

Correlated Migration: The Hidden Patterns of City Location Choices

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Abstract

The extent to which households migrate across cities in response to negative economic shocks is a crucial channel through which such shocks are mitigated. And yet, almost all existing models assume that all cities are equally substitutable for all households. In contrast, this paper introduces a model with correlated location choices, where household heterogeneity in occupation-specific skills interacts with the productivity of cities in those occupations, leading to endogenous city substitutability as a function of similarity in city specific economic structures. Using publicly available data, I estimate this model and demonstrate that migration decisions are significantly correlated. These findings have important implications for the design and effectiveness of place-based policies and deepen our understanding of household migration responses to local economic shocks.

Keywords: Quantitative Spatial Models; Urban Economics; Comparative Advantage; Migration; Agglomeration

1 Introduction

Why do people live where they do? What makes a city more attractive to a household? These questions are far from trivial; they lie at the heart of understanding geographic distributions of economic activity, with significant implications for welfare outcomes. Everyone must choose where to live, and the importance of this choice cannot be overstated - for many, it is one of the most crucial decisions they will make in their lives. Given the importance of this choice, understanding the factors that drive it is crucial for policymakers, urban planners, and individuals alike.

The literature on city location choices has presented many models and theories explaining why people choose to live where they do. One of the most well-known theories is that of agglomeration, which posits that people are attracted to cities because of the benefits that come with living in a dense urban area. These benefits include access to jobs, amenities, and social networks. However, while these benefits are often considered universal to all households, regardless of their occupation-specific skills, the advantages of each city clearly vary for different households. For instance, an auto worker from Detroit will not view New York as an equivalent substitute for a city to live in compared to a finance worker from New York. This paper aims to address the question: what drives city location choices? More specifically, what drives migration across cities?

Forces of spatial inequality and agglomeration have been well documented in the literature. Behrens et al. (2014) and Behrens and Robert-Nicoud (2015) show that large, dense cities have higher levels of productivity, resulting in higher wages. This raises the question: do people earn more in cities because they are more productive, or because productive individuals self-select into cities? The answer is likely both. Lagakos and Waugh (2013) show that households will self-select into occupations where they are most productive, meaning that the occupations concentrated in cities tend to be the most productive, attracting households who specialize in them. This also implies that while households who choose to live in smaller cities earn less, they do so because the occupation they specialize in is comparatively less productive. This form of self-selection has also been documented within cities by Diamond (2016) and Diamond and Gaubert (2022), who show that highly educated households tend to live in areas of high productivity and wages. A disparity between these groups is not necessarily detrimental, however, as Davis and Dingel (2019) show that agglomeration forces can lead to knowledge spillovers, resulting in higher productivity for all households.

The urban literature has made successful attempts at creating models to explain city location choices. Redding and Rossi-Hansberg (2017) has developed a class of quantitative spatial models (QSM), adapted

from the wider class of trade models proposed by Eaton and Kortum (2002). These models treat productivity as random draws from Fréchet distributions, allowing for non-zero production of goods, which helps account for small cities. Redding (2016) applies this model to an urban setting by loading city heterogeneity onto amenities, meaning that each city captures a different share of households based on the amenities they provide. Because the model originated in the trade literature, robust techniques have been developed to estimate its parameters. Migration elasticity has been estimated by Albert and Monras (2022), and the elasticity of labor market adjustments to trade shocks has been estimated by Kim and Vogel (2021). As shown in Autor et al. (2013), it is also possible to use Bartik (1991) shift-share instruments to estimate parameters, a convenient feature that only requires one to either take a stance on exogenous shares (Goldsmith-Pinkham et al. (2020)) or exogenous shifts (Borusyak et al. (2021)). Another convenient feature of this model is that it makes it possible to capture the effects of trade shocks at the group level, similar to the work of Galle et al. (2022). This is important as trade shocks have heterogeneous effects on industries with differing exposure to trade shocks, leading to sharp movements in wages but slow adjustments in labor market outcomes (Artuç et al. (2010)).

The development of a correlational structure in Eaton and Kortum (2002)-style models by Lind and Ramondo (2023) has made it possible to capture correlated choices in import varieties in trade. This paper adapts this structure to the urban setting, bringing correlated choices to quantitative spatial models. My contribution to the literature is threefold. First, I break the independence of irrelevant alternatives assumption (IIA) by allowing for correlated draws of productivity across cities, providing another dimension of heterogeneity and extending the literature that has thus far explained city heterogeneity through differences in amenities. Second, I back out the additional dimension of heterogeneity in the form of occupations from amenities to better explain location choices in the theoretical model. Third, I contribute to our empirical understanding of city location choices by taking this model to data and investigating what happens when there are shocks in occupations or cities.

In the second section, I will adapt the Eaton and Kortum (2002) structure to accommodate three dimensions of absolute advantage. First, there is a city-specific advantage that makes all occupations more productive in that city, primarily due to its size and population, resulting in better amenities, more jobs, and a larger social network. Second, there is an occupation-specific advantage that is universal across all cities; some jobs are simply more productive than others, and cities specializing in these jobs will be observed as having higher overall choice shares of households. Third, there is a city-occupation-specific advantage, where a city may have specific policies that make it more attractive for a particular occupation, such as tax breaks for mechanics in Chicago. It is crucial to distinguish between occupations and sectors: sectors employ

broad categories of jobs (e.g., manufacturing, services, agriculture), while occupations are specific jobs (e.g., mechanic, clerk). Cities can specialize in occupations by focusing on sectors that intensively use those occupations.

I will then adapt the model of Lind and Ramondo (2023) to the urban setting, integrating a cross-nested CES (CNCES) structure into Redding and Rossi-Hansberg (2017)’s QSM framework. More explicitly, I will model occupations as nests, unlike their original paper where nests are implied. This approach allows me to capture correlated draws of productivity within a given occupation across cities, leading to unbalanced substitution patterns. In other words, households in specific occupations will have productivities that are similar across cities. This structure will also allow me to derive elasticities for the three dimensions of absolute advantage.

In section three, I will present my estimation strategy, explicitly laying out my estimation equations. Here, I exploit variation over time to recover a correlation parameter, which, as I will explain later on, can be interpreted as a within-occupation migration parameter. I will also use previously estimated parameters of across-occupation migration elasticity from Redding (2016) to recover my city, occupation, and city-occupation-specific shifters.

