, we present the supervised classification algorithms used in this thesis. As we mention in section (3.1), the classification algorithms that will be evaluated are: k-nearest neighbours, logistic regression, naive Bayes, linear discriminant analysis, support vector machines and random forest. We will also mention the way in which we evaluate the algorithms with the K-fold cross validation. All the source code can be found in appendix (B).

### 3.4.1 k-nearest neighbours

The first algorithm we will be presenting is the k-nearest neighbours (k-NN) algorithm. The k-NN algorithm (Fix and Hodges Jr, 1951) is a widely used algorithm, and often for good reason. It is very intuitive and simple to understand. In addition, the algorithm performs very well in many cases. This classifier is a memory-based algorithm that classifies a given observation based on the  $k$  nearest neighbours of that observation in the feature space. Mathematically, given a query point  $x_0$ , the k-NN algorithm tries to find the  $k$  training points  $x_{(r)}, r = 1, \dots, k$  closest in distance to  $x_0$ , and thus classify the point  $x_0$  according to the majority rule of the  $k$  closest points to  $x_0$ , see (Friedman et al., 2009) and (James et al., 2013). The pseudocode for the algorithm is given below. Based on the pseudocode, we can see that the k-NN algorithm starts out by taking as input the training data  $\mathbf{X}$  which is a subset of the full dataset  $\mathbf{X} \subseteq \mathbf{D}$ , the class labels  $\mathbf{Y}$  of  $\mathbf{X}$  and the distance measure to be used  $d$ . The distance measure between two data points are typically assumed to be a Minkowski distance:

$$d[i, j] = \left( \sum_{i=1}^n |X_{i,k} - X_{j,k}|^p \right)^{1/q} \quad (3.9)$$

where if  $p = 1$  or  $2$ , the distance  $d$  will correspond to the Manhattan or the Euclidean distance. As  $q$  approaches infinity, the distance measure  $d$  convergence to the maximum distance, i.e. the largest coordinate difference between data points. After computing the distance between data points, the algorithm classifies the labels of the unknown sample  $x$  based on the mapping learned by the training data done with the majority rule.

The observant reader will probably wonder how the unknown sample  $x$  is determined. This is something we will address in a later section dealing with cross-validation. However, what we can say is that the implementation of the k-NN algorithm used in this thesis is that of the `knn()` function from the stats package in `r` (R Core Team, 2018b). We also need to emphasize that the k-NN algorithm is not without disadvantages. That is, the k-NN algorithm is slow when one has many observations, since it does not generalize over data in advance. It scans all the data each time a prediction is needed. It also has disadvantages with higher dimensional data as even normalizing the data makes the distances "blurred". This is because the distance to all neighbors becomes more or less the same in

higher dimensional space. Another critique of the k-NN algorithm is that it in many ways classifies observations based on heuristics, i.e. it lacks probabilistic intuition and rational similar to other classification algorithms. Still, it is very popular and one that we will attempt to examine in this thesis.

---

**Algorithm 4:** k-NN classification algorithm

---

```

1 initialization;
2   X: training data
3   Y: class labels of X
4   x: unknown sample
5   Distance measure d
6 for  $i = 1, \dots, n$  do
7   | Compute distance  $d(\mathbf{X}_i, x)$ 
8 end
9 Compute set I containing indices for the k smallest
10  distances  $d(\mathbf{X}_i, x)$ .
11 return Majority label for  $\{\mathbf{Y}_i \text{ where } i \in I\}$ 

```

---

### 3.4.2 Logistic regression

Logistic regression is a very popular classification algorithm in medical research. The algorithm uses a logistic function to model the dependent discrete class labels corresponding to a given observation. In our example, the algorithm tries to model the probability that a given patient "belongs" to a particular clinical outcome (mortality or readmission) using a probabilistic approach. In the case of modeling this probability using multiple predictors, the algorithm tries to estimate the probability using the following generalized logistic function (Friedman et al., 2009):

$$P(X) = \frac{\exp \{\beta_0 + \sum_{i=1}^p \beta_i X_i\}}{1 + \exp \{\beta_0 + \sum_{i=1}^p \beta_i X_i\}} \quad (3.10)$$

Where  $X = (X_1, \dots, X_p)$  are the independent variables. The slope parameters  $\beta_0, \dots, \beta_p$  are estimated using the maximum likelihood, i.e. each slope parameter  $\beta_i$  is estimated so that the following holds:

$$\hat{\beta} \in \left\{ \arg \max_{\beta \in \Theta} \sum_{i=1}^p \log p(x_i, \beta) \right\} \quad (3.11)$$

Unlike linear regression, logistic regression uses the logistic function (3.10) to map the patient to a given clinical outcome. The mapping is done by selecting a threshold  $p^*$  and if the calculated probability is above this threshold, we assign the given patient to that particular clinical outcome. In our case, we use  $p^* = 0.50$  as this is the default value in the implementation. Logistic regression works well for categorical outcomes, but has a significant disadvantage in working with response variables of continuous scale. The algorithm also requires that each data point be independent of all other data points. Should this not be the case, then the model may tend to overweight the significance of those observations, [Friedman et al. \(2009\)](#) and [James et al. \(2013\)](#). Still, logistic regression is one of the most used algorithms in medical statistics. It is a relatively "simple" algorithm that perform very well in classification, see e.g. [Austin et al. \(2013\)](#) and [Zolfaghar et al. \(2013\)](#). The implementation of this algorithm is done using the `glm()` function from the `stats`-package in `r` ([R Core Team, 2018b](#)). All default arguments are used with the exception of `family = binomial(link='logit')` which guarantees that the link function is the logistic function (eq. 3.10).

### 3.4.3 Naive Bayes

The naive Bayes algorithm (also called "simple" Bayes) is a popular probabilistic classifier used to classify data based on the probability that a given observation belongs to a particular class. It is in many ways very similar to logistic regression, but the classifier is based on the Bayes theorem and assumes that the effect of an attribute value on a given class is independent of the value of the other attributes. For a given classification problem, we want to determine  $P(H|X)$ , i.e. the probability that the hypothesis  $H$  holds given the "evidence" (i.e. the *observed* data sample  $X$ ). The probability  $P(H|X)$  is also known as the posteriori probability and is according to Bayes' theorem calculated by the following:

$$p(H|X) = \frac{p(X|H)p(H)}{p(X)} \quad (3.12)$$

The probabilities  $p(X|H)$ ,  $p(X)$  and  $p(H)$  can all be estimated from the given data sample. The procedure for which the algorithm classifies a given observation into a discrete categorical outcome is given by the following (Leung, 2007). Given a sample  $X$ , the naive Bayes' classifier will predict that  $X$  belongs to the class having the highest posteriori probability, *conditioned* on  $X$ . That is  $X$  is predicted to belong to the class  $C_i$  if and only if  $P(C_i|X) > P(C_j|X)$  for  $1 \leq j \leq n, j \neq i$ . Rather than using a threshold value  $p^*$  as with logistic regression, one seeks to maximize the posteriori probability and accordingly assign labels to observations. For large sample data sets the naive Bayes' classifier is especially appropriate as it can outperform many sophisticated algorithms. However, the assumption of independence among the variables is often very unrealistic and although it simplifies the estimation, the risk of high bias is very much present with the algorithm. In this thesis we will be implementing the Naive Bayes algorithm using the `nb()` function in the `caret` package (Kuhn et al., 2018).

### 3.4.4 Linear discriminant analysis

The LDA algorithm is very similar to principal component analysis (PCA). Both try to look for linear combinations that best explain the data. However, LDA, tries explicitly to model the difference between the classes of data. This is done by modeling the distribution of the predictors  $X$  separately in each of the response classes. The objective of LDA is to perform dimension reduction (similar to PCA), while preserving as much of the class discrimination information as possible. Assuming we have a  $p$  dimensional random variable  $X$ , where  $X$  follows a multivariate normal distribution, i.e.  $X \sim N(\mu, \Sigma)$ . This distribution is formally given by the following, see Friedman et al. (2009) and James et al. (2013):

$$f(x) = \frac{1}{(2\pi)^{p/2} |\Sigma|^{1/2}} \exp \left\{ -\frac{1}{2} (x - \mu)^T \Sigma^{-1} (x - \mu) \right\} \quad (3.13)$$

In the case where we have  $p > 1$  independent variables, the LDA classifier assumes that the observation in the  $k$ th class is drawn from a multivariate normal distribution  $N(\mu_k, \Sigma)$ . Plugging eq. (3.13) into the formula for the posterior probability and solving for the Bayes classifier yields:

$$\delta_k(x) = x^T \Sigma^{-1} \mu_k - \frac{1}{2} \mu_k^T \Sigma^{-1} \mu_k + \log \pi_k \quad (3.14)$$

Where  $\pi_k$  is the prior probability that an observation belongs to the  $k$ th class. The LDA algorithm assigns a new observation  $X = x$  by plugging the estimates of  $\mu_1, \dots, \mu_K, \pi_1, \dots, \pi_K$  and  $\Sigma$  into (3.14) and classifying  $X$  to the class for which  $\hat{\delta}_K(x)$  is the largest. The LDA is considered to be an approximation of the Bayes' classifier similar to the naive Bayes. The major difference being that the LDA is more flexible. It does not rely on the assumption of independence between predictors (Friedman et al., 2009). For large samples and many variables, the LDA is also preferred to other discriminant classifiers due to its dimensional reduction nature. The same can be said in the opposite direction. LDA suffers from two main problems: the small sample size and the linearity problem (Tharwat et al., 2017). The linearity problem is present if the underlying structure in the data is non-linear. Should this be the case (which is very common in many domains), then the LDA cannot find a LDA space where the discriminatory information exists in the mean, since it exists in the variance. In a two class situation with a non-linear structure in the data, this means that the means are equal. Either way, the LDA is one of the most popular classification algorithms used in the literature related to HF and accordingly, the implementation of this algorithm is done using the `lda()` function from the MASS-package in R (Venables and Ripley, 2002).

### 3.4.5 Support vector machines

The next classification algorithm is the support vector machines (SVM) (Vapnik, 1963). This classifier is based on the concept of a separating hyper-plane, i.e. a flat affine subspace of dimension  $p - 1$ . A major drawback to the LDA and other linear classifiers is the fact that they fail to address the underlying non-linear nature of data. This is where the SVM has a clear advantage. The support vector machine algorithm can be generalized to classify clinical outcomes with non-linear decision boundaries. By choosing a radial kernel (function that quantifies the similarities between two observations), we can create a classifier that takes into account the non-linear nature that is often assumed on higher dimensional data. This radial kernel is defined by the generalized inner product function:

$$K(x_i, x'_i) = \exp \left\{ -\gamma \sum_{j=1}^p (x_{ij} - x'_{ij})^2 \right\} \quad (3.15)$$

Where  $\gamma$  is a positive constant and is often described as a hyperparameter that controls the tradeoff between errors due to bias and variance in our model. The kernel function works by having training observations that are far away from the test observation  $x^*$  playing essentially no role in the predicted class label for  $x^*$ . If the euclidean distance between the test observation and training observation is large, then the radial kernel  $\exp\{-\gamma \sum_{j=1}^p (x_{ij} - x_{i'j})^2\}$  becomes very small, because the term  $\sum_{j=1}^p (x_{ij} - x_{i'j})^2$  is large. This means that the radial kernel has very local behaviour, i.e. that only nearby training observations will have an effect on the class label of a test observation, see (Friedman et al., 2009) and (James et al., 2013). The advantage of classifying using a SVM with a kernel like the radial one described above, is that computationally one only needs to compute  $K(x_i, x_{i'})$  for all  $\binom{n}{2}$  distinct pairs of  $i$  and  $i'$ . However, the classification results are very sensitive to the chosen  $\gamma$  parameter. The algorithm is also very complex and requires extensive memory for large scale tasks. This is not relevant in our thesis as our datasets are relatively small. Still, the implementation of the svm algorithm with the radial kernel is done with the help of the `svm()` function in the `e1071` package (Meyer et al., 2018).

### 3.4.6 Random forest

The random forest algorithm (Ho, 1995) is a decision tree based ensemble learning classifier that is used for both classification and regression tasks. The random forest algorithm uses a multitude of decision trees to classify the outcome/class of a classification problem. There is also an important part about the decision trees that the algorithm generates, and that is that they are decorrelated. The decision trees are build using the bootstrap re-sampling algorithm, and each time a split in the decision tree is considered, a random sample of  $m$  predictors are chosen from the full sample of  $p$  predictors. At each split, a fresh sample of  $m$  predictors are chosen, where the number  $m$  is typically defined as  $\sqrt{p}$ . By doing this, the random forest algorithm overcomes the problem of small reductions in variance due to correlated decision trees as is often the case for algorithm like Bootstrap aggregating algorithms, e.g. bagging. The pseudocode for the random forest algorithm is mentioned below. As the random forest algorithm can be used for both classification and regression, we present only the pseudocode for the classification case. This is true for all classification algorithms used,

see (Friedman et al., 2009) and (James et al., 2013).

Advantages of the random forest algorithm are, as mentioned, that one reduces the risk of overfitting since the algorithm averages all the decision trees generated. It also reduces the overall variance since it splits the variables at random each time it builds a decision tree from the given bootstrapped data set. The disadvantages are that it is often difficult to interpret how the algorithm works. The results may also vary significantly with the number of trees that are to be produced. Regardless, the random forest algorithm is one of the most popular algorithms for doing classification and accordingly has good performance on many problems including non-linear ones. The actual implementation of this algorithm in this thesis is done using the `randomforest()` function in the `randomForest`-package in `r` (Liaw and Wiener, 2002).

---

**Algorithm 5:** Random forest

---

```

1 initialization;
2   X: training data
3   x: unknown sample
4   Number of Bootstrap samples  $B$ 
5 for  $i = 1, \dots, B$  do
6   | Draw a bootstrap sample  $\mathbf{Z}^*$  of size  $N$  from the training data  $\mathbf{X}$ 
7   | Grow a random forest  $T_b$  by the following:
8   | (i). Select  $m$  variables at random from the  $p$  variables.
9   | (ii). Pick the best variable/split-point among the  $m$ .
10  | (iii). Split the node into two daughter nodes.
11 end
12 Output the assembled trees  $\{T_b\}_1^B$ .
13 return  $\hat{C}_{rf}^B(x) = \text{majority vote } \{\hat{C}_b(x)\}_i^B$ .
```

---

### 3.5 k-fold cross-validation

When talking about evaluating a given classification algorithm, one typically mentions the test error rate, i.e. the average prediction error that results from using a statistical learning algorithm. The most common way of estimating the average prediction error is through the way of cross-validation (CV). This is a direct method of estimating the expected extra-



sample error  $Err = E [L(Y, \hat{f}(X))]$ , i.e. the average generalization error when the method  $\hat{f}(X)$  is applied to an independent test sample from the joint distribution of  $X$  and  $Y$ , see (Friedman et al., 2009) and (James et al., 2013). In the  $K$ -fold cross-validation method (Geisser, 1975) one typically splits the data into  $K$  roughly equal-sized parts (also called folds) and for a  $k$ th part, we fit the model on the remaining  $K - 1$  parts of the data and test/predict the classes in the  $k$ th part. This is done for  $k = 1, \dots, K$  and after this is done we are left with  $K$  estimates of the prediction error. This prediction error is typically defined as the mean square error (MSE), but could be any evaluation parameter, e.g. the accuracy, absolute mean square error etc. Assuming that the evaluation parameter was the MSE, then after calculating it for the  $k = 1, \dots, K$  folds, we average the MSEs to produce the  $k$ -fold cross-validation estimate. The formula is given by the following:

$$CV_k = \frac{1}{nk} \sum_{i=1}^k \sum_{j=1}^n (Y_{ij} - \hat{Y}_{ij})^2 \quad (3.16)$$

The  $K$ -fold cross-validation estimate is one of many criteria used to evaluate the performance of various classifiers. One clear advantage of using a  $K$ -fold cross-validation estimate is computational, i.e. the runtime properties

---

**Algorithm 6:**  $K$ -fold cross validation

---

```

1 initialization;
2   X: training data
3   Set of evaluation parameters  $\Theta$ 
4   Learning algorithm  $A$ 
5   Number of folds  $K$ 
6 Partition X into  $X_1, \dots, X_k$ 
7 for each  $\theta \in \Theta$  do
8   | for  $i = 1, \dots, K$  do
9   |    $h_{i,\theta} = A(X_i, \theta)$ 
10  | end
11  |  $error(\theta) = \frac{1}{K} \sum_{i=1}^K L_{X_i}(h_i, \theta)$ 
12 end
13 return  $\theta^* \in \Theta^*$ 
```

---

of the  $K$ -fold cross-validation algorithm is good as one limits the number of splits of the data to  $K$ -folds. This can also lower the variance of the prediction error since there is a higher chance that all the  $K$ -folds are less similar compared to a choice of  $K = N$  (also called leave-one-out cross validation), see (Friedman et al., 2009). In the setting of this thesis, we will evaluate the classification algorithm mentioned earlier using only the  $K$ -fold cross validation algorithm. The psedo-code for the  $K$ -fold algorithm is illustrated above. The implementation of the algorithm is done using the `trainControl()` function in the `caret` package in `r` (Kuhn et al., 2018). We have chosen to use  $K = 10$  folds for all algorithms to be evaluated. This is a very common choice in the literature, see e.g. Liu et al. (2014), Alonso-Betanzos et al. (2015), Masetic and Subasi (2016) and Koulaouz-idis et al. (2016).

# Chapter 4

## Experiments

In this chapter, we present the results of the experiments done in this thesis. The results are split into two sections. The first section presents the results from the cluster analysis and the second section that of the classification of clinical outcomes. For each of the sections we present an overview of the statistical learning problems that the algorithms are to solve. In this, we also present the assumptions and the evaluation criteria that are used to rank the algorithms and the final results.

### 4.1 Cluster analysis

In the cluster analysis, we try to see how well the various clustering algorithms perform in producing phenotypically distinct clinical patient groups with HFpEF and HFmrEF. We organize this section in the following way: we start out by looking at the full sample data set, i.e. `HFfullDataSet.Rdat`. After the pre-processing, we will run the principal components thought the clustering algorithms. The idea is to see how well the clustering algorithms perform in producing patient groups that are more homogeneous compared to the physicians evaluation. Our measure of success is the number of unique baseline characteristics that are statistically significant using the Person  $\chi^2$  test for categorical variables, ANOVA for normally distributed variables and Kruskal–Wallis test for non-normally distributed variables (Kruskal and Wallis, 1952). Significance used is that of the conventional 5% level. The implementation is done using the `multigrps`-function from the `CBCgrps`-package in `r` (Zhang et al., 2018). The algorithms are first going to

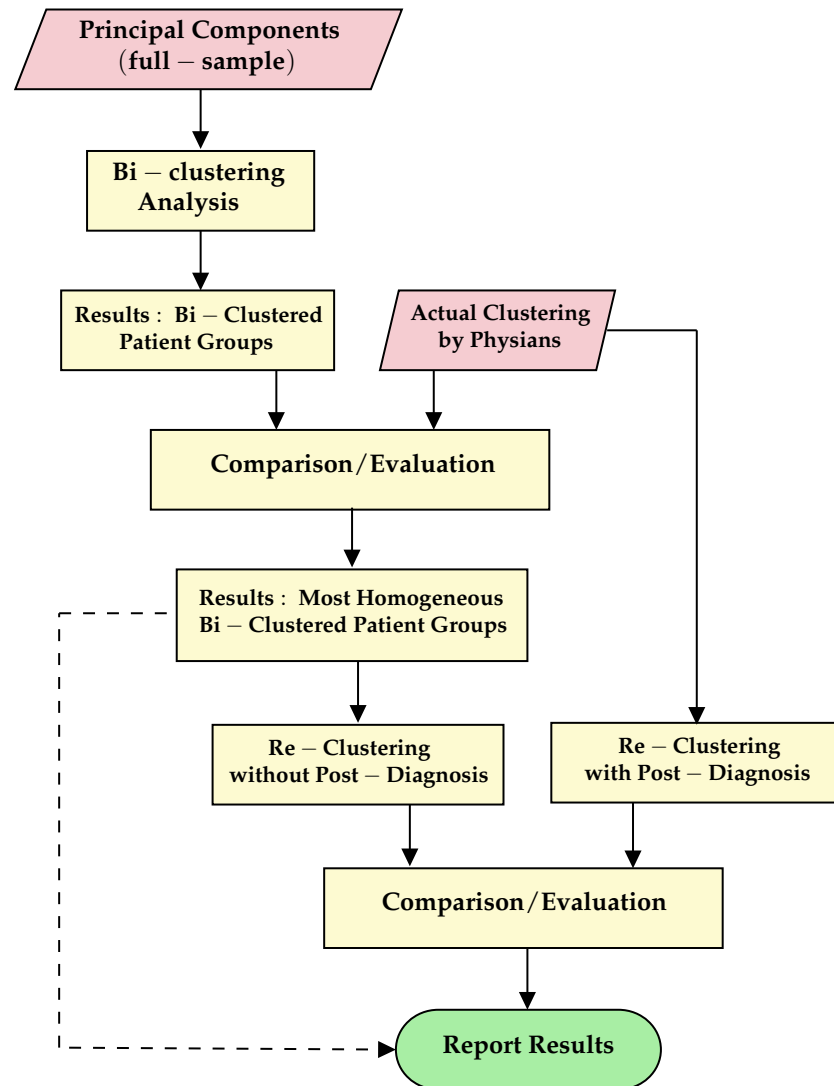
be performed on the binary clustering HF problem, i.e. to see how unique the patient groups produced are given that the only HF subtypes in the dataset is HFmrEF and HFpEF. This means that we assume a priori that there are only two clusters in the data set. After this we will see how well the algorithms perform in producing "new clusters" within the already defined patient groups from the first round. We will do the same analysis on both the groups that have been defined by the physicians and the "best" first round clustering algorithm. The full process flow for the cluster analysis is illustrated in Figure (4.1).

