Stat 201: Statistics I Week 8





Week 8 Hypothesis Testing

Section 8.1 More on Confidence Intervals

Sample size

A confidence interval defines a region of probable values for a population parameter. Often, it is desirable to design an experiment which will estimate a population parameter within a specified accuracy. The sample size needed to achieve a desired margin of error can be calculated.

Calculating sample size

Recall, a confidence interval is defined as,

$$CI(1-\alpha)\% = x \pm ME$$

where the margin of error is calculated by,

$$ME = z_{\alpha/2} \left(\frac{s}{\sqrt{n}} \right)$$

Solving for n (sample size) results in, after some algebra,

$$n = \left(\frac{s \times z_{\alpha/2}}{ME}\right)^2$$

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A sample size calculation requires the following values:

- The critical value $z_{\alpha/2}$ specified by the desired confidence level $(1-\alpha)\%$
- The desired accuracy of the estimate specified by an acceptable margin of error
- The sample standard deviation s. Finding a suitable value for s is often the most difficult part of a sample size calculation.

A reasonable estimate for sample standard deviation must be determined when calculation sample sizes for confidence intervals of means.

Possible sources:

3/24/2019

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- Pilot studies
- Sometimes a sample size calculation is performed using a margin of error defined as a proportion of an unknown stand deviation (i.e. a margin of error of half a standard deviation)

Standard deviations for proportions

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- Proportion estimates may be estimated from previous work or known values in a similar manner as standard deviations for means
- \bullet If no reasonable estimate can be made, a conservative value of $\hat{p}=0.5$ should be used.

Then, the sample size calculation for a confidence interval of proportions in,

$$n = \left(\frac{\sqrt{\hat{p} \times (1 - \hat{p})} \times z_{\alpha/2}}{ME}\right)^2 = \hat{p} \times (1 - \hat{p}) \times \left(\frac{z_{\alpha/2}}{ME}\right)^2$$

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- Previous studies have estimated the mean height of adult males in the U.S. is 69.2 inches with a standard deviation of 5.79.

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• Calculated sample sizes should always be rounded up.

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- If the value of interest **is not** contained within the confidence interval, then there is evidence that the population parameter differs from the value.
- If the value if interest **is** contained within the confidence interval, then there is not evidence the the parameter differs from the value. [Note: this is not the same as saying there is evidence that the parameter is the same as the value.]

Confidence intervals as inference, example

Example

Suppose Metro State conducts a study of height of male students which results in a 95% confidence interval of (63.3, 67.9). What can be said about Metro State students as compared to the general U.S. population?

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Example

Suppose Metro State conducts a study of height of male students which results in a 95% confidence interval of (63.3, 67.9). What can be said about Metro State students as compared to the general U.S. population?

• Since the mean height of U.S. males, 69.2 inches, is not contained in the confidence interval, there is evidence that Metro State students differ from the general U.S. population.

Group work

• For all questions, complete parts (a) and (b).

Section 8.2 Basics of Hypothesis Testing

Statistical inference

Previously, statistics from random samples were used to learn something about populations by estimating population parameters. Knowledge about populations was inferred from the data of the sample.

A similar question can be posed: Is a sample drawn from a population that is the same in an important way to a known population, or is the sample drawn from a population that is significantly different?

Hypothesis tests

An **hypothesis test** is a formal statistical procedure to test claims about population parameters based on samples drawn from populations. Such claims, or **hypotheses**, are often written as simple mathematical statements.

It is important to be clear as to which population the claims or the tests are about,

Example

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 - $\mu > 36$

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Remember, both the null and alternative hypotheses are statements about populations, which will be tested using a sample.

Hypotheses, cont.

Null hypothesis:

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Alternative hypothesis:

- ullet Denoted by H_1 or H_a
- Can be a statement that a parameter is **less than**, **greater than** or **not equal to** some value
- Is usually a statement representing the research question

One-sided vs. two sided tests

If an alternative hypothesis has the form of a parameter being less than or greater than some value, the hypothesis test is called a **one-sided test**.

If an alternative hypothesis has the form of a parameter being not equal to some value, the hypothesis test is called a **two-sided test**.

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$$\bullet \ \ H_0: \mu = 36 \qquad H_a: \mu \neq 36 \qquad {\sf Two\text{-sided}}$$

Starting with null and alternative hypotheses derived from the research question and a random sample, all hypothesis tests have the same basic structure.

• A test statistic is calculated which indicates the location of the sample within the sampling distribution, assuming the null hypothesis is true.

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- If the calculated probability is not below the pre-specified threshold, the null
 hypothesis is not rejected and it is said that there is not evidence to support the
 alternative hypothesis.

P-values

In a hypothesis test, the **p-value** is the probability of getting a sample with the test statistic or one more extreme, assuming the null hypothesis is true.

• Not to be confused with the population proportion p or the probability function P(A), though a p-value does represent a probability.



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Calculating a p-value is that same as calculating probabilities in sampling distributions already learned.