Section four is where I take my model to data and estimate the parameters. Using data from the American Community Survey at the metropolitan area and occupational levels, I will begin by presenting stylized facts about cities and their compositions, comparing similarities among top cities. I will then discuss my estimation results, focusing on the correlation parameter and my city, occupation, and city-occupation-specific shifters. This fully calibrated model will then be used to conduct counterfactual analyses and simulate the effects of shocks at both the city and occupation levels. This exercise will demonstrate the comparative statics presented in section two, illustrating the difference between this model with correlated choices and the standard model with CES preferences.

2 Model

Consider an economy consisting of N cities and K occupations. Each household has a productivity Z_{ck} working in city c and occupation k . Households maximize their utility by simultaneously choosing a city and occupation that maximizes their productivity. I assume that every city has a common price index that remains fixed over time. I also assume that wages are constant, providing a partial equilibrium model of correlated migration across cities.

The productivity of a household within a given city-occupation is drawn from a Fréchet distribution. In Redding (2016), the Fréchet distribution is used to model productivity draws in a trade setting and has two main components. The shape parameter θ which determines the dispersion of draws across the distribution and reflects the heterogeneity of cities¹. And the scale parameter T_{ck} is a level shifter that determines the absolute advantage of a city-occupation pair, reflecting its attractiveness. The standard approach in the literature is to assume independent draws of productivity across cities, which would yield the following joint distribution:

$$\begin{aligned} P[Z_1 < z_1, \dots, Z_N < z_N] &= \prod_c^N P[Z_c < z_c] \\ &= \exp \left\{ - \sum_c^N T_{ck} Z_c^{-\theta} \right\} \end{aligned}$$

This result implies that the choice shares of households for a given city is equal to the probability of households choosing that city. So far, I have stuck with the base EK specification with the only modification being the mapping of productivity onto wages rather than prices which allows me to obtain city choice shares. The unique contribution of this model in the literature will lie in the next step where I will now abandon the independence assumption and introduce a structure that allows for correlated draws across cities.

$$P[Z_1 < z_1, \dots, Z_N < z_N] = \exp \left\{ - \left(\sum_c^N (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}} \right)^{1-\rho} \right\}$$

Notice with this structure that the shape of the distribution is no longer purely determined by θ but also by the correlation parameter ρ . Where the distribution of productivity within a given occupation decreases as ρ increases. Meaning that within a given occupation, the higher correlation will result in cities being more similar with each other in terms of productivity. When $\rho = 0$, the distribution reduces down to the original joint distribution with the shape being purely determined by θ and where draws are independent. As $\rho \rightarrow 1$, the draws become perfectly correlated and the distribution of productivities become identical across cities. Note that while the distribution remains the same, the realized productivity may be different.

¹In the trade literature (Eaton and Kortum (2002)), θ is the trade elasticity and determines the extent to which countries are not perfect substitutes. In the case of Redding (2016) and my model, θ is the migration elasticity and determines the extent to which cities are not perfect substitutes.

2.1 Cross Nested CES

$$P[Z_1(\nu) < z, \dots, Z_N(\nu) < z] = \exp \left\{ - \sum_k^K \left[\sum_c^N (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k} \right\} \quad (1)$$

I assume that productivity is distributed as a max-stable multivariate Fréchet distribution with T_{ck} being the scale parameter for city c and occupation k . The shape parameter $\theta > 0$ determines the dispersion of draws across the distribution, and ρ_k is the occupation-specific correlation parameter. Following Lind and Ramondo (2023), I adopt a cross-nested CES structure with a correlational structure within independent occupational nests. This results in distributions not purely determined by θ but also by the correlation parameter. The correlation parameter determines the degree of correlation between productivity draws across cities. It's important to note that correlation only occurs within a given occupation and not across occupations for a given household. This means that within a given city, households make independent draws across occupations.

In order to identify the three dimensions of absolute advantage, I will be separating out the scale parameter into three components where $T_{ck} = T_c T_k t_{ck}$. T_c is the city specific scale parameter which captures the attractiveness of a city, shifting the distribution of all productivity draws within that city upwards. T_k is the occupation specific scale parameter which is common across all cities, this captures the effect that any occupation has across all cities. And t_{ck} is the city-occupation specific scale parameter which captures the effect of a city on a specific occupation. This will give me the final dimension of absolute advantage.

A household's schedule of productivity is characterized by a vector of draws from different Fréchet distributions for each city occupation pair. The realized productivity a household has in city c is the occupation k that maximizes the productivity has in the city. Unlike sequential games where households might pick a city before picking an occupation, I assume that households pick both simultaneously. A way to contextualize this is to think of households as already having an ideal occupation in mind when picking a city, hence $Z_c = \max_k \{Z_{ck}\}$. This productivity is then scaled by the price index of a city to reflect how high prices reduces the purchasing power of the household within that city, hence making it less attractive.

2.2 Equilibrium

The city choice shares π_c is derived by solving the maximization problem where households are choosing cities and occupations that maximize their Productivity. In order to obtain this share, I will use the solution developed by Lind and Ramondo (2023) for Fréchet distributions with nested CES preferences². This is given by:

$$\pi_c = \frac{Z_c^{-\theta} G_c(Z_1^{-\theta}, \dots, Z_N^{-\theta})}{G(Z_1^{-\theta}, \dots, Z_N^{-\theta})}$$

Where $G(Z_1^{-\theta}, \dots, Z_N^{-\theta})$ is a correlation function that allows me to capture the correlated draws of productivity within a given occupation across cities and $G_c(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \partial G(Z_1^{-\theta}, \dots, Z_N^{-\theta}) / \partial Z_c^{-\theta}$. In other words, the correlation function determines how similar the draws of productivity are within a given occupation across cities. The higher the correlation, the more likely it is for households to choose cities that have the same occupations across draws³. The expression the correlation function is given by:

$$G(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \sum_k^K T_k \left[\sum_c^N (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k} \quad (2)$$

I now define $Z_c^{-\theta} = (\gamma)^{-\theta} (T_c)^{\theta}$ and $\gamma = \Gamma(\frac{\theta+1-\rho_k}{\theta})^{\frac{1}{1-\rho_k}}$. Given my definition of $Z_c^{-\theta}$, T_c will be absorbed within $Z_c^{-\theta}$, giving me the correlation function $G(Z_1^{-\theta}, \dots, Z_N^{-\theta})$ as defined in expression 2. In order to evaluate the expression, I make the simplifying assumption that the correlation parameter is the same across all occupations $\rho_k = \rho$.

$$\lambda_k = \sum_c^N (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}}$$

I introduce the above expression which measures the appeal of occupation k . Given that the expression does

²This solution can be applied to all models within the class developed by Eaton and Kortum (2002), but the solution itself was developed by Lind and Ramondo (2023).

