

**Math 53 (Multivariable Calculus), Section 102 & 108**

**Week 9, Friday**

**Oct 21, 2022**

**For the other materials: [seewoo5.github.io/teaching/2022Fall](https://seewoo5.github.io/teaching/2022Fall)**

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1. Find the volume of the solid below the plane  $2x + y + z = 4$  and above the disk  $x^2 + y^2 \leq 1$ .
2. Compute  $\int_0^{1/2} \int_{\sqrt{3}y}^{\sqrt{1-y^2}} xy^2 dx dy$  using 1) rectangular coordinate and 2) polar coordinate.
3. A lamina occupies the part of the disk  $x^2 + y^2 \leq 1$  in the first quadrant. Find its center of mass if the density at any point is proportional to its distance from the  $x$ -axis.