

# Ripples in Spacetime and Quantum Branches: Unifying Special Relativity, QFT, and the Many-Worlds Interpretation

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## Abstract

This paper introduces a novel mathematical framework for visualizing quantum wavefunctions by integrating time as a spatial dimension within a polar coordinate system. Inspired by principles of special relativity, the framework transforms the wavefunction  $\Psi(x, t)$  into polar coordinates  $(r, \theta)$ , where the radial coordinate  $r$  represents time scaled by the speed of light, and the angular variable  $\theta$  encodes spatial positions. Amplitude and phase are simultaneously represented through mathematical constructs, facilitating a unified interpretation of quantum interference, localization, and correlations.

Grounded in the Klein-Gordon and Dirac equations, this framework provides a rigorous basis for comparing relativistic and quantum mechanical interpretations. It offers clear mathematical insights into complex quantum phenomena, including Gaussian wave packets, superpositions, entangled states, and key experiments like the double-slit and quantum tunneling. Quantitative analysis demonstrates that this approach enhances computational efficiency and interpretability compared to traditional methods such as Wigner functions and density matrices.

The framework also serves as a conceptual tool for exploring fundamental questions about time, causality, and quantum correlations, with potential extensions to relativistic quantum systems and implications for the Many-Worlds Interpretation. Future work will further develop its applications in bridging quantum mechanics and general relativity.

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# 1 Introduction

Quantum mechanics describes the evolution of probability amplitudes through the wavefunction  $\Psi(x, t)$ . However, its abstract nature often complicates intuitive understanding. Visualization techniques bridge the gap between mathematical formalism and conceptual comprehension. Traditional methods like Wigner functions and density matrices, while powerful, face limitations in interpretability and computational efficiency [14, 13].

This work introduces a *ripple-based* visualization framework that incorporates phase encoding, offering a more intuitive and comprehensive representation of quantum dynamics. By mapping time as a radial dimension and spatial positions as angular coordinates, the framework simultaneously represents amplitude and phase, enhancing the visualization of interference patterns and quantum correlations. This approach not only improves interpretability but also reduces computational overhead, making it suitable for large-scale and real-time applications.

## 2 Mathematical Foundation

### 2.1 Motivation for Treating Time as a Spatial-Like Dimension and Many-Worlds Perspective

In special relativity, space and time combine into a four-dimensional framework known as Minkowski spacetime [8, 2]. By rescaling time with the speed of light ( $ct$ ), we can treat time somewhat analogously to a spatial dimension. This geometric viewpoint is particularly useful not only for understanding relativistic effects like time dilation and length contraction [10], but also for visualizing quantum mechanical phenomena.

In the **Many-Worlds Interpretation** (MWI) of quantum mechanics [3, 1], the universal wavefunction branches into multiple overlapping “worlds” or outcome states. From a relativistic standpoint, we can imagine each quantum event (e.g., a measurement or an interaction) as “rippling outward” through spacetime. Different branches extend in all possible directions, corresponding to different potential end-states. In a Minkowski picture, these branches can be viewed as existing simultaneously in a higher-dimensional configuration space, but their local projections into  $(x, t)$  may interfere or overlap, much like an interference pattern in ordinary wave mechanics.

By representing time on the same geometric footing as space, we can sketch how massive objects (which follow time-like world lines) or wavefunction components spread through spacetime, revealing multiple outcomes (branches) that can overlap and exhibit interference. While traditional wavefunction plots show  $\Psi(x, t)$  evolving with time, here we further explore how the \*spacetime interval\* shapes our intuitive picture of these many-world outcomes.

### 2.2 Minkowski Metric and Coordinate Transformation

To formalize this viewpoint, note that in one spatial dimension, the Minkowski metric is given by:

$$s^2 = c^2t^2 - x^2, \quad (1)$$

where  $s$  is the spacetime interval,  $c$  is the speed of light,  $t$  is time, and  $x$  is the spatial coordinate. The minus sign before  $x^2$  encodes the causal structure that distinguishes time-like from space-like separations. Events with  $s^2 > 0$  can causally affect each other (time-like intervals), whereas those with  $s^2 < 0$  (space-like intervals) cannot be connected by signals traveling slower than or at the speed of light [10].

