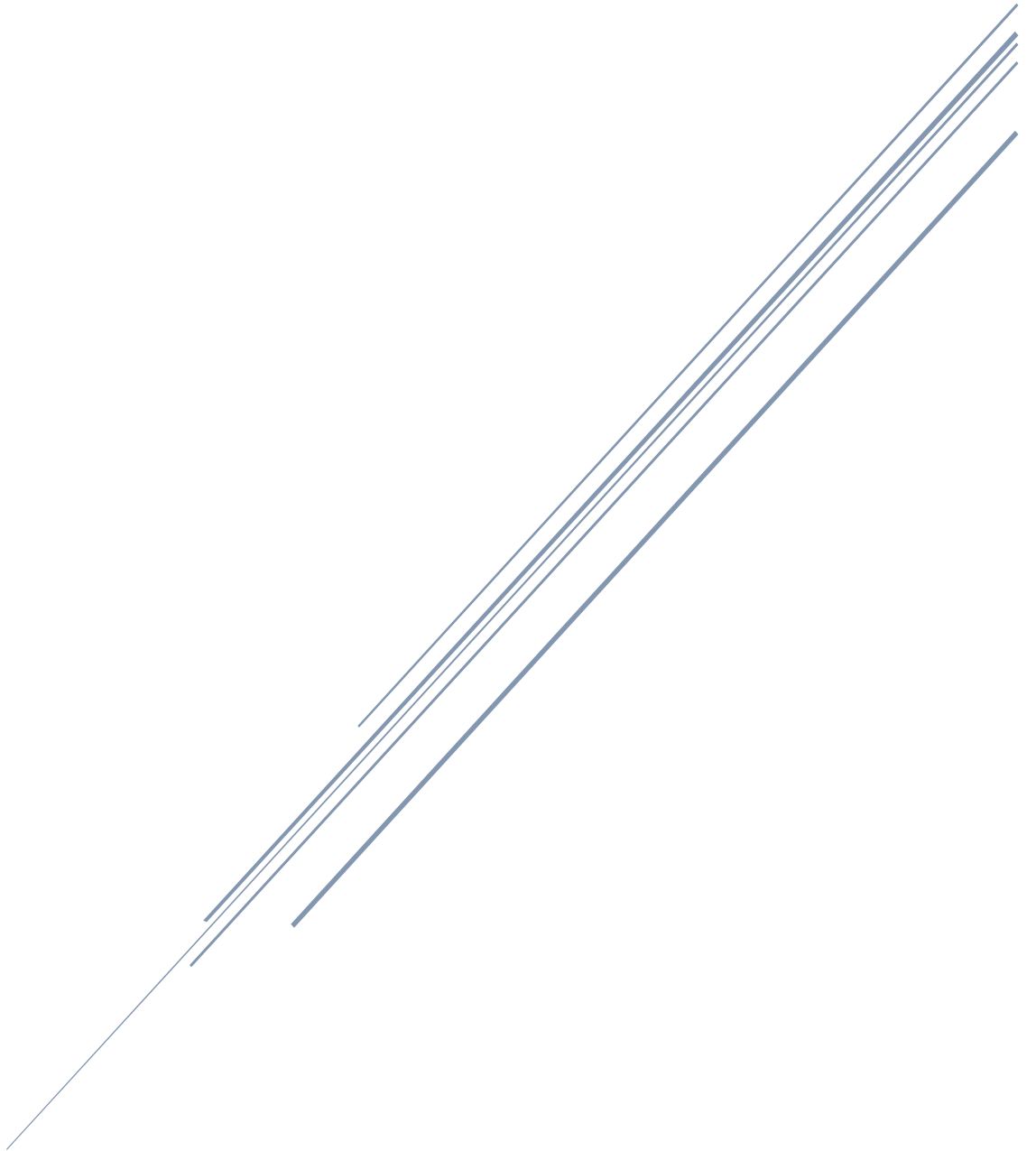


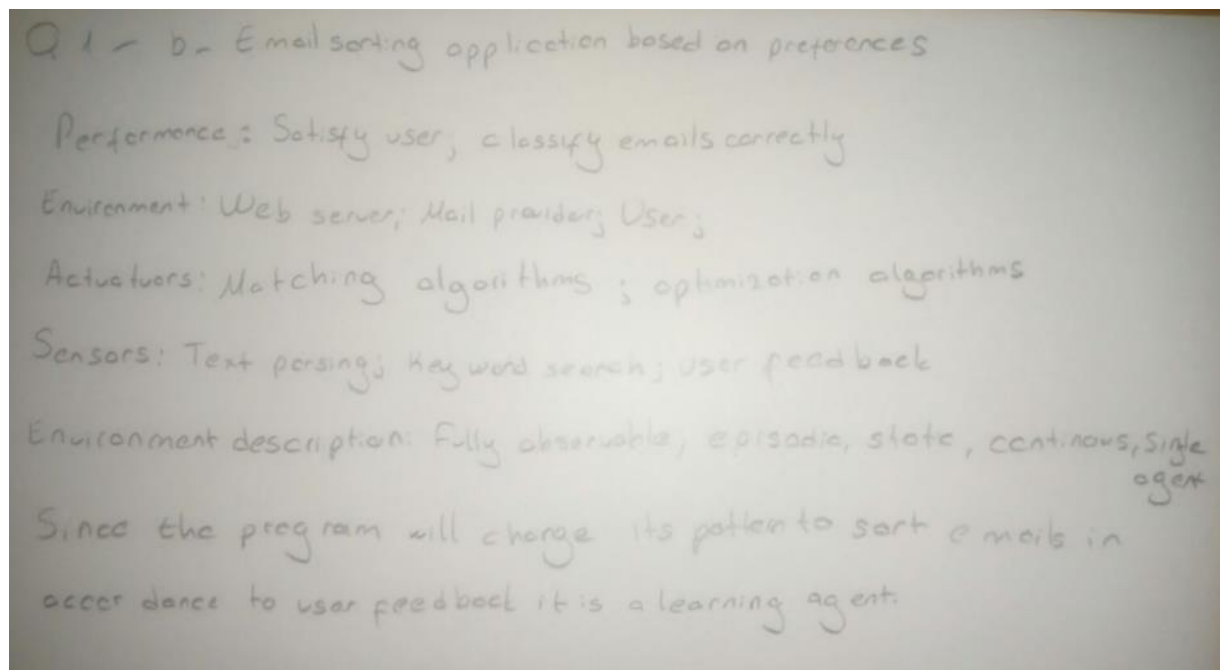
# ASSIGNMENT #1

BLG 435E



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1)



2)

Q2 -  $h(n)$ : cost of the cheapest path from  $n$  to the goal node.  
 prove by induction on the number of steps to the goal that  $h(n) \leq k(n)$

Base case: If 0 steps between goal node and  $n$ ,  $n$  is goal node  $\Rightarrow$

$$h(n) = 0 \leq k(n)$$

Induction Step: If  $n$  is  $i$  steps away from the goal, there must exist some successor  $n'$  of  $n$  generated by some action  $a$  st  $n'$  is on the optimal path from  $n$  to the goal and  $n'$  is  $i-1$  steps away from the goal.

$$\text{Therefore } h(n) \leq c(n, a, n') + h(n')$$

But by the induction hypothesis,  $h(n') \leq k(n')$ . Therefore,

$$h(n) \leq c(n, a, n') + k(n') = k(n)$$

$n'$  is on the optimal path from  $n$  to the goal via action  $a$

Consider a search problem where the states are nodes along a path  $P: n_0, n_1, \dots, n_m$ .  $n_0$  is start state,  $n_m$  is goal state and there is one action from each state  $n_i$  which gives  $n_{i+1}$  as a successor with cost 1. The cheapest cost to the goal from a state  $n_i$  is then  $k(n_i) = m - i$ . Define heuristic function:

$$h(n_i) = m - 2 \lceil i/2 \rceil$$

For all states  $n_i$ ,  $h(n_i) \leq k(n_i)$  and so  $h$  is admissible. However if  $i$  is odd, then  $h(n_i) = h(n_{i+1}) > 1 + h(n_{i+1})$ . Thus  $h$  not consistent.

