Sergio Garcia Tapia

Computer Systems: A Programmer's Perspective, by Bryant and O'Hallaron

Chapter 4: Processor Architecture April 7, 2024

## **Practice Problems**

Exercise 4.1. Determine the byte encoding of the Y86-64 instruction sequence that follows. The line .pos 0x100 indicates that the starting address of the object code should be 0x100.

```
.pos 0x100 # Start code at address 0x100
   irmovq $15,%rbx
   rrmovq %rbx,%rcx
loop:
   rmmovq %rcx,-3(%rbx)
   addq %rbx,%rcsx
   jmp loop
```

Solution: The irmovq instruction has a code part of 0x3 and control part of 0x0, which we put together as 0x30. Its instruction format does not use a source register, and a 0x15 indicates; the destination register %rbx is encoded as 0x3. Finally, \$15 is hexadecimal 0xf, which after extending to 64 bits gives 0x00000000000000; we reserve the byte orders to get 0f00000000000000 for the encoding of the instruction. Altogether this takes up 10 bytes, so the next instruction has address 0x10A, an offset of .pos by 10.

The rrmovq is encoded as 0x20. Its source register is %rbx with encoding 0x3, and its destination %rcx with encoding 0x1. Overall, this instruction takes up 2 bytes, so the next instruction has address 0x10C.

The loop is a placeholder for an address, so it will be replaced by the address 0x1c.

The addq has encoding 0x60. Its source and destination registers have encodings 0x3 and 0x1, respectively. The whole instruction takes up 2 bytes, so the next starting address is 0x118.

The jmp is encoded as 0x70, and loop is replaced by the address 0x010c, whose bytes we reverse to 0c0100000000000. The entire translation is:

Exercise 4.2. For each byte sequence listed, determine the Y86-64 instruction sequence it encodes. IF there is some invalid byte in the sequence, show the instruction sequence up

to that point, and indicate where the invalid byte occurs. For each sequence, we show the starting address then a colon, and then the byte sequence.

(b) 0x200: a06f800c02000000000000030f30a0000000000000

(c) 0x300: 5054070000000000000010f0b01f

(d) 0x400: 61137300040000000000000

(e) 0x500: 6362a0f0

#### Solution:

(a) The initial 30 makes this a irmovq instruction. The following f represents that a source is not needed, and the 3 that the destination register is %rbx. The 8-byte value is fcffffffffffffff, which is -4 in decimal. This instruction takes up 10 bytes.

The 40 that follows means we have a rmmovq instruction expecting two registers an an offset. The 6 means the source is %rsi, and the 3, means the destination if %rbx. The 0008000000000 reverses to 0000000000000, completing the instruction and taking up 9 bytes. The last two 00 indicate the halt instruction. Altogether, we have:

0x100: irmovq -4, %rbx

0x10C: rmmovq %rsi0x800(%rbx)

0x115: halt

(b) The a0 makes this a pushq instruction, the following 6 is source register %rsi, and the following f that there is no destination register.

Starting at 80, we have the start of the encoding for a call instruction. The destination is encoded by the 8 bytes 0c0200000000000, which we reverse to 00000000000000c, or simply 0x020c.

The next 0x00 indicates a halt instruction.

0x200: pushq %rsi

0x202: call 0x0000000000000020c

0x20b: halt

0x20c: irmovq \$10,%rbx

(c) The initial 50 makes this a mrmovq instruction. The following byte 54 means that the source and destination registers are %rsp and %rbp, respectively. The source is a

memory reference with a an offset given by the following 8 bytes0x07000000000000, which we reverse to 0x0000000000000, or decimal 7.

The 10 means we have a nop. The f0 is an invalid byte. b01f means popq %rcx. Altogether we have:

0x300: mrmovq 7(%rsp),%rbp

0x30a: nop

0x30b: # invalid
0x30c: popq %rcx

(d) The 61 makes this a subq instruction, with source register %rcx and destination register %rbx, as given by 0x13. The instruction is subq %rcx, %rbx.

0004000000000000 The 73 that follows indicates a je instruction, followed by the reversed constant address 00040000000000, which we reverse to 000000000000000. The last 00 indicates a halt:

0x400: subq %rcx, %rbx

0x402: je 0x0000000000000400

0x40b: halt

(e) The 63 makes this a xorq instruction, with source register %rsi and destination register %rdx, as indicated by the 62. The instruction is xorq %rsi, %rdx. We then have a0 for a pushq instruction, but the f says that there is no source register, which is invalid:

0x500: xorq %rsi, %rdx

0x502: pushq f0 # invalid byte register f0

**Exercise 4.3.** One common pattern in machine-level programs is to add a constant value to a register. With the Y86-64 presented thus far, this requires first using an irmovq to set a register to the constant, then an addq instruction to add this value to the destination register. Suppose we now want to add a new instruction iaddq with the following format:

Byte	0		1		2	3	4	5	6	7	8	9
iddq V, rB	С	0	F	rB				1	I			

This instruction adds the constant value V to register rB.