³Recall our discussion about $\rho \rightarrow 1$. If you draw a productivity that's 99th percentile within a given occupation for a city, then you will be within the 99th percentile in that occupation across all cities, but the actual value of the productivity may differ.

not include T_k , it does not capture the attractiveness of occupation k . Instead the expression captures the extent to which a given occupation k exhibits city-specific productivities which are correlated with aggregate city-level attractiveness. The following definition will be useful in simplifying the expression for city shares.

$$\pi_{ck} = \frac{Z_c^{-\theta} G_c^k(Z_1^{-\theta}, \dots, Z_N^{-\theta})}{G^k(Z_1^{-\theta}, \dots, Z_N^{-\theta})}$$

To obtain occupation specific choice shares, I can evaluate the derivative for city shares at the occupation level. More specifically, rather than $G(Z_1^{-\theta}, \dots, Z_N^{-\theta})$, I will be evaluating $G^k(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \sum_c^N (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}}$. This will give me the following:

$$\pi_{ck} = \frac{(t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}}}{\lambda_k} \quad (3)$$

Moving forward, it will be convenient for me to provide the following definitions. First, I define ϕ_{ck} as the absolute advantage of city c in occupation k . This can be interpreted as an occupation's within city choice shares. As such ϕ_{ck} will be between 0 and 1. I define this formally as:

$$\phi_{ck} \equiv \frac{t_{ck}^{\frac{1}{1-\rho_k}} T_k \lambda_k^{-\rho}}{\sum_k t_{ck}^{\frac{1}{1-\rho_k}} T_k \lambda_k^{-\rho}} \quad (4)$$

Second, I define an occupation specific choice share which takes into account both the size of each occupation, as measured by productivity T_k , and the extent to which individual city-occupation productivities are correlated with overall city attractiveness. This is defined as the following expression:

$$\omega_k \equiv \frac{T_k \lambda_k^{1-\rho}}{\sum_k T_k \lambda_k^{1-\rho}} \quad (5)$$

From the perspective of discrete choice demand models, ω_k can be interpreted as the "market share" of

occupation k . This is because it captures the extent to which the productivity of occupation k is correlated with overall city attractiveness. The expression is normalized by the sum of all ω_k to ensure that the sum of all market shares is equal to 1.

$$\pi_c \equiv \frac{\omega_k}{\phi_{ck}} \pi_{ck} \quad (6)$$

The expression above tells me the extent to which a given occupation k is concentrated in city c above and beyond the predicted concentration, given the size of the city π_c is equivalent to the within-city choice share in occupation k divided by the aggregate choice share of that occupation.

$$\pi_c = \sum_k^K \frac{(Z_c^{-\theta} t_{ck})^{\frac{1}{1-\rho}}}{\lambda_k} \frac{T_k \lambda_k^{1-\rho}}{\sum_k^K T_k \lambda_k^{1-\rho}}$$

$$\pi_c = \sum_k^K \pi_{ck} \omega_k \quad (7)$$

By using my definitions, I arrive at the above expression for city shares, which is now the sum of all occupation specific shares weighted by the market share of each occupation.

2.3 City-Occupation Elasticities

The main purpose of this model is to highlight the dynamics of city location choices, which leads to unbalanced substitution patterns. First, I aim to demonstrate how, when there is a shock in a city that specializes in a particular occupation, such as trades, households will choose to relocate to other cities that are also specialized in that occupation. Second, I want to show how a shock in a specific occupation will affect cities based on their relative concentration or specialization in that occupation, similar to what Autor et al. (2013) demonstrate with their shift-share instrument. In this section, I will highlight some comparative statics using simple closed-form expressions. Here, we will see why this model leads to correlated migration elasticities across cities and occupations.

I now turn to the city-occupation derivatives: city c 's own technology elasticity and cross technology elasticity with respect to another city c' . This derivative will be approximated by assuming that each city is small, and therefore $\partial \ln \lambda_k / \partial \ln t_{ck} \approx 0$. That is, the aggregate "price index" associated with location choice in occupation k is not affected by a marginal change in the productivity of a given city-occupation pair. I then obtain the following for the own technology shock:

$$\frac{\partial \ln \pi_{ck}}{\partial \ln t_{ck}} \approx \phi_{ck} \left(\frac{1}{1 - \rho} \right) \quad (8)$$

This elasticity is positive and increasing in a city's absolute advantage in occupation k . The intuition is that a city that is more attractive for occupation k will see a larger increase in the choice share of that occupation in response to a marginal increase in the productivity of that occupation. The more specialized the city is in that occupation, the larger the effect of a productivity shock in that occupation. As $\rho \rightarrow 1$, the elasticity approaches infinity, as within any given occupation, if they become more correlated, cities within that given occupation become perfect substitutes for each other.

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = -\pi_{c'} \phi_{ck} \left[1 + \left(\frac{\rho}{1 - \rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \quad (9)$$

Turning my attention to the cross city technology elasticity, we see that the first term captures the CES element of consumer choice. As the city c' increases in size and becomes increasingly competitive in that occupation, any shocks to this city-occupation pair will have an increasingly negative effects on all other cities. How much the other cities will be affected is captured by the second term which captures the unbalanced substitution patterns. If a city is relatively concentrated in occupation k , then the affects of a shock in that given occupation will be felt more severely, this is shown by the ratio π_{ck}/π_c . Notice also that if $\rho = 0$, this elasticity simplified to the standard CES elasticity. As $\rho \rightarrow 1$, the elasticity approaches infinity and the correlated choices start to dominate.

