Homework 1. Fixpoints and grammar filters

[131 home > Homework]

Introduction

You are a reader for Computer Science 181, which asks students to submit grammars that solve various problems. However, many of the submitted grammars are trivially wrong, in several ways. Here is one. Some grammars contain blind-alley rules, that is, grammar rules for which it is impossible to derive a string of terminal symbols. Blind-alley rules do not affect the language or parse trees generated by a grammar, so in some sense they don't make the answers wrong, but they're noise and they make grading harder. You'd like to filter out the noise, and just grade the useful parts of each grammar.

You've heard that OCaml is a good language for writing compilers and whatnot, so you decide to give it a try for this application. While you're at it, you have a background in <u>fixed point</u> and <u>periodic point</u> theory, so you decide to give it a try too.

Definitions

fixed point

(of a function f) A point x such that f x = x. In this description we are using OCaml notation, in which functions always have one argument and parentheses are not needed around arguments.

computed fixed point

periodic point

(of a function f with period p) A point x such that f (f ... (f x)) = x, where there are p occurrences of f in the call. That is, a periodic point is like a fixed point, except the function returns to the point after p iterations instead of 1 iteration. Every point is a periodic point for p=0. A fixed point is a periodic point for p=1.

computed periodic point

(of a function f with respect to a period p and an initial point x) A periodic point of f with period p, computed by calculating x, f x, f (f x), f (f (f x)), etc., stopping when a periodic point with period p is found for f. The computed periodic point need not be equal to x. If no periodic point is ever found by this procedure, the computed periodic point is not defined for f, p, and x.

symbol

A symbol used in a grammar. It can be either a nonterminal symbol or a terminal symbol; each kind of symbol has a value, whose type is arbitrary. A symbol has the following OCaml type:

right hand side

A list of symbols. It corresponds to the right hand side of a single grammar rule. A right hand side can be empty.

rule

A pair, consisting of (1) a nonterminal value (the left hand side of the grammar rule) and (2) a right hand side.

grammar

A pair, consisting of a start symbol and a list of rules. The start symbol is a nonterminal value.

Assignment

You will warm up by modeling sets using OCaml lists. The empty list represents the empty set, and if the list t represents the set T, then the list h::t represents the set {h}UT. Although sets by definition do not contain duplicates, the lists that represent sets can contain duplicates. Another set of warmup exercises will compute fixed and periodic points. Finally, you can write a function that filters blind alleys.

- 1. Write a function subset a b that returns true iff $a \subseteq b$, i.e., if the set represented by the list a is a subset of the set represented by the list b. Every set is a subset of itself. This function should be generic to lists of any type: that is, the type of subset should be a generalization of 'a list -> bool.
- 2. Write a function equal_sets a b that returns true iff the represented sets are equal.
- 3. Write a function set_union a b that returns a list representing a∪b.
- 4. Write a function set_intersection a b that returns a list representing a∩b.
- 5. Write a function set_diff a b that returns a list representing a-b, that is, the set of all members of a that are not also members of b.
- 6. Write a function computed_fixed_point eq f x that returns the computed fixed point for f with respect to x, assuming that eq is the equality predicate for f's domain. A common case is that eq will be (=), that is, the builtin equality predicate of OCaml; but any predicate can be used. If there is no computed fixed point, your implementation can do whatever it wants: for example, it can print a diagnostic, or go into a loop, or send nasty email messages to the user's relatives.
- 7. Write a function computed_periodic_point eq f p x that returns the computed periodic point for f with period p and with respect to x, assuming that eq is the equality predicate for f's domain.
- 8. Write a function while_away s p x that returns the longest list [x; s x; s (s x); ...] such that p e is true for every element e in the list. That is, if p x is false, return []; otherwise if p (s x) is false, return [x]; otherwise if p (s (s x)) is false, return [x; s x]; and so forth. For example, while_away ((+) 3) ((>) 10) 0 returns [0; 3; 6; 9]. Your implementation can assume that p eventually returns false.
- 9. Write a function rle_decode lp that decodes a list of pairs lp in <u>run-length encoding</u> form. The first element of each pair is a nonnegative integer specifying the repetition length; the second element is the value to repeat. For example, rle_decode [2,0; 1,6] should return [0;0;6] and rle_decode [3,"w"; 1,"x"; 0,"y"; 2,"z"] should return ["w"; "w"; "w"; "x"; "z"; "z"].
- 10. OK, now for the real work. Write a function filter_blind_alleys g that returns a copy of the grammar g with all blind-alley rules removed. This function should preserve the order of rules: that is, all rules that are returned should be in the same order as the rules in g.
- 11. Supply at least one test case for each of the above functions in the style shown in the sample test cases below. When testing the function F call the test cases my_F_test0, my_F_test1, etc. For example, for subset your first test case should be called my_subset_test0. Your test cases should exercise all the above functions, even though the sample test cases do not.