Re-write the Y86-64 sum function of Figure 4.6 to make use of the iaddq instruction. In the original version, we dedicate registers %r8 and %r9 to hold constant values. Now, we can avoid using those registers altogether.

#### Solution:

```
long sum(long *start, long count)
   start in %rdi, count in %rsi
sum:
   xorq   %rax,%rax # sum = 0
```

```
andq
          %rsi,%rsi # Set condition code
   jmp test
loop:
   mrmovq (%rdi),%r10 # Get *start
          %r10,%rax # Add to sum
   iaddq $1,%rdi
                     # start++
          $-1,%rsi
   iaddq
                     # count--, set condition code
test:
                     # Stop when 0
   jne
          loop
   ret
```

Exercise 4.4. Write Y86-64 code to implement a recursive sum function rsum, based on the following code:

```
long rsum(long *start, long count)
{
   if (count <= 0)
      return 0;
   return *start + rsum(start+1, coount-1);
}</pre>
```

Use the same argument passing and register saving conventions as x86-64 code does. You might find it helpful to compile the C code on an x86-64 machine and then translate the instructions to Y86-64.

Solution: I compiled rsum.c with the flags: gcc -S -01 rsum.c, and got the following x86-64 output:

```
"rsum.c"
   .file
   .text
   .globl rsum
   .type rsum, @function
rsum:
.LFB0:
   .cfi_startproc
   endbr64
           $0, %eax
   movl
   testq %rsi, %rsi
   ile .L5
   pushq %rbx
   .cfi_def_cfa_offset 16
   .cfi_offset 3, -16
           %rdi, %rbx
   movq
           $1, %rsi
   subq
           8(%rdi), %rdi
   leaq
   call
           rsum
           (%rbx), %rax
   addq
```

```
popq
           %rbx
   .cfi_def_cfa_offset 8
   ret
.L5:
   .cfi_restore 3
   ret
   .cfi_endproc
.LFEO:
   .size rsum, .-rsum
   .ident "GCC: (Ubuntu 11.4.0-1ubuntu1~22.04) 11.4.0"
               .note.GNU-stack,"",@progbits
   .section
   .section
               .note.gnu.property, "a"
   .align 8
   .long 1f - Of
   .long 4f - 1f
   .long 5
0:
   .string "GNU"
1:
   .align 8
   .long 0xc0000002
   .long
          3f - 2f
2:
   .long
           0x3
3:
   .align 8
4:
```

I used it as the based for the following Y86-64 code, which I have annotated:

```
long rsum(long *start, long count)
   start in %rdi, count in %rsi
rsum:
   irmovq $0,%rax
                     # Set return value to 0
   iaddq $0,%rsi
                     # Set condition code
                     # if <= 0 goto .L5
   jle
           .L5:
   pushq %rbx
                     # Callee-saved register
   rrmovq %rdi,%rbx # save start (memory address)
   iaddq $1,%rsi
                     # count--
   iaddq $8,%rdi
                     # start++ (add 8 bytes to pointer, pointing to next)
                     # rsum(start++, count--)
   call rsum
   mrmovq (%rbx), %rax # add *start to return value
   popq
          %rbx
                     # restore register
   ret
                     # return
.L5:
   ret
                     # return
```

**Exercise 4.5.** Modify the Y86-64 code for the sum function (Figure 4.6) to implement a function absSum that computes the sum of absolute values of an array. Use a *conditional jump* instruction within your inner loop.

**Solution:** My implementation uses the fact that if x is negative, then  $^{\sim}x + 1$  negates it, making it positive.

```
long absSum(long *start, long count)
   start in %rdi, count in %rsi
absSum:
   irmovq $-1,%r11
                         # Constant -1
   xorq
           \frac{\pi x}{\pi x} # sum = 0
           %rsi,%rsi # Set condition code
   andq
   jmp test
loop:
   mrmovq (%rdi),%r10 # Get *start
   iadd0 $0,%r10
                      # Set condition code
           .nonneg
                      # if >= goto .nonneg
   jge
           %r11,%r10 # -1 XOR *start
   xorq
   iaddq $1,%r10
                      # finish computing abs(*start)
.nonneg:
   addq
           %r10,%rax # Add to sum
   iaddq $1,%rdi
                      # start++
   iaddq $-1,%rsi
                      # count--, set condition code
test:
                      # Stop when 0
           loop
   jne
   ret
```

Exercise 4.6. Modify the Y86-64 code for the sum function (Figure 4.6) to implement a function absSum that computes the sum of absolute values of an array. Use a *conditional move* instruction within your inner loop.