2.3.1 Aggregate Elasticities

I now consider the elasticity of city shares with respect to aggregate city technology shocks T_c and aggregate occupation shocks T_k . Beginning with the former, if I assume again that each city is small and that $\partial \ln \lambda_k / \partial \ln T_c \approx 0$, I get the following for a city's own technology shock:

$$\frac{\partial \ln \pi_c}{\partial \ln T_c} \approx \frac{1}{1 - \rho}$$

This is simply the summation of city-occupation elasticities which was derived in expression 8. And given that by definition $\sum_k^K \phi_{ck} = 1$, I get the following derivations:

$$\begin{aligned} \frac{\partial \ln \pi_c}{\partial \ln T_c} &= \sum_k \frac{\partial \ln \pi_c}{\partial \ln t_{ck}} \\ &= \sum_k \phi_{ck} \left(\frac{1}{1 - \rho} \right) \\ &= \left(\frac{1}{1 - \rho} \right) \sum_k \phi_{ck} = \frac{1}{1 - \rho} \end{aligned}$$

The result tells me that if $\rho = 0$ and there's no correlation between occupations, then the elasticity is simply 1. I get a similar story when deriving the cross city technology elasticity. Using the same assumption, I arrive at the result:

$$\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} = -\pi_{c'} \left[\sum_k \phi_{c'k} \left[1 + \left(\frac{\rho}{1 - \rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \right] \quad (10)$$

Similarly, this is simply the sum over all city-occupation elasticities derived in expression 9. This is shown in the following derivation:

$$\begin{aligned}
\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} &= \sum_k \frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} \\
&= \sum_k \left[-\pi_{c'} \phi_{ck} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \right] \\
&= -\pi_{c'} \left[\sum_k \phi_{c'k} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \right]
\end{aligned}$$

The interpretation of this elasticity is the same as expression 9. The first term captures the CES element of consumer choice and the second term captures the unbalanced substitution patterns, with ρ governing the strength of this unbalanced substitution. Now I simply sum over all occupations to get the aggregate elasticities.

Lastly, I derive the elasticity of city shares with respect to aggregate occupation shocks T_k . This is fairly straightforward as well can simply evaluate the following:

$$\begin{aligned}
\frac{\partial \ln \pi_c}{\partial \ln T_k} &= \left(\frac{\partial \phi_{ck}}{\partial T_k} \right) \left(\frac{T_k}{\phi_{ck}} \right) - \left(\frac{\partial \omega_k}{\partial T_k} \right) \left(\frac{T_k}{\omega_k} \right) \\
&= \phi_{ck} - \omega_k
\end{aligned}$$

By using the identity in expression 6, I can rewrite the elasticity as the following:

$$\frac{\partial \ln \pi_c}{\partial \ln T_k} = \omega_k \left[\frac{\pi_{ck}}{\pi_c} - 1 \right] \tag{11}$$

You should first notice that the second term in brackets can be either positive or negative depending on the city's relative concentration in that occupation. Assuming that there is a positive shock to occupation k , if the city is relatively concentrated in that occupation and $\pi_{ck}/\pi_c > 1$, then this city will have a positive elasticity. If the city is relatively less concentrated in that occupation and $\pi_{ck}/\pi_c < 1$, then this city's elasticity is negative. As certain occupations start to become more productive, cities that are less concentrated in that occupation will become less attractive and face a negative shock as households start to move to cities that are more concentrated in that occupation. This second term is scaled by the market share of that occupation, ω_k , which is simply the market share of that occupation across all cities.

3 Estimation Strategy

This model not only produces simple and clean closed-form solutions but also allows for empirical estimation to address the central question of the paper: does migration occur primarily within occupations or across occupations? A significant strength of this model is that it does not require specialized data for parameter estimation; publicly available census data is sufficient for this purpose. In this section, I will outline my estimation strategy and detail the main estimation equations for the model.

3.1 Within-Occupation Migration

Notice that for me to estimate my shifters, I have to first recover my ρ parameter. To do so, I exploit a variation in city-occupation shares over time. Consider the following expression at the city-occupation-year level. From expression 3, I can get the following⁴:

$$\ln \pi_{ck} = \frac{1}{1-\rho} \ln t_{ckt} - \frac{1}{1-\rho} \ln Z_{ct}^{-\theta} - \ln \lambda_{kt}$$

Now I assume the following relationship productivity and wages at the city-occupation level: $t_{ckt} = w_{ckt} \eta_{ckt}$. Where w_{ckt} are wages paid and η_{ckt} is productivity. This will give me the following model:

$$\ln \pi_{ckt} = \left(\frac{1}{1-\rho} \right) \ln w_{ckt} + \delta_{ct} + \delta_{kt} + \eta_{ckt}$$

With some abuse of notation, I have defined $\eta_{ckt} = \ln \eta_{ckt}$. I can estimate this equation by regressing wages on city occupation shares and using city and occupation fixed effects at the city-occupation level for every year with δ_{ct} being city fixed effects and δ_{kt} being occupation fixed effects. Given that $\hat{\rho} \in (0, 1)$, I will end up with the restriction $\hat{\beta} \in [1, +\infty)$. With this regression, I am testing whether migration decisions are primarily within occupations rather than across occupations. If the correlation parameter is close to 1, then migration decisions are purely within occupations. Notice that as $\hat{\rho}$ increases, $\hat{\beta}$ increases. From this perspective, I can interpret ρ as governing within-occupation migration and θ as governing across-occupation

⁴This estimation can also be achieved by using ϕ_{ck}

migration.