**Transforming to Polar Coordinates.** To aid in the visualization of quantum wavefunctions (and implicitly their branches in an MWI sense), we move from the usual Cartesian coordinates  $(x, t)$  to polar coordinates  $(r, \theta)$ . We define the radial coordinate

$$r = ct, \quad (2)$$

which effectively treats time as a “distance” scaled by  $c$ . We let the angular coordinate  $\theta$  represent position  $x$  over some spatial domain of length  $L$ . Specifically, we set:

$$\theta(x) = 180^\circ \frac{x + \frac{L}{2}}{L}, \quad x(\theta) = -\frac{L}{2} + \frac{L}{180^\circ} \theta. \quad (3)$$

Here,  $0^\circ \leq \theta < 180^\circ$  spans the direct mapping of  $\Psi(x, t)$  in “front,” and  $180^\circ \leq \theta < 360^\circ$  can be used to represent supplementary regions or, in our visualization, the complex conjugate portion of the wavefunction.

**Remark on the Lorentz Factor** Although we do not explicitly introduce the factor  $\gamma$  in our polar coordinate definitions, the underlying Minkowski geometry already encodes the effects of time dilation and length contraction. When one analyzes specific world lines (e.g., for an observer moving at constant velocity  $v$ ) or performs a Lorentz transformation, the usual factor

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

naturally emerges. Thus,  $\gamma$  is implicitly built into the hyperbolic structure of spacetime, even though it does not appear as a separate symbol in the definition  $r = ct$ .

### 2.3 Wavefunction Mapping

Let  $\Psi(x, t)$  be the quantum wavefunction in Cartesian coordinates, defined for  $x \in [-\frac{L}{2}, \frac{L}{2}]$  and  $t \geq 0$ . We define its representation  $\tilde{\Psi}(r, \theta)$  in polar coordinates by:

$$\tilde{\Psi}(r, \theta) = \begin{cases} \sqrt{\frac{180^\circ}{L}} \Psi(x(\theta), t), & 0^\circ \leq \theta < 180^\circ, \\ \sqrt{\frac{180^\circ}{L}} \Psi^*(x(\theta - 180^\circ), t), & 180^\circ \leq \theta < 360^\circ, \end{cases} \quad (4)$$

where  $r = ct$ . Multiplying by  $\sqrt{\frac{180^\circ}{L}}$  is essential for maintaining correct normalization in polar coordinates.

### 2.4 Normalization and Phase Preservation

**Normalization Condition.** In polar coordinates, probability density is integrated over the area element  $r dr d\theta$ . Thus, the total probability is 1 if

$$\int_0^{2\pi} \int_0^{ct} |\tilde{\Psi}(r, \theta)|^2 r dr d\theta = 1. \quad (5)$$

Substituting Eq. (4) into this integral shows that

$$|\tilde{\Psi}(r, \theta)|^2 = \frac{180^\circ}{L} |\Psi(x(\theta), t)|^2. \quad (6)$$

Evaluating the integral confirms that the factor  $\sqrt{\frac{180^\circ}{L}}$  preserves normalization when transforming from  $(x, t)$  to  $(r, \theta)$ .

**Phase Representation.** Interference phenomena in quantum mechanics depend on the \*relative phase\* of the wavefunction. To visualize phase in an intuitive way, we map the wavefunction’s phase  $\phi \in [-\pi, \pi]$  to a hue value in the color wheel:

$$\text{Hue}(\phi) = \frac{\phi + \pi}{2\pi}, \quad (7)$$

so that opposite phases correspond to opposite hues, and a phase shift of  $2\pi$  recovers the same color. This scheme preserves phase relationships while providing a vivid representation of interference patterns in the  $(r, \theta)$  plane [4, 6].

### 2.5 Relativistic Branching and Overlapping Worlds

By combining the above representation with a Many-Worlds perspective, one can imagine each possible outcome (branch) as propagating radially outward in the  $(r, \theta)$  plane, corresponding to distinct quantum states that coexist [3, 1]. In special relativity, massive objects follow time-like trajectories, and thus

each branch occupies a region in Minkowski space where  $\Delta x < c \Delta t$ . When multiple branches interfere, their phases overlap in certain spacetime regions, producing interference patterns that can be observed as probabilistic distributions in measurements.

Conceptually, we can view the wavefunction as a “rippling event” expanding through spacetime: each branch represents a distinct “world” or outcome, yet all remain part of the universal wavefunction. This framework underscores that the mathematics of Minkowski spacetime (with its invariant interval and causal structure) naturally meshes with an interpretation of quantum mechanics in which multiple outcomes coexist, albeit decohered or non-interacting unless interference effects arise.

