

**Math 53 (Multivariable Calculus), Section 102 & 108**

**Week 2, Monday**

**Aug 29, 2022**

**For the other materials: [seewoo5.github.io/teaching/2022Fall](https://seewoo5.github.io/teaching/2022Fall)**

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1. Find  $dy/dx$  for a curve parametrized by  $x = 1/(1+t)$ ,  $y = \sqrt{1+t}$  (for  $t > -1$ ).
2. Consider an ellipse parametrized as  $x = 2 \cos t$ ,  $y = \sin t$ .
  - (a) Eliminate  $t$  to find an equation in  $x$  and  $y$ .
  - (b) Find  $dy/dx$ . Can you express it without  $t$  (only in  $x$  and  $y$ )?
  - (c) Find the tangent line at  $t = \pi/3$ .
3. Find  $dy/dx$  for a curve parametrized by  $x = \sin t \cos t$ ,  $y = \sin^2 t$ . Also, find the points where the tangent line is horizontal or vertical. (Hint: use the double angle formula.)