One concern with the initial specification is the endogeneity of wages with the error term, more explicitly $cov[w_{ckt}, \eta_{ckt}] \neq 0$. In order to instrument for the change in wages, I will use a shift share instrument in which I make use of sectors. I will use the share of occupation k in sector s with shifts in productivity in sector s over time as an instrument for the change in wages. A_{st} will be the total factor productivity of sector s in year t . The intuition being: if certain sectors grow faster than others, ie become more productive, then city-occupation pairs which are originally concentrated in those sectors will see larger wage gains.

$$w_{ckt}^{IV} = \sum_s^S \gamma_{ks} \kappa_{cs} A_{st}$$

where κ_{cs} is the share of occupation k in sector s in city c . This will give me the following first stage regression:

$$\ln w_{ckt}^{IV} = \beta^{IV} \ln w_{ckt}^{IV} + \delta_{ct} + \delta_{kt}^{IV} + \eta_{ckt}^{IV}$$

I will then use the predicted values of $\ln w_{ckt}^{IV}$ as my instrument in the second stage regression.

$$\ln \pi_{ckt} = \left(\frac{1}{1 - \rho} \right) \ln w_{ckt}^{IV} + \delta_{ct} + \delta_{kt} + \eta_{ckt}$$

3.2 City Shifters

Given that we've identified ρ , I can now proceed to estimate my city scale parameter T_c . I start with occupation market shares ω_k in expression 5. By taking relative shares, I get the following:

$$\frac{\omega_{kt}}{\omega_{k't}} = \frac{T_{kt} \lambda_{kt}^{1-\rho}}{T_{k't} \lambda_{k't}^{1-\rho}}$$

Subject to normalization to some base occupation year, I can estimate $T_{kt}\lambda_{kt}^{1-\rho}\forall(k,t)$. I can then use this to recover the denominator in ω_k and get $\sum_k^K T_{kt}\lambda_{kt}^{1-\rho}\forall t$. Now consider the city-occupation shares from expression 3 taken in logs and transformed into a form with fixed effects:

$$\begin{aligned}\ln \pi_{ckt} &= \frac{1}{1-\rho} \ln t_{ckt} - \frac{1}{1-\rho} \ln Z_{ct}^{-\theta} - \ln \lambda_{kt} \\ &= \hat{\epsilon}_{ckt} + \hat{\delta}_{ct} + \hat{\delta}_{kt} \\ \hat{\lambda}_{kt} &= \exp\left(-\hat{\delta}_{kt}\right) \\ \hat{t}_{ckt} &= \exp\left((1-\rho)\hat{\epsilon}_{ckt}\right)\end{aligned}$$

I can then use the estimated $\hat{\lambda}_{kt}$ to recover my occupation specific scale parameters:

$$\hat{T}_{kt} = \frac{\sum_k^K \widehat{T_{kt}\lambda_{kt}^{1-\rho}}}{\hat{\lambda}_{kt}^{1-\rho}}$$

In order to recover my city specific scale parameter, I will have to assume a parameter θ which can be obtained from the literature. Explicitly, Redding (2016) assumes $\theta = 3$ which is the elasticity of trade taken from Artuç et al. (2010). This is reasonable, given our discussion in the beginning of the paper since the elasticity of trade is also explicitly modeled as θ in the wider class of models developed by Eaton and Kortum (2002) and also determines the imperfect substitutability of choices. With that, we can recall the definition of $Z_c^{-\theta} = (\gamma)^{-\theta}(T_c)^\theta$. Using this with my estimates of $\hat{\delta}_{ct}$, we get:

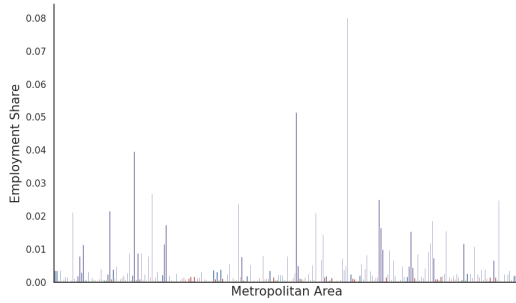
$$\hat{T}_{ct} = \gamma \exp\left(-\frac{1-\rho}{\theta}\hat{\delta}_{ct}\right)$$

4 Empirical Results

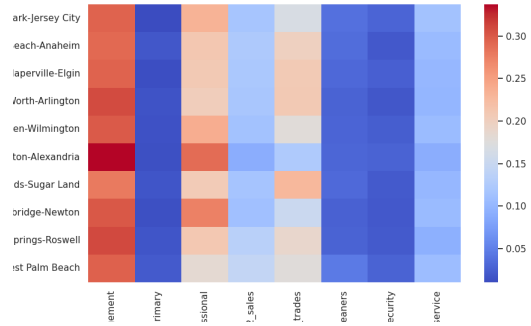
4.1 Data

I will be using data from the American Community Survey (ACS) (Ruggles et al. (2024)) which is a survey conducted by the US Census Bureau. The ACS is a survey that collects data on the metropolitan area and occupational level. I will be using data from 2010 to 2019. The ACS provides data on the household level, detailing wages, metropolitan area, occupation and sector of employment based on NAICS codes. This will be used to construct my share data π_c , π_{ck} , ω_k , ϕ_{ck} and ϕ_{cs} as well as obtain wage data w_{ckt} . I will also be using data from the Bureau of Labour Statistics (Bureau of Labor Statistics, U.S. Department of Labor (2024)) to obtain total factor productivity data at the sector level A_{st} .

Figure 1: Summary Statistics of Metropolitan Statistical Areas (MSA) in 2019



(a) Employment Share by MSA in 2019



(b) Composition of Top 10 MSAs in 2019

Note: I will be referring to MSAs as cities throughout the paper. MSAs in Figure 1a are arranged in alphabetical order on the x axis.

From the data in Figure 1a, I see that a few metropolitan areas own a disproportionate share of employment which illustrates the size effects of cities to attract employment and households. Intuitively, I should expect these cities to be very different from each other in terms of their specialization, otherwise I would expect the largest city with a particular composition to dominate in the share of households. When zooming into the compositions of the top 10 cities however, I see a different story. In Figure 1b, I see that the top 10 cities are very similar with each other in terms of their specialization. With all cities specializing in occupations like management and professional services. While there is some heterogeneity in the composition of cities, the specialization of cities is not as pronounced as I would expect. This indicates to me that the occupations will play a large role in determining the attractiveness of a city.

4.2 Results

To recover my ρ parameter, I run a two stage least squares regression with a shift share instrument. I find that this regression yields a high F-Statistic and a significantly higher estimate for $\hat{\beta}$ compared to ols as seen in Table 1. This ultimately results in a fairly high estimate of $\hat{\rho} = 0.64$. The result means that draws across cities within any given occupation id highly correlated and indicates to me that people are very likely to migrate within occupations. This is consistent with the idea that people are more likely to move to cities where they can find jobs in their occupation.

