
Milestone #4:

Moving to Experiment Data

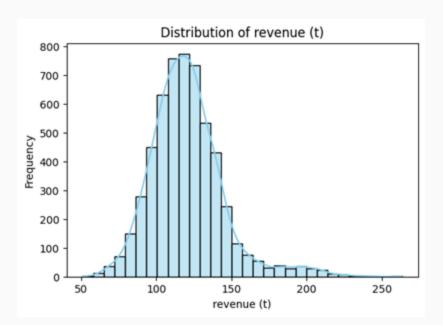


01 + Univariate Exploration

(Distribution of each variable)

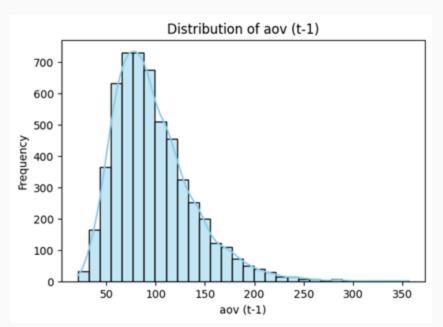


Histogram - revenue (t)



This histogram of distribution of revenue appears to be normally distributed with a slight right skew. This shows that most customers contribute a similar level of revenue while, a few outliers show that a few customers spend more than average.

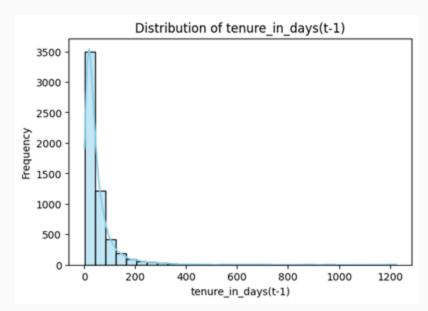




This histogram of distribution of average order value is right-skewed. This means that the majority of costumes spend similar, moderate amounts per order, while a few customers spend a higher number extending the right of the histogram.



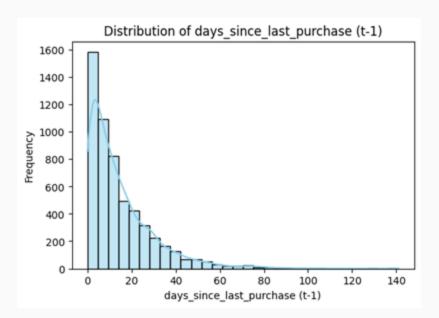
Histogram - tenure in days(t-1)



This histogram of distribution of tenure in days shows a strong right skew showing customers have short tenures so they are new, (less than 100 days), while a few have a longer period (been with the company longer).



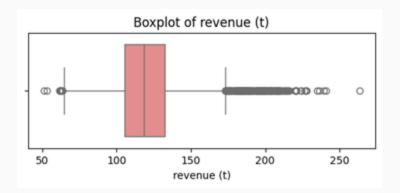
Histogram - days since last purchase (t-1)



This histogram of distribution of days since last purchase is right-skewed, the data points are to the left side of the graph with a tail extended to the right. The graph is showing a large group of active customers who made recent purchases and a few customers who haven't made purchases in a long time on the tail.



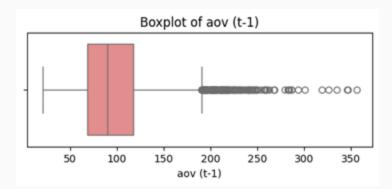
Boxplot - revenue (t)



This distribution of revenue box plot shows the data is right-skewed with a median around 120. The IQR suggests that most revenue values fall between 100 to 135. The outliers are on the low end (\$50-60), and large amount of outliers on the high end 200+. This shows customers behaviors, the regular everyday purchases, and the less frequent but large sales.