As the solution provided: [http://reason.cs.uiuc.edu/eyal/classes/f06/cs440/hw/hw6/hw6\\_sol.pdf](http://reason.cs.uiuc.edu/eyal/classes/f06/cs440/hw/hw6/hw6_sol.pdf)

3)

- Only code implementations done on search.py

About references and implementation

```

def aStarSearch(problem, heuristic=nullHeuristic):
    "Search the node that has the lowest combined cost and heuristic first."
    """ YOUR CODE HERE """
    print "Start:", problem.getStartState()
    print "Is the start a goal?", problem.isGoalState(problem.getStartState())
    print "Start's successors:", problem.getSuccessors(problem.getStartState())
    print problem

    frontier = util.PriorityQueue()
    visited = dict()

    state = problem.getStartState()
    node = {}
    node["parent"] = None
    node["action"] = None
    node["state"] = state
    node["cost"] = 0
    node["eval"] = heuristic(state, problem)
    # A* use f(n) = g(n) + h(n)
    frontier.push(node, node["cost"] + node["eval"])

    while not frontier.isEmpty():
        node = frontier.pop()
        state = node["state"]
        cost = node["cost"]
        v = node["eval"]
        #print state

        if visited.has_key(state):
            continue

        visited[state] = True
        if problem.isGoalState(state) == True:
            break

        for child in problem.getSuccessors(state):
            if not visited.has_key(child[0]):
                sub_node = {}
                sub_node["parent"] = node
                sub_node["state"] = child[0]
                sub_node["action"] = child[1]
                sub_node["cost"] = child[2] + cost
                sub_node["eval"] = heuristic(sub_node["state"], problem)
                frontier.push(sub_node, sub_node["cost"] + node["eval"])

    actions = []
    while node["action"] != None:
        actions.insert(0, node["action"])
        node = node["parent"]

    return actions

```

From the repository of user *weixsong* code on the below link is used for improvements on personally written code. <https://github.com/weixsong/pacman/blob/master/search.py>

```

node = {}
node["parent"] = None
node["action"] = None
node["state"] = problem.getStartState()
node["cost"] = 1

```

To ease the node definition by using dictionary data type of python,

```

visited=dict()