#### 4.1.1 The binary clustering HF problem

The current clustering problem assumes that the dataset is only comprised of two clusters, i.e. HFmrEF and HFpEF. Accordingly, we allow the algorithms to determine the patients that best correspond to each cluster. We have plotted the results of the binary clustering problem in Figure (A.3). This plot can in many ways seem very misleading as it only displays the results along the first two principal components. Still, the figure illustrates that even if one only cluster based on the first four principal components (27.32% of variance explained), one can produce more distinct patient

**Table 4.1:** Baseline characteristics of actual clustering

	Total	Cluster1	Cluster2	<i>p</i> -value
hb	109.34±20.29	107.85±21.22	110.93±19.18	0.141
pcv	0.34±0.06	0.33±0.06	0.34±0.06	0.159
age	78.64(69.22,84.17)	78.9(69.46,85.37)	78.08(68.73,82.74)	0.141
ewave	0.9(0.74,1.05)	0.92(0.8,1.1)	0.9(0.7,1.01)	0.056
gfr	48(32.5,70)	47(32,72)	51.96(33,67.77)	0.968
k	4.4(4,4.7)	4.4(4.1,4.7)	4.4(4,4.78)	0.664
los	10(4,22)	10(4,22)	10.5(4,21)	0.880
lvef	50(45,57.5)	57.5(55,60)	45(42,47.5)	0.000***
mcv	90.55(85.5,95)	89(85,94)	91.33(87,96)	0.011*
na	139(136,141)	139(136,141)	139(136,141)	0.650
ntprobnp	2848(1230.5,7374)	2217(997,5305)	4063.5(1886.5,9968.25)	0.000***
plts	204(156,268)	217(163,284)	190.87(148.5,241)	0.003**
wbc	7.8(5.9,10.5)	7.6(6,10.5)	8.1(5.9,10.4)	0.727
Total number of significant baseline char:			59	
Continuous:			4	
Categorical:			55	



**Figure 4.1:** *Process flow clustering of patient groups*

**Table 4.2:** Baseline characteristics of Hierarchical and K-Means clustering

	Total	Cluster1	Cluster2	<i>p</i> -value
hb	109.34±20.29	106.79±21.29	111.73±19.06	0.019*
pcv	0.34±0.06	0.33±0.07	0.35±0.06	0.035*
age	78.64(69.22,84.17)	78.9(68.94,85.36)	78.26(69.73,82.8)	0.416
ewave	0.9(0.74,1.05)	0.97(0.8,1.1)	0.9(0.7,1)	0.002**
gfr	48(32.5,70)	46(31,70)	54.44(34,71)	0.205
k	4.4(4,4.7)	4.4(4,4.7)	4.4(4,4.8)	0.219
los	10(4,22)	10(4,22)	11(4.25,21)	0.889
lvef	50(45,57.5)	57.5(52.5,60)	45(42.5,47.5)	0.000***
mcv	90.55(85.5,95)	89(84,94)	91.14(87,96)	0.002**
na	139(136,141)	139(136,141)	139(136,141)	0.321
ntprobnp	2848(1230.5,7374)	2327(1007,5695)	3723.5(1731.5,9557.75)	0.000***
plts	204(156,268)	215(163,287)	194(151,241)	0.007**
wbc	7.8(5.9,10.5)	7.7(5.9,10.5)	8.05(5.92,10.47)	0.731
Total number of significant baseline char:			62	
Continuous:			7	
Categorical:			55	

groups than the physicians. As we can see from Table (4.2), the hierarchical and k-means clustering algorithms both give the highest number of significant baseline characteristics (7 continuous and 55 categorical variables) compared with the actual clustering done by the physicians (4 continuous and 55 categorical variables, see table 4.1). The EM algorithm produces overall the lowest number of significant baseline characteristics (5 continuous and 49 categorical variables). Both the hierarchical and k-means algorithm produce the same clustering configurations. The baseline characteristics in the clustering of the patients using the hierarchical and k-means clustering show that for the HFpEF cluster the LVEF is on average 57.5% and for the second cluster (HFmrEF) the LVEF is on average 45%. These are very similar values to what the physicians produced. We can also see that for other baseline characteristics such as ntprobnp the average is at 2327 ng/L for the HFpEF group which is significantly different than that of the HFmrEF group 3723.5 ng/L. This is also very similar to what the physicians concluded with. For characteristics that are significantly different in the clustering with hierarchical and k-means, but not found in the clustering done by the physicians one can include the following continuous variables: hemoglobin (hb), packed cell volume (pcv) and the ewave (ewave). This may suggest that both the hierarchical and k-means clustering algorithms

**Table 4.3:** Baseline characteristics of EM clustering

	Total	Cluster1	Cluster2	<i>p</i> -value
hb	109.34±20.29	111.2±19.07	107.48±21.34	0.075
pcv	0.34±0.06	0.34±0.06	0.33±0.06	0.115
age	78.64(69.22,84.17)	77.81(69.22,82.76)	78.9(69.22,85.36)	0.199
ewave	0.9(0.74,1.05)	0.9(0.71,1.01)	0.93(0.8,1.1)	0.040*
gfr	48(32.5,70)	51.96(33,68.25)	47(32,72)	0.956
k	4.4(4,4.7)	4.4(4,4.8)	4.4(4,4.7)	0.363
los	10(4,22)	11(4,21)	10(4,22)	0.906
lvef	50(45,57.5)	45(42,47.5)	57.5(53.75,60)	0.000***
mcv	90.55(85.5,95)	91.14(87,96)	89(84.5,94)	0.007**
na	139(136,141)	139(136,141)	139(136,141)	0.330
ntprobnp	2848(1230.5,7374)	3985(1849.5,10038.25)	2226(990,5500)	0.000***
plts	204(156,268)	192.64(149.5,241.5)	217(163.5,286)	0.002**
wbc	7.8(5.9,10.5)	8.1(5.97,10.63)	7.6(5.9,10.35)	0.561
Total number of significant baseline char:			54	
Continuous:			5	
Categorical:			49	

can be used as appropriate tools for physicians. The results from the EM algorithm (Table 4.3) show that a lot of the similar baseline characteristics are not statistically significant. The LVEF (lvef) and NTproBNP (ntprobnp) is very similar to both the hierarchical and k-means clustering, but other characteristics such as hemoglobin (hb) and the packed cell volume (pcv) are not. Throughout the analysis we have found that the EM algorithm does not a good job of clustering patient groups compared to the hierarchical and k-means clustering algorithms. This could be because of the assumption of multivariate normal distribution does not hold for this data set or the fact that there is a high presence of categorical variables in the data set.

### 4.1.2 Analysis of post-diagnosis

In this section we will investigate the clustering results discussed previously. We have place an assumption of whether the physicians diagnosis is representative given an objective of producing the most unique patient groups. The clustering problem in this section assumes that the diagnosis done by the physicians is sufficient in regards to this objective, i.e. the clustering based on the *post-diagnosis* done by the physicians produces the

**Table 4.4:** Number of significant baseline characteristics

$C = 3$	With Post-Diagnosis		Without Post-Diagnosis		Mean
	HFpEF	HFmrEF	HFpEF	HFmrEF	
Hierarchical	53 (tab. A.5)	53 (tab. A.8)	48 (tab. A.11)	51 (tab. A.14)	51.25
K-Means	49 (tab. A.6)	53 (tab. A.9)	48 (tab. A.12)	53 (tab. A.15)	50.75
EM	56 (tab. A.7)	44 (tab. A.10)	42 (tab. A.13)	42 (tab. A.16)	46.00
Mean	52.67	50.00	46.00	48.67	

most unique patient groups. We compare these results to a clustering without an assumption of post-diagnosis done by the physicians and see if there are any substantial differences in results. We will only use the first two principal components (14.64% of variance explained) to cluster the patients. The evaluation criteria is the same as in the previous section. The number of clusters for the k-means and EM algorithm recommended by the `NbClust()` (Charrad et al., 2014) function in `r` was three, i.e. 13 of the 23 indices in the procedure recommended using  $C = 3$  as the optimal number of clusters for both the HFmrEF and HFpEF data sets. We can see from Table (4.4) that the hierarchical and k-means clustering algorithms produces the same number of significant baseline characteristics in half of the cases examined. We can also see from Table (4.4) that all algorithms analyzed produce on average more statistically significant baseline characteristics with the post-diagnosis assumption compared to without. The EM algorithm produces overall the lowest number of significant baseline characteristics (in three cases). An exception is when the EM algorithm is clustering HFpEF with post-diagnosis.

Beginning with the subtype HFpEF given the assumption of post-diagnosis, we can see from tables (A.5) and (A.6) that cluster 2 (hierarchical & k-means) seems to contain patients that have a higher average age (85.45) with a packed cell volume (pcv) that is on average  $0.33 \pm 0.05$ . This cluster is very similar to cluster 1 produced by the EM algorithm. The `ntprobnp` (`ntprobnp`) of cluster 3 (hierarchical & k-means) is the lowest at 1417 ng/L which is also statistically significant. The average number of red blood cells, i.e. the mean corpuscular volume (mcv) is at its lowest for cluster 1 (hierarchical & k-means) with an average of 87 femtolitres. The number of significant baseline characteristics produced by the hierarchical clustering is 53 (8 cont. and 48 categorical) and for the k-means its 49 (8 cont. and 41 categorical). The EM algorithm produces almost similar results for the



subgroup HFpEF as the hierarchical and k-means algorithm (table A.7). The second cluster produced by the EM algorithm is very similar to the third cluster produced by the hierarchical and the k-means algorithm. The ntprobnp (ntprobnp) for cluster one and two produced by the EM are very similar. Both are approximately 2750 ng/L. The third cluster produced by the EM algorithm has the lowest values for the ntprobnp (1525 ng/L). The total number of significant baseline characteristics for the EM algorithm is 56 (8 cont. and 48 categorical).

When looking at the HFmrEF clustering based on post-diagnosis (tables A.8, A.9 and A.10), we can see that a somewhat different results shows up, i.e. there are on average less significantly different baseline characteristics in all clusters produced by the algorithms regardless of whether the assumption of post-diagnosis is intact. For cluster 3 (hierarchical and k-means), we find the lowest ntprobnp (ntprobnp) at 2898.5 ng/L with a packed cell volume of  $0.38 \pm 0.04$ . This cluster also contains the patients with the lowest length of stay (7 days). The length of stay (LOS) is also a uniquely statistical significant baseline characteristic that is only significant in the HFmrEF subgroup of patients for all algorithms studied. Cluster 3 also has the highest hemoglobin (hb) at  $123.79 \pm 12.89$  g/100mL. The clustering results without the post-diagnosis assumption shows very different results. In general, Figure (A.6) and (A.7) show that the assignment of clustering happens with very little similarities, i.e. the cluster numbering as well as the baseline characteristics vary more when the assumption of post-diagnosis is removed. Comparing the number of significant baseline characteristics between the HFmrEF groups both with and without the post-diagnosis assumption shows that the latter has on average fewer baseline characteristics, see table (4.4). The same goes for the HFpEF group, i.e. we have reasons to believe that assuming the physicians diagnosis is representative, one can get additional clustered patient groups with higher degree of homogeneity compared to when this assumption is not intact. We have also demonstrated that the ML algorithms can be very useful in producing patient groups that are more phenotypically unique given that the objective is to challenge the diagnosis of the physicians, see section (4.1.1). Now that we have presented the results of the clustering analysis, we move on to the results of the classification of the clinical outcomes. The source code, relevant plots and tables can be found in the appendix (A).

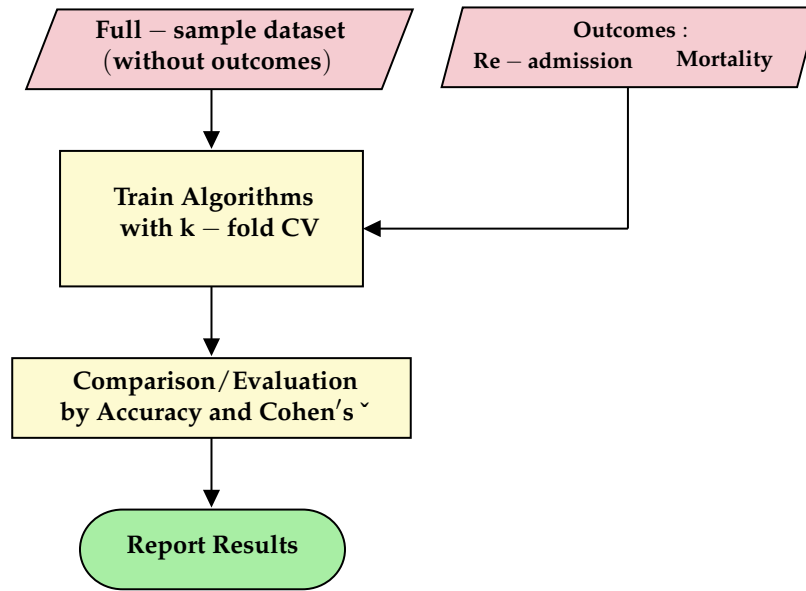


Figure 4.2: Process flow classification of clinical outcomes

## 4.2 Classification

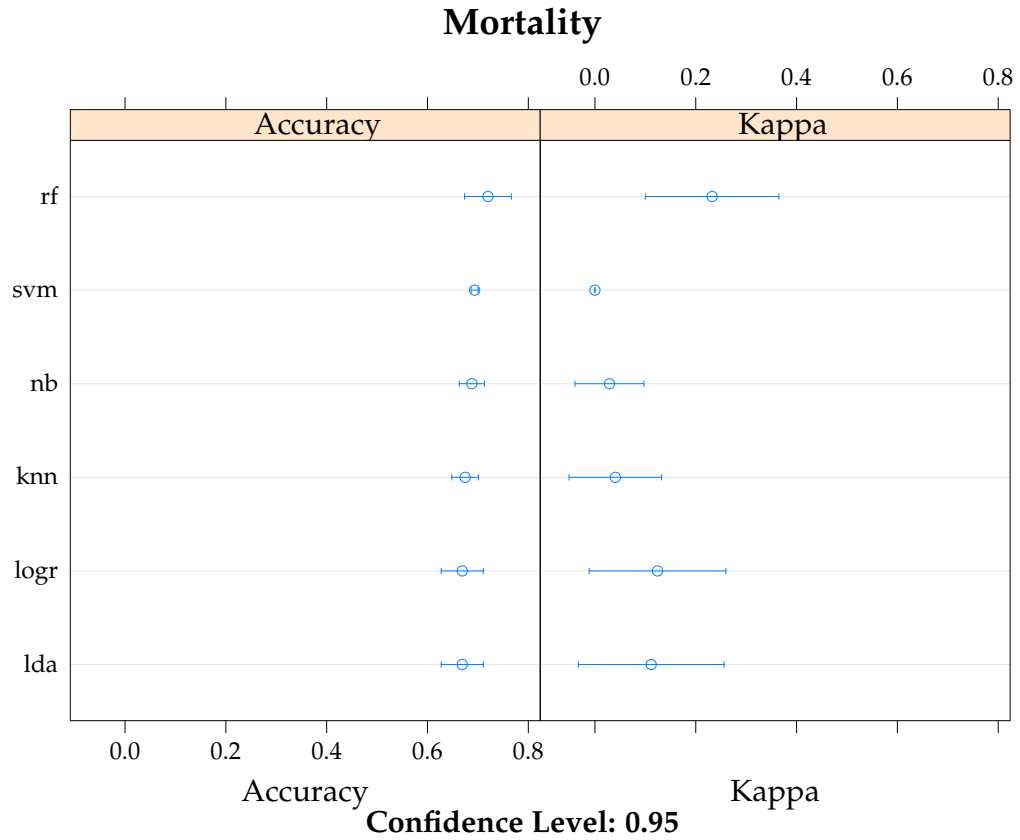
In this section we will present the results of the classification analysis. As mentioned in the ML procedure (figure 3.1), we run the imputed data set through the various classification algorithms and accordingly run a cross validation in order to estimate the accuracy of the various algorithms. The accuracy along with Cohen's kappa are the two evaluation criteria we use to rank the algorithms in this section. The process flow for the mentioned classification section is illustrated in Figure (4.2).

### 4.2.1 Mortality classifier

The statistical learning problem in this section is given by a two-class classification problem where mortality is the clinical outcome in question. Our objective is to see how well the algorithms mentioned in Figure (3.1) perform in predicting the probability of mortality. We will train the algorithms using 10-fold cross validation and evaluate the results using the accuracy, i.e. the proportion of true results and the Cohen's kappa defined by:

$$\kappa \equiv \frac{p_0 - p_e}{1 - p_e} \quad (4.1)$$

where  $p_0$  is the accuracy given by  $ACC = (TP + TN) / (P + N)$ , and  $p_e = 1 / N^2 \sum_k n_{k1} n_{k2}$ , where  $k$  is the number of categories / classes,  $N$  the number of items and  $n_{k1}$  the number of times rater  $i$  predicted category  $k$ .  $p_e$  is also referred to as the expected accuracy, i.e. what the accuracy that any *random* classifier would be expected to achieve. Accordingly, Cohen's kappa is also regarded as the inter-rater agreement for qualitative (categorical) items, i.e. it is similar to the classification accuracy, except that it is normalized at the baseline of random chance on a dataset. A possible interpretation of this



**Figure 4.3:** Binary classification results: mortality

statistics is given by the following (Ashby, 1991): less than 0.20 = Poor agreement, 0.20 to 0.40 = Fair agreement, 0.40 to 0.60 = Moderate agreement, 0.60 to 0.80 = Good agreement and 0.80 to 1 = Very good agreement. As mentioned earlier, the statistical learning problem is that of a Binary classification problem given by whether readmission / mortality occurred (TRUE) or not (FALSE), i.e. the expected accuracy is  $p_e = 0.50$ . The total number of patients with post-confirmed mortality in this data set is 115 (approx 36% of the total number of patients, see table 3.1). The results of the mortality classification is illustrated in Figure (4.3) and Table (4.5). In the table we notice that there are three algorithm that overall yield very decent results given the accuracy and the kappa. These are in order of importance: the random forest (rf), logistic regression (logr) and linear discriminant analysis (lda). As we can see the random forest (rf) (Ho, 1995) produces the best overall accuracy and kappa. The mean accuracy of the random forest classifier is estimated at 72% with a kappa at 0.23. The next classifier which compared to random forest also yields decent results is the logistic regression (logr) with a mean accuracy of 67% and a kappa of 12. The last algorithm is the linear discriminant analysis (lda). With the LDA the estimated prediction of the mortality in the HF patients is 67% with a

**Table 4.5:** Summary statistics mortality classification

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's
PANEL I: Accuracy							
knn	0.622	0.651	0.667	0.675	0.709	0.730	0.000
logr	0.568	0.628	0.680	0.669	0.709	0.763	0.000
lda	0.568	0.628	0.680	0.669	0.709	0.763	0.000
nb	0.649	0.658	0.684	0.688	0.723	0.737	0.000
svm	0.684	0.684	0.693	0.693	0.703	0.703	0.000
rf	0.595	0.703	0.711	0.720	0.745	0.838	0.000
PANEL II: Kappa							
knn	-0.146	-0.027	0.013	0.041	0.100	0.245	0.000
logr	-0.228	0.012	0.149	0.124	0.221	0.412	0.000
lda	-0.228	0.000	0.121	0.112	0.257	0.412	0.000
nb	-0.101	-0.022	0.000	0.029	0.094	0.215	0.000
svm	0.000	0.000	0.000	0.000	0.000	0.000	0.000
rf	-0.117	0.146	0.217	0.232	0.286	0.566	0.000

kappa of 11. We need to emphasize that even though one gets a somewhat high accuracy, the kappa is often considered to be a more robust evaluation criteria compared to the accuracy. This is because it takes into account that the agreement between estimated classification and actual classification can occur by chance. As the kappa is very low for all the classifiers mentioned in table (4.5), we cannot say with certainty that the classification algorithms can systematically predict mortality. However, we have reasons to believe that the three algorithms (random forest, logistic regression and linear discriminant analysis) all show signs of being fair algorithms when it comes to predicting mortality in HF patients. This is not discouraging results as similar results are reported in the literature, see e.g. [Shah et al. \(2014\)](#) and [Panahiazar et al. \(2015\)](#).

