

**Math 53 (Multivariable Calculus), Section 102 & 108**

**Week 7, Monday**

**Oct 3, 2022**

**For the other materials: [seewoo5.github.io/teaching/2022Fall](https://seewoo5.github.io/teaching/2022Fall)**

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1. Show that

$$c(x, t) = \frac{1}{\sqrt{4\pi Dt}} e^{-x^2/(4Dt)}$$

is a solution of the *diffusion equation*

$$\frac{\partial c}{\partial t} = D \frac{\partial^2 c}{\partial x^2}.$$

2. Let

$$f(x, y) = \begin{cases} \frac{x^2 y^2}{x^2 + y^2} & (x, y) \neq (0, 0) \\ 0 & (x, y) = (0, 0) \end{cases}$$

- (a) Compute  $f_x(0, 0)$ ,  $f_y(0, 0)$ ,  $f_{xy}(0, 0)$ ,  $f_{yx}(0, 0)$ . Check that  $f_{xy}(0, 0) = f_{yx}(0, 0)$ .  
(b) Show that both  $f_{xy}$  and  $f_{yx}$  are not continuous at  $(0, 0)$ .