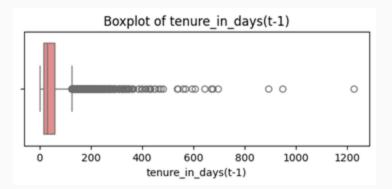
Boxplot - aov (t-1)



This plot shows the data is right skewed, The median is about \$95, the IQR falls between 75-110, meaning 50% of aov falls between that range. There are many outliers on the right \$200+, which represent transaction of aov being higher than the norm. Overall this graph shows an average range of \$75-110, and transactions with a higher average value are transactions of more expensive products.



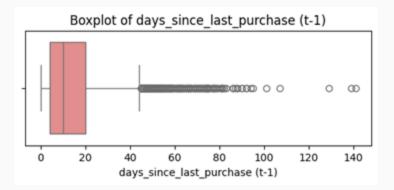
Boxplot - tenure in days (t-1)



This boxplot shows the data is right skewed and the median is low, so 50% of the tenures are shorter than around 50 days while 50% are longer. The IQR shows that 50% of the tenures fall between roughly 25-100 days. There appears to be some outliers going beyond 600 days. Overall this plot shows customers have a short tenure but a small number have long tenure.



Boxplot - days since last purchase (t-1)



This boxplot show days since last purchase. The data is right skewed showing that customers made a recent purchase while others haven't purchased in a while. The median is around 15 days so half the customers made their last purchase within the past 15 days. The IQR spans from 3 to about 35 days so 50% of customers made their purchase around that time. There are many outliers beyond 45 days some beyond 100, which represent customers who haven't purchased in a while.

02 + comparisons +

Control vs. Treatment

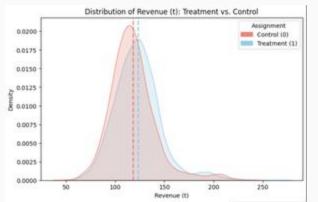
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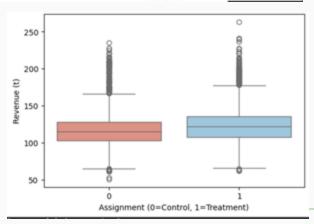
Compare distributions of revenue (t) between groups

		cun_rrcucmono	Mean_Control	SMD	p-value
0	aov (t-1)	97.09	97.86	-0.019	0.4747
1 da	ays_since_last_purchase (t-1)	14.34	14.75	-0.027	0.3145
2	tenure_in_days(t-1)	49.40	49.81	-0.006	0.8119
3	loyalty_membership	0.07	0.06	0.014	0.6060

- **Goal:** To confirm the experiment was fair by ensuring the treatment and control groups were statistically similar *beforehand*.
- Evidence 1: Standardized Mean Difference (SMD)
 - All SMD values are near zero (well below the 0.1 industry standard), indicating excellent balance.
- Evidence 2: p-values
 - All p-values are high, confirming there were no significant pre-existing differences between the groups.
- Conclusion: The randomization was successful. We have a reliable foundation to trust that our results are due to the gift strategy itself. 12

Revenue Distributions (Control vs. Treatment)





Primary Observation: A qualitative comparison of the revenue distributions reveals a separation between the treatment and control groups, although there is considerable overlap.

Evidence from Density Plot:

• The density plot for the treatment group (sky blue) exhibits a slight but observable rightward shift relative to the control group (salmon). The average revenue for the treatment group is higher than the control group.

Evidence from Box Plot:

• This directional difference is quantified in the box plot, which indicates an elevated median revenue for the treatment group.

Preliminary Conclusion:

The exploratory evidence is inconsistent with a null hypothesis
of no effect. Formal statistical testing is required to determine the
significance of this observed difference.