#### 4.2.2 Readmission classifier

In this section, we examine the classification problem related to readmission. We have defined the readmission outcome as whether a given patient was re-admitted in some form during the one-year period. As we mentioned in section (3.2) this could be either within 30 days (patient group V) or any other way (patient groups U). The results of the readmission classification is illustrated in Figure (4.4) and Table (4.6). The results are very much different than what we found with the mortality classification. Surprisingly, three algorithms seem to distinguish themselves from the others, namely the random forest (rf), support vector machines (svm) and logistic regression (logr). Interestingly, all three of these algorithm score very high both in terms of accuracy and kappa. The algorithm with the most promising results is the random forest. It has an estimated mean prediction accuracy

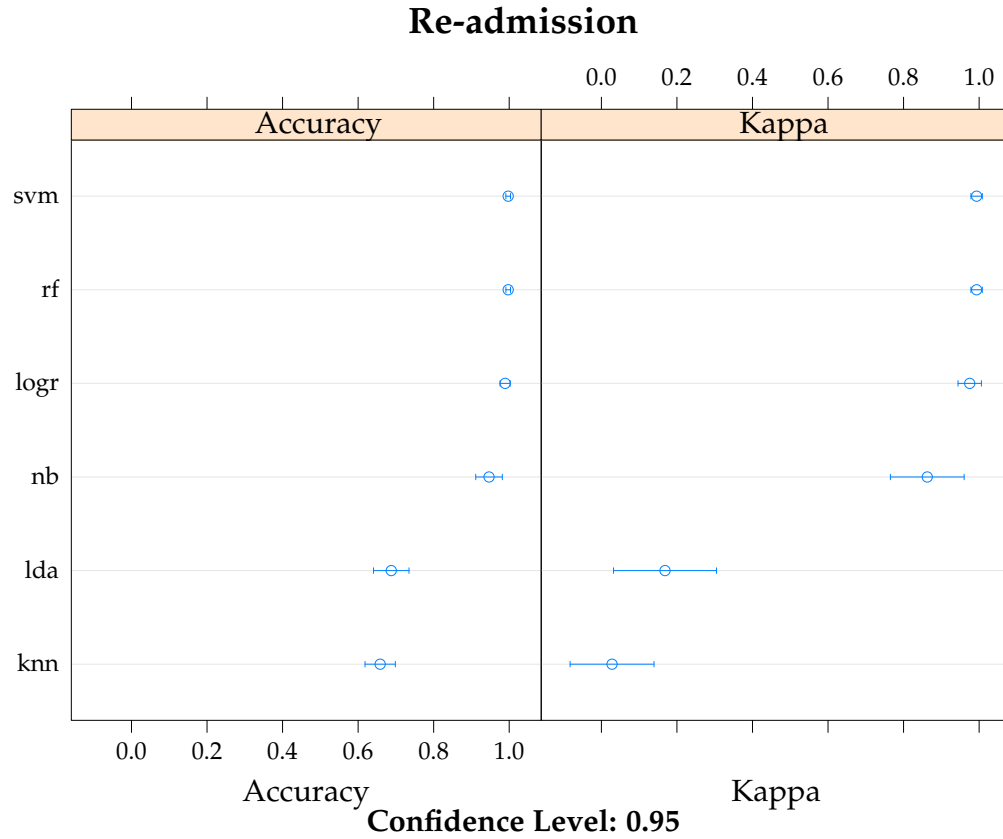
**Table 4.6:** Summary statistics re-admission classification

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's
PANEL I: Accuracy							
knn	0.595	0.609	0.654	0.658	0.698	0.737	0.000
lda	0.568	0.649	0.694	0.688	0.735	0.763	0.000
nb	0.838	0.921	0.960	0.947	0.974	1.000	0.000
logr	0.946	0.980	1.000	0.989	1.000	1.000	0.000
svm	0.973	1.000	1.000	0.997	1.000	1.000	0.000
rf	0.973	1.000	1.000	0.997	1.000	1.000	0.000

**Table 4.6:** Summary statistics re-admission classification (*continued*)

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's
PANEL II: Kappa							
knn	-0.183	-0.106	0.020	0.028	0.124	0.258	0.000
lda	-0.101	0.037	0.193	0.168	0.327	0.408	0.000
nb	0.539	0.806	0.899	0.863	0.937	1.000	0.000
logr	0.877	0.955	1.000	0.975	1.000	1.000	0.000
svm	0.934	1.000	1.000	0.993	1.000	1.000	0.000
rf	0.934	1.000	1.000	0.993	1.000	1.000	0.000

of 99.3% with a kappa of 0.997. The random forest is found to be the most superior classification algorithm in both predicting mortality and readmission. This is not uncommon as in the literature there are many studies that report of the random forest being a very effective algorithm for classifying clinical outcomes, see e.g. [Austin et al. \(2013\)](#) and [Zolfaghar et al. \(2013\)](#). The next algorithm that show potential in predicting readmission is the support vector machines (svm) algorithm. It also has an estimated mean accuracy of 99.3% with a kappa of 0.997. We consider this to be interesting as in the previous section we found that the SVM was one of the lowest performing algorithms when it comes to predicting mortality. This might suggest that modelling re-admission with a non-linear structure is more realistic than doing so with mortality. The last algorithm that show potential is that of the logistic regression (logr). The estimated mean accuracy for this algorithm was 97.5% with a kappa of 0.989. In addition to having a very good accuracy and kappa, its worth mentioning that given its level of simplicity, one can argue that the logistic regression algorithm is more preferable to more advanced classification algorithm. In both the cases that we have examined, we have found that the random forest and the logistic regression algorithm perform decently. Both algorithms are also very different in terms of their level of complexity. They are also very much used in the literature and is often a favourite among practitioners of medical statistical analysis, see e.g. [Austin et al. \(2013\)](#), [Zolfaghar et al. \(2013\)](#), [Shah et al. \(2014\)](#) and [Panahiazar et al. \(2015\)](#). Accordingly, we have reasons to believe that both the random forest and the logistic regression are the two main algorithms that show the most potential in predicting both the mortality and readmission of HF patients.



**Figure 4.4:** Binary classification results: readmission

### 4.3 Discussion

The objective of this thesis was two fold: (i) we attempted to give a thorough analysis of how well various clustering algorithms (hierarchical, k-means and expectation-maximization) perform in producing phenotypically distinct clinical patient groups (i.e. phenomapping) with HFpEF and HFmrEF. Our strategy for answering this research question has been to compare the level of dissimilarity between patient groups that are produced at two levels. Firstly, we looked at the binary clustering problem where we compared the patient groups produced by the algorithms with those produced by the physicians. We found that if one defines the optimal clustering as that which has the highest number of significantly different baseline characteristics. Then we have reasons to believe that the hierarchical and

k-means clustering algorithms show signs of being better at clustering patients with HF compared to the physicians. Overall these algorithms produce 62 significantly different baseline characteristics compared to 59 produced by the physicians. Secondly, we looked at how well the clustering algorithms performed in producing "new" patient groups within both subtypes of HF. We analyzed this by attempting to re-cluster patient groups from both subtypes (HFmrEF and HFpEF) produced by the physicians and the "best" ML algorithms. Re-clustering within the subtypes generated by the physicians (also called the 'post-diagnosis' assumption) seem to show the greatest potential as the average number of significantly different baseline characteristics is the highest for this clustering compared to when the assumption is removed. On average all algorithm produce approximately 53 (HFpEF) and 50 (HFmrEF) significantly different baseline characteristics when the post-diagnosis assumption is present compared to when its removed (46, HFpEF and 49, HFmrEF). However, if the objective is to use the results to find additional "new clusters", we cannot say with certainty that the choice of clustering algorithms or the clustering data used (whether it is with or without post-diagnosis) will systematically enhance the "uniqueness" of the patient groups. We need to emphasize that the results need to be treated with great caution as they are very sensitive to the number of principal components used, the imputation method and the sample size. Nevertheless, the hierarchical and k-means algorithm seems to have the potential to be used as a tool by physicians to cross-check their assumptions and rational in order to further improve the diagnosis of patients with the preserved and mid-range subtypes of HF. Similar finding are also reported in the literature, see e.g. [Shah et al. \(2014\)](#), [Ahmad et al. \(2014\)](#), [Alonso-Betanzos et al. \(2015\)](#), [Kao et al. \(2015\)](#), [Ahmad et al. \(2016\)](#) and [Katz et al. \(2017\)](#).

In the second (ii) part of the thesis we attempted to evaluate the performance of various classification algorithms (k-nearest neighbour, logistic regression, linear discriminant analysis, support vector machines and random forest) in predicting mortality and readmission. The results seem to suggest that the random forest and logistic regression are good candidates for doing just that. They both rank very high compared to the other algorithms evaluated. The random forest has an estimated accuracy of approximately 72% for mortality and 99.7% for readmission. The logistic regression had similar results with approximately 67% accuracy for mortality and 97.5% for readmission. The results seem promising, but we



need to emphasize that these results also need to be treated with great causation. As we mentioned in chapter (3), both the logistic regression and random forest have disadvantages. One of the strongest disadvantages for the logistic regression is the fact that one assumes a priori that the independent variables that are inputted into the algorithm are just that, i.e. independent among each other. This is a very strong assumption that we have not conducted a rigorous examination of. This may in many ways affect the results. If the assumption of independence is not present then the model estimated may tend to overweight the significance of the observations that are not independent. The logistic regression also assumes little or no multicollinearity among the independent variables. This is also something that we have not tested in detail due to limitations. However, a way of testing this is thought the use of variance-inflation-factors (VIF) or other measures of multicollinearity severity. This may imply that the results are susceptible to invalid inference and this is a major drawback to the results that we need to make the reader informed about. The random forest algorithm does not directly assume independence ([Friedman et al., 2009](#)), but it assumes that the data is representative. As we mentioned in section (3.2), the data set used in this thesis had 15% missing values. This is an aspect about our study that should not be neglected. We addressed the problem of missing values by imputation with a bootstrapped EM algorithm ([Honaker et al., 2011](#)). Maximum likelihood method such as this one is praised by many in the literature for its ability to impute missing values, even if the variables in question are mixed, see [Schafer \(1997\)](#), [Schafer and Olsen \(1998\)](#) and [Allison \(1999\)](#). However, we cannot with certainty say that this is the most optimal method of treating the missing values in the data set. Similarly to the clustering results, we need to emphasize that the results of the classification is sensitive to the choice of imputation method. Nevertheless, our findings seem to confirm the finding reported in the literature, see e.g. [Austin et al. \(2012\)](#), [Zolfaghar et al. \(2013\)](#), [Shah et al. \(2014\)](#), [Panahiazar et al. \(2015\)](#) and [Koulaouzidis et al. \(2016\)](#).

For future analysis, we recommend broadening this study by evaluating more algorithms. This is especially the case for the clustering analysis. All the algorithms that we analyzed have an assumption of no noise, i.e. that all the patients belong to a cluster. This is a somewhat strong assumption as it could be the case that some patients lay in an area that is "too uncertain" to assign to either subtypes. It could be interesting to see how density-based algorithm such as DBSCAN ([Ester et al., 1996](#)) would fair in producing phe-

notypically distinct patient groups. It could also be interesting to see how the classification results vary with the subtype of HF, i.e. is it reasonable to assume that some algorithm predict mortality and readmission more accurately if one is to limit the data to one subtype of HF? These are all suggestions for future analysis that can broaden our understanding of the complex syndrome that is heart failure.

# Chapter 5

## Conclusion

In this thesis, we attempt to investigate how well various clustering algorithms (hierarchical clustering, k-means and expectation–maximization) perform in producing phenotypically distinct clinical patient groups (i.e. phenomapping) with heart failure with preserved ejection fraction (HFpEF) and mid-range ejection fraction (HFmrEF). Furthermore, we evaluate the performance of various classification algorithms (k-nearest neighbours, logistic regression, naive Bayes, linear discriminant analysis, support vector machines and random forest) in predicting patient mortality and readmission. All the algorithms were applied on a data set consisting of 375 patients with symptomatic heart failure (HF) identified at a tertiary hospital in the United Kingdom.

In the clustering of the patients based on the subtypes HFmrEF and HFpEF, we found that the hierarchical and k-means clustering algorithms show signs of being better at clustering patients with HF compared to the physicians. Overall these algorithms produced 62 significantly different baseline characteristics compared to 59 produced by the physicians. However, if the objective is to use the results to find additional “new clusters”, then we cannot say with certainty that the choice of clustering algorithms or the clustering data used (whether it’s with or without post-diagnosis) will systematically enhance the “uniqueness” of the patient groups.

In the classification of mortality and readmission, we found that the random forest and logistic regression show promising potential. That is, the level of accuracy for which the algorithms predicted mortality and readmission rank high compared to the other algorithms evaluated. The random forest predicted mortality with 72% accuracy and readmission

with 99.7%. The logistic regression had similar results with approximately 67% accuracy for mortality and 97.5% for readmission. Similar results are reported in the literature. Our findings lend support to the idea that the application of such algorithms may help in better understanding the complex nature of a clinical syndrome such as HF.

# Appendix A

## Data Description

In this appendix we present a descriptive overview of the data used in this thesis. This includes: an overview and explanation of the variables used (A.1), the R-packages (A.2) used and some relevant plots (A.4) to support the finding in the thesis. The source code used to produce the relevant plots can be found in appendix (B).

### A.1 Variables

**Table A.1:** Phenotype domains used for clinical metrics

Phenotype domain	Clinical Variables
Demographics	Age, gender, ethnicity
Admission symptoms	Breathless, chest pain, orthnopea, paroxysmal nocturnal dyspnoea, peripheral oedema, palpitations, syncope
Admission signs	Admission heart rate (HR), admission systolic blood pressure (SBP), admission diastolic blood pressure (DBP), admission mean blood pressure (MAP), admission weight, height, admission body mass index, discharge weight

**Table A.1 Continued:** Phenotype domains used for clinical metrics

Phenotype domain	Clinical Variables
Risk factors	Atrial fibrillation, hypertension, diabetes, chronic obstructive pulmonary disease, coronary artery disease, history of cerebrovascular disease, hypercholesterolaemia, obstructive sleep apnoea, iron deficiency, obesity
Comorbidities	Depression, dementia, amyloidosis, cancer
12 lead electrocardiogram (ECG)	Rhythm, rate, QRS duration, evidence of atrioventricular (AV) block, T wave inversion (TWI), evidence of left ventricular hypertrophy (LVH), presence of pacemaker
Laboratory tests	Haemoglobin, mean cell volume (MCV), packed cell volume (PCV), white blood cells (WBC), platelets, sodium, potassium, glomerular filtration rate (GFR), albumin, HbA1C, glucose, iron levels, transferrin saturations (TSAT), ferritin, troponin
Echocardiography	Left ventricular ejection fraction (LVEF), left atrial diameter left atrial area, right atrial area, E wave, E deceleration time, Lateral e', lateral S, E/e', dilated LV, A wave, E:A, gradient, regional wall motion abnormalities, left ventricular hypertrophy, tricuspid annular planesystolic excursion (TAPSE), pulmonary artery systolic pressure (PASP), mitral regurgitation, tricuspid regurgitation, aortic regurgitation, aortic stenosis
Outcome	Length of stay, time to heart failure hospitalization, time to mortality

## A.2 R-packages

**Table A.2:** Packages used in thesis

Package	Title	Version
Amelia	A Program for Missing Data	1.7.5
BaylorEdPsych	R Package for Baylor University Educational Psychology Quantitative Courses	0.5
caret	Classification and Regression Training	6.0-80
CBCgrps	Compare Baseline Characteristics Between Groups	2.3
docstring	Provides Docstring Capabilities to R Functions	1.0.0
factoextra	Extract and Visualize the Results of Multivariate Data Analyses	1.0.5
FactoMineR	Multivariate Exploratory Data Analysis and Data Mining	1.41
ggpubr	'ggplot2' Based Publication Ready Plots	0.1.8
gridExtra	Miscellaneous Functions for "Grid" Graphics	2.3
Hmisc	Harrell Miscellaneous	4.1-1
mclust	Gaussian Mixture Modelling for Model-Based Clustering, Classification, and Density Estimation	5.4.1
mice	Multivariate Imputation by Chained Equations	3.3.0
mlbench	Machine Learning Benchmark Problems	2.1-1
NbClust	Determining the Best Number of Clusters in a Data Set	3.0
plotrix	Various Plotting Functions	3.7-4
reporttools	Generate LaTeX Tables of Descriptive Statistics	1.1.2
rlist	A Toolbox for Non-Tabular Data Manipulation	0.4.6.1
tikzDevice	R Graphics Output in LaTeX Format	0.11
VIM	Visualization and Imputation of Missing Values	4.7.0
xtable	Export Tables to LaTeX or HTML	1.8-2

## A.3 Descriptive statistics

**Table A.3:** Patient characteristics: HFpEF

Variable	$n$	#Na	Min	Max	$\bar{x}$	$\tilde{x}$	$s$	$q_1$	$q_3$
PANEL II: Demographics									
age	193	0	29.0	100.8	76.3	78.9	12.1	69.5	85.4
gender	193	0	0.0	1.0	0.6	1.0	0.5	0.0	1.0
white	193	0	0.0	1.0	0.7	1.0	0.5	0.0	1.0
asian	193	0	0.0	1.0	0.1	0.0	0.2	0.0	0.0
black	193	0	0.0	1.0	0.3	0.0	0.4	0.0	1.0
PANEL III: Admission symptoms									
breathless	185	8	0.0	1.0	0.8	1.0	0.4	1.0	1.0
PANEL IV: Admission signs									
sbp	182	11	55.0	242.0	146.9	145.0	31.7	125.0	167.0
dbp	183	10	25.0	195.0	80.5	80.0	22.1	67.0	89.0
admissionwgt	160	33	41.5	158.0	78.9	76.7	23.3	60.1	93.9
bp	192	1	0.0	1.0	0.8	1.0	0.4	1.0	1.0
bmiadmission	148	45	16.8	107.1	30.7	29.3	10.5	23.6	35.4
pulse	182	11	44.0	211.0	84.7	83.0	22.1	70.0	95.0
PANEL V: Risk factors									
a-fib	189	4	0.0	1.0	0.5	0.0	0.5	0.0	1.0
copdasthma	190	3	0.0	1.0	0.4	0.0	0.5	0.0	1.0
irondef	69	124	0.0	1.0	0.6	1.0	0.5	0.0	1.0
dm	188	5	0.0	1.0	0.5	1.0	0.5	0.0	1.0
obesity	185	8	0.0	1.0	0.5	1.0	0.5	0.0	1.0
copdasthma.1	190	3	0.0	1.0	0.4	0.0	0.5	0.0	1.0
ihd	186	7	0.0	1.0	0.4	0.0	0.5	0.0	1.0
PANEL VI: Comorbidities									
comorbidities	193	0	0.0	9.0	4.2	4.0	1.8	3.0	5.0
PANEL VII: Electrocardiography									
ecgqrsduration	157	36	55.0	177.0	101.3	98.0	20.8	88.0	112.0
ecgqrsother	193	0	0.0	1.0	0.0	0.0	0.2	0.0	0.0
ecgrate	159	34	41.0	191.0	83.0	80.0	23.1	70.0	92.0
ecgrhythmother	193	0	0.0	1.0	0.1	0.0	0.2	0.0	0.0
lvh	169	24	0.0	1.0	0.1	0.0	0.3	0.0	0.0
normalecgqrs	193	0	0.0	1.0	0.6	1.0	0.5	0.0	1.0
lbbb	193	0	0.0	1.0	0.0	0.0	0.2	0.0	0.0
rbbb	193	0	0.0	1.0	0.1	0.0	0.3	0.0	0.0
sr	193	0	0.0	1.0	0.6	1.0	0.5	0.0	1.0
PANEL VIII: Laboratory tests									
hb	192	1	47.0	185.0	107.6	107.5	21.1	91.8	123.0
wbc	192	1	2.9	209.4	10.2	7.6	15.8	6.0	10.5
tsat	94	99	4.0	92.0	20.4	18.0	13.8	11.0	24.8
plts	192	1	51.0	497.0	229.4	217.0	89.5	163.0	284.2
pcv	193	0	0.2	0.6	0.3	0.3	0.1	0.3	0.4



Table A.3: Patient characteristics: HFpEF (*continued*)