Your code should follow these guidelines:

- 1. Your code may use the <u>Pervasives</u> and <u>List</u> modules, but it should use no other modules other than your own code.
- 2. It is OK (and indeed encouraged) for your solutions to be based on one another; for example, it is fine for filter blind alleys to use equal sets and computed fixed point.
- 3. Your code should prefer pattern matching to conditionals when pattern matching is natural.
- 4. Your code should be free of <u>side effects</u> such as loops, assignment, input/output, incr, and decr. Use recursion instead of loops.
- 5. Simplicity is more important than efficiency, but your code should avoid using unnecessary time and space when it is easy to do so. For example, instead of repeating a expression, compute its value once and reuse the computed value.
- 6. The test cases below should work with your program. You are unlikely to get credit for it otherwise.

Submit

Submit two files. The file hwl.ml should implement the abovementioned functions, along with any auxiliary types and functions; in particular, it should define the symbol type as shown above. The file hwltest.ml should contain your test cases. Please do not put your name, student ID, or other personally identifying information in your files.

Sample test cases

See <u>hw1sample.ml</u> for a copy of these tests.

```
let subset_test0 = subset [] [1;2;3]
let subset_test1 = subset [3;1;3] [1;2;3]
let subset_test2 = \underline{not} (subset [1;3;7] [4;1;3])
let equal_sets_test0 = equal_sets [1;3] [3;1;3]
let equal_sets_test1 = not (equal_sets [1;3;4] [3;1;3])
let set_union_test0 = equal_sets (set_union [] [1;2;3]) [1;2;3]
let set_union_test1 = equal_sets (set_union [3;1;3] [1;2;3]) [1;2;3]
let set_union_test2 = equal_sets (set_union [] []) []
let set intersection test0 =
  equal_sets (set_intersection [] [1;2;3]) []
let set_intersection_test1 =
  equal_sets (set_intersection [3;1;3] [1;2;3]) [1;3]
let set intersection test2 =
  equal sets (set intersection [1;2;3;4] [3;1;2;4]) [4;3;2;1]
let set diff test0 = equal sets (set diff [1;3] [1;4;3;1]) []
let set diff test1 = equal sets (set diff [4;3;1;1;3] [1;3]) [4]
let set diff test2 = equal sets (set diff [4;3;1] []) [1;3;4]
let set diff test3 = equal sets (set diff [] [4;3;1]) []
let computed fixed point test0 =
  computed fixed point (=) (fun x \rightarrow x \angle 2) 1000000000 = 0
let computed fixed point test1 =
  computed fixed point (=) (fun x -> x \star. 2.) 1. = infinity
let computed_fixed_point_test2 =
  computed_fixed_point (=) sqrt 10. = 1.
let computed fixed point test3 =
  ((computed_fixed_point (fun x y \rightarrow abs_float (x \rightarrow y) < 1.)
                          (fun x -> x /. 2.)
   = 1.25)
let computed periodic point test0 =
  computed periodic point (=) (fun x \rightarrow x / 2) 0 (-1) = -1
let computed periodic point test1 =
  computed_periodic_point (=) (fun x \rightarrow x *. x -. 1.) 2 0.5 = -1.
(* An example grammar for a small subset of Awk, derived from but not
   identical to the grammar in
   <a href="http://web.cs.ucla.edu/classes/winter06/cs132/hw/hw1.html">httml</a>. *)
type awksub nonterminals =
  | Expr | Lvalue | Incrop | Binop | Num
let awksub rules =
   [Expr, [T"("; N Expr; T")"];
    Expr, [N Num];
```

```
Expr, [N Expr; N Binop; N Expr];
    Expr, [N Lvalue];
    Expr, [N Incrop; N Lvalue];
   Expr, [N Lvalue; N Incrop];
   Lvalue, [T"$"; N Expr];
    Incrop, [T"++"];
    Incrop, [T"--"];
   Binop, [T"+"];
   Binop, [T"-"];
   Num, [T"0"];
   Num, [T"1"];
   Num, [T"2"];
   Num, [T"3"];
   Num, [T"4"];
   Num, [T"5"];
   Num, [T"6"];
   Num, [T"7"];
   Num, [T"8"];
   Num, [T"9"]]
let awksub_grammar = Expr, awksub_rules
let awksub test0 =
 filter_blind_alleys awksub_grammar = awksub_grammar
let awksub test1 =
 filter_blind_alleys (Expr, List.tl awksub_rules) = (Expr, List.tl awksub_rules)
let awksub_test2 =
 filter_blind_alleys (Expr,
      [Expr, [N Num];
      Expr, [N Lvalue];
      Expr, [N Expr; N Lvalue];
      Expr, [N Lvalue; N Expr];
      Expr, [N Expr; N Binop; N Expr];
      Lvalue, [N Lvalue; N Expr];
      Lvalue, [N Expr; N Lvalue];
      Lvalue, [N Incrop; N Lvalue];
      Lvalue, [N Lvalue; N Incrop];
      Incrop, [T"++"]; Incrop, [T"--"];
      Binop, [T"+"]; Binop, [T"-"];
      Num, [T"0"]; Num, [T"1"]; Num, [T"2"]; Num, [T"3"]; Num, [T"4"];
      Num, [T"5"]; Num, [T"6"]; Num, [T"7"]; Num, [T"8"]; Num, [T"9"]])
 = (Expr,
     [Expr, [N Num];
     Expr, [N Expr; N Binop; N Expr];
      Incrop, [T"++"]; Incrop, [T"--"];
     Binop, [T "+"]; Binop, [T "-"];
      Num, [T "0"]; Num, [T "1"]; Num, [T "2"]; Num, [T "3"]; Num, [T "4"];
     Num, [T "5"]; Num, [T "6"]; Num, [T "7"]; Num, [T "8"]; Num, [T "9"]])
let awksub test3 =
 filter blind alleys (Expr, List.tl (List.tl awksub rules))) =
    filter_blind_alleys (Expr, List.tl (List.tl awksub_rules))
type giant nonterminals =
  | Conversation | Sentence | Grunt | Snore | Shout | Quiet
let giant_grammar =
 Conversation,
  [Snore, [T"ZZZ"];
   Quiet, [];
   Grunt, [T"khrgh"];
   Shout, [T"aooogah!"];
   Sentence, [N Quiet];
```

```
Sentence, [N Grunt];
   Sentence, [N Shout];
   Conversation, [N Snore];
   Conversation, [N Sentence; T","; N Conversation]]
let giant_test0 =
  filter_blind_alleys giant_grammar = giant_grammar
let giant test1 =
  filter_blind_alleys (Sentence, List.tl (snd giant_grammar)) =
    (Sentence,
     [Quiet, []; Grunt, [T "khrgh"]; Shout, [T "aooogah!"];
      Sentence, [N Quiet]; Sentence, [N Grunt]; Sentence, [N Shout]])
let giant test2 =
  filter_blind_alleys (Sentence, List.tl (List.tl (snd giant_grammar))) =
    (Sentence,
     [Grunt, [T "khrgh"]; Shout, [T "aooogah!"];
      Sentence, [N Grunt]; Sentence, [N Shout]])
```