Table 1: Estimates Of The Effect Of Wages On City Shares With City And Occupation Fixed Effects

	<i>Dependent variable: City Shares</i>	
	OLS	IV
	(1)	(2)
Wage	0.291*** (0.023)	2.777*** (0.041)
R^2	0.956	
F Statistic		145.8***

*Note: This is the results of the regression using the estimation equation discussed in section 3.1. All city and occupation fixed effects are omitted for brevity. Standard errors are clustered on city-occupation pairs and are in parenthesis. * $p < 0.1$; ** $p < 0.05$; *** $p < 0.01$*

In 2019, I find that occupation shifters are generally lower compared to city shifters⁵. However, since cities are scaled by an additional factor of theta, the resulting effect from occupation shifters remains higher than city shifters. For occupation shifters, it's unsurprising that professional and management services have the highest values, given the proportion of households employed in these occupations. Conversely, primary sector occupations have the lowest shifters. Coupled with the fact that these occupations are generally performed in cities with low shifters themselves, this results in cities specializing in primary occupations having low shares of households. It's important to note, however, that while a city-occupation pair may be generally unattractive to most households, those who specialize in these occupations will be very willing to move to cities with occupations matching their abilities.

Most dense metropolitan areas tend to specialize in occupations with high shifters, explaining the large pattern of rural-urban migration to these cities in the past. However, now that most cities have developed similar occupational compositions, I see large cities competing with each other for household shares, which

⁵Refer to appendix 8.2 for more details

is why no particular city is universally most attractive to all households. While large cities tend to have similar overall compositions, they still manage to distinguish themselves by having distinct compositions in other occupations. For example, although New York may be concentrated in management and professional services, it has a higher concentration in sales compared to Los Angeles. This suggests that these cities are large because of their dominant occupations, but they don't compete purely based on scale with other cities.

Unsurprisingly, cities with the highest city shifters are dense metropolitan areas such as New York and Los Angeles, reflecting the large populations they attract. Notable in my estimates is the variance in shifter values between cities, with some shifters being up to three times larger than others, indicating significant heterogeneity in city attractiveness. This makes sense as large cities tend to offer more and better amenities as well as better access to jobs, making them more attractive to households. I also find that city shifters tend to be fairly stable over time, with changes generally below 10% over the 10-year period. Given the time required for cities to build infrastructure and other amenities, in addition to needing to differentiate themselves from other cities, this stability is not surprising.

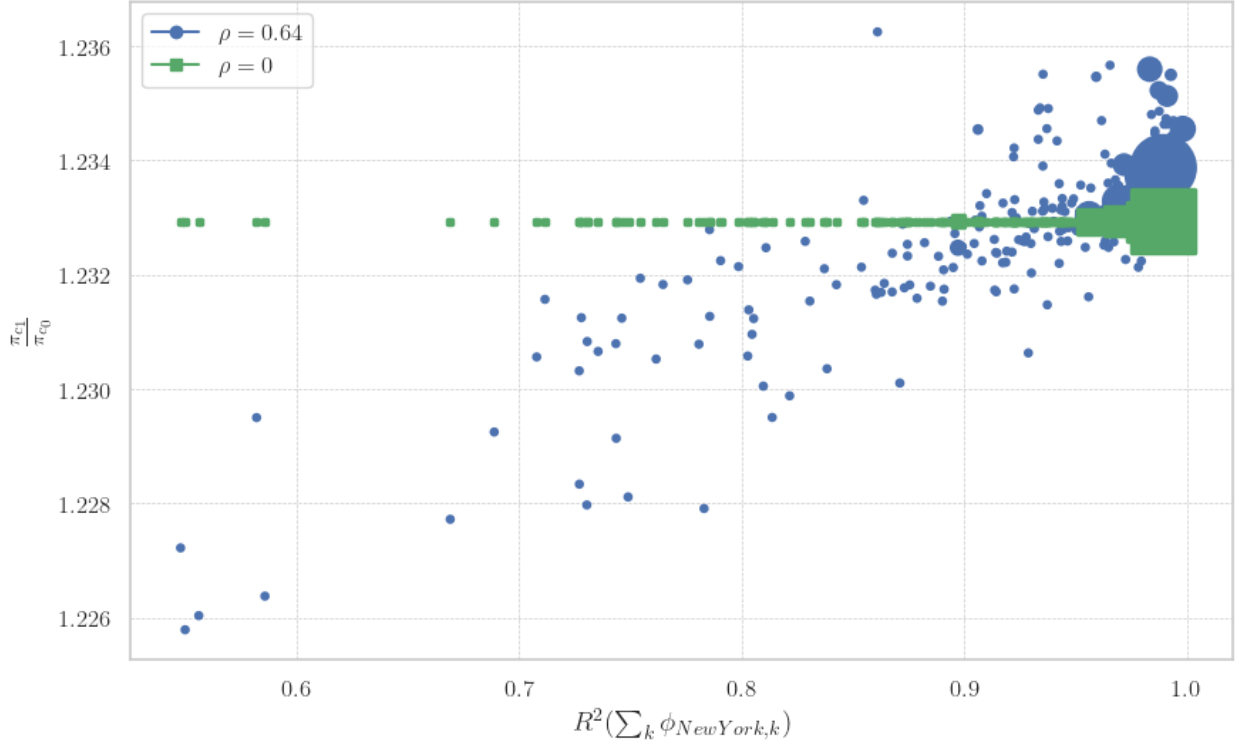
5 Quantitative Exercises

Using my parameter and shifter estimates, I can now perform two counterfactual exercises. First, I will simulate a city-specific shock to observe migration patterns across cities, focusing on the unbalanced substitution patterns that favor similar cities. Second, I will examine the migration patterns resulting from a shock to a particular occupation. This effectively simulates the effects of a trade shock that impacts some occupations more than others, such as the China shock (Autor et al. (2013)). These exercises will provide insights into how different types of economic shocks affect urban migration and occupation choices. In order to perform these exercises, I will assume a parameter θ of 3 which is an estimate used by Redding (2016) that is obtained from the literature. This will give me my across occupation elasticity.

5.1 City Specific Shock

My results from the previous section suggest that while I may observe some migration to large cities purely due to their size, I should expect to see more migration to cities with similar occupational makeups. To test this, I induce a negative shock of 5% to all occupations in New York, a city primarily focused on management and professional services occupations. The results are shown in Figure 2.