Variable	$n$	#Na	Min	Max	$\bar{x}$	$\tilde{x}$	$s$	$q_1$	$q_3$
ferritin	71	122	9.0	2223.0	378.2	173.0	533.8	61.5	443.5
k	189	4	2.4	8.7	4.4	4.4	0.6	4.1	4.7
ironlevels	95	98	2.0	23.0	8.6	7.0	4.8	5.0	11.0
chol	190	3	0.0	1.0	0.5	1.0	0.5	0.0	1.0
ntprobnp	193	0	81.0	70000.0	5047.3	2217.0	8487.4	997.0	5305.0
gfr	193	0	3.0	221.0	54.1	47.0	31.1	32.0	72.0
mcv	193	0	57.0	117.0	88.8	89.0	8.9	85.0	94.0
na	193	0	110.0	148.0	138.2	139.0	4.9	136.0	141.0
PANEL IX: Echocardiography									
lvef	191	2	50.0	72.5	57.1	57.5	4.5	55.0	60.0
ewave	174	19	0.4	1.6	0.9	0.9	0.3	0.7	1.1
pasp	122	71	14.0	85.0	43.5	42.5	14.2	34.0	51.8
ee	152	41	2.0	37.0	13.4	12.5	5.8	9.0	16.0
mr	193	0	0.0	2.0	0.5	0.0	0.7	0.0	1.0
tr	193	0	0.0	3.0	0.9	1.0	0.8	0.0	1.0
as	193	0	0.0	2.0	0.1	0.0	0.3	0.0	0.0
ai	193	0	0.0	2.0	0.2	0.0	0.5	0.0	0.0
rvfunction	192	1	0.0	4.0	0.6	0.0	1.2	0.0	0.2
af	193	0	0.0	1.0	0.2	0.0	0.4	0.0	0.0
PANEL X: Outcomes									
timetohfadm	69	124	3.8	718.8	192.5	122.7	197.8	33.0	270.0
hfhospitalisation	193	0	0.0	1.0	0.4	0.0	0.5	0.0	1.0
los	171	22	1.0	372.0	15.8	8.0	31.3	4.0	19.0

Table A.4: Patient characteristics: HFmrEF

Variable <sup>i</sup>	$n$	# Na	Min	Max	$\bar{x}$	$\tilde{x}$	$s$	$q_1$	$q_3$
PANEL I: Identification									
patientid	182	0	1.0	193.0	96.9	97.5	56.6	47.2	146.5
PANEL II: Demographics									
gender	182	0	0.0	1.0	0.4	0.0	0.5	0.0	1.0
white	182	0	0.0	1.0	0.7	1.0	0.5	0.0	1.0
asian	182	0	0.0	1.0	0.1	0.0	0.3	0.0	0.0
black	182	0	0.0	1.0	0.2	0.0	0.4	0.0	0.0
PANEL III: Admission symptoms									
breathless	55	127	0.0	3.0	2.4	3.0	1.0	2.0	3.0
PANEL IV: Admission signs									
sbp	98	84	86.0	242.0	132.6	126.5	27.7	114.2	147.8
dbp	95	87	45.0	591.0	80.2	72.0	55.7	62.0	85.0
admissionwtg	51	131	21.0	134.9	80.6	80.6	21.8	66.7	96.4
bp	182	0	0.0	1.0	0.7	1.0	0.5	0.0	1.0
bmiadmission	4	178	18.7	36.1	26.0	24.7	8.0	20.2	30.5
pulse	98	84	54.0	144.0	88.8	85.0	21.9	71.2	100.0



**Table A.4:** Patient characteristics: HFmrEF (*continued*)

Variable	$n$	#Na	Min	Max	$\bar{x}$	$\tilde{x}$	$s$	$q_1$	$q_3$
timetohfadm	122	60	0.4	575.9	84.5	44.9	109.6	11.9	114.7
hfhospitalisation	182	0	0.0	1.0	0.2	0.0	0.4	0.0	0.0
los	169	13	1.0	196.0	16.9	9.0	24.2	4.0	19.0

<sup>i</sup> Note:  $n$  - number of observations, #Na - number of missing data, Min - minimal, Max - maximal,  $\bar{x}$  - arithmetic mean,  $\tilde{x}$  - median,  $s$  - standard deviation,  $q_1$  - first quartile and  $q_3$  - third quartile.

**Table A.5:** Baseline characteristics of Hierarchical clustering HFpEF based on post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	89.62±15.25	107.37±15.78	120.22±19.61	0.000***
pcv	0.28±0.05	0.33±0.05	0.37±0.06	0.000***
age	77.07(64.44,81.8)	85.45(77.81,88.81)	75.27(67.08,82.06)	0.000***
ewave	1.02(0.9,1.2)	0.9(0.77,1)	0.9(0.7,1)	0.000***
gfr	31(22.75,45)	47(38.25,70.75)	60(41,84)	0.000***
k	4.45(4.17,4.8)	4.2(3.7,4.6)	4.4(4.1,4.7)	0.030*
los	11(5,21.29)	10.5(5,22.18)	7(4,20.87)	0.217
lvef	57.5(55,60)	55.5(52.5,57.5)	57.5(55,60)	0.063
mcv	87(80.75,92)	90(85.25,95)	90(86,95.5)	0.010*
na	138(134.75,141)	139(137,142)	139(137,141)	0.107
ntprobnp	2745(1622,7647.25)	2432(1269.75,5920.5)	1417(714.5,3601.5)	0.001**
plts	244.5(170,307.25)	212(164,247)	215(162,286.5)	0.393
wbc	7.65(5.37,10.35)	7.15(5.72,10.7)	8.1(6.45,10.3)	0.270
Total number of significant baseline char:			53	
Continuous:			8	
Categorical:			45	

**Table A.6:** Baseline characteristics of K-Means clustering HFpEF based on post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	120.22±19.61	107.37±15.78	89.62±15.25	0.000***
pcv	0.37±0.06	0.33±0.05	0.28±0.05	0.000***
age	75.27(67.08,82.06)	85.45(77.81,88.81)	77.07(64.44,81.8)	0.000***
ewave	0.9(0.7,1)	0.9(0.77,1)	1.02(0.9,1.2)	0.000***
gfr	60(41,84)	47(38.25,70.75)	31(22.75,45)	0.000***
k	4.4(4.1,4.7)	4.2(3.7,4.6)	4.45(4.17,4.8)	0.030*
los	7(4,20.87)	10.5(5,22.18)	11(5,21.29)	0.217
lvef	57.5(55,60)	55.5(52.5,57.5)	57.5(55,60)	0.063
mcv	90(86,95.5)	90(85.25,95)	87(80.75,92)	0.010*
na	139(137,141)	139(137,142)	138(134.75,141)	0.107
ntprobnp	1417(714.5,3601.5)	2432(1269.75,5920.5)	2745(1622,7647.25)	0.001**
plts	215(162,286.5)	212(164,247)	244.5(170,307.25)	0.393
wbc	8.1(6.45,10.3)	7.15(5.72,10.7)	7.65(5.37,10.35)	0.270
Total number of significant baseline char:			49	
Continuous:			8	
Categorical:			41	

**Table A.7:** Baseline characteristics of EM clustering HFpEF based on post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	105.98±17.53	89.37±14.55	118.61±19.42	0.000***
pcv	0.33±0.05	0.28±0.04	0.37±0.06	0.000***
age	85.45(77.81,88.65)	75(63.26,80.41)	77.03(68.05,82.11)	0.000***
ewave	0.9(0.79,1)	1.1(0.9,1.2)	0.9(0.7,1)	0.000***
gfr	45.5(38,67.75)	31(21.25,45)	60(40,84)	0.000***
k	4.2(3.7,4.6)	4.4(4.13,4.8)	4.5(4.1,4.7)	0.012*
los	11(5,22.18)	11.5(4.25,21.76)	8(4,20.14)	0.269
lvf	56.75(52.5,57.5)	57.5(55,60)	57.5(55,60)	0.194
mcv	89.5(85.25,94)	87(80.25,92)	90(86,97)	0.008**
na	139.5(137,142)	138(135,141)	139(136,141)	0.102
ntprobnp	2755(1451.5,6684.25)	2745(1566,7993.75)	1525(727,3590)	0.000***
plts	212(164,247)	235.5(170,309.75)	219(163,284)	0.402
wbc	7.15(5.8,10.77)	7.55(5.42,10.17)	7.9(6.4,10.3)	0.506
Total number of significant baseline char:			56	
Continuous:			8	
Categorical:			48	

**Table A.8:** Baseline characteristics of Hierarchical clustering HFmrEF based on post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	91.01±14.72	109.11±16.81	123.79±12.89	0.000***
k	4.58±0.66	4.51±0.58	4.18±0.48	0.000***
pcv	0.28±0.04	0.34±0.05	0.38±0.04	0.000***
age	71.53(65.87,82.74)	77.15(70.09,82.04)	79.19(68.12,82.9)	0.455
ewave	0.8(0.7,1)	0.96(0.8,1.14)	0.83(0.67,0.96)	0.003**
gfr	49.98(22,77)	43(30,55)	62(44.5,77.25)	0.000***
los	17(10,36)	12(4,21.48)	7(3,14.25)	0.000***
lvef	45(42,47.5)	45(42,47.5)	42.75(42.5,45)	0.344
mcv	91(87,96)	90(85,95)	93(88,97)	0.159
na	138(135,141)	139(135,141)	139(137.02,142)	0.049*
ntprobnp	6598(2857,27818)	4953(1861,10914)	2898.5(1587.75,5163.5)	0.005**
plts	210(147,285)	204(153,250)	174.74(149.5,215.75)	0.107
wbc	8.2(6.3,9.6)	8.3(6.9,9.8)	7.31(5.7,8.6)	0.025
Total number of significant baseline char:			53	
Continuous:			8	
Categorical:			45	

**Table A.9:** Baseline characteristics of K-Means clustering HFmrEF based on post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	91.01±14.72	109.11±16.81	123.79±12.89	0.000***
k	4.58±0.66	4.51±0.58	4.18±0.48	0.000***
pcv	0.28±0.04	0.34±0.05	0.38±0.04	0.000***
age	71.53(65.87,82.74)	77.15(70.09,82.04)	79.19(68.12,82.9)	0.455
ewave	0.8(0.7,1)	0.96(0.8,1.14)	0.83(0.67,0.96)	0.003**
gfr	49.98(22,77)	43(30,55)	62(44.5,77.25)	0.000***
los	17(10,36)	12(4,21.48)	7(3,14.25)	0.000***
lvef	45(42,47.5)	45(42,47.5)	42.75(42.5,45)	0.344
mcv	91(87,96)	90(85,95)	93(88,97)	0.159
na	138(135,141)	139(135,141)	139(137.02,142)	0.049*
ntprobnp	6598(2857,27818)	4953(1861,10914)	2898.5(1587.75,5163.5)	0.005**
plts	210(147,285)	204(153,250)	174.74(149.5,215.75)	0.107
wbc	8.2(6.3,9.6)	8.3(6.9,9.8)	7.31(5.7,8.6)	0.025
Total number of significant baseline char:			53	
Continuous:			8	
Categorical:			45	



**Table A.10:** Baseline characteristics of EM clustering HFmrEF based on post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	83.17±14.19	105.83±17.56	120.8±14.91	0.000***
k	4.65±0.84	4.53±0.57	4.22±0.51	0.001**
pcv	0.26±0.04	0.33±0.05	0.37±0.04	0.000***
age	68.63(41.33,74.15)	76.91(69.62,82.01)	80.97(68.7,83.32)	0.031
ewave	0.88(0.7,1.01)	0.94(0.79,1.12)	0.82(0.67,0.95)	0.009**
gfr	27(13.75,82.25)	42.5(27.5,58)	61(45.75,76.25)	0.000***
los	27.5(13.75,62)	12.5(5,21)	8(3,16.5)	0.006**
lvef	45(42,45.62)	45(42,47.5)	43(42.5,45)	0.517
mcv	91.5(86,96)	89.94(85.06,94)	93(89,97)	0.027*
na	136.5(133.75,141)	139(135.25,141)	139(137,142)	0.175
ntprobnp	19446.5(4178.5,59423.25)	5640.5(1953.25,11400.75)	2898.5(1636,5163.5)	0.001**
plts	155(117,236.25)	205.36(157.25,256)	177.5(147,224)	0.081
wbc	6.55(5.6,7.77)	8.4(7.1,10.3)	7.25(5.7,8.8)	0.001**
Total number of significant baseline char:			44	
Continuous:			9	
Categorical:			35	

**Table A.11:** Baseline characteristics of Hierarchical clustering HFpEF with-out post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	87.94±13.31	110.91±17.01	117.31±20.34	0.000***
pcv	0.28±0.04	0.34±0.05	0.37±0.06	0.000***
age	75(64.94,81.79)	84.31(77.36,88.63)	74.08(65.25,82.89)	0.000***
ewave	1.1(0.92,1.27)	0.9(0.7,1)	0.94(0.7,1.1)	0.000***
gfr	29(20.5,44.25)	47(38,68)	55.5(40.25,83.75)	0.000***
k	4.44(4.1,4.8)	4.2(3.7,4.5)	4.45(3.92,4.78)	0.008**
los	12(5,22.19)	10(4,23.83)	8(4,20.76)	0.246
lvef	55(52.5,58.12)	57.5(55,60)	57.5(55,60)	0.203
mcv	87(79.25,92)	89(85,94)	90.5(85.25,96)	0.039
na	137.5(134.75,141)	140(137,142)	139.5(137,141)	0.024*
ntprobnp	3852(1879.5,9806.75)	1995(934,5573)	1653.5(870.25,3760.75)	0.000***
plts	226(162,303.75)	210(170,251.5)	217(160.25,296.5)	0.889
wbc	7.75(5.7,9.92)	7.2(5.55,10.55)	8.1(6.63,11.13)	0.121
Total number of significant baseline char:			48	
Continuous:			8	
Categorical:			40	

**Table A.12:** Baseline characteristics of K-Means clustering HFpEF without post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	117.31±20.34	87.94±13.31	110.91±17.01	0.000***
pcv	0.37±0.06	0.28±0.04	0.34±0.05	0.000***
age	74.08(65.25,82.89)	75(64.94,81.79)	84.31(77.36,88.63)	0.000***
ewave	0.94(0.7,1.1)	1.1(0.92,1.27)	0.9(0.7,1)	0.000***
gfr	55.5(40.25,83.75)	29(20.5,44.25)	47(38,68)	0.000***
k	4.45(3.92,4.78)	4.44(4.1,4.8)	4.2(3.7,4.5)	0.008**
los	8(4,20.76)	12(5,22.19)	10(4,23.83)	0.246
lvef	57.5(55,60)	55(52.5,58.12)	57.5(55,60)	0.203
mcv	90.5(85.25,96)	87(79.25,92)	89(85,94)	0.039
na	139.5(137,141)	137.5(134.75,141)	140(137,142)	0.024*
ntprobnp	1653.5(870.25,3760.75)	3852(1879.5,9806.75)	1995(934,5573)	0.000***
plts	217(160.25,296.5)	226(162,303.75)	210(170,251.5)	0.889
wbc	8.1(6.63,11.13)	7.75(5.7,9.92)	7.2(5.55,10.55)	0.121
Total number of significant baseline char:			48	
Continuous:			8	
Categorical:			40	

**Table A.13:** Baseline characteristics of EM clustering HFpEF without post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	106.38±16.53	84.31±14.29	109.8±21.75	0.000***
pcv	0.33±0.05	0.27±0.04	0.34±0.07	0.000***
age	84.69(76.93,88.61)	71.3(60.76,82.33)	77.79(68.05,84.04)	0.001**
ewave	0.9(0.68,1)	1.1(0.96,1.2)	0.98(0.8,1.1)	0.007**
gfr	44(36.5,56.5)	26.5(10,38.5)	48(31,73)	0.000***
k	4.1(3.7,4.5)	4.4(4.17,4.75)	4.4(4.1,4.7)	0.024*
los	10(4,21.54)	8.5(4,16.5)	10(5,22.08)	0.652
lvef	57.5(54.38,60.62)	57.5(54.38,60.62)	57.5(52.5,60)	0.357
mcv	89(85,93.25)	89(83,93.25)	89(84,95)	0.914
na	140(137,142)	137(134,141.25)	139(136,141)	0.233
ntprobnp	2191.5(1048,5046.25)	4114.5(1707,10007.75)	2184(976,4895)	0.098
plts	206.5(163.75,243.75)	206.5(154,296.75)	221(163,301)	0.494
wbc	7.1(5.5,9.35)	7.05(4.75,9.1)	8.1(6.4,10.9)	0.045*
Total number of significant baseline char:			42	
Continuous:			6	
Categorical:			36	

**Table A.14:** Baseline characteristics of Hierarchical clustering HFmrEF without post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	89.5±14.24	122.31±13.84	113.5±15.95	0.000***
k	4.55±0.66	4.32±0.49	4.46±0.61	0.114
age	72.08(67.43,82.83)	81.14(74.51,85.01)	77.02(67.73,81.93)	0.006**
ewave	0.8(0.7,1)	0.82(0.62,0.99)	0.9(0.8,1.05)	0.026*
gfr	41(21.75,76.25)	64(47,82.5)	44(31,60.86)	0.000***
los	15.5(8.75,34.5)	9(4,24)	9(3,18)	0.003**
lvef	45(41.61,47.5)	45(42.5,47.5)	42.5(40,47.5)	0.001***
mcv	91(86,96.25)	93(88.71,96)	90(86.75,94)	0.136
na	138(134.75,141)	139(136,141)	139(136.92,141)	0.663
ntprobnp	8937.5(3303.5,26619.5)	2898.5(1440.75,5004.5)	3817.5(1647.25,10311.75)	0.000***
pcv	0.28(0.26,0.31)	0.38(0.35,0.4)	0.36(0.33,0.38)	0.000***
plts	210.5(151.5,285.5)	193(148.5,231.5)	191.27(153.75,226.5)	0.466
wbc	8.65(6.25,12.45)	7.45(6.07,9.22)	8.3(5.87,11.15)	0.375
Total number of significant baseline char:			51	
Continuous:			8	
Categorical:			43	

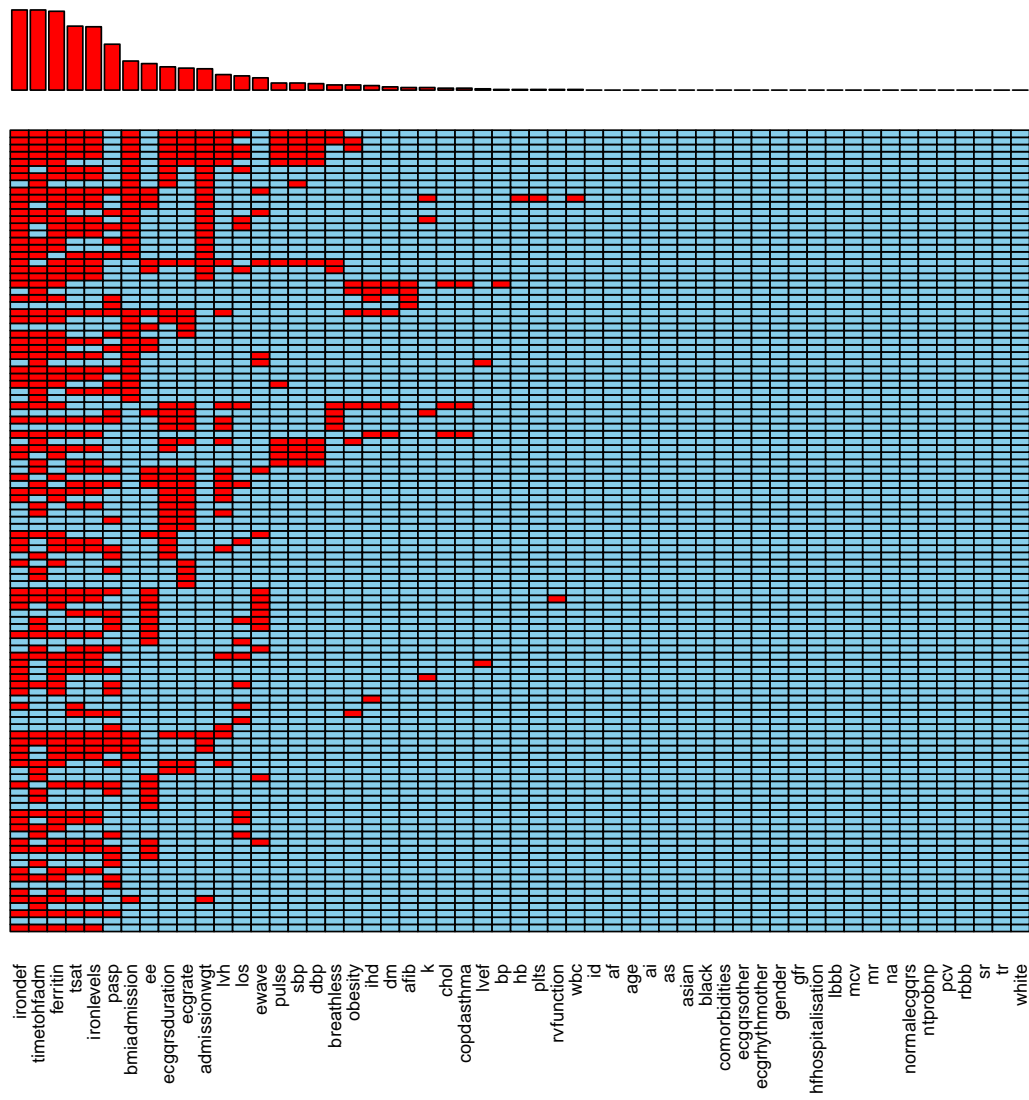
**Table A.15:** Baseline characteristics of K-Means clustering HFmrEF without post-diagnosis