**Solution:** My implementation uses the fact that if x is negative, then  $^{\sim}x + 1$  negates it, making it positive.

```
long absSum(long *start, long count)
       start in %rdi, count in %rsi
absSum:
       irmovq $-1,%r11
                             # Constant -1
       xorq
              \frac{\pi x}{\pi x} # sum = 0
       andq
              %rsi,%rsi # Set condition code
       jmp test
loop:
       mrmovq (%rdi),%r10 # Get *start
       xorq
              %r10,%r11 # -1 XOR *start
       iaddq
              $1,%r11
                          # Finishes computing -*start
       cmovge %r11,%r10 # if %r11 is positive, then %r10 was negative
```

```
addq %r10,%rax # Add to sum
iaddq $1,%rdi # start++
iaddq $-1,%rsi # count--, set condition code
test:
jne loop # Stop when 0
ret
```

Exercise 4.7. Let us determine the behavior of the instruction pushq %rsp for an x86-64 processor. We could try reading the Intel documentation on this instruction, but a simpler approach is to conduct an experiment on an actual machine. The C compiler would not normally generate this instruction, so we must use hand-generated assembly code for this task. Here is a test function we have written (Web Aside ASM:EASM on page 178 describes how to write programs that combine C code with handwritten assembly code):

```
.text
.global pushtest
pushtest:
  movq   %rsp,%rax # Copy stack pointer
  pushq   %rsp # Push stack pointer
  popq   %rdx # Pop it back
  subq   %rdx,%rax # Return 0 or 4
  ret
```

In our experiments, we find that pushtest always returns 0. What does this imply about the behavior of the instruction pushq %rsp under x86-64?

**Solution:** The first instruction stores the old value of the pointer in %rax Since the output is always 0, this means that pushq %rsp pushes the original value of %rsp.

Exercise 4.8. The following assembly-code function lets us determine the behavior of popq %rsp on x86-64:

```
.text
.global poptest
poptest:
   movq
           %rsp,%rdi # Save stack pointer
          $0xabcd
                      # Push test value
   pushq
                      # Pop to stack pointer
           %rsp
   popq
           %rsp,%rax # Set popped value as returned value
   movq
           %rdi,%rsp # Restore stack pointer
   movq
   ret
```

We find this function always returns Oxabcd. What does this imply about the behavior of pop %rsp? What other Y86-64 instruction would have the same behavior?

Solution: It implies that pop %rsp sets the stack pointer to the value read from memory. We could use mrmovq to read this value instead. This would give the correct return value;

however, the value we pushed would remain on the stack, and would therefore point to a lower address than the popq approach.

Exercise 4.9. Write an HCL expression for a signal xor, equal to the *exclusive-or* of inputs a and b. What is the relation between the signals xor and eq defined above?

**Solution:** If we let  $\oplus$  be the XOR symbol, we can define it to mean

```
a \oplus b = (a \&\& !b) || (!a \&\& b)
```

xor and eq are negations of one another, because xor is 1 when a and b are distinct, and 0 otherwise. Meanwhile, eq is 1 when a and b are equal, and 0 otherwise.

**Exercise 4.10.** Suppose you want to implement a word-level equality circuit using the *EXCLUSIVE-OR* circuits from Problem 4.9 rather than bit-level equality circuits. Design such a circuit for a 64-bit *EXCLUSIVE-OR* circuits and two additional logic gates.

**Solution:** The circuit will have two 64-bit buses A and B as inputs. We use a total of 64 bit-level *EXCLUSIVE-OR* circuits operating in parallel. If *any* of them outputs 1, then the two inputs are distinct, and the overall output should be 0. If all of the bit-level XORs output 0, then the circuit should output 1. We therefore feed the outputs of the bit-level XORs into a 64-bit OR gate, and pass its output through an inverter.

**Exercise 4.11.** The HCL code for computing the minimum of three words contains four comparison expressions of th form X := Y. Rewrite the code to compute the same result, but using only three comparisons.

**Solution:** The given HCL was:

If the first inequality fails, then A is not the minimum. Therefore either B or C is the minimum. This means it's enough to check that B := C:

**Exercise 4.12.** Write HCL code describing a circuit that for word inputs A, B, and C selects the *median* of the three values. That is, the output equals the word lying between the minimum and the maximum of the three inputs.

