

**Math 53 (Multivariable Calculus), Section 102 & 108**

**Week 6, Friday**

**Sep 30, 2022**

**For the other materials: [seewoo5.github.io/teaching/2022Fall](https://seewoo5.github.io/teaching/2022Fall)**

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1. Compute  $f_x, f_y, f_{xx}, f_{xy}, f_{yx}, f_{yy}$  of  $f(x, y) = \sin(xy)$ . Check that  $f_{xy} = f_{yx}$ .

2. Use implicit differentiation to find  $\partial z / \partial x$  and  $\partial z / \partial y$ .

(a)  $\sin x + \sin y + \sin z = 1$

(b)  $e^x + e^y + e^z = xyz$

3. If

$$f(x, y) = y \tan^2(x^2) + \frac{x + y}{(x^2 + y^2)^{3/2}} e^{\sin(x\sqrt{y})}$$

compute  $f_x(1, 0)$  and  $f_y(0, 1)$ .