	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	121.6±14.29	114.24±15.78	90.02±14.5	0.000***
k	4.32±0.48	4.47±0.62	4.54±0.65	0.106
age	81.23(75.02,85.37)	77.02(67.73,81.84)	72.08(66.39,82.08)	0.002**
ewave	0.82(0.63,1)	0.9(0.8,1.05)	0.8(0.71,1)	0.045*
gfr	64(46.75,81.5)	44(31,59.35)	44(22.25,76)	0.000***
los	9(4,24)	8.5(3,16.25)	16.5(9.25,35.5)	0.000***
lvef	45(42.5,47.5)	42.5(40,47.5)	45(42,47.5)	0.001**
mcv	93(88.9,96)	89.88(85.75,94)	91(86.25,96)	0.105
na	139(136,141)	139(136.66,141)	138(135,141)	0.804
ntprobnp	2898.5(1526.25,4967.5)	3817.5(1647.25,10807.75)	8656(3176.5,25270.5)	0.001**
pcv	0.38(0.34,0.4)	0.36(0.33,0.39)	0.28(0.26,0.31)	0.000***
plts	193(147,232.5)	193.67(153.75,226.5)	209(153.25,284.75)	0.598
wbc	7.55(6.22,9.32)	8.3(5.87,11.35)	8.5(6.15,12.18)	0.451
Total number of significant baseline char:			53	
Continuous:			8	
Categorical:			45	

**Table A.16:** Baseline characteristics of EM clustering HFmrEF without post-diagnosis

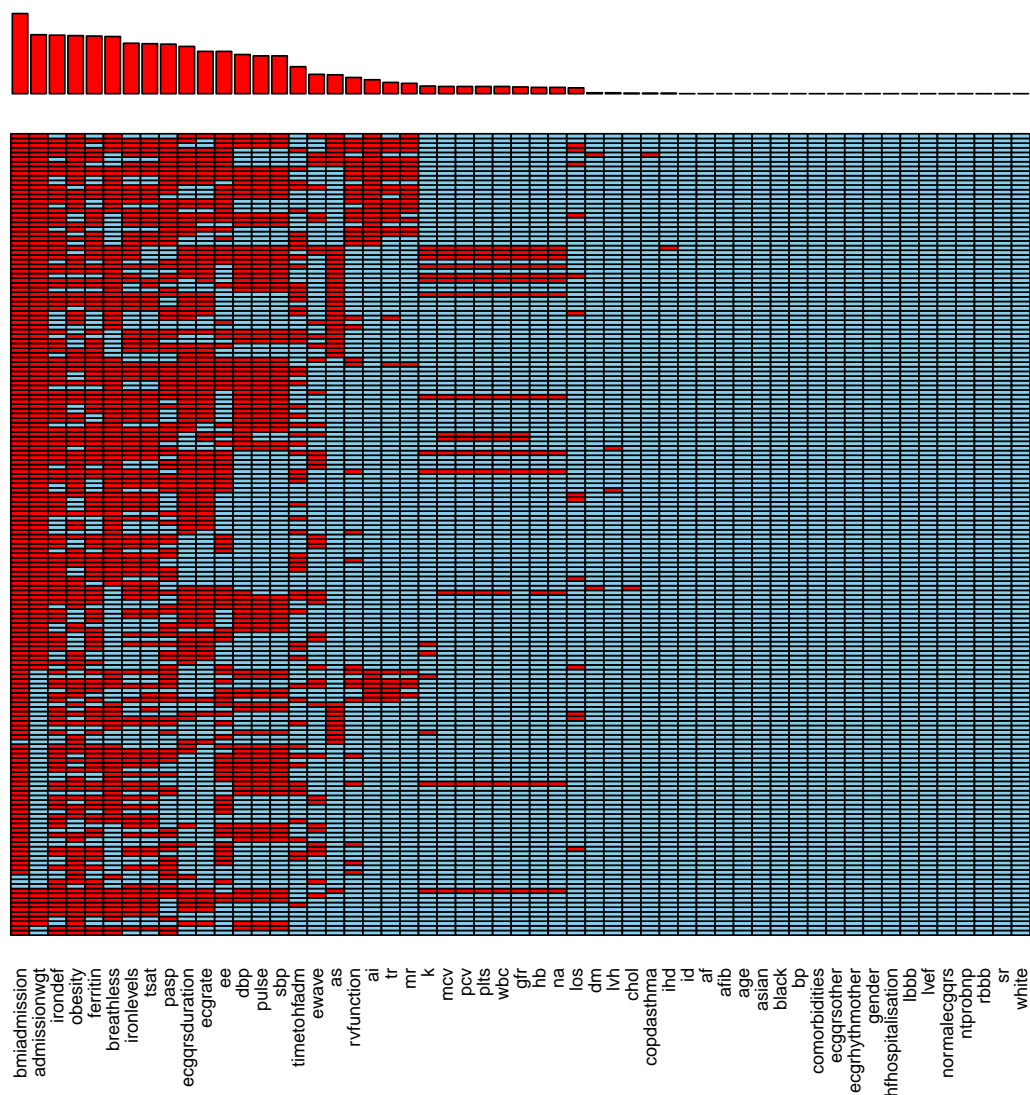
	Cluster1	Cluster2	Cluster3	<i>p</i> -value
hb	81.25±12.6	117.97±16.32	106.63±16.19	0.000***
k	4.77±0.69	4.31±0.53	4.59±0.6	0.001**
age	71.4(59.57,76.83)	80.88(72.81,84.45)	73.36(60.94,78.65)	0.000***
ewave	0.8(0.7,1)	0.9(0.7,1)	0.9(0.75,1.06)	0.192
gfr	21(9.5,77.5)	59(42,76)	38(25.5,58)	0.000***
los	16.5(12.75,51)	9(5,20.5)	11(3,21)	0.036*
lvef	45(41.5,45.62)	45(42.5,47.5)	42.5(40,45)	0.006**
mcv	89.5(83,93)	93(88.16,96.5)	89.34(85,94)	0.023*
na	138(134.75,141)	139(136,141)	139(135.79,141)	0.840
ntprobnp	6880(2886.25,40414.75)	3405(1760,7809)	4396(1515,10597)	0.177
pcv	0.26(0.23,0.28)	0.37(0.33,0.39)	0.34(0.3,0.36)	0.000***
plts	204(145,267)	193(153,239)	194.8(141,234.4)	0.923
wbc	6.55(5.2,8.95)	8.2(6.2,10.45)	8.2(6.05,10.85)	0.293
Total number of significant baseline char:			42	
Continuous:			8	
Categorical:			34	

# A.4 Relevant plots

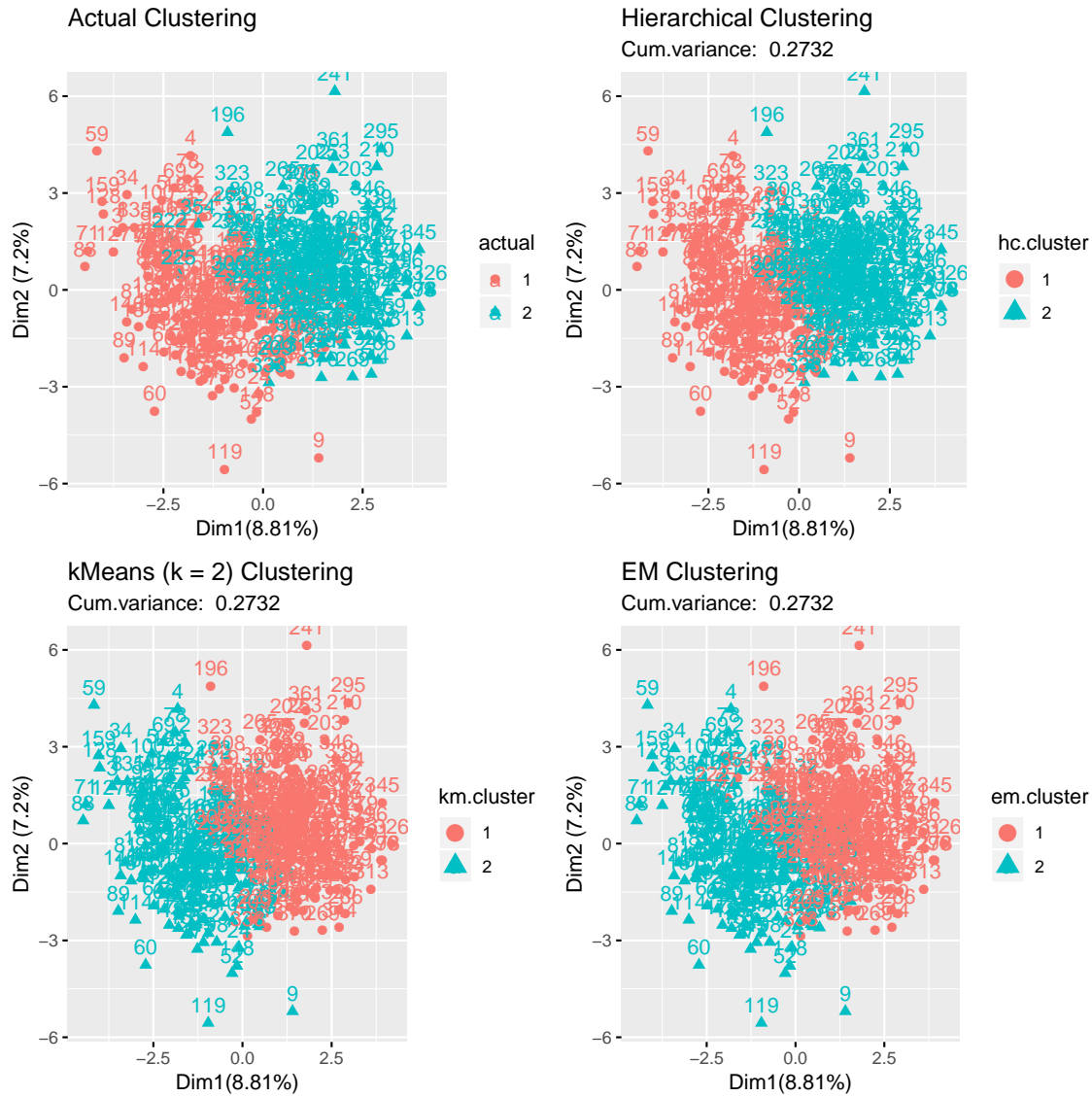


**Figure A.1:** Missing values in HFpEF data set. Top: the amount of missing values in each variable sorted in ascending order. Bottom: plot of the combinations of missing (red) and non-missing (blue) values in the HFpEF data set.

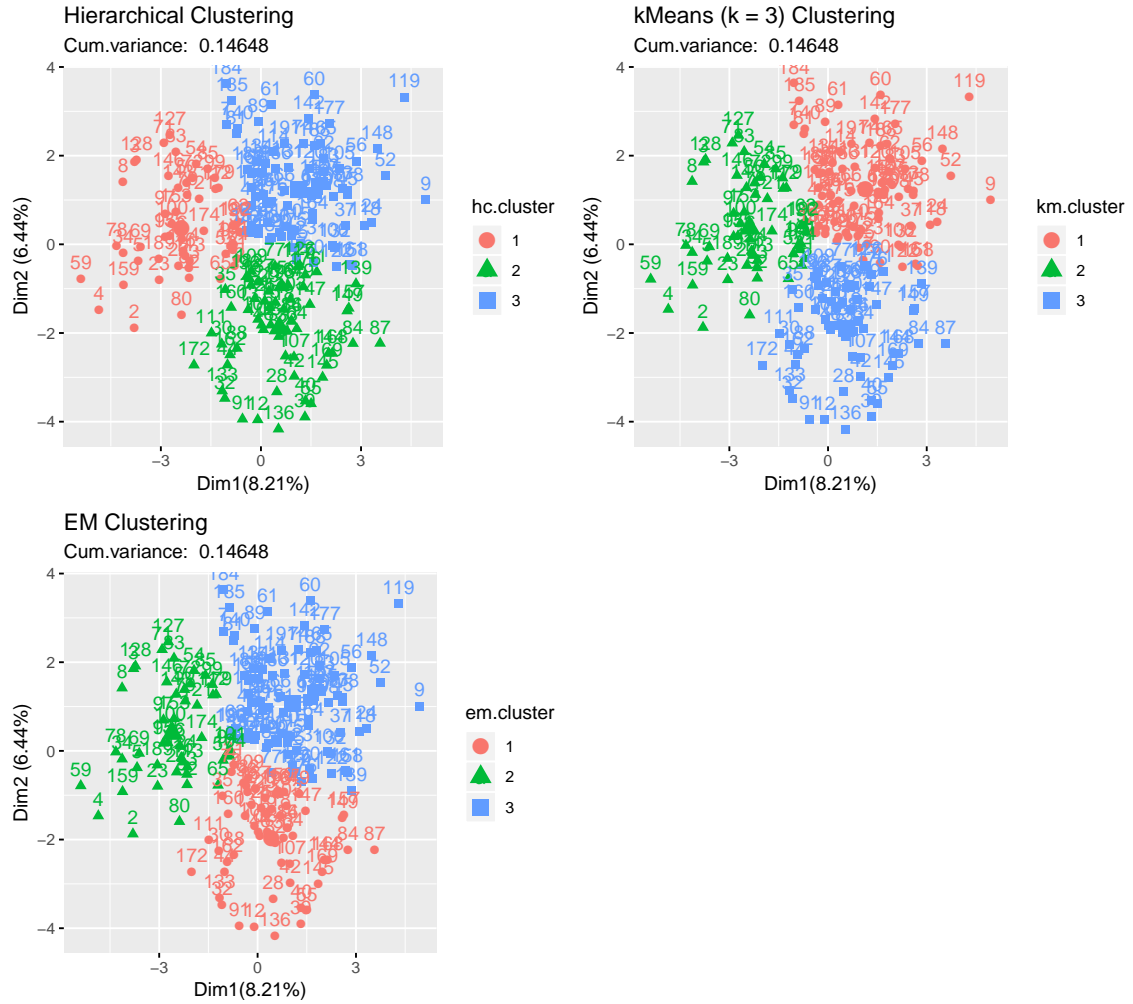




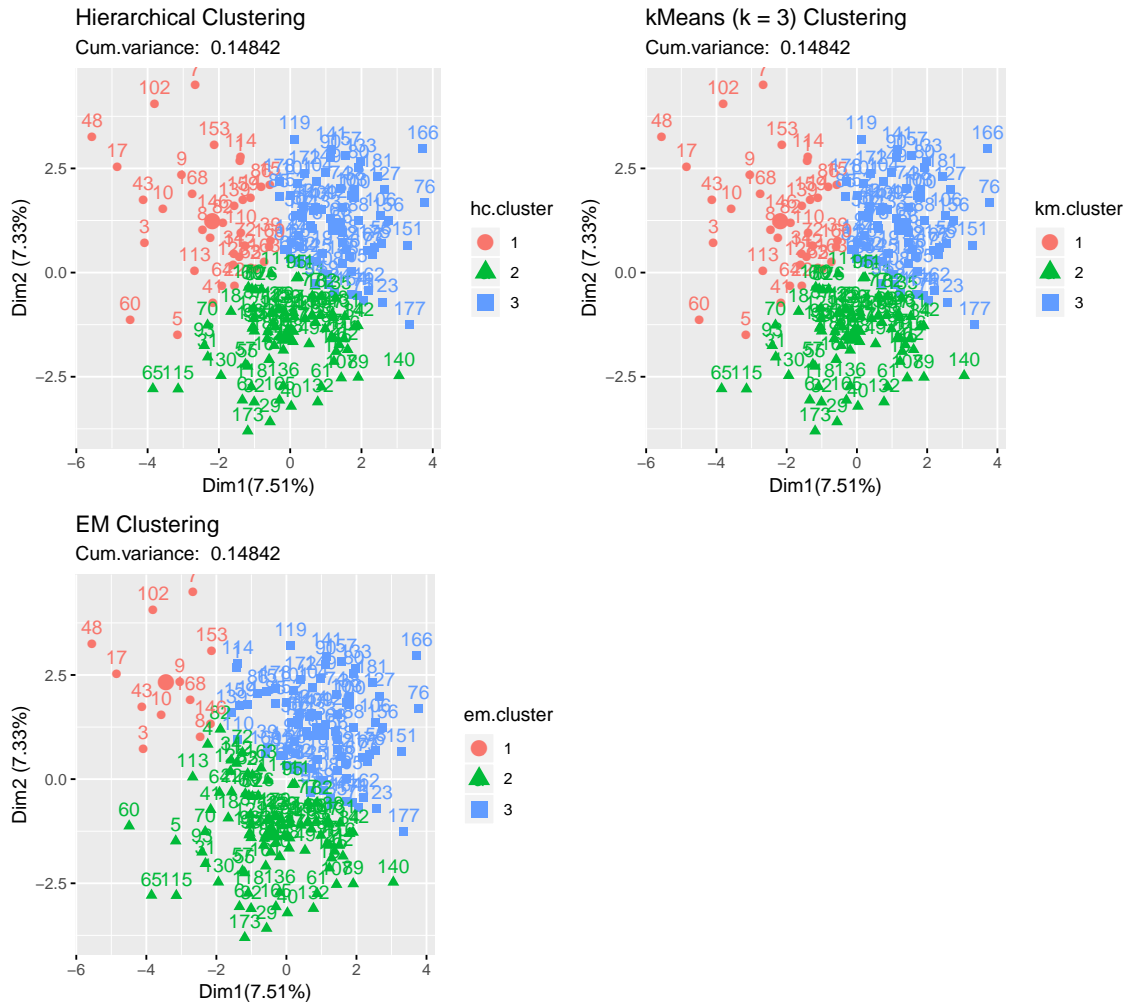
**Figure A.2:** Missing values in HFmrEF data set. Top: the amount of missing values in each variable sorted in ascending order. Bottom: plot of the combinations of missing (red) and non-missing (blue) values in the HFmrEF data set.