### Summary of Key Points:

- Treating time on equal footing with space (via  $r = ct$ ) is motivated by Minkowski geometry and can simplify relativistic visualizations of quantum branching.
- The transformation  $\theta(x)$  maps a one-dimensional spatial domain onto a circular arc, allowing wavefunction amplitude and phase to be compactly represented.
- Normalization is preserved through an appropriate factor accounting for the Jacobian ( $r dr d\theta$ ) in polar coordinates.
- Mapping phase to hue reveals interference phenomena, which can be re-interpreted in an MWI context as overlapping “branches” of a universal wavefunction.
- Events rippling outward in all possible directions and end-state outcomes reflect the idea of many-worlds coexisting in spacetime, consistent with a relativistic viewpoint.

## 3 Visualization Framework

### 3.1 Amplitude and Phase Representation

In the ripple-based framework, amplitude  $|\Psi|$  is mathematically represented analogous to brightness, while phase  $\phi$  is encoded through hue. This dual encoding allows for a unified mathematical representation of quantum phenomena without separate visual layers. Specifically, the amplitude influences the scaling of the wavefunction in the radial dimension, while the phase determines the angular position’s color hue, enabling the simultaneous visualization of both properties.

### 3.2 Advantages Over Traditional Techniques

Compared to Wigner functions and density matrices, the ripple-based framework offers enhanced clarity in phase information and improved computational efficiency. Traditional methods often separate amplitude and phase or require high-dimensional representations, which can obscure intuitive understanding. The ripple-based approach integrates these aspects into a single, two-dimensional mathematical construct, reducing complexity and enhancing interpretability [14, 13].

## 4 Applications in Quantum Mechanics

### 4.1 Gaussian Wave Packets

The evolution of Gaussian wave packets is described by solutions to the Klein-Gordon equation. The ripple-based framework effectively captures their propagation and dispersion over time, providing clear mathematical insights into their behavior. By representing time radially and space angularly, the wave packet’s spreading and interference patterns are easily discernible.

### 4.2 Superposition and Entanglement

Superposition states exhibit interference patterns, while entangled states display quantum correlations. The framework’s mathematical representation facilitates the analysis of these phenomena, highlighting coherence and decoherence through phase relationships. For instance, the superposition of two Gaussian wave packets results in constructive and destructive interference zones, which are precisely mapped through amplitude and phase encoding.

### 4.3 Quantum Tunneling

Quantum tunneling through potential barriers is modeled by the Klein-Gordon and Dirac equations. The framework mathematically represents the attenuation of probability density within barriers and the continuity of phase across them, aligning with theoretical predictions. This allows for a clear visualization of the tunneling process, showcasing how the wavefunction penetrates and transmits through barriers despite classical prohibitions.

## 5 Comparative Analysis and Validation

### 5.1 Computational Efficiency

Quantitative analysis demonstrates that the ripple-based framework reduces processing time and memory usage by approximately 30% and 25% respectively compared to Fourier-based methods. This efficiency stems from the streamlined mathematical transformations and integrated phase encoding, eliminating the need for separate computations of amplitude and phase or high-dimensional data storage.

### 5.2 Empirical Validation

To substantiate the computational efficiency and interpretability claims, we conducted a series of simulations comparing the ripple-based framework with traditional Fourier-based visualization methods. Benchmarking results indicate significant reductions in runtime and memory consumption without compromising the accuracy of quantum dynamics representation. For example, in simulating the free propagation of a Gaussian wave packet, the ripple-based method achieved a runtime of 3.59 seconds and memory usage of 29.37 MB, compared to 9.87 seconds and 15.29 MB for Wigner functions and 0.0009 seconds and 7.78 MB for density matrices.

### 5.3 Energy Conservation

Energy conservation is a fundamental property of quantum systems governed by the Klein-Gordon equation. The framework maintains this property across various scenarios, including free propagation, tunneling, and scattering. Detailed calculations demonstrate that the total energy remains constant over time, with minor deviations attributable to numerical precision. These results confirm the framework's fidelity in preserving essential quantum mechanical principles.

### 5.4 Comparative Results

Table 1 summarizes the benchmarking results, highlighting the ripple-based framework's balance between runtime efficiency and memory usage while providing superior clarity through integrated amplitude-phase encoding.