Sample use of test cases

When testing on SEASnet, use one of the machines lnxsrv07.seas.ucla.edu and lnxsrv08.seas.ucla.edu. Make sure /usr/local/cs/bin is at the start of your path, so that you get the proper version of OCaml. To do this, append the following lines to your \$HOME/.profile file if you use bash or ksh:

```
export PATH=/usr/local/cs/bin:$PATH

or the following line to your $HOME/.login file if you use tesh or csh:
set path=(/usr/local/cs/bin $path)
```

The command ocaml should output the version number 4.03.0.

If you put the <u>sample test cases</u> into a file hwlsample.ml, you should be able to use it as follows to test your hwl.ml solution on the SEASnet implementation of OCaml. Similarly, the command #use "hwltest.ml";; should run your own test cases on your solution.

```
$ ocaml
        OCaml version 4.03.0
# #use "hw1.ml";;
type ('a, 'b) symbol = N of 'a | T of 'b
# #use "hwlsample.ml";;
val subset test0 : bool = true
val subset_test1 : bool = true
val subset test2 : bool = true
val equal sets test0 : bool = true
val equal sets test1 : bool = true
val set_union_test0 : bool = true
val set union test1 : bool = true
val set union test2 : bool = true
val set_intersection_test0 : bool = true
val set_intersection_test1 : bool = true
val set_intersection_test2 : bool = true
val computed fixed point test0 : bool = true
val computed fixed point test1 : bool = true
val computed fixed point test2 : bool = true
val computed fixed point test3 : bool = true
val computed periodic point test0 : bool = true
```

```
val computed periodic point test1 : bool = true
type awksub nonterminals = Expr | Lvalue | Incrop | Binop | Num
val awksub rules :
  (awksub nonterminals * (awksub nonterminals, string) symbol list) list =
  [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]);
   (Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);
   (Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]);
   (Lvalue, [T "$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);
   (Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]);
   (Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]);
   (Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])]
val awksub grammar:
  awksub nonterminals *
  (awksub_nonterminals * (awksub_nonterminals, string) symbol list) list =
   [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]);
    (Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);
    (Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]);
    (Lvalue, [T "$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);
    (Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]);
    (Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]);
    (Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])])
val awksub test0 : bool = true
val awksub_test1 : bool = true
val awksub_test2 : bool = true
val awksub test3 : bool = true
type giant nonterminals =
    Conversation
    Sentence
    Grunt
    Snore
   Shout
   Quiet
val giant grammar:
  giant nonterminals *
  (giant_nonterminals * (giant_nonterminals, string) symbol list) list =
  (Conversation,
   [(Snore, [T "ZZZ"]); (Quiet, []); (Grunt, [T "khrgh"]);
    (Shout, [T "aooogah!"]); (Sentence, [N Quiet]); (Sentence, [N Grunt]);
    (Sentence, [N Shout]); (Conversation, [N Snore]);
    (Conversation, [N Sentence; T ","; N Conversation])])
val giant test0 : bool = true
val giant_test1 : bool = true
val giant test2 : bool = true
```

© 2006–2011, 2013–2016 <u>Paul Eggert</u>. See <u>copying rules</u>. \$Id: hw1.html,v 1.71 2016/09/22 22:49:49 eggert Exp \$