Revenue	(t)	Summary by mean	Group: median	std	count
assignm	ent				
Contro	ol	117.952016	115.5700	23.870081	2773
Treatme	ent	123.053486	121.8105	24.174141	2783

The group summary table shows:

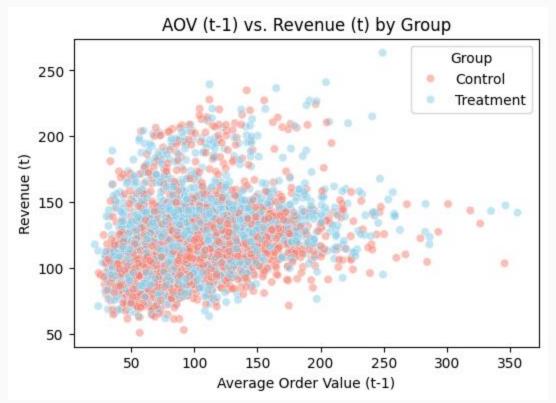
- **Objective:** To quantitatively summarize the directional difference observed in the visual analysis of the revenue distributions.
- Key Metrics: The treatment group exhibits a higher mean revenue (+\$5.10) and a higher median revenue (+\$6.24) compared to the control.
- **Variance:** The standard deviations of the two groups are comparable, suggesting the intervention did not substantially increase revenue volatility.
- **Implication:** These descriptive statistics provide quantitative support for the visual evidence. The next step is to assess the statistical significance of this observed difference.

03 +

Explore relationships

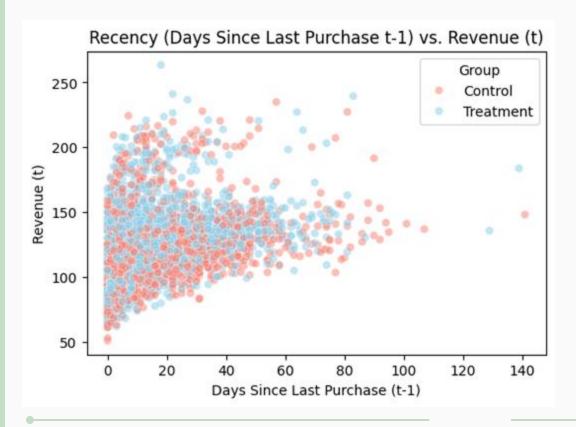
Goal: See correlations & treatment heterogeneity patterns





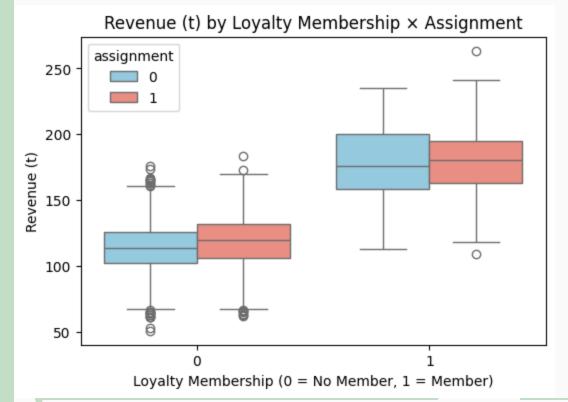
- **Question:** Did the treatment work better on customers who spend more per order?
- Analysis: We plotted each customer's pre-experiment Average Order Value (AOV) against their post-experiment revenue.
- **Finding:** The treatment group (blue) is consistently and slightly higher than the control group (salmon) across **all AOV levels**.
- Conclusion: The modest revenue lift was broad-based and not driven by a specific spending segment like high-value customers.





- Question: Was the treatment more effective on our recent, most active customers?
- Analysis: We plotted the days since a customer's last purchase (Recency) against their postexperiment revenue.
- Finding: The treatment group again shows a consistent, modest lift over the control group, regardless of how recently a customer made a purchase.
- Conclusion: The treatment's small, positive effect is also consistent across different levels of customer engagement.