```

Use visited as dictionary.

```

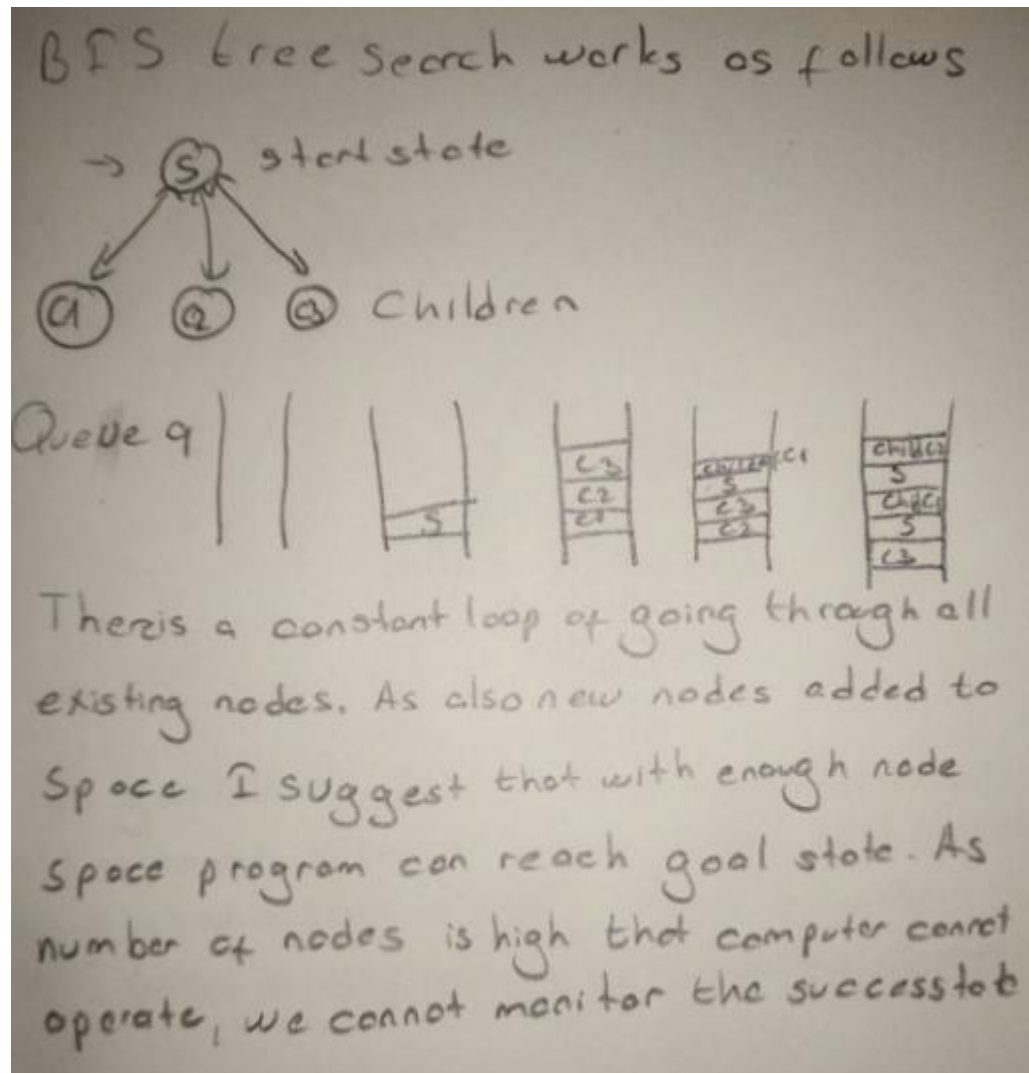
actions = []
while node["action"] != None:
    actions.insert(0, node["action"])
    node = node["parent"]

return actions

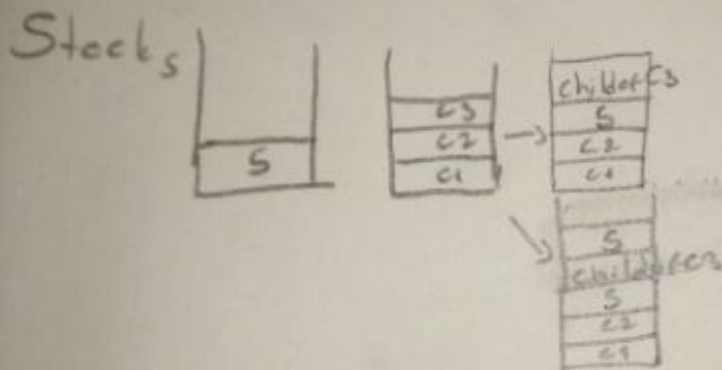
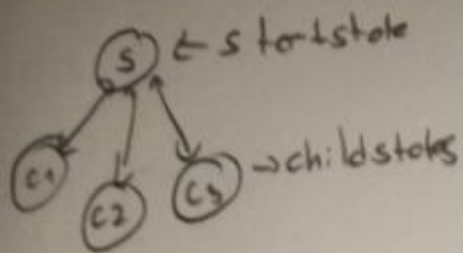
```

Iterate through parent processes from reached goal state up to start state and construct a path.

(a) Depth-First Search (DFS) and Breadth-First Search (BFS)