Figure 2: Relative Change in City Shares Following New York Shock ($\rho = 0$ vs $\rho = 0.64$)



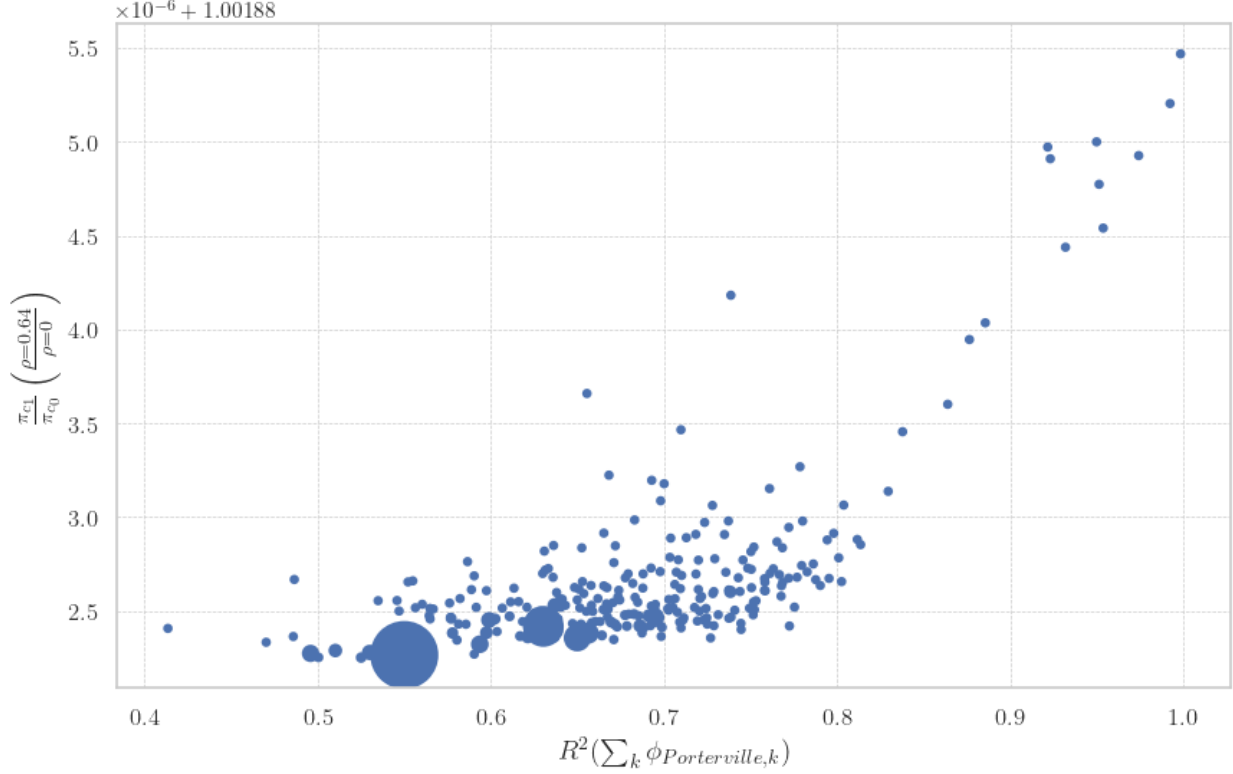
Note: The x axis represents the correlation of city compositions of other cities relative to New York. The size of each plot is relative to the size of each city before the negative shock of 5% to New York. π_{c0} is the city share before the shock, and π_{c1} is the city share after the shock. $\phi_{c,k}$ is the share of occupation k in city c . New York is excluded from the plot.

Analysis of these results reveals that cities benefiting most from this shock have occupational compositions highly correlated with New York. This finding is consistent with our previous observations that households are more likely to move to cities with similar occupational compositions. However, city size also plays a significant role in determining migration patterns. At the top end of the correlation spectrum, large cities such as Los Angeles and Chicago benefit the most from the New York shock. This suggests that while households looking to relocate prefer cities similar to New York, the determining factor among top cities becomes city size, which in our model correlates perfectly with the benefits each city provides.

Interestingly, when I turn off within-occupation migration by setting $\rho = 0$, the distribution reduces to a standard CES model, as discussed in section 2.1. In this case, households are much more evenly redistributed across cities. With all occupations equally attractive to all households, all cities become perfect substitutes for each other⁶.

⁶Expression 10 tells me that the elasticity of each city is governed by ρ . When $\rho = 0$, $\sum_k \phi_{c',k} = 1$, all cities will share the same elasticity of $\pi_{c'}$.

Figure 3: Relative Change in City Shares Following Porterville Shock ($\rho = 0$ vs $\rho = 0.64$)



Note: The x axis represents the correlation of city compositions of other cities relative to Porterville. The size of each plot is relative to the size of each city before the negative shock of 5% to Porterville. π_{c_0} is the city share before the shock, and π_{c_1} is the city share after the shock. $\phi_{c,k}$ is the share of occupation k in city c . The y axis is the ratio between $\frac{\pi_{c_1}}{\pi_{c_0}}$ when $\rho = 0.64$ and when $\rho = 0$. This ratio was basically flat when $\rho = 0$. The ratio was chosen for the y axis to illustrate the difference in the relative change in city shares when $\rho = 0$ and $\rho = 0.64$. Porterville is excluded from the plot. Note that the scale for the y axis is very small, significantly smaller than the shock to New York.