## **Solution:**

Exercise 4.13. Fill in the right-hand column of the following table to the describe the processing of the irmovq on line 4 of the object code in Figure 4.17:

	Generic	Specific
Stage	irmovq V, rB	irmovq \$128,%rsp
Fetch	$icode:ifun \leftarrow M_1[PC]$	
	$\mathtt{rA:rB} \leftarrow \mathrm{M}_1[\mathrm{PC}+1]$	
	$\mathtt{valC} \leftarrow \mathrm{M_8[PC} + 2]$	
	$\mathtt{valP} \leftarrow \mathrm{PC} \! +  10$	
Decode		
Execute	$\mathtt{valE} \leftarrow 0 + \mathtt{valC}$	
Memory		
Write back	$\texttt{R[rB]} \leftarrow \texttt{valE}$	
PC update	$\texttt{PC} \leftarrow \texttt{valP}$	

How does this instruction execution modify the registers and the PC?

### Solution:

	Generic	Specific
Stage	irmovq V, rB	irmovq \$128,%rsp
Fetch	icode:ifun $\leftarrow M_1[PC]$	$M_1[0x00a] = 3:0$
	$\mathtt{rA:rB} \leftarrow \mathrm{M}_1[\mathrm{PC}+1]$	$\texttt{rA:rB} \leftarrow M_1 \texttt{[0x00b]} = \texttt{f:3}$
	$\mathtt{valC} \leftarrow \mathrm{M_8[PC} + 2]$	$\texttt{valC} \leftarrow M_8 \texttt{[0x00c] = 0x15}$
	$\mathtt{valP} \leftarrow \mathrm{PC} \! + 10$	$\mathtt{valP} \leftarrow \mathtt{0x00a} + 10 = \mathtt{0x014}$
Decode		
Execute	$\mathtt{valE} \leftarrow 0 + \mathtt{valC}$	$\mathtt{valE} \leftarrow 0 + \mathtt{0x15}$
Memory		
Write back	$\texttt{R[rB]} \leftarrow \texttt{valE}$	$R[rB] \leftarrow valE = 0x15$
PC update	$\texttt{PC} \leftarrow \texttt{valP}$	$PC \leftarrow valP = 0x014$

The stack pointer %rsp is updated with the value 0x15, and the PC is updated with the value 0x014.

Exercise 4.14. Fill in the right-hand column of the following table to describe the processing of the popq instruction on line 7 of the object in Figure 4.17.

	Generic	Specific
Stage	popq rA	popq %rax
Fetch	icode:ifun $\leftarrow M_1[PC]$	
	$\texttt{rA:rB} \leftarrow \texttt{M}_1\texttt{[PC+1]}$	
	$\mathtt{valP} \leftarrow \mathtt{PC} + 2$	
Decode	$\texttt{valA} \leftarrow \texttt{R[\%rsp]}$	
	$\texttt{valB} \leftarrow \texttt{R[\%rsp]}$	
Execute	$\mathtt{valE} \leftarrow \mathtt{valB} + 8$	
Memory	$\mathtt{valM} \leftarrow \mathtt{M}_8 \mathtt{[valA]}$	
Write back	$\texttt{R[\%rsp]} \leftarrow \texttt{valE}$	
	$\texttt{R[rA]} \leftarrow \texttt{valM}$	
PC update	$\texttt{PC} \leftarrow \texttt{valP}$	

What effect does this instruction have on the registers and the PC?

# Solution:

	Generic	Specific
Stage	popq rA	popq %rax
Fetch	icode:ifun $\leftarrow M_1[PC]$	icode:ifun $\leftarrow M_1[PC] = b:0$
	$\texttt{rA:rB} \leftarrow \texttt{M}_1\texttt{[PC+1]}$	$\texttt{rA:rB} \leftarrow \texttt{M}_1 \texttt{[PC+1]} = \texttt{0:f}$
	$\mathtt{valP} \leftarrow \mathtt{PC} + 2$	$\mathtt{valP} \leftarrow \mathtt{PC} + 2 = \mathtt{0x02e}$
Decode	$\texttt{valA} \leftarrow \texttt{R[\%rsp]}$	$valA \leftarrow R[\%rsp] = 128$
	$\mathtt{valB} \leftarrow \texttt{R[\%rsp]}$	$valA \leftarrow R[\%rsp] = 128$
Execute	$\mathtt{valE} \leftarrow \mathtt{valB} + 8$	$\mathtt{valE} \leftarrow \mathtt{valB} + 8 = 136$
Memory	$\mathtt{valM} \leftarrow \mathtt{M}_8 \mathtt{[valA]}$	$\mathtt{valM} \leftarrow \mathtt{M}_8[\mathtt{valA}] = 9$
Write back	$\texttt{R[\%rsp]} \leftarrow \texttt{valE}$	$\texttt{R[\%rsp]} \leftarrow \texttt{valE} = 136$
	$\texttt{R[rA]} \leftarrow \texttt{valM}$	$\texttt{R[rA]} \leftarrow \texttt{valM} = 9$
PC update	$\texttt{PC} \leftarrow \texttt{valP}$	$\texttt{PC} \leftarrow \texttt{valP} = \texttt{0x02e}$