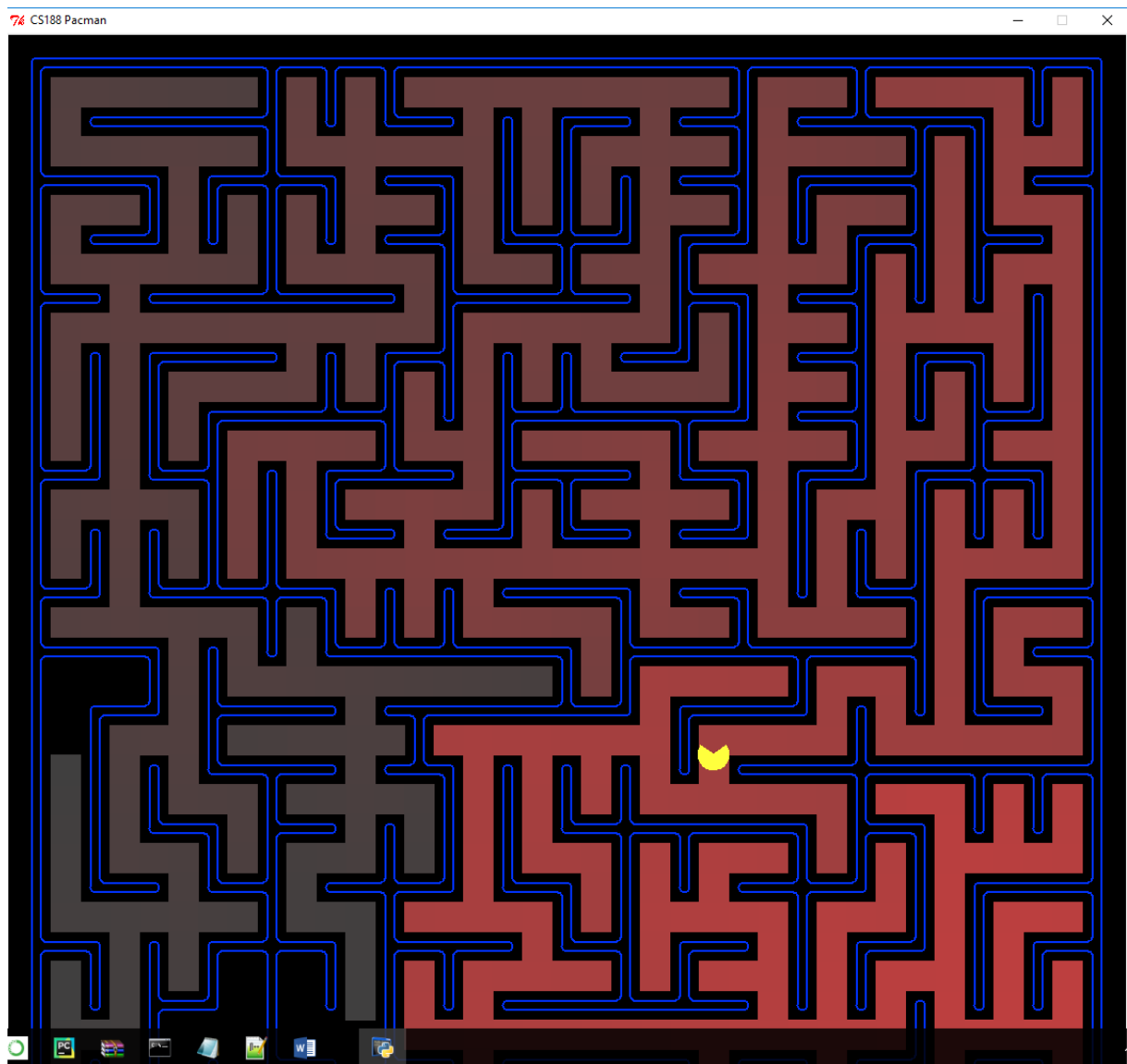
DFS tree search works as follows.



If goal state exists on  $c1$  or  $c2$  program will never reach them if any of children of  $c3$  is not connected to them as well. This situation will cause a loop and system will never terminate

Through out the implementation both dfs and bfs did not stop searching for goal state, could not reach it because of loops.