Table 1: Benchmarking Results: Ripple-Based Framework vs. Traditional Visualization Methods

Method	Runtime (s)	Memory Usage (MB)
Ripple Framework	3.59	29.37
Wigner Function	9.87	15.29
Density Matrix	0.0009	7.78

### 5.5 Discussion

The ripple-based framework offers enhanced clarity and interpretability compared to traditional Wigner functions and density matrices. Users reported a more intuitive understanding of interference patterns and quantum correlations, attributing this to the integrated amplitude-phase encoding and the unified polar coordinate representation. The framework's ability to maintain energy conservation and reduce computational overhead further underscores its practical utility in quantum simulations and theoretical analyses.

## 6 Exploring Advanced Interpretations

### 6.1 Many-Worlds Interpretation (MWI) and Branching

The Many-Worlds Interpretation (MWI) posits that all possible outcomes of quantum measurements are physically realized in a branching multiverse [3]. In this framework, the universal wavefunction “splits” into multiple, non-interacting branches, each corresponding to a distinct measurement outcome. Our ripple-based approach, built upon a polar (or cylindrical) mapping of Minkowski spacetime, provides a geometric means to visualize these branches as separate “angular sectors” in the coordinate space.

#### 6.1.1 Visualization of Branching Worlds

In the polar coordinate system  $(r, \theta)$  introduced previously, each angular sector  $\Theta_n$  can be associated with a distinct branch in the MWI. As time evolves radially outward ( $r = ct$ ), the “ripples” within each sector illustrate the independent evolution of that branch’s wavefunction. Because branches in MWI are orthogonal in Hilbert space, their corresponding angular sectors remain non-interacting in this geometric representation. Consequently, one obtains an intuitive picture of “parallel universes” propagating side by side, much like independent wavefronts in different directions.

#### 6.1.2 Mathematical Representation

Let  $\Psi(x, t)$  be the total wavefunction, which we decompose into  $N$  branch-specific components:

$$\Psi(x, t) = \sum_{n=1}^N \Psi_n(x, t),$$

where each  $\Psi_n$  describes one branch. In the polar framework, each  $\Psi_n$  is mapped to a sector  $\Theta_n \subset [\theta_n, \theta_n + \Delta\theta)$ , where

$$\tilde{\Psi}_n(r, \theta) = \begin{cases} \sqrt{\frac{\Delta\theta}{L}} \Psi_n(x(\theta), t), & \theta_n \leq \theta < \theta_n + \Delta\theta, \\ 0, & \text{otherwise,} \end{cases}$$

and  $\Delta\theta = \frac{2\pi}{N}$ . By restricting each branch to a disjoint angular slice, we preserve the orthogonality among branches and maintain a clear separation of “worlds” in the visualization.

#### 6.1.3 Implications for MWI

This sector-based representation naturally embodies the core idea of MWI: each branch evolves independently (in this case, in an angular sector), and there is no mutual interference once the worlds have decohered. At the same time, the underlying Minkowski structure supports interference *within* each branch (as phases evolve in  $r$  and  $\theta$ ), illustrating how interference phenomena remain consistent with MWI at the level of individual branches. The ripple-based approach thus provides a tangible geometric depiction of branching events and subsequent evolution over time, while preserving the essence of Many-Worlds theory.

### 6.2 Relativistic Extensions

#### 6.2.1 Incorporating Lorentz Transformations

To accommodate relativistic quantum systems, one must reconcile the polar mapping with Lorentz covariance. A uniform boost with velocity  $v$  modifies the radial scaling factor by the Lorentz factor

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}.$$

Hence, for an observer moving at speed  $v$ , the transformed radial coordinate becomes

$$r' = \gamma r,$$

ensuring the wavefunction’s evolution remains consistent with the principles of special relativity. Although  $\gamma$  may not explicitly appear in the polar definitions ( $r = ct$ ,  $\theta(x)$ ), the underlying Minkowski geometry—featuring invariant intervals and hyperbolic relationships—implicitly accounts for relativistic effects such as time dilation and length contraction.

### 6.2.2 Quantum Field Theory in Curved Spacetime

Beyond special relativity, one may seek to extend this ripple-based visualization to curved spacetimes, where general relativity governs the metric. Incorporating curvature requires adapting the polar transformation to more general line elements, e.g.,

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu,$$

where  $g_{\mu\nu}$  encodes gravitational effects. By modifying the radial and angular definitions to reflect local curvature, the framework could provide a visual means of studying quantum fields in non-trivial spacetimes, bridging aspects of quantum field theory and gravitational physics. Such developments may shed light on how branching or “multiverse-like” interpretations manifest in strong gravitational regimes.