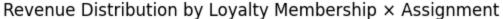


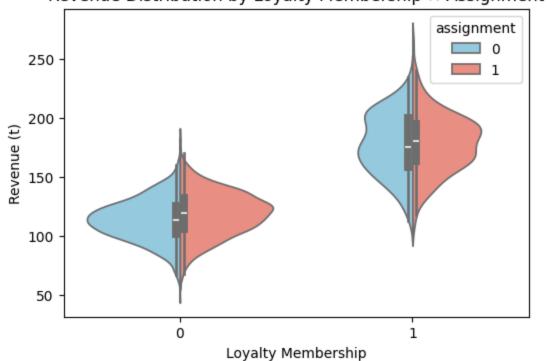


- Loyalty members (1) show much higher median revenue than nonmembers (0) across both groups.
- The treatment group's box is slightly higher within each loyalty category, especially for members, hinting at a modest uplift among loyal customers.
- Interpretation summary: Loyalty membership strongly predicts higher revenue overall. The treatment effect appears somewhat stronger among loyalty members, suggesting possible heterogeneous treatment impact.



Violin Plot - Revenue Distribution by





- The wider, higher violins for loyalty = 1 confirm greater spending variation among members.
- The treatment violin (salmon) for members skews slightly upward relative to control (blue), reinforcing the idea of a small positive effect in that subgroup.
- Non-members show overlapping distributions, implying little or no effect there.
- Interpretation summary:

Treatment shows a slightly higher and broader revenue distribution among loyalty members but minimal change among non-members — indicating treatment heterogeneity by loyalty status.



Overall Takeaway

Across relationships, revenue aligns
 positively with prior AOV and negatively
 with recency. Treatment effects are subtle
 overall but may be somewhat stronger for
 loyal, high-spending customers.

04 + Analyze & Understand

Skews & Outliers

```
Skewness of numeric features:
aov (t-1): 1.26
days_since_last_purchase (t-1): 2.00
tenure_in_days(t-1): 5.06
revenue (t): 1.07
Outlier Summary (IQR method):
                          Feature Num Outliers % Outliers
                                                              Lower Bound
0
                        aov (t-1)
                                             165
                                                    2.969762
                                                                 -3.93625
   days_since_last_purchase (t-1)
                                             277
                                                    4.985601
                                                                -20.00000
              tenure_in_days(t-1)
                                             428 7.703384
                                                                -51.00000
                      revenue (t)
                                             213
                                                    3.833693
                                                                 64.53825
   Upper Bound
     190.53375
                                             The distributions are not symmetric
      44.00000
                                             and around 3 - 8% of rows per
     125.00000
                                             feature have outliers
     172.89825
```



Interpretation Summary:

Feature	Skew	Num Outliers	% Outliers	Notes
aov (t-1)	1.26	165	3%	Moderately right-skewed; few high-spenders drive mean up
days_since_last_purchase	2.00	277	5%	Highly skewed; most customers purchased recently, some very inactive
tenure_in_days	5.06	428	7.7%	Extremely skewed; few long-term customers dominate upper range
revenue (t)	1.07	213	3.8%	Moderately skewed; high-revenue customers influence mean

- The numeric features in the experiment dataset show right-skewed distributions, indicating that most customers cluster at lower values while a few high-value customers form a long tail.
- Specifically, tenure_in_days is extremely skewed (5.06), reflecting a small number of very long-term customers, while days_since_last_purchase is highly skewed (2.00), showing that most customers purchased recently but some had long gaps. aov (t-1) (1.26) and revenue (t) (1.07) are moderately skewed, suggesting a few high spenders drive up average values.
- Outlier analysis using the IQR method shows that outliers are mostly on the high end, including customers with exceptionally high spending, long tenure, or infrequent purchases.
- These points represent real customer behavior and are important for modeling, though they should be monitored as they may influence variance and effect estimates.



Interpretation Notes:

- Right-skewed distributions are common in customer datasets. Outliers mostly reflect high-value or long-tenure customers, not data errors.
- These outliers should generally be kept for modeling but monitored for impact on variance or treatment effect estimates. Also based off the previous diagrams above.

↑ Thank you! ◆

Notebook Link