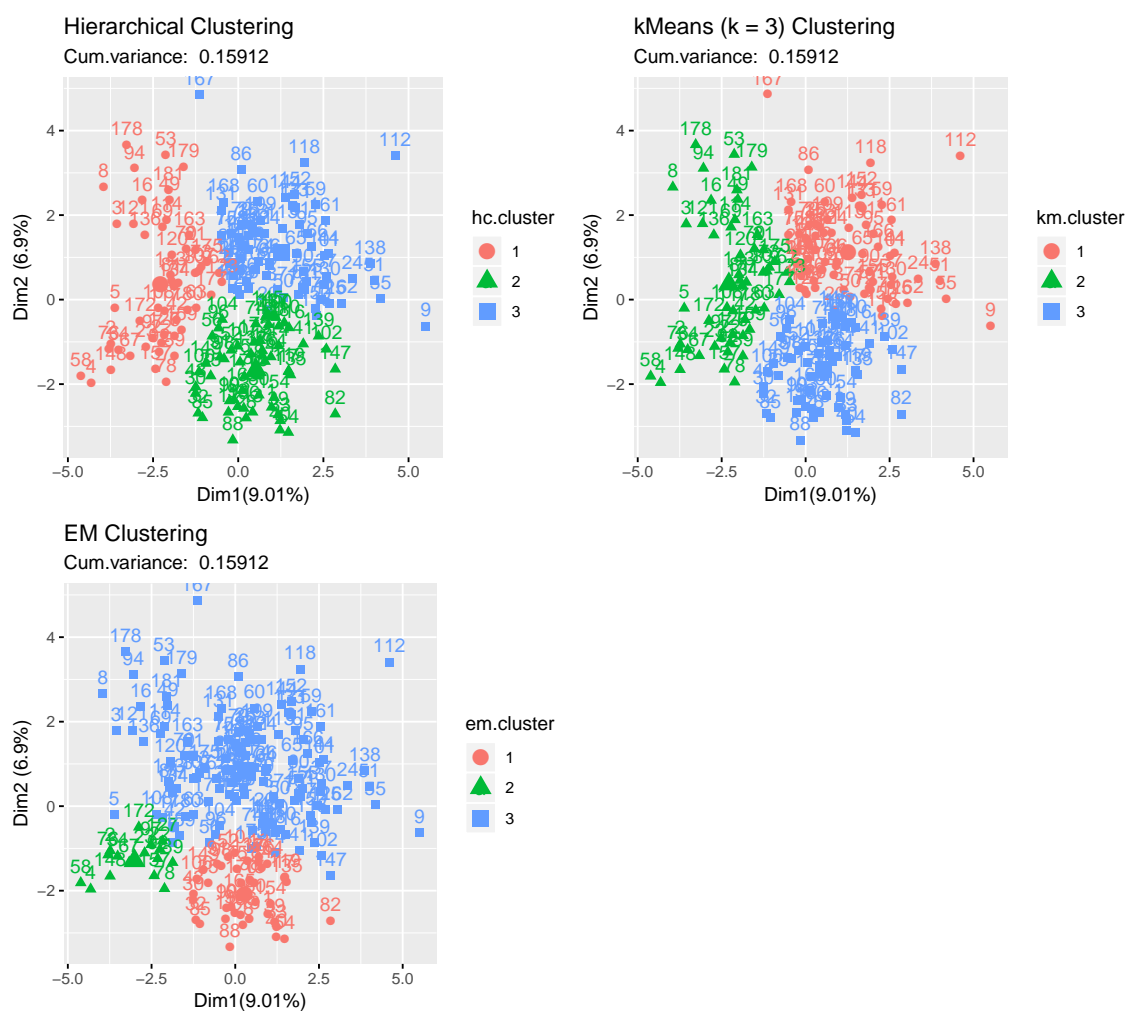
**Figure A.3:** Results of Binary clustering problem



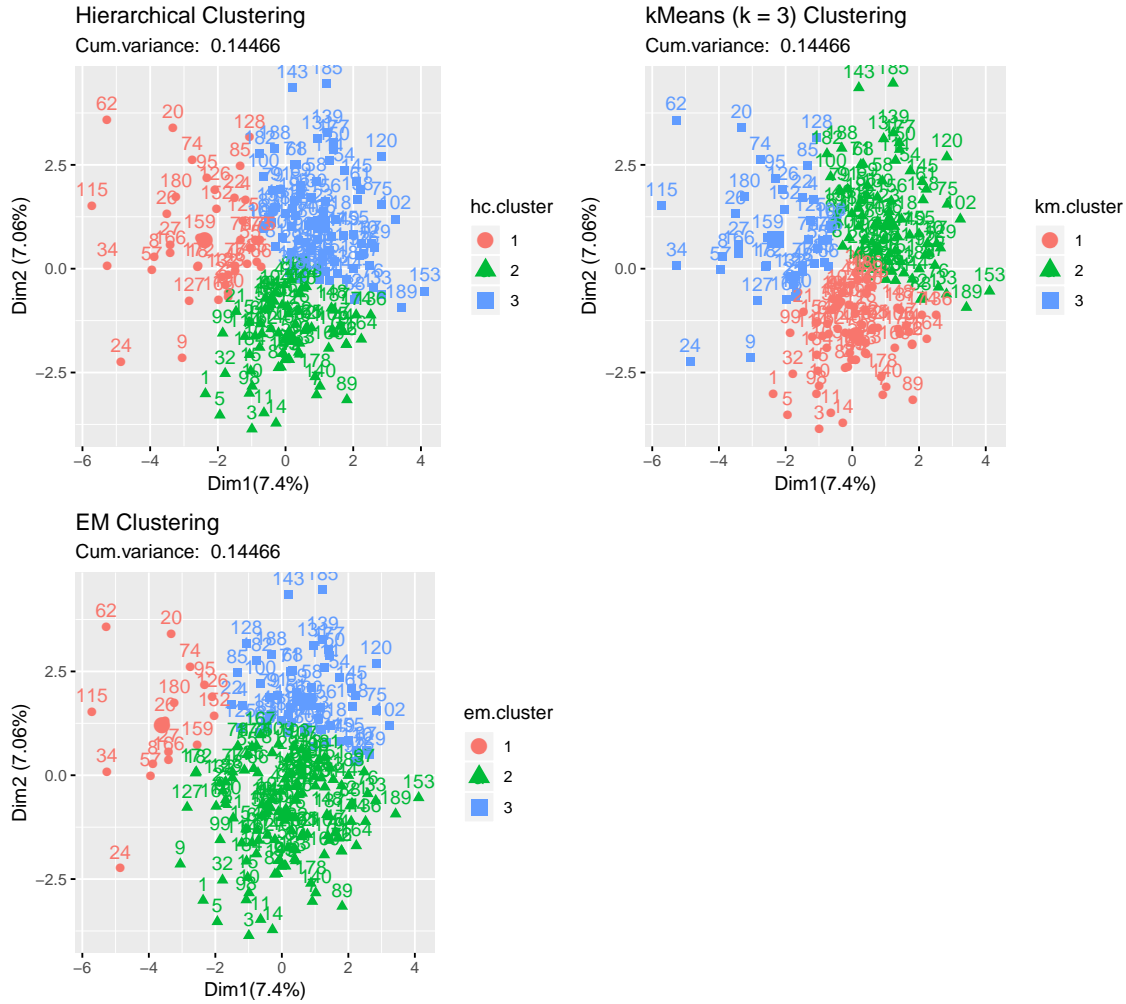
**Figure A.4:** Clustering results of HFpEF with Post-Diagnosis



**Figure A.5:** Clustering results of HFmrEF with Post-Diagnosis



**Figure A.6:** Clustering results of HFpEF without Post-Diagnosis



**Figure A.7:** Clustering results of HFmrEF without Post-Diagnosis

# Appendix B

## Source code

The following appendix presents all the relevant R-code used in this thesis. We have organized the chapter in accordance with the various steps in the machine learning procedure adopted in this thesis, see figure (3.1). We have tried to comment as much of the source code in order to ensure that an eventual re-examination of the results can be as easy and smooth as possible. Inquires about the code can be forwarded to the author on request.

### B.1 Packages

```
1 # ----- #
2 # Function for sourcing package info
3 # ----- #
4 source_lines <- function(file, lines){
5   source(textConnection(readLines(file, warn = F)[lines]))
6 }
7
8 # ----- #
9 # Extract all package installed in all files
10 # ----- #
11 packages <- c()
12 files <- c("utilities.R", "desc_stat.R", "pre_process.R",
13           "clustering.R", "classification.R",
14           "../raw_data/consolidation.R")
15
16 for (file in files){
17   source_lines(file, 1:10)
18   packages <- c(packages, Packages)
```

```

19 }
20
21 # ----- #
22 # Extract title , version and author information
23 # ----- #
24 title <- c(); version <- c()
25 for (package in packages){
26   title <- c(title , packageDescription(package)$Title)
27   version <- c(version , packageDescription(package)$Version)
28 }
29
30 # ----- #
31 # Build LaTeX table with all the package info
32 # ----- #
33 packagesUsed <- as.data.frame(matrix(c(packages , title ,
34                                       version),ncol = 3))
35 colnames(packagesUsed) <- c("Package" , "Title" , "Version")
36 packagesUsed <- unique(packagesUsed[packagesUsed$Package,])
37 packagesUsed <- packagesUsed[order(packagesUsed$Package) ,]
38 rownames(packagesUsed) <- 1:nrow(packagesUsed)
39 print(xtable(packagesUsed) , include.rownames=FALSE)
40
41 # ----- #

```

## B.2 Utilities

```

1 # ----- #
2 # Install packages (if not already installed)
3 # ----- #
4 Packages <- c("docstring" , "plotrix" , "FactoMineR" ,
5               "factoextra" , "gridExtra" , "NbClust" ,
6               "ggpubr" , "mclust" , "CBCgrps")
7 # install.packages(Packages)
8
9 # ----- #
10 # Load package for docstring
11 # ----- #
12 lapply(Packages , library , character.only = TRUE)
13
14 # ----- #
15 # Helper function used in this thesis
16 # ----- #
17 if.not.class <- function(var , class){
18   #' Utility function for error messages
19   #'

```



```

20 #' @description Utility function for error messages given
21 #' wrong input class as function argument.
22
23 if (!any(class(var) %in% class)){
24   stop(paste("first argument must be of class(es) ",
25             class, "!", sep = ""))
26 }
27 }
28
29 # ----- #
30 make.na <- function(data){
31   #' Converts all the NaN in a matrix to NA
32   #'
33   #' @description This function returns a matrix in which all
34   #' the NaN values are replaced with NA values. Note! NaN
35   #' ("not a number") is not the R syntax for missing values.
36   #' The correct syntax is NA ("not available").
37   #'
38   #' @param data matrix. Matrix containing NaN values
39
40   data[is.nan(data)] <- NA
41   return(data)
42 }
43
44 # ----- #
45 summary.missing <- function(data){
46   #' Summary of the missing values in a dataset
47   #'
48   #' @description This function returns a list with the total
49   #' number of na values and the total percentage in the entire
50   #' dataset, including the percentage of missing values for
51   #' all variables (columns) and the relative percentage of
52   #' missing values to the total (both as vectors).
53   #'
54   #' @param data matrix. Matrix containing missing values
55
56   num.na <- sum(is.na(data))
57   tot.pmv <- num.na/prod(dim(data))
58   num.na.vec <- apply(data, 2, function(col) sum(is.na(col)))
59   pmv.vec <- num.na.vec / prod(dim(data))
60   rel.pmv.vec <- num.na.vec / num.na
61   rel.pmv.v <- num.na.vec / dim(data)[1]
62
63   outp <- list(num.na, tot.pmv, num.na.vec, pmv.vec,
64               rel.pmv.vec, rel.pmv.v)

```

```

65   names(outp) <- c("num.na", "tot.pmv", "num.na.vec",
66                   "pmv.vec", "rel.pmv.vec", "rel.pmv.v")
67   return(outp)
68 }
69
70 # ----- #
71 summary.zeros <- function(data){
72   #' Summary of the zero values in a dataset
73   #'
74   #' @description The function returns a list with the
75   #' percentage of zero values for all variables in a dataset ,
76   #' including the total number of zero values and the total
77   #' percentage and the relative percentage of zero values
78   #' to the total.
79   #'
80   #' @param data matrix. Matrix containing zero values
81
82   num.zeros <- sum(colSums(data == 0, na.rm = T))
83   tot.pzv <- num.zeros / prod(dim(data))
84   num.zeros.vec <- colSums(data == 0, na.rm = T)
85   pzv.vec <- num.zeros.vec / nrow(data)
86   rel.pzv.vec <- num.zeros.vec / num.zeros
87
88   outp <- list(num.zeros, tot.pzv, num.zeros.vec, pzv.vec,
89               rel.pzv.vec)
90   names(outp) <- c("num.zeros", "tot.pzv", "num.zeros.vec",
91                   "pzv.vec", "rel.pzv.vec")
92   return(outp)
93 }
94
95 # ----- #
96 rm.indicator <- function(data, n.uniq){
97   #' Removes indicator variable columns from a dataset based on
98   #' predefined number of unique element in that column
99   #'
100  #' @description This function return a matrix without
101  #' indicator variable columns. A indicator variable column is
102  #' defined as a column containing less that a predefined
103  #' number of unique elements (n.uniq)
104  #'
105  #' @param data matrix. Matrix containing indicator variables
106  #' @param n.uniq integer. Number of unique element in a
107  #' column needed for that column to be defined as a indicator
108  #' variable column.
109

```

```

110 non.indicator <- data[, apply(data, 2, function(col)
111   length(unique(col)) > n.uniq)]
112 ind.var.idx <- !(colnames(data) %in% colnames(non.indicator))
113 indicator <- data[, ind.var.idx]
114
115 outp <- list(non.indicator, indicator)
116 names(outp) <- c("non.indicator", "indicator")
117 return(outp)
118 }
119
120 # ----- #
121 rm.missing <- function(data, cut.off = 0.8, near.zero.var = T){
122   #' Remove variables with near zero variance or more missing
123   #' values than a percentage threshold.
124   #'
125   #' @description This function removes all variables in a
126   #' matrix or dataframe with suspected of having near zero
127   #' variance or more missing values than a given percentage
128   #' threshold.
129   #'
130   #' @param data matrix. Matrix like object
131   #' @param cut.off integer. Percentage threshold for missing
132   #' values.
133   #' @param near.zero.var logical. Boolean indicating if
134   #' criteria for near zero variance is to be used.
135
136   if (near.zero.var){
137     near.zero <- nearZeroVar(data)
138     if (length(near.zero) != 0){
139       data <- data[, -near.zero]
140     }
141   }
142   miss.col <- summary.missing(data)$rel.pmv.v
143   miss.cut <- miss.col < cut.off
144   data <- data[, miss.cut]
145   return(data)
146 }
147
148 # ----- #
149 zero.to.na <- function(data, except=NULL){
150   #' Convert zero datapoints to na in a dataset.
151   #'
152   #' @description This function converts all the zero datapoints
153   #' in a dataset into na. One can also supply a vector of
154   #' columnnames (except) corresponding to variables that this

```

```

155 #' function should not be applied on.
156 #'
157 #' @param data matrix. Matrix containing zero datapoints
158 #' @param except character vector. Names of matrix column not
159 #' to apply function on.
160
161 exp.idx <- colnames(data) %in% except
162 exp.data <- data[, exp.idx]; not.exp.data <- data[, !exp.idx]
163 not.exp.data[not.exp.data == 0] <- NA
164 data <- cbind(not.exp.data, exp.data)
165 return(data)
166 }
167
168 # ----- #
169 move.columns <- function(from.mat, to.mat, column.name){
170 #' Move one column from one matrix to another.
171 #'
172 #' @description This function moves one column with name
173 #' column.name from matrix called from.mat to matrix called
174 #' to.mat.
175 #'
176 #' @param from.mat matrix. Matrix to move column from
177 #' @param to.mat matrix. Matrix to move column to
178 #' @param column.name character. Name of column to be moved
179
180 to.mat <- cbind(to.mat, from.mat[, colnames(from.mat) ==
181                                     column.name])
182 colnames(to.mat)[ncol(to.mat)] <- column.name
183 from.mat <- from.mat[, colnames(from.mat) != column.name]
184 outp <- list(from.mat, to.mat)
185 names(outp) <- c("from.mat", "to.mat")
186 return(outp)
187 }
188 # ----- #
189 sort.column.names <- function(data, id.col = T){
190 #' Sorts columns from data
191 #'
192 #' @description This function sorts the columns names of an
193 #' matrix like object.
194 #'
195 #' @param data matrix. Matrix with columns names
196 #' @id.col boolean. Logical indicating if data contains
197 #' an id column.
198
199 if(id.col){

```

```

200     id <- data[, 1]
201     data <- data[, -1]
202     data <- cbind(id, data[, sort(colnames(data))])
203   } else {
204     data <- data[, sort(colnames(data))]
205   }
206   return(data)
207 }
208
209 # ----- #
210 split.matrix <- function(data){
211   #' Split matrix in two parts.
212   #'
213   #' @description This function splits a matrix into two parts.
214   #' Both halves can be accessed by the user as an output.
215   #'
216   #' @param data matrix. Matrix like object
217   #'
218   #' @note The function assumes that the input matrix has more
219   #' than one column.
220
221   if (ncol(data)==1){
222     stop("data must have more than one column!")
223   }
224   mid <- trunc(ncol(data)/2); end <- ncol(data)
225   first.half <- data[, 1:mid]
226   second.half <- data[, (mid+1):end]
227   outp <- list(first.half, second.half)
228   names(outp) <- c("first.half", "second.half")
229   return(outp)
230 }
231
232 # ----- #
233 data.bounds <- function(data, lower.bound, upper.bound){
234   #' Generate an Amelia compatible bound matrix
235   #'
236   #' @description This function produces a three column matrix
237   #' to hold logical bounds on the imputations done in Amelia
238   #' II. Each row of the matrix is of the form c(column.number,
239   #' lower.bound, upper.bound).
240   #'
241   #' @param data matrix. Matrix like object
242   #' @param lower.bound numeric.
243   #' @param upper.bound numeric.
244

```

```

245 len <- ncol(data); column.number <- seq(1, len)
246 lower <- rep(lower.bound, len)
247 upper <- rep(upper.bound, len)
248 outp <- cbind(column.number, lower, upper)
249 return(outp)
250 }
251
252 # ----- #
253 boot.em.impute <- function(data, bounds, n.boot = 30){
254   #' Impute data using a mean collapsing bootstrapped EM
255   #' algorithm.
256   #'
257   #' @description This function imputes a data matrix using the
258   #' bootstrapped EM algorithm from the Amalie II package. The
259   #' algorithm creates n.boot number of bootstrapped datasets
260   #' after which the datasets are collapsed into one dataset
261   #' using the mean of all imputed values as final estimate
262   #' of the given missing value.
263   #'
264   #' @param data matrix. Matrix like object
265   #' @param bounds matrix. Three column matrix of the form
266   #' c(column.number, lower.bound, upper.bound).
267   #' @param n.boot numeric. Number of bootstrapped datasets
268   #' to create.
269
270   data.em = list()
271   for (i in 1:n.boot){
272     print(paste("Bootstrap: ", i, " (", i/n.boot*100, " %)",
273               sep=""))
274     data.em[[i]] <- amelia(data, m = 1, p2s = 0,
275                           bounds = bounds)$imputations$imp1
276   }
277   return(Reduce("+", data.em) / n.boot)
278 }
279
280 # ----- #
281 top.n.missing <- function(data, n, decreasing=T){
282   #' Summary of top n missing variables in data set.
283   #'
284   #' @description This function produces a summary table of the
285   #' top n missing variables in an inputted dataset.
286   #'
287   #' @param data matrix. Matrix like object
288   #' @param n integer. Top n highest missing variables
289   #' @param decreasing logical. Logical argument indicating

```

```

290 #' wheater values should be sorted in decreasing order.
291
292 missing <- summary.missing(data)
293 count <- missing$num.na.vec
294 if (sum(count) == 0){
295   stop("no missing values!")
296 }
297 perc <- missing$pmv.vec
298 relp <- missing$rel.pmv.vec
299 relv <- missing$rel.pmv.v
300 outp <- apply(as.matrix(cbind(count, perc, relp, relv)), 2,
301               sort, decreasing)[1:n,]
302 grand.tot <- c(missing$num.na, missing$tot.pmv, sum(relp),
303               NA)
304 outp <- rbind(grand.tot, outp)
305 colnames(outp) <- c("#Na", "%N", "%Na", "%V")
306 return(outp)
307 }
308
309 # ----- #
310 label.summary <- function(labels, label.col, col.names, digits,
311                           sort.col, ignore.id.col = T,
312                           decr = T){
313   #' Summary of class labels in data set
314   #'
315   #' @description The function returns a table with the number
316   #' unique labels in a labels matrix and the percentage of
317   #' all the labels that occure.
318   #'
319   #' @param labels matrix. Matrix like object of characters
320   #' @param label.col integer. Column number of primary labels
321   #' @param col.names character vector. Vector of column
322   #' names
323   #' @param digits integer. Integer indicating the number of
324   #' decimal places to be used.
325   #' @param sort.col integer. Column number to sort
326   #' @param ignore.id.col logical. Boolean indicating whether
327   #' first column of id numbers should be ignored.
328   #' @param decr logical. Boolean indicating if values in
329   #' sort.col should be sorted in decreasing order.
330
331   uniq <- unique(if(ignore.id.col){
332     labels[order(labels[, label.col]), -1]} else {labels})
333   tabl <- table(labels[, label.col])
334   perc <- round(tabl/sum(tabl), digits)

```

```

335 outp <- cbind(uniq, tabl, perc)
336 colnames(outp) <- col.names
337 return(outp[order(outp[, sort.col], decreasing = decr),])
338 }
339
340 # ----- #
341 little.mcar <- function(data){
342   #' Little's test to assess for missing completely at
343   #' random.
344   #'
345   #' @description This function uses Little's test (from
346   #' BaylorEdPsych package) to assess for missing completely at
347   #' random for multivariate data with missing values. It
348   #' return the chi.squared test statistics, df and p.value.
349   #'
350   #' @param data matrix like object. Matrix or data frame with
351   #' values that are missing.
352   #'
353   #' @note This function cannot accept data with more than 50
354   #' variables, and may in some cases take long time to
355   #' complete.
356
357   l <- LittleMCAR(data[, summary.missing(data)$num.na.vec > 0])
358   outp <- c(dim(data)[2], l$missing.patterns, l$chi.square,
359             l$df, l$p.value)
360   names(outp) <- c("n var", "missing.patterns", "chi.square", "
361                   "df",
362                   "p.value")
363   outp[1:2] <- round(outp[1:2])
364   return(outp)
365 }
366 # ----- #
367 pca.var.plot <- function(pca, n.comp=NA, digits=4, title = NA){
368   #' Plot the explained and cumulative variance from a
369   #' principal component analysis (PCA).
370   #'
371   #' @description This function produces a plot of the
372   #' explained and cumulative variance extracted from a
373   #' principal component analysis.
374   #'
375   #' @param pca princomp object.
376   #' @param n.comp integer. Number of components to be plotted
377   #' @param digits integer. Integer indicating the number of
378   #' decimal places to be used.