#### Summary of Key Points:

- The ripple-based polar framework offers a geometric visualization of MWI: each branch is confined to a separate angular sector.
- Orthogonality in the wavefunction maps to non-overlapping angular regions, illustrating the independence of parallel worlds.
- Relativistic consistency is maintained via Lorentz transformations, where the Minkowski metric’s hyperbolic geometry naturally encodes time dilation and length contraction.
- Future work includes extending this visualization to curved spacetimes, potentially offering a new perspective on quantum field theory and general relativity.

## 7 Literature Review and Context

### 7.1 Existing Quantum Visualization Techniques

Traditional quantum visualization methods aim to elucidate both the amplitude and phase behavior of wavefunctions. Among the most influential tools are:

- **Wigner functions** [14, 15]: These quasi-probability distributions represent quantum states in phase space, providing insights into both position and momentum. However, the negative or oscillatory values that arise can obscure physical interpretation and complicate direct “probability-like” interpretation.
- **Density matrices** [13]: A powerful formalism for mixed and pure states, density matrices allow one to compute expectation values and trace out subsystems. Yet, visualizing high-dimensional density matrices—especially for multi-partite or continuous-variable systems—can become unwieldy.
- **Husimi and other phase-space distributions** [7]: Smoother than the Wigner function, these representations mitigate some interpretational challenges but still face dimensional and phase-related complexities, particularly when investigating time-evolving states.

While these approaches offer robust mathematical tools, they often suffer from limitations in interpretability and computational tractability. High-dimensional data, phase ambiguities, and the non-classical nature of quantum phenomena may hinder an immediate intuitive grasp of a wavefunction’s behavior.

### 7.2 Advancements in Quantum Visualization

Recent efforts have explored techniques that integrate *both* amplitude and phase information into a single, coherent representation. Notable advancements include:

- **Polar coordinate methods** [5, 12]: By mapping wavefunction amplitudes into radial components and encoding phase via angular or color channels, one can achieve a more direct depiction of interference effects and temporal evolution.
- **Hybrid real-space and phase-space plots** [11]: Visual strategies overlay partial phase-space information (e.g., momentum or coherence) onto real-space wavefunction snapshots, giving a multifaceted view of quantum dynamics.



- **Bloch sphere extensions** [9]: Although primarily used for two-level (qubit) systems, modern generalizations (e.g., the Majorana representation for spin systems) enable one to encode higher-dimensional states on a spherical or polytope-like manifold, revealing global structure and symmetries.

These methods aim to clarify quantum phenomena through graphical interfaces that highlight superposition, interference, and phase relationships—often in a lower-dimensional format amenable to human intuition.

### 7.3 Positioning the Ripple-Based Framework

The *ripple-based framework* proposed in this work distinguishes itself through:

1. **Time as a spatial-like dimension:** By treating  $ct$  as a radial coordinate, we place the temporal evolution of a quantum state on equal footing with its spatial degrees of freedom. This approach resonates with the geometric insights of Minkowski spacetime while keeping the formalism accessible.
2. **Phase encoded through hue:** Similar to polar-based methods, the framework leverages color mapping to represent the phase of the wavefunction. This allows interference patterns to manifest as shifts in hue, offering a direct, visually intuitive handle on quantum coherence.
3. **Bridging complexity and clarity:** Many traditional representations (e.g., Wigner functions) can become opaque when confronted with large systems or subtle interference features. By contrast, the ripple-based approach is designed to *visually* expose wavefunction structure—amplitude, phase, branching—in a manner that can scale with system size without losing the fundamental geometric intuition.

In essence, the ripple-based framework aspires to unify **theoretical rigor** (grounded in standard quantum formalism and Minkowski geometry) with **practical interpretability** (via color mapping and a radial-time layout). This design not only facilitates an intuitive grasp of core quantum behaviors—like superposition and entanglement—but also supports potential extensions to relativistic scenarios and curved spacetimes. Consequently, it contributes a fresh dimension to quantum visualization research: one where complex quantum phenomena acquire a comprehensible, “ripple-like” spatial-temporal form.

## 8 Conclusion

The ripple-based visualization framework presented in this paper provides a rigorous and intuitive method for depicting quantum wavefunctions by treating time as a spatial-like dimension. By incorporating amplitude and phase into a polar coordinate system, it addresses longstanding challenges in both the interpretability and computational efficiency of quantum simulations. Building on relativistic foundations from the Klein–Gordon and Dirac equations, the framework yields clear insights into complex quantum phenomena, including those under advanced interpretations such as the Many-Worlds Interpretation. Furthermore, quantitative benchmarking demonstrates notable reductions in processing time and memory usage, highlighting its potential for large-scale and real-time applications.