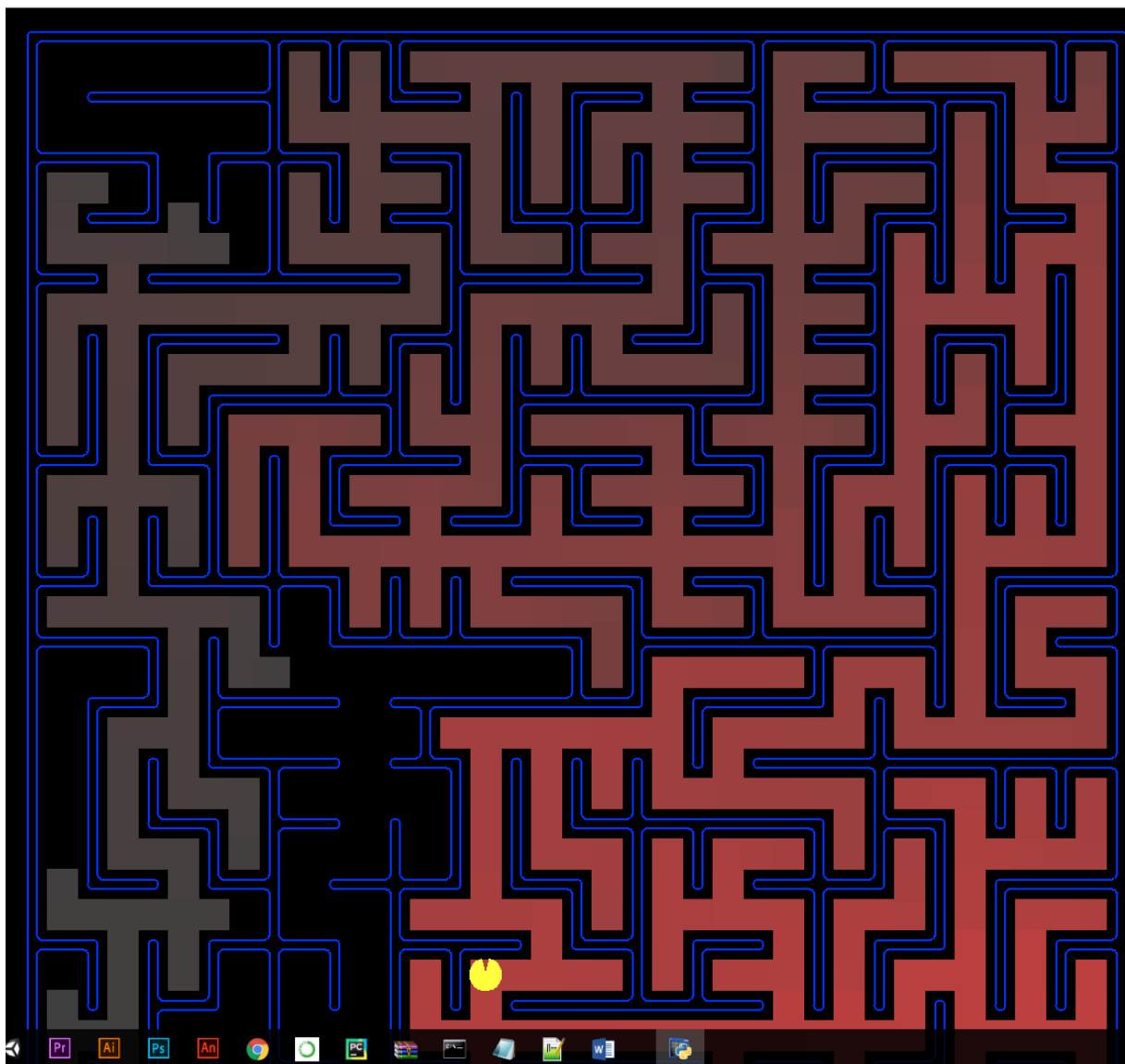
(b) A\* Search



Gamemat discovered by  $h(n) = 1$

```
[SearchAgent] using function astar and heuristic nullHeuristic
[SearchAgent] using problem type PositionSearchProblem
Path found with total cost of 210 in 0.0 seconds
Search nodes expanded: 620
Pacman emerges victorious! Score: 300
Average Score: 300.0
Scores:      300.0
Win Rate:    1/1 (1.00)
Record:      Win
```

Output of run with  $h(n)=1$



Gamemat discovered by  $h(n) = \text{manhattanHeuristic}$



```

[SearchAgent] using function astar and heuristic nullHeuristic
[SearchAgent] using problem type PositionSearchProblem
Path found with total cost of 210 in 0.0 seconds
Search nodes expanded: 556
Pacman emerges victorious! Score: 300
Average Score: 300.0
Scores:      300.0
Win Rate:    1/1 (1.00)
Record:      Win

```

Output of run with  $h(n) = \text{manhattanHeuristic}$

```

#heuristicN=node["cost"]+searchAgents.manhattanHeuristic(node["state"],problem)
heuristicN=1
frontier.push(node,heuristicN)

```

By uncommenting

```

heuristicN=node["cost"]+searchAgents.manhattanHeuristic(node["state"],problem)

```

we use  $h(n) = \text{manhattanHeuristic}$

By uncommenting

```

heuristicN=1

```

we use  $h(n) = 1$

From above output of two A\* implementations, it can be seen that there was not a big difference on time consumption. However, `manhattanHeuristic` showed better performance on node generation as it is more successful on deciding cost of the system.

Admissiblity of  $h(n) = \text{manhattanHeuristic}$  is proven by

For the second function Manhattan distance computation is chosen as  $k(n)$