```



```

379 #' @param title character. Name of title.
380
381 if.not.class(pca, "princomp")
382 sd <- pca$sdev
383 n <- 1:ifelse(is.na(n.comp), length(sd), n.comp)
384 vr <- (sd^2/sum(sd^2))[n]
385 cm <- cumsum(vr)
386 colfunc <- colorRampPalette(c("lightblue", "blue"))
387 twoord.plot(n, vr, n, cm, type = c("bar", "s"),
388           lcol = colfunc(length(n)), main = title,
389           cex.axis = 0.5); grid()
390 lines(vr); points(vr, pch = 20)
391 leg <- c(paste("Number comp:", length(n)),
392         paste("Cum.variance:", round(sum(vr), digits)))
393 legend("top", legend = leg, bty = "n")
394 }
395
396 # ----- #
397 pca.cluster.plot <- function(pca, ncp, km.clust = 2,
398                             hc.clust = -1, em.clust = 2,
399                             digits = 5, ellipse = T,
400                             actual = NA, fcp=1, scp = 2,
401                             ellipse.type = "convex",
402                             ggtheme = theme_gray(),
403                             return.clust=F){
404   #' Side-by-side cluster plots with Hierarchical Clustering,
405   #' kMeans and EM clustering on principal components.
406   #'
407   #' @description This function runs Hierarchical, kMeans and
408   #' EM clustering on a predefined number of principal
409   #' components. The results are scatterplots with the
410   #' results from the clustering.
411   #'
412   #' @param pca princomp object.
413   #' @param ncp numeric. Number of principal components
414   #' @param km.clust numeric. Number of clusters to be used
415   #' in the kMeans algorithm.
416   #' @param hc.clust numeric. Number of clusters to be used
417   #' in the Hierarchical clustering.
418   #' @param em.clust numeric. Number of clusters to be used
419   #' in the expectation maximization algorithm.
420   #' @param digits numeric. Number of decimal places for
421   #' cumulative variance in plot title.
422   #' @param ellipse logical value. Boolean indicating if
423   #' ellipse around clusters should be drawn.

```

```

424 #' @param ellipse.type. Type of ellipse to be drawn.
425 #' See ggscatter for more information.
426 #' @param ggtheme. function, ggplot2 theme name.
427 #' @param return.clust. logical. Boolean indicating wheather
428 #' one want to return the cluster partioning.
429
430 if .not.class(pca, "princomp")
431 data <- as.data.frame(pca$scores[,1:ncp])
432 sdev <- pca$sdev
433 rdev <- sdev^2 / sum(sdev^2)
434 cdev <- cumsum(rdev)
435 subt <- paste("Cum.variance: ", round(cdev[ncp], digits))
436 hc.title <- labs(title=paste("Hierarchical Clustering"),
437                 subtitle= subt)
438 km.title <- labs(title = paste("kMeans (k = ", km.clust,
439                               ") Clustering", sep = ""), subtitle = subt)
440 em.title <- labs(title = paste("EM Clustering"),
441                 subtitle = subt)
442 xlab <- paste("Dim", fcp, "(",
443              round((rdev[fcf])*100, 2),
444              "%)", sep = "")
445 ylab <- paste("Dim", scp, "(",
446              round((rdev[scf])*100, 2), "%)",
447              sep = "")
448 hc.cluster <- HCPC(data, nb.clust = hc.clust,
449                   graph = F)$data.clust$clust
450 km.cluster <- as.factor(kmeans(data, km.clust)$cluster)
451 em.cluster <- as.factor(Mclust(data[,1:ncp],
452                               em.clust)$classification)
453 if (all(is.na(actual))){
454   data <- cbind(data[, fcp:scf], hc.cluster, km.cluster,
455               em.cluster)
456 } else {
457   actual <- as.factor(actual)
458   data <- cbind(data[, fcp:scf], hc.cluster, km.cluster,
459               em.cluster,
460               actual)
461 }
462 hc <- ggscatter(data, paste("Comp.", fcp, sep=""),
463               paste("Comp.", scp, sep=""),
464               color = "hc.cluster", ylab=ylab, xlab=xlab,
465               shape = "hc.cluster", ellipse = ellipse,
466               ellipse.type = ellipse.type,
467               ggtheme = ggtheme, mean.point = T,
468               label = seq(nrow(data))) + hc.title

```

```

469 km <- ggscatter(data, paste("Comp.", fcp, sep=""),
470                paste("Comp.", scp, sep=""),
471                color = "km.cluster", ylab=ylab, xlab=xlab,
472                shape = "km.cluster", ellipse = ellipse,
473                ellipse.type = ellipse.type,
474                ggtheme = ggtheme, mean.point = T,
475                label = seq(nrow(data))) + km.title
476 em <- ggscatter(data, paste("Comp.", fcp, sep=""),
477                paste("Comp.", scp, sep=""),
478                color = "em.cluster", ylab=ylab, xlab=xlab,
479                shape = "em.cluster", ellipse = ellipse,
480                ellipse.type = ellipse.type,
481                ggtheme = ggtheme, mean.point = T,
482                label = seq(nrow(data))) + em.title
483 if (all(is.na(actual))){
484   grid.arrange(hc, km, em, nrow = 2)
485 } else {
486   act <- ggscatter(data, paste("Comp.", fcp, sep=""),
487                   paste("Comp.", scp, sep=""),
488                   color = "actual", shape = "actual",
489                   ellipse = ellipse,
490                   ellipse.type = ellipse.type,
491                   ggtheme = ggtheme,
492                   label = seq(nrow(data)), ylab=hc$labels$y,
493                   xlab = hc$labels$x) +
494     labs(title = "Actual Clustering", subtitle = "")
495   grid.arrange(act, hc, km, em, nrow = 2)
496 }
497 if (return.clust){
498   clust.list <- list(as.numeric(actual),
499                     as.numeric(hc.cluster),
500                     as.numeric(km.cluster),
501                     as.numeric(em.cluster))
502   names(clust.list) <- c("ACT", "HC", "KMC", "EMC")
503   return(clust.list)
504 }
505 }
506
507 # ----- #
508 compare.baseline <- function(data, grp, alpha=0.05){
509   #' Compare baseline characteristics between two groups.
510   #'
511   #' @description This function compares the baseline charact-
512   #' eristics between two sample groups using an automated
513   #' process for determining the distribution of continous

```

```

514 #' variabls and the appropriate tests. The Wilcoxon rank
515 #' sum test is applied for categorical variables.
516 #'
517 #' @param data matrix like object. Matrix or data frame.
518 #' @param grp. group variable
519 #'
520 #' @references Zhang Z. Univariate description and bivariate
521 #' statistical inference: the first step delving into data.
522 #' Ann Transl Med. 2016 Mar;4(5):91.
523
524 if (length(unique(data[, grp]))>2){
525   grp.table <- multigrps(data, grp, sim=T)$table
526 }else{
527   grp.table <- twogrps(data, grp, sim=T)$table
528 }
529 grp.list <- list(sum(grp.table[, ncol(grp.table)]<alpha),
530                 grp.table)
531 return(grp.list)
532 }
533
534 # ----- #

```

## B.3 Descriptive statistics

```

1 # ----- #
2 # Install relevant packages (if not already done)
3 # ----- #
4 Packages <- c("reporttools", "VIM", "Hmisc", "xtable",
5              "tikzDevice")
6 # install.packages(Packages)
7
8 # ----- #
9 # Load relevant packages and source helper functions
10 # ----- #
11 lapply(Packages, library, character.only = T)
12 source("_helper_func.R")
13
14 # ----- #
15 # Load HFpEF and HFmrEF datafiles
16 # ----- #
17 path <- "data_files/"; r <- ".Rdat"
18 fileNames <- c("HFpEFdataSet", "HFmrEFdataSet",
19               "HFpEFoutcomes", "HFmrEFoutcomes",
20               "HFfullDataSet", "HFfullOutcomes")

```

```

21 lapply(gsub(" ", "", paste(path, fileNames, r)),
22        load, .GlobalEnv)
23
24 # ----- #
25 # Plot of missing values distribution
26 # ----- #
27 pathTolImages <- "../..../doc/thesis/images/"
28
29 tikz(file=paste(c(pathTolImages, "HFpEF_miss_dist.tex"),
30                collapse = ""))
31 aggr(HFpEFdataSet, plot = T, sortVars = T,
32      bars = F, combined = T, ylabs = "", cex.axis = 0.7)
33 dev.off()
34
35 tikz(file = paste(c(pathTolImages, "HFmrEF_miss_dist.tex"),
36                  collapse = ""))
37 aggr(HFmrEFdataSet, plot = T,
38      sortVars = T, bars = F, combined = T, ylabs = "",
39      cex.axis = 0.7)
40 dev.off()
41
42 # ----- #
43 # Summary of variables
44 # ----- #
45 # Reorder data matrix by phenotype domains
46 # ----- #
47 nameOrder <- c("age", "gender", "white", "asian", "black",
48               "breathless", "sbp", "dbp", "admissionwgt",
49               "bp", "bmiadmission", "pulse", "afib",
50               "copdasthma", "irondef", "dm", "obesity",
51               "copdasthma", "ihd", "comorbidities",
52               "ecgqrsduration", "ecgqrsother", "ecgrate",
53               "ecgrhythmother", "lvh", "normalecgqrs", "lbbb",
54               "rbbb", "sr", "hb", "wbc", "tsat", "plts", "pcv",
55               "ferritin", "k", "ironlevels", "chol",
56               "ntprobnp", "gfr", "mcv", "na", "lvef", "ewave",
57               "pasp", "ee", "mr", "tr", "as", "ai",
58               "rvfunction", "af", "timetohfadm",
59               "hfhospitalisation", "los")
60
61 # ----- #
62 # Descriptive statistics
63 # ----- #
64 capHFpEF <- "Patient characteristics: HFpEF"
65 labHFpEF <- "tab:desc_stat_HFpEF"

```

```

66 tableContinuous(HFpEFdataSet[, nameOrder],
67                 stats = c("n", "na", "min", "max", "mean",
68                           "median", "s", "q1", "q3"),
69                 cap = capHFpEF, lab = labHFpEF)
70
71 # ----- #
72 capHFmrEF <- "Patient characteristics: HFmrEF"
73 labHFmrEF <- "tab:desc_stat_HFmrEF"
74 tableContinuous(HFmrEFdataSet[, nameOrder],
75                 stats = c("n", "na", "min", "max", "mean",
76                           "median", "s", "q1", "q3"),
77                 cap = capHFmrEF, lab = labHFmrEF)
78
79 # ----- #
80 # Outcomes table
81 # ----- #
82 r <- rep("", 5)
83
84 tabOutHFfull <- rbind(label.summary(as.matrix(HFfullOutcomes),
85                                             2, cbind("Group", "Mort?", "Readm?", "n",
86                                                     "%Tot"), 3, 5))
87
88 tabOutHFpEF <- rbind(label.summary(as.matrix(HFpEFoutcomes),
89                                           2, c("Group", "Mort?", "Readm?", "n",
90                                               "% Tot"), 3, 5), r, r)
91
92 tabOutHFmrEF <- label.summary(as.matrix(HFmrEFoutcomes),
93                               2, c("Group", "Mort?", "Readm?",
94                                   "n", "% Tot"), 3, 5)
95
96 print(xtable(tabOutHFfull), include.rownames = F)
97 print(xtable(cbind(tabOutHFpEF, tabOutHFmrEF)),
98       include.rownames = F)
99
100 # ----- #
101 # Tables of top 10 missing values variables in both data sets
102 # ----- #
103 HFfullMiss <- top.n.missing(HFfullDataSet, 10)
104 HFpEFmiss <- top.n.missing(HFpEFdataSet, 10)
105 HFmrEFmiss <- top.n.missing(HFmrEFdataSet, 10)
106
107 # ----- #
108 # Combine missing values table and convert to Latex code
109 # ----- #
110 xtable(HFfullMiss, digits = c(0,0,3,3,3))

```

```

111 xtable(cbind(round(HFpEFmiss,3), rownames(HFmrEFmiss),
112           round(HFmrEFmiss,3)))
113
114 # ----- #

```

## B.4 Pre-processing

```

1 # ----- #
2 # Install packages (if not already installed)
3 # ----- #
4 Packages <- c("BaylorEdPsych", "Amelia", "mice", "NbClust",
5               "caret", "rlist", "xtable")
6 # install.packages(Packages)
7
8 # ----- #
9 # Load package for docstring
10 # ----- #
11 lapply(Packages, library, character.only = TRUE)
12
13 # ----- #
14 # Load data set with same variables and source helper functions
15 # ----- #
16 allDataFiles <- c("HFpEFInd", "HFmrEFInd",
17                  "HFpEFNoInd", "HFmrEFNoInd",
18                  "HFfullDataSet", "SyndClass")
19 lapply(gsub(" ", "", paste("data_files/", allDataFiles,
20                             ".Rdat")), load, .GlobalEnv)
21 source("utilities.R")
22
23 # ----- #
24 # Summary of missing variables
25 # ----- #
26 top.n.missing(HFfullDataSet, 10)
27 top.n.missing(cbind(HFmrEFNoInd, HFmrEFInd), 10)
28 top.n.missing(cbind(HFpEFNoInd, HFpEFInd), 10)
29
30 # ----- #
31 # Split variables into indicator and categorical variables
32 # ----- #
33 HFfullRmInd <- rm.indicator(HFfullDataSet, 8)
34 HFfullInd <- HFfullRmInd$indicator
35 HFfullNoInd <- HFfullRmInd$non.indicator
36
37 # ----- #

```

```

38 # Little 's test to assess for missing completely at random.
39 # Remove variables with more than a given cut.off missing
40 # values and that have near zero variance (not for indicator
41 # variables).
42 # ----- #
43 # In Full data set
44 # ----- #
45 CutOff <- 0.20 # cut.off percentage
46 HFfullInd <- rm.missing(HFfullInd, cut.off = CutOff,
47                        near.zero.var = F)
48 HFfullNoInd <- rm.missing(HFfullNoInd, cut.off = CutOff)
49 HFfullList <- list(HFfullInd, HFfullNoInd)
50 HFfullMcar <- do.call(rbind, lapply(HFfullList, little.mcar))
51 HFfullCarNames <- c("indicator", "continuous")
52 rownames(HFfullMcar) <- HFfullCarNames
53
54 # ----- #
55 # In HFpEF
56 # ----- #
57 CutOff <- 0.15 # cut.off percentage
58 HFpEFInd <- rm.missing(HFpEFInd, cut.off = CutOff,
59                      near.zero.var = F)
60 HFpEFNoInd <- rm.missing(HFpEFNoInd, cut.off = CutOff)
61 HFpEFList <- list(HFpEFInd, HFpEFNoInd)
62 HFpEFMcar <- do.call(rbind, lapply(HFpEFList, little.mcar))
63 HFpEFMcarNames <- c("indicator", "continuous")
64 rownames(HFpEFMcar) <- HFpEFMcarNames
65
66 # ----- #
67 # In HFmrEF
68 # ----- #
69 CutOff <- 0.25 # cut.off percentage
70 HFmrEFInd <- rm.missing(HFmrEFInd, cut.off = CutOff,
71                       near.zero.var = F)
72 HFmrEFNoInd <- rm.missing(HFmrEFNoInd, cut.off = CutOff)
73 HFmrEFList <- list(HFmrEFInd, HFmrEFNoInd)
74 HFmrEFMcar <- do.call(rbind, lapply(HFmrEFList, little.mcar))
75 HFmrEFMcarNames <- c("indicator", "continuous")
76 rownames(HFmrEFMcar) <- HFmrEFMcarNames
77 xtable(rbind(HFfullMcar, HFpEFMcar, HFmrEFMcar),
78        digits = c(0,0,0,4,0,5))
79
80 # ----- #
81 # Report missing data after removing variables
82 # ----- #

```



```

83 top.n.missing(cbind(HFfullNoInd, HFfullInd), n = 10)
84 top.n.missing(cbind(HFpEFnoInd, HFpEFInd), n = 10)
85 top.n.missing(cbind(HFmrEFnoInd, HFmrEFInd), n = 10)
86
87 # ----- #
88 # Impute data using Bootstrap EM and CART
89 # ----- #
90 # In Full data set
91 # ----- #
92 m <- 100 # number of bootstrap samples
93 bnd <- data.bounds(HFfullNoInd, 0, Inf)
94 HFfullEm <- boot.em.impute(HFfullNoInd, bnd, n.boot = m)
95 HFfullCart <- complete(mice(HFfullInd, method = "cart"))
96
97 # ----- #
98 # In HFpEF
99 # ----- #
100 HFpEFconImpEmList <- HFmrEFconImpEmList <- list()
101 HFpEFbound <- data.bounds(HFpEFnoInd, 0, Inf)
102 HFpEFem <- boot.em.impute(HFpEFnoInd, bounds = HFpEFbound,
103                          n.boot = m)
104 HFpEFcart <- complete(mice(HFpEFInd, method = "cart"))
105
106 # ----- #
107 # In HFmrEF
108 # ----- #
109 HFmrEFbound <- data.bounds(HFmrEFnoInd, 0, Inf)
110 HFmrEFem <- boot.em.impute(HFmrEFnoInd,
111                          bounds = HFmrEFbound,
112                          n.boot = m)
113 HFmrEFcart <- complete(mice(HFmrEFInd, method = "cart"))
114
115 # ----- #
116 # Combine imputed data sets into one
117 # ----- #
118 HFfullImp <- cbind(HFfullEm, HFfullCart)
119 HFpEFImp <- cbind(HFpEFem, HFpEFcart)
120 HFmrEFImp <- cbind(HFmrEFem, HFmrEFcart)
121
122 # ----- #
123 # Sort columns
124 # ----- #
125 HFfullImp <- sort.column.names(HFfullImp, id.col = T)
126 HFpEFImp <- sort.column.names(HFpEFImp, id.col = T)
127 HFmrEFImp <- sort.column.names(HFmrEFImp, id.col = T)

```

```

128
129 # ----- #
130 # Consolidate naming of columns for HFpEF
131 # ----- #
132 HFpEFimp <- HFpEFimp[, colnames(HFfullImp)]
133
134 # ----- #
135 # Save full data set
136 # ----- #
137 path <- "data_files/"; r <- ".Rdat"
138 fileNames <- c("HFfullImp", "HFpEFimp", "HFmrEFimp")
139
140 for (name in fileNames){
141   save(list = (name), file = paste(path, name, r, sep = ""))
142 }
143
144 # ----- #
145 # Principal component analysis
146 # ----- #
147 HFfullpca <- princomp(HFfullImp, cor = T)
148 HFpEFpca <- princomp(HFpEFimp, cor = T)
149 HFmrEFpca <- princomp(HFmrEFimp, cor = T)
150
151 # ----- #
152 # Explained variance
153 # ----- #
154 pca.var.plot(HFfullpca, 31, title = "HF same variables")
155 pca.var.plot(HFpEFpca, 34, title = "HFpEF")
156 pca.var.plot(HFmrEFpca, 31, title = "HFmrEF")
157
158 # ----- #
159 # Save pca objects
160 # ----- #
161 path <- "data_files/"; r <- ".Rdat"
162 objects <- c("HFfullpca", "HFpEFpca", "HFmrEFpca")
163
164 for (object in objects){
165   save(list = (object), file = paste(path, object, r, sep = ""))
166 }
167
168 # ----- #

```

### B.4.1 Consolidation

```

1 # ----- #
2 # Install packages (if not already installed)
3 # ----- #
4 Packages <- c("R.matlab", "data.table", "stringr")
5 # install.packages(Packages)
6
7 # ----- #
8 # Load relevant packages
9 # ----- #
10 lapply(Packages, library, character.only = TRUE)
11 source("../source/utilities.R")
12
13 # ----- #
14 # Read matlab files into R
15 # ----- #
16 dataSetHFpEF <- readMat('data_use_HFpEF.mat')
17 dataSetHFmrEF <- readMat('data_use_HFmrEF.mat')
18
19 # ----- #
20 # Extract the data matrix from matlab files
21 # ----- #
22 HFpEFmat <- dataSetHFpEF$All.data
23 HFmrEFmat <- dataSetHFmrEF$All.data
24
25 # ----- #
26 # Add all column names
27 # ----- #
28 colnames(HFpEFmat) <- c(as.vector(unlist(
29   dataSetHFpEF$Varnames)))
30 colnames(HFmrEFmat) <- c(as.vector(unlist(
31   dataSetHFmrEF$Varnames)))
32
33 # ----- #
34 # Consolidate naming conventions for some variables
35 # ----- #
36 # In the HFpEF matrix
37 # ----- #
38 setnames(as.data.frame(HFpEFmat),
39   old = c("E_e", "LVfunction", "ECGRhythm_other",
40     "ECGQRS_other", "Other_ethnicity", "Plt",
41     "COPD"),
42   new = c("Ee", "LVEF", "ECGRhythmother", "ECGQRSother",
43     "Otherethnicity", "Plts", "COPDasthma"))
44
45 # ----- #