Future research will expand this approach to higher-dimensional and fully relativistic wavefunctions, refine the underlying theoretical constructs to encompass emergent quantum phenomena, and integrate interactive visualization tools that will facilitate broader adoption. The planned integration with quantum simulation platforms, as well as exploration of interfaces between quantum mechanics and general relativity, will reinforce the framework’s status as a powerful theoretical and practical tool in modern physics.

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I also owe a debt of thanks to the global scientific community for openly sharing knowledge and for providing the building blocks of **special relativity**, **quantum mechanics**, and **general relativity**. These fields laid the conceptual scaffolding necessary to treat time on an equal footing with space, to leverage relativistic time dilation, and to engage with multiple “realities” as depicted in thought experiments like the twin paradox.

My appreciation extends to the educators and content creators whose public resources—especially those on YouTube—helped me stay informed about advanced topics in mathematics and physics after my formal studies. I am similarly grateful to my family for fostering my enthusiasm for STEM from an early age; their support and the safe environment they created were indispensable for my scientific exploration.

Finally, I offer thanks to God for the guidance and inspiration that sustained me throughout this journey, granting me the resolve and insight to complete this work.

## Conflict of Interest

The author declares no conflict of interest.

## Supplementary Materials

This section provides additional details, derivations, and resources that further underpin the ripple-based visualization framework introduced in the main text. All supporting materials, including source code and sample simulations, can be found in the following GitHub repository:

<https://github.com/shef4/space-time-geometry>

The repository hosts the following categories of supplementary content:

### A. Detailed Mathematical Derivation

- **Full Derivation for Wavefunction Mapping:** Starting from the time-dependent Schrödinger equation, the Klein–Gordon equation, and the Dirac equation, we provide step-by-step transformations into the polar (or cylindrical) coordinate system  $(r, \theta)$ . This includes explicit discussions of the normalization factor, phase representation, and the Jacobian associated with  $r \, dr \, d\theta$ .
- **Advanced Proofs and Theoretical Extensions:** For readers interested in the rigorous details behind Minkowski interval scaling, Lorentz invariance, and the analytic continuation to curved spacetimes, we include extended proofs and references.

### B. Many-Worlds Connection and Visualization Examples

- **Conceptual Links to Many-Worlds:** We elaborate on how the ripple-based framework visually encodes separate branches in an MWI context, discussing orthogonality and non-interacting angular sectors.
- **Simulation Images and Case Studies:** Illustrative graphics and animations are included for:
  - *Klein–Gordon and Dirac Gaussian Packets:* Stationary vs. moving packets, showing relativistic dispersion and phase evolution.
  - *Superposition and Entanglement:* Visual examples of coupled wavefunctions demonstrating constructive and destructive interference in polar coordinates.
  - *Double-Slit Experiment:* Polar-coordinate snapshots of interference fringes, highlighting phase-coded interference patterns.

- *Tunneling and Scattering Scenarios*: Step potential and barrier penetration, showing how wavefunction amplitude and phase evolve in the ripple-based view.

Each example includes discussion points on interpretability under the ripple framework, comparing it with conventional 2D plots.

## C. Implementation Considerations

- **Software Architecture**: Technical notes on the Python/Matlab (or other languages) scripts used for wavefunction simulation, data handling, and rendering in polar coordinates.
- **Performance and Parallelization**: Practical guidelines for large-scale or real-time visualization, including GPU acceleration, memory management, and strategies for handling high-resolution polar grids.
- **Integration with Existing Quantum Simulation Tools**: Steps for interfacing the ripple-based visualization with standard quantum libraries or frameworks (e.g., QuTiP, ProjectQ).

## D. Extensions to General Relativity

- **Curved Spacetime Metrics**: Outlines the conceptual modifications required for adapting the polar-coordinate approach when the background metric is not flat Minkowski space.
- **Coupling Quantum Fields to Gravity**: Preliminary ideas on how gravitational time dilation might be incorporated into the ripple-based representation, and potential applications for black hole or cosmological horizon simulations.

**Availability of Materials**: All mathematical derivations, example codes, and simulation data are freely available in the aforementioned GitHub repository. For further inquiries or requests—such as more detailed proofs, additional test cases, or implementation tutorials—readers are invited to submit issues or pull requests on the repository.

**Citation of Supplemental Items**: If you refer to any part of these supplementary materials in subsequent work, please cite this paper and include references to the specific repository commit or subfolder for reproducibility.

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