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Sergio E. Garcia Tapia

Algorithms by Sedgewick and Wayne (4th edition) [SW11]

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## 1.2: Data Abstraction

Exercise 1. Write a Point2D client that takes an integer value n from the command line, generates n random points in the unit square, and computes the distance separating the *closest pair* of points.

Solution. See the com.segarciat.algs4.ch1.sec2.ex01.ClosestPointPair class. The Point2D objects can simply by stored in an array of size n. We can use StdRandom.uniformDouble(to generate random x and y coordinates for each point, and then leverage the distanceTo() method available in the Point2D API. I employed a nested for loop to compute the closest pair.

Exercise 2. Write an Interval1D client that takes an int value n as command-line argument, reads n intervals (each defined by a pair of double values) from standard input, and prints all pairs that intersect.

Solution. See the com.segarciat.algs4.ch1.sec2.ex02.IntervalIntersection class. It's much the same as in Exercise 1, but instead of using StdRandom.uniformDouble() to generate the coordinates, I use StdIn.readDouble() to read coordinate from standard input. Also, instead of the distanceTo() method from the Point2D API, I leveraged the intersects() method from the Interval1D API.

Exercise 3. Write an Interval2D client that takes command-line arguments n, min, and max and generates n random 2D intervals whose width and height are uniformly distributed between min and max in the unit square. Draw them on StdDraw and print the number of pairs of intervals that intersect and the number of intervals that are contained in one another.

**Solution.** See the com.segarciat.algs4.ch1.sec2.ex03.IntersectingRectangles class.

One important consideration is that since the widths and heights are generated uniformly between  $\min$  and  $\max$ , we must ensure the bottom left corner of each point isn't so large that it would exceed the dimensions of the unit square. That is, given width and height, each of the x and y coordinates of the bottom left vertex of all rectangles must not exceed 1 - width and 1 - height, respectively.

Another important consideration is that, to check if rectangle A contains rectangle B, we must check that the bottom-left and top-right vertices of rectangle B are contained in rectangle A. Since the Interval2D API does not expose methods for obtaining these quantities, it's necessary to save them while doing the computations to necessary to create the rectangles.

**Exercise 4.** What does the following code fragment print?

```
String string1 = "hello";
String string2 = string1;
```

```
string1 = "word";
StdOut.println(string1);
StdOut.println(string2);
```

Solution. When string1 is assigned tostring2, the string2 variable receives a copy of the reference to the current value of string1. When string1 is assigned the String with value "word", the reference in string2 is unchanged. Thus the output is:

```
world
hello
```

Exercise 5. What does the following code fragment print?

```
String s = "Hello World";
s.toUpperCase();
s.substring(6, 11);
StdOut.println(s);
```

Solution. String objects are immutable, so the calls to the toUpperCase() and the substring() methods do not change the object that s references; they return new String objects. In this case, those objects are not stored, so they are immediately available for garbage collection. Thus the output is simply:

```
Hello World
```

Exercise 6. A string s is a circular shift (or *circular rotation*) of a string t if it matches when the characters are circularly shifted by any number of positions; e.g., ACTGACG is a circular shift of TGACGAC, and viceversa. Detecting this condition is important in the study of genomic sequences. Write a program that checks whether two given strings s and t are circular shifts of one another. *Hint*: The solution is a one liner with indexOf(), length(), and string concatenation.

Solution. See the com.segarciat.algs4.ch1.sec2.ex06.CircularShift class. A prerequisite for s and t to be circular shifts of one another is that they have the same length. After establishing this, we can detect the condition by concatenating s with itself to create a new string, and then check whether t is a substring of this new string.

**Exercise 7.** What does the following recursive function return?

```
public static String mystery(String s)
{
   int n = s.length();
   if (n <= 1) return s;
   String a = s.substring(0, n/2);
   String b = s.substring(n/2, n);
   return mystery(b) + mystery(a);
}</pre>
```

Solution. It reverses the string s.

Exercise 8. Suppose a[] and b[] are each integer arrays consisting of millions of integers. What does the following code do? Is it reasonably efficient?

```
int[] t = a; a = b; b = t;
```

**Solution.** It swaps arrays **a** and **b**. It's very efficient because the array values are not copied.

Exercise 9. Instrument BinarySearch (page 47) to use a Counter to count the total number of keys examined during all searches and then print the total after all searches are complete. *Hint*: Create a Counter in main() and pass it as an argument to indexOf().

**Solution.** See the See the com.segarciat.algs4.ch1.sec2.ex09.BinarySearchCounter class.

Exercise 10. Develop a class VisualCounter that allows both increment and decrement operations. Take two arguments n and max in the constructor, where n specifies the maximum number of operations and max specifies the maximum absolute value of the counter. As a side effect, create a plot showing the value of the counter each time its tally changes.

Solution. See the com.segarciat.algs4.ch1.sec2.ex10.VisualCounter class.

Exercise 11. Develop an implementation SmartDate of our Date API that raises an exception if the date is not legal.

Solution. See the com.segarciat.algs4.ch1.sec2.ex11.SmartDate class.

Exercise 12. Add a method dayOfTheWeek() to SmartDate that returns a String value Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, or Sunday, giving the appropriate day of the week for the date. You may assume that the date is in the 21st century.

Solution. See the com.segarciat.algs4.ch1.sec2.ex12.SmartDate class.

## References

[SW11] Robert Sedgewick and Kevin Wayne. *Algorithms*. 4th ed. Addison-Wesley, 2011. ISBN: 9780321573513.