- Identify sampling distribution:
 - z distribution for proportions
 - t distribution for means
- Calculate **test statistic**: z-score or t-score
- Find probability of test statistic or more extreme values in sampling distribution
- That probability is the p-value

Luckily, all these steps can be accomplished easily with technology.

Once the p-value is calculated, it is compared against a pre-specified threshold. This threshold is called the **significance level** of the test.

ullet Denoted by lpha

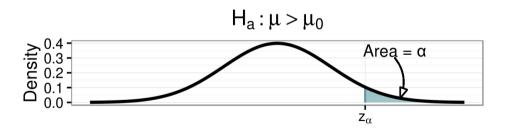
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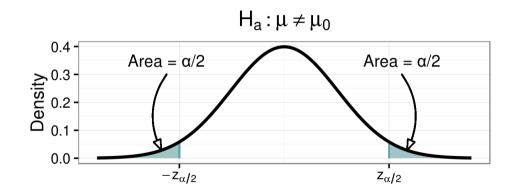
Significance level for one-sided test

In a one-sided test, the entire rejection region is located at one end of the distribution or the other.



Significance level for two-sided test

In a two-sided test, the rejection region is split between the lower and upper extremes of the distribution.



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 - The null hypothesis is never "accepted".
- State the conclusion in terms of the research question
 - "There is evidence for..."
 - "There is not evidence for..."

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A study is conducted to test the claim that male Metro State students are shorter than the general population height of 69.2 inches. The test at a $\alpha=0.05$ level of significance produces a test statistic t=-1.859 and a p-value of 0.0358. State the conclusion of the test

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- $H_0: \mu = 69.2, \quad H_a: \mu < 69.2$
- $p=0.0358<\alpha=0.05$. Reject the null hypothesis. There is evidence to conclude that male Metro students are shorter than the general population.

Example

A patient diagnosed with a particular rare disease has an expected survival time of 36 months. A clinical trial is conducted to see if a new experimental treatment will change the survival time. The hypothesis test at $\alpha=0.01$ level of significance produces a p-value of 0.098. State the conclusion of the test.

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• $H_0: \mu = 36$ $H_a: \mu \neq 36$

Example

A patient diagnosed with a particular rare disease has an expected survival time of 36 months. A clinical trial is conducted to see if a new experimental treatment will change the survival time. The hypothesis test at $\alpha=0.01$ level of significance produces a p-value of 0.098. State the conclusion of the test.

- $H_0: \mu = 36$ $H_a: \mu \neq 36$
- $p=0.098>\alpha=0.01$. Do not reject the null hypothesis. There is not evidence to conclude that the experimental treatment changes survival time.

Steps for hypothesis test

- Identify null and alternative hypotheses from research question
- Oetermine appropriate sampling distribution
- Calculate test statistic
- Calculate p-value
- **1** Compare p-value to significance level α and report decision
- State conclusion in terms of original research question

Note: Steps 3 and 4 are often accomplished with technology

Making a decision with p-value

A **small** p-value ($p < \alpha$) means a low probability of getting the observed sample if the null hypothesis is true. Thus, the null hypothesis is rejected.

A large p-value $(p > \alpha)$ then means that the sample is not unlikely under the null hypothesis. Thus, the null hypothesis is not rejected.

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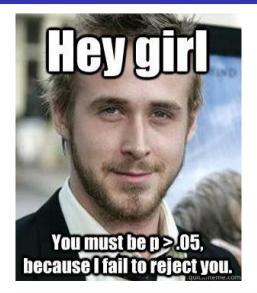
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To remember...

If p is low, the null must go.

Or if this helps...



Critical value method

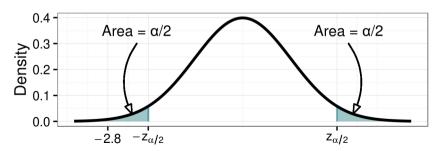
The hypothesis test procedure discussed thus far is known as the p-value method. An alternative method, known as the **critical value** method, does not use p-values, but rather compares test statistics directly to appropriate critical values. If the test statistic is more extreme than the critical value, the null hypothesis is rejected.

Critical value method, example

Example

A two-sided test with $\alpha=0.05$ level of significance is conducted and results in a test statistic z=-2.8.

- Recall, critical value $z_{\alpha/2} = \pm 1.96$.
- Since -2.8 is more extreme than -1.96 (-2.8 < -1.96), reject the null hypothesis.



In an hypothesis test, either the null hypothesis is true or it is not, and either the null hypothesis is rejected or it is not. Thus, there are four possible outcomes.

	Reject H_0	Do not reject H_0
H_0 is true	Type I error (α)	Correct decision
H_0 is not true	Correct decision	Type II error (β)

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- There is a trade-off between α and β . Smaller α result in larger β (and lower power) and vice versa.

It can be useful to use a legal system analogy to help understand how hypothesis tests work. Consider a criminal trial:

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- A jury can make two kinds of mistakes: they can convict an innocent defendant or they can fail to convict a guilty defendant.

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- A conclusion can be in error one of two ways: a type I error (convict an innocent defendant) or a type II error (fail to convict a guilty defendant).

Group work

• For all questions, complete part (c).