- 1. What you have learned in Math 1A and 1B?
- 2. Sketch the following curves: $(-\infty < t < \infty)$

(a)
$$x = 2t - 1, y = 3t + 1$$

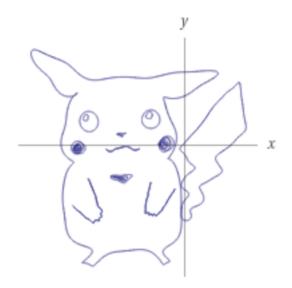
(b)
$$x = e^t, y = e^{2t}$$

(c)
$$x = |\cos t|, y = |\sin t|$$

(d)
$$x = e^{-t} \cos t, y = e^{-t} \sin t$$

3. Consider a parametrized curve (x,y)=(f(t),g(t)) parametrized by t. Could you explain a difference between it with another curve parametrized by (x,y)=(f(2t),g(2t))?

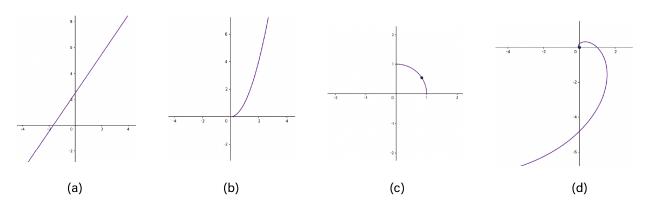
Here's a Pikachu curve for you:



Reference: https://www.wolframalpha.com/input?i=pikachu+curve

Solution

- 1. Single variable functions, limit and continuity, differentiation, integration, and their applications, ...
- 2. (a) Using $x=2t-1 \Leftrightarrow t=(x+1)/2$, one can eliminate t and get a line $y=\frac{3}{2}(x+1)+1=\frac{3}{2}x+\frac{5}{2}$.
 - (b) We have $y=x^2$, but be careful since $x=e^t$, we should have x>0 and the curve will be the right half of the parabola.
 - (c) We have $x^2 + y^2 = 1$. However, both x and y should be non-negative, so the curve is the part of the unit circle on the first quadrant.
 - (d) Observe that $x^2 + y^2 = e^{-t}$ and $y/x = \tan t$. It is similar to a parametrization of a circle centered at origin, but the distance between (x, y) and the origin decreases exponentially as t increase. Hence, it is a spiral.



3. Graphically they are the same - the second curve is traced twice times as fast.