```

```

46 # In the HFmrEF matrix
47 # ----- #
48 setnames(as.data.frame(HFmrEFmat),
49         old=c("Admissionweight", "BMI", "Numberofcomorbidities",
50              "Afrocaribbean", "Caucasian", "Pulse", "NtproBNP",
51              "E", "ECGRhythm_other", "LVHand_orLAE",
52              "ECGQRS_other", "iron", "Timetoadmission"),
53         new = c("admissionwgt", "Bmladmission", "comorbidities",
54               "Black", "White", "pulse", "NTproBNP", "Ewave",
55               "ECGRhythmother", "LVHandorLAE",
56               "ECGQRSother", "Ironlevels", "TimetoHFadm"))
57
58 # ----- #
59 # Lowercase letters for all the colnames
60 # ----- #
61 colnames(HFpEFmat) <- tolower(colnames(HFpEFmat))
62 colnames(HFmrEFmat) <- tolower(colnames(HFmrEFmat))
63
64 # ----- #
65 # Rename duplicate names in variables af and ar
66 # ----- #
67 if(all(colnames(HFmrEFmat)[c(2,4)] == c("af", "ar"))){
68   colnames(HFmrEFmat)[c(2,4)] <- c("afib", "ai")
69 }
70 # ----- #
71 if(all(colnames(HFpEFmat)[c(3,7)] == c("af", "ar"))){
72   colnames(HFpEFmat)[c(3,7)] <- c("afib", "ai")
73 }
74
75 # ----- #
76 # Address error in HFmrEF – lvef data point nr. 1
77 # ----- #
78 HFmrEFmat[1, "lvef"] <- 40.45
79
80 # ----- #
81 # Replace NaN values with NA using the make_na function
82 # ----- #
83 HFpEFmat <- make_na(HFpEFmat)
84 HFmrEFmat <- make_na(HFmrEFmat)
85
86 # ----- #
87 # Create one file with all the common variables in both
88 # HFpEF and HFmrEF data sets.
89 # ----- #
90 # Find common columns in both data sets

```

```

91 # ----- #
92 HFpEFcol <- colnames(HFpEFmat) %in% colnames(HFmrEFmat)
93 HFmrEFcol <- colnames(HFmrEFmat) %in% colnames(HFpEFmat)
94
95 # ----- #
96 # Test that all columns are equal
97 # ----- #
98 all(sort(colnames(HFpEFmat)[HFpEFcol]) ==
99      sort(colnames(HFmrEFmat)[HFmrEFcol]))
100
101 # ----- #
102 # Get and sort the column names
103 # ----- #
104 HFpEFcol <- sort(colnames(HFpEFmat)[HFpEFcol])
105 HFmrEFcol <- sort(colnames(HFmrEFmat)[HFmrEFcol])
106 HFpEFsame <- HFpEFmat[, HFpEFcol]
107 HFmrEFsame <- HFmrEFmat[, HFmrEFcol]
108
109 # ----- #
110 # Create syndrome class matrix
111 # ----- #
112 syndrome <- rep(c(1, 2),
113                times = c(nrow(HFpEFmat), nrow(HFmrEFmat)))
114 SyndName <- rep(c("HFpEF", "HFmrEF"),
115                times = c(nrow(HFpEFmat), nrow(HFmrEFmat)))
116
117 # ----- #
118 # Add patient id, create full data set and syndrome classes
119 # ----- #
120 HFfullDataSet <- rbind(HFpEFsame, HFmrEFsame)
121 id <- seq(1, nrow(HFfullDataSet))
122 HFfullDataSet <- as.data.frame(cbind(id, HFfullDataSet))
123 SyndClass <- as.data.frame(cbind(id, syndrome, SyndName))
124
125 # ----- #
126 # Store indicator and non-indicator variables using the
127 # rm_indicator function
128 # ----- #
129 HFfullrmInd <- rm.indicator(HFfullDataSet, n.uniq = 8)
130
131 # ----- #
132 # Store the non-indicator and in variables for later
133 # ----- #
134 HFfullInd <- HFfullrmInd$indicator
135 HFfullNoInd <- HFfullrmInd$non.indicator

```

```

136
137 # ----- #
138 # Convert zeros to missings, the following variables are not to
139 # be converted.
140 # ----- #
141 notZeros <- c("comorbidities", "timetohfadm")
142 HFfullNoInd <- zero.to.na(HFfullNoInd, notZeros)
143
144 # ----- #
145 # Concatenate indicator and non-indicator variables to one
146 # data set and sort column names.
147 # ----- #
148 HFfullDataSet <- cbind(HFfullNoInd[, -1], HFfullInd)
149 HFfullDataSet <- HFfullDataSet[, sort(colnames(HFfullDataSet))]
150 HFfullDataSet <- cbind(id, HFfullDataSet)
151
152 # ----- #
153 # Split data according to syndroms
154 # ----- #
155 # Full data set
156 # ----- #
157 HFpEFrow <- SyndClass[,3] == "HFpEF"
158 HFmrEFrow <- SyndClass[,3] == "HFmrEF"
159 # ----- #
160 HFpEFdataSet <- HFfullDataSet[HFpEFrow,]
161 HFmrEFdataSet <- HFfullDataSet[HFmrEFrow,]
162
163 # ----- #
164 # Non-indicator variables
165 # ----- #
166 HFpEFnoInd <- HFfullNoInd[HFpEFrow, ]
167 HFmrEFnoInd <- HFfullNoInd[HFmrEFrow, ]
168
169 # ----- #
170 # Indicator variables
171 # ----- #
172 HFpEFind <- HFfullInd[HFpEFrow, ]
173 HFmrEFind <- HFfullInd[HFmrEFrow, ]
174
175 # ----- #
176 # Re-code patient group labels
177 # ----- #
178 # Get patient groups
179 # ----- #
180 patientGroupsHFpEF <- as.matrix(unlist(

```

```

181                                     dataSetHFpEF$Patient.group))
182 patientGroupsHFmrEF <- as.matrix(unlist(
183                                     dataSetHFmrEF$Patient.group))
184
185 # ----- #
186 # Labels of clinical outcomes
187 # ----- #
188 deceased <- c("IN", "Z", "Y", "X")
189 reAdmission <- c("V", "U")
190
191 # ----- #
192 # Split labels
193 # ----- #
194 HFpEFsplit <- str_split_fixed(patientGroupsHFpEF, ",", n = 2)
195 HFmrEFsplit <- str_split_fixed(patientGroupsHFmrEF, ",", n = 2)
196
197 # ----- #
198 # Re-coding mortality labels
199 # ----- #
200 isDeceasedHFpEF <- HFpEFsplit[,1] %in% deceased
201 isDeceasedHFmrEF <- HFmrEFsplit[,1] %in% deceased
202 deceasedHFpEF <- ifelse(isDeceasedHFpEF, "yes", "no")
203 deceasedHFmrEF <- ifelse(isDeceasedHFmrEF, "yes", "no")
204
205 # ----- #
206 # Re-coding re-admission labels
207 # ----- #
208 isReAdmittedHFpEF <- HFpEFsplit[,1] %in% reAdmission |
209                                     HFpEFsplit[,2] %in% reAdmission
210 isReAdmittedHFmrEF <- HFmrEFsplit[,1] %in% reAdmission |
211                                     HFmrEFsplit[,2] %in% reAdmission
212 reAdmissionHFpEF <- ifelse(isReAdmittedHFpEF, "yes", "no")
213 reAdmissionHFmrEF <- ifelse(isReAdmittedHFmrEF, "yes", "no")
214
215 # ----- #
216 # Add outcomes to matrix
217 # ----- #
218 HFpEFoutcomes <- cbind(id[HFpEFrow], patientGroupsHFpEF,
219                                     deceasedHFpEF, reAdmissionHFpEF)
220 HFmrEFoutcomes <- cbind(id[HFmrEFrow], patientGroupsHFmrEF,
221                                     deceasedHFmrEF, reAdmissionHFmrEF)
222
223 # ----- #
224 # Add colnames to matrices
225 # ----- #

```

```

226 colnames(HFpEFoutcomes) <- colnames(HFmrEFoutcomes) <-
227   c("id", "patientgroup", "deceased", "readmitted")
228
229 # ----- #
230 # Create outcomes data frames
231 # ----- #
232 HFfullOutcomes <- as.data.frame(rbind(HFpEFoutcomes,
233                                       HFmrEFoutcomes))
234 rownames(HFfullOutcomes) <- HFfullOutcomes[,1]
235 # ----- #
236 HFpEFoutcomes <- HFfullOutcomes[HFpEFrow,]
237 HFmrEFoutcomes <- HFfullOutcomes[HFmrEFrow,]
238
239 # ----- #
240 # Save all data frames (13 df in all)
241 # ----- #
242 path <- "../source/data_files/"; r <- ".Rdat"
243 fileNames <- c("HFfullDataSet", "HFfullNoInd", "HFfullInd",
244               "HFpEFdataSet", "HFpEFnoInd", "HFpEFInd",
245               "HFmrEFdataSet", "HFmrEFnoInd", "HFmrEFInd",
246               "HFfullOutcomes", "HFpEFoutcomes",
247               "HFmrEFoutcomes", "SyndClass")
248 for (name in fileNames){
249   save(list = (name), file = paste(path, name, r, sep = ""))
250 }
251
252 # ----- #

```

## B.5 Clustering

```

1 # ----- #
2 # Install relevant packages (if not already done)
3 # ----- #
4 Packages <- c("NbClust", "xtable")
5 # install.packages(Packages)
6
7 # ----- #
8 # Load relevant packages
9 # ----- #
10 lapply(Packages, library, character.only = TRUE)
11 source("utilities.R")
12
13 # ----- #
14 # Load pca objects and data files

```



```

15 # ----- #
16 allDataFiles <- c("HFfullpca", "HFpEFpca", "HFmrEFpca",
17                  "HFfullImp", "HFpEFImp", "HFmrEFImp",
18                  "SyndClass")
19 lapply(gsub(" ", "", paste("data_files/", allDataFiles,
20                             ".Rdat")), load, .GlobalEnv)
21
22 # ----- #
23 # Determine optimal number of clusters
24 # ----- #
25 NbClust(HFpEFpca$scores[,1:2], min.nc = 2, max.nc = 4,
26         method = "kmeans")
27 NbClust(HFmrEFpca$scores[,1:2], min.nc = 2, max.nc = 4,
28         method = "kmeans")
29
30 # ----- #
31 # PCA cluster plot for all data sets
32 # ----- #
33 path_to_images <- "../..../doc/thesis/images/"
34 pdf(file = paste(path_to_images, "ClustFull.pdf"), width = 8,
35     height = 8)
36 clustFull <- pca.cluster.plot(HFfullpca, 4, km.clust = 2,
37                               hc.clust = 2, em.clust = 2,
38                               actual = SyndClass[,2],
39                               return.clust = T, ellipse = F)
40 dev.off()
41
42 # ----- #
43 # Extract cluster configuration and add to data frame
44 # ----- #
45 ACTfull <- clustFull$ACT
46 HCfull <- clustFull$HC
47 KMfull <- clustFull$KM
48 EMfull <- clustFull$EM
49
50 # ----- #
51 # Compare baseline characteristics
52 # ----- #
53 act_full <- compare.baseline(cbind(HFfullImp, ACTfull),
54                             "ACTfull")
55 act_hc <- compare.baseline(cbind(HFfullImp, HCfull),
56                             "HCfull")
57 act_km <- compare.baseline(cbind(HFfullImp, KMfull),
58                             "KMfull")
59 act_em <- compare.baseline(cbind(HFfullImp, EMfull),

```

```

60                                     "EMfull")
61
62 xtable(act_full[[2]][1:15,])
63 xtable(act_hc[[2]][1:15,])
64 xtable(act_km[[2]][1:15,])
65 xtable(act_em[[2]][1:15,])
66
67 # ----- #
68 # Assuming clustering by physicians is correct
69 # ----- #
70 pdf(file = paste(path_to_images, "ClustpPhy.pdf"), width = 9,
71      height = 8)
72 clustPefFull <- pca.cluster.plot(HFpEFpca, 2, km.clust = 3,
73                                 hc.clust = 3, em.clust = 3,
74                                 return.clust = T, ellipse = F)
75 dev.off()
76
77 pdf(file = paste(path_to_images, "ClustmrPhy.pdf"), width = 9,
78      height = 8)
79 clustMrFull <- pca.cluster.plot(HFmrEFpca, 2, km.clust = 3,
80                                 hc.clust = 3, em.clust = 3,
81                                 return.clust = T, ellipse = F)
82 dev.off()
83
84 # ----- #
85 # Compare baseline characteristics HFpEF
86 # ----- #
87 HCpEFphy <- clustPefFull$HC
88 KMpEFphy <- clustPefFull$KM
89 EMpEFphy <- clustPefFull$EM
90
91 post_HC_p <- compare.baseline(cbind(HFpEFimp, HCpEFphy),
92                               "HCpEFphy")
93 post_KM_p <- compare.baseline(cbind(HFpEFimp, KMpEFphy),
94                               "KMpEFphy")
95 post_EM_p <- compare.baseline(cbind(HFpEFimp, EMpEFphy),
96                               "EMpEFphy")
97
98 xtable(post_HC_p[[2]][1:15, -1])
99 xtable(post_KM_p[[2]][1:15, -1])
100 xtable(post_EM_p[[2]][1:15, -1])
101
102 # ----- #
103 # Compare baseline characteristics HFmrEF
104 # ----- #

```

```

105 HCrEFphy <- clustMrFull$HC
106 KMrEFphy <- clustMrFull$KM
107 EMrEFphy <- clustMrFull$EM
108
109 post_HC_mr <- compare.baseline(cbind(HFmrEFimp, HCrEFphy),
110                                "HCrEFphy")
111 post_KM_mr <- compare.baseline(cbind(HFmrEFimp, KMrEFphy),
112                                "KMrEFphy")
113 post_EM_mr <- compare.baseline(cbind(HFmrEFimp, EMrEFphy),
114                                "EMrEFphy")
115
116 xtable(post_HC_mr[[2]][1:15, -1])
117 xtable(post_KM_mr[[2]][1:15, -1])
118 xtable(post_EM_mr[[2]][1:15, -1])
119
120 # ----- #
121 # Assumin clustering by physicians is incorrect
122 # ----- #
123 hiKmeansClust <- clustFull$HC
124 HFpEFhiKmeans <- HFfullImp[hiKmeansClust==1,]
125 HFmrEFhiKmeans <- HFfullImp[hiKmeansClust==2,]
126
127 # ----- #
128 # Re-calculate principal components
129 # ----- #
130 HFpEFNewpca <- princomp(HFpEFhiKmeans, cor = T)
131 HFmrEFNewpca <- princomp(HFmrEFhiKmeans, cor = T)
132
133 # ----- #
134 # Plot clusters
135 # ----- #
136 pdf(file = paste(path_to_images, "ClustpNoPhy.pdf"), width = 9,
137      height = 8)
138 clustNewPef <- pca.cluster.plot(HFpEFNewpca, 2, km.clust = 3,
139                                hc.clust = 3, em.clust = 3,
140                                return.clust = T, ellipse = F)
141 dev.off()
142
143 pdf(file = paste(path_to_images, "ClustmrNoPhy.pdf"), width=9,
144      height = 8)
145 clustNewMr <- pca.cluster.plot(HFmrEFNewpca, 2, km.clust = 3,
146                                hc.clust = 3, em.clust = 3,
147                                return.clust = T, ellipse = F)
148 dev.off()
149

```

```

150 # ----- #
151 # Compare baseline characteristics HFpEF
152 # ----- #
153 HCpEFnoPhy <- clustNewPef$HC
154 KMpEFnoPhy <- clustNewPef$KM
155 EMpEFnoPhy <- clustNewPef$EM
156
157 noPost_HC_p <-compare.baseline(cbind(HFpEFhiKmeans,
158                                     HCpEFnoPhy),"HCpEFnoPhy")
159 noPost_KM_p <-compare.baseline(cbind(HFpEFhiKmeans,
160                                     KMpEFnoPhy),"KMpEFnoPhy")
161 noPost_EM_p <-compare.baseline(cbind(HFpEFhiKmeans,
162                                     EMpEFnoPhy),"EMpEFnoPhy")
163
164 xtable(noPost_HC_p[[2]][1:15, -1])
165 xtable(noPost_KM_p[[2]][1:15, -1])
166 xtable(noPost_EM_p[[2]][1:15, -1])
167
168 # ----- #
169 # Compare baseline characteristics HFmrEF
170 # ----- #
171 HCmrEFnoPhy <- clustNewMr$HC
172 KMmrEFnoPhy <- clustNewMr$KM
173 EMmrEFnoPhy <- clustNewMr$EM
174
175 noPost_HC_mr<- compare.baseline(cbind(HFmrEFhiKmeans,
176                                     HCmrEFnoPhy),
177                                     "HCmrEFnoPhy")
178 noPost_KM_mr<- compare.baseline(cbind(HFmrEFhiKmeans,
179                                     KMmrEFnoPhy),
180                                     "KMmrEFnoPhy")
181 noPost_EM_mr<- compare.baseline(cbind(HFmrEFhiKmeans,
182                                     EMmrEFnoPhy),
183                                     "EMmrEFnoPhy")
184
185 xtable(noPost_HC_mr[[2]][1:15, -1])
186 xtable(noPost_KM_mr[[2]][1:15, -1])
187 xtable(noPost_EM_mr[[2]][1:15, -1])
188
189 # ----- #
190 # Result of all the significant baseline characteristics
191 # ----- #
192 results_post <- c(post_HC_p[[1]], post_KM_p[[1]],
193                  post_EM_p[[1]], post_HC_mr[[1]],
194                  post_KM_mr[[1]], post_EM_mr[[1]])

```

```

195 results_no_post <- c(noPost_HC_p[[1]], noPost_KM_p[[1]],
196                     noPost_EM_p[[1]], noPost_HC_mr[[1]],
197                     noPost_KM_mr[[1]], noPost_EM_mr[[1]])
198
199 results <- cbind(matrix(results_post, 3),
200                 matrix(results_no_post, 3))
201
202 colnames(results) <- rep(c("HFpEF", "HFmrEF"), 2)
203 rownames(results) <- c("Hierarchical", "K-Means", "EM")
204
205 xtable(results)
206
207 # ----- #

```

## B.6 Classification

```

1 # ----- #
2 # Install relevant packages (if not already done)
3 # ----- #
4 Packages <- c("mlbench", "caret", "elasticnet", "klaR",
5             "xtable", "tikzDevice")
6 # install.packages(Packages)
7
8 # ----- #
9 # Load relevant packages
10 # ----- #
11 lapply(Packages, library, character.only = TRUE)
12 source("utilities.R")
13
14 # ----- #
15 # Load data files
16 # ----- #
17 allDataFiles <- c("HFfullImp", "HFfullOutcomes")
18 lapply(gsub(" ", "", paste("data_files/", allDataFiles,
19                             ".Rdat")), load, .GlobalEnv)
20
21 # ----- #
22 # Add cross validation configuration
23 # ----- #
24 kfold <- trainControl(method = "cv", number = 10)
25 seed <- 902109
26 metric <- "Accuracy"
27
28 # ----- #
29 # Train and evaluate the classification algorithms with kfold

```

[illegible]

```

75 xtable(summary(resultsMortalityKfold)$statistics$Accuracy,
76         digits = 3)
77 xtable(summary(resultsMortalityKfold)$statistics$Kappa,
78         digits = 3)
79
80 pathTolImages <- "../..../doc/thesis/images/"
81 tikz(file=paste(pathTolImages,"classificationMortality.tex",
82                sep = ""), height = 5.5, standAlone = F)
83 dotplot(resultsMortalityKfold, main = "Mortality")
84 dev.off()
85
86 # ----- #
87 # Readmission
88 # ----- #
89 # kfold CV evaluation of classifiers
90 # ----- #
91 set.seed(seed)
92 fitKnnKfoldReadm <- train(dataset, readmission, method="knn",
93                           metric=metric, trControl=kfold)
94
95 set.seed(seed)
96 fitLLKfoldReadm <- train(dataset, readmission, method = "glm",
97                           metric=metric, trControl = kfold)
98
99 set.seed(seed)
100 fitLDAKfoldReadm <- train(dataset[, -19], readmission,
101                           method = "lda", metric = metric,
102                           trControl = kfold)
103
104 set.seed(seed)
105 fitNbKfoldReadm <- train(dataset, readmission, method = "nb",
106                           metric = metric, trControl = kfold)
107
108 set.seed(seed)
109 fitSvmKfoldReadm <- train(dataset, readmission,
110                           method="svmRadial", metric=metric,
111                           trControl=kfold)
112
113 set.seed(seed)
114 fitRfKfoldReadm <- train(dataset, readmission, method="rf",
115                           metric = metric, trControl = kfold)
116
117 # ----- #
118 # Produce summary statistics and plots
119 # ----- #

```

```
120 # Kfold CV
121 # ----- #
122 resultsReadmKfold <- resamples(list(knn = fitKnnKfoldReadm ,
123                                   lda = fitLDAKfoldReadm ,
124                                   nb = fitNbKfoldReadm ,
125                                   logr = fitLLKfoldReadm ,
126                                   svm = fitSvmKfoldReadm ,
127                                   rf = fitRfKfoldReadm))
128 xtable(summary(resultsReadmKfold)$statistics$Accuracy ,
129         digits = 3)
130 xtable(summary(resultsReadmKfold)$statistics$Kappa ,
131         digits = 3)
132 pathToImages <- "../..../doc/thesis/images/"
133 tikz(file=paste(pathToImages,"classificationReadmission.tex",
134                sep = ""), height = 5.5, standAlone = F)
135 dotplot(resultsReadmKfold, main = "Re-admission")
136 dev.off()
137
138 # ----- #
```



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