

**Math 53 (Multivariable Calculus), Section 102 & 108**

**Week 3, Wednesday**

**Sep 7, 2022**

**For the other materials: [seewoo5.github.io/teaching/2022Fall](https://seewoo5.github.io/teaching/2022Fall)**

---

1. Consider two curves  $r = 2 \cos \theta$  and  $r = 2 \sin \theta$ .
  - (a) Find the area of the region that lies inside both curves.
  - (b) Find the perimeter of the above region.
2. (a) Sketch a graph of a curve with polar equation  $r^2 = \sin 2\theta$ .
  - (b) Find the area enclosed by the curve.
  - (c\*) Show that the length of the curve equals to

$$2 \int_0^{\pi/2} \frac{d\theta}{\sqrt{\sin 2\theta}}$$