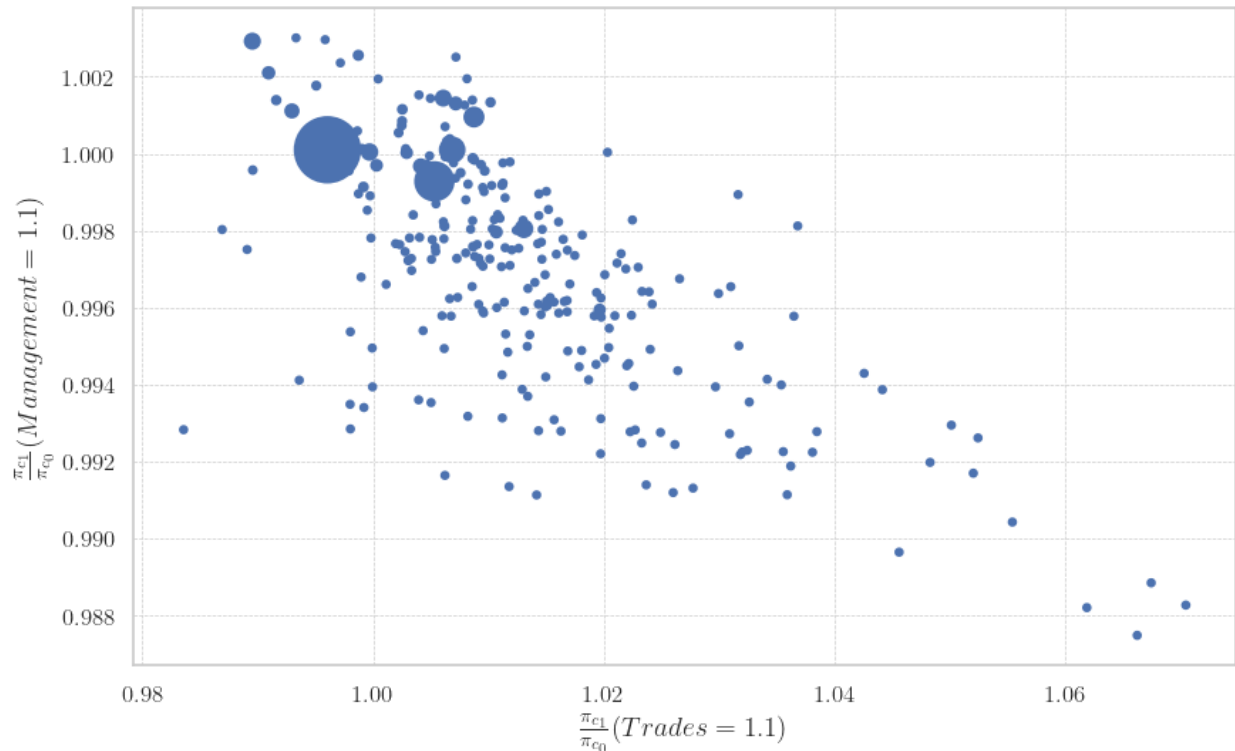
To further illustrate the importance of within-occupation migration, I induce a negative shock of 5% to all occupations in Porterville, a city with a relatively low household shares and one which specializes in trade occupations. The results are shown in Figure 3. I find that the shock to Porterville has a much smaller effect on city shares compared to the shock to New York, which is expected given Porterville's significantly smaller size. However, the relative change in city shares still remains, with the correlation of occupational composition, or how similar the cities are, being the deciding factor for household migration. In this case, I observe that even large cities such as New York benefit less than smaller cities which have occupations more similar to Porterville. While not explicitly illustrated in the figure, I also find that when setting $\rho = 0$, the relative change in city shares is almost identical across all cities. In fact, the differences were so minimal that I encountered limitations in precision when calculating the relative change in city shares for $\rho = 0$.

My findings show that migration patterns are mainly determined by within occupation migration. Households

are willing to relocate, but primarily to cities offering opportunities in their field. Within the set of cities meeting this criteria, city size becomes the deciding factor. This contrasts with the standard QSM model proposed by Redding (2016), which would predict that households simply move to the city with the highest amenity value.

5.2 Occupation Specific Shock

Figure 4: Relative Change in City Shares Following A Shock in Management and Trade Occupations



Note: π_{c0} is the share of households in city c before the positive shock of 10% to both Management and Primary occupations, and π_{c1} is the share of households in city c after the shock. The size of each plot represents the size of each city before the shock. Both the x and y axis do not start from 1, some cities experience a decrease in the shares of households and some experience an increase. There are also some cities that experience an increase in shares with both shocks.

What happens when there's a shock to particular occupations? We've established that households move to cities with similar occupational profiles when there's a negative shock to specific cities. But how do they respond when a shock affects all cities within a particular occupation? To explore this, we induce a positive shock of 10% to management and trade occupations across all cities.

Examining the relative change in shares during a shock to management occupations, as shown on the y -axis

of Figure 4, we observe that it’s mainly the large cities specializing in these occupations that benefit from the positive shock. Conversely, smaller cities that are less concentrated in these occupations tend to lose out. This aligns with our model’s predictions, which state that the effect of a shock on a city is determined by that city’s relative concentration in the affected occupation. When we plot this change against the relative shares following a positive shock to trade occupations, an even clearer picture emerges. Small cities that specialize in trades benefit from positive shocks to this occupation and lose out when there’s a positive shock to management occupations. The opposite is true for large cities that specialize in management occupations. These results highlight the importance of a city’s occupational composition in determining its resilience to occupation-specific shocks. They also underscore the potential for divergent outcomes across cities in response to broader economic shifts that affect particular occupations differently.

6 Discussion

Given the empirical and counterfactual results, I believe there are a couple of important policy implications to consider. Place-based policies that aim to make a city overall more productive in all occupations will generally be ineffective in attracting migration. This is because households tend to pick cities based on their occupations rather than the city itself. A more effective place-based policy should target either occupations that the city already specializes in, or occupations that have a high productivity shifter. Importantly, to increase a city’s relative competitiveness, policymakers should focus on occupations that make it less similar to other cities in order to decrease direct competition.

Policies aimed at responding to trade shocks should be focused on transitioning households to other occupations. Unlike city shocks where households can simply move to other cities for better opportunities, trade shocks will result in households being persistently unemployed due to the lack of opportunities in their given occupation specialization. To tackle this form of unemployment, policy makers need to facilitate the transition of these households to other occupations. This can be done through retraining programs or by providing incentives for firms to hire these workers. Such measures will not only help households find jobs, but will also help cities that are highly specialized in these affected occupations to attract more households. By adopting these targeted approaches, policymakers can more effectively address the challenges posed by both localized economic changes and broader trade shocks, ultimately fostering more resilient urban economies and labor markets.

7 Conclusion

In this paper, I have developed a model of city and occupation choice that enables me to recover city and occupation-specific shifters and substitution parameters. My findings demonstrate that occupations play a more significant role in migration decisions compared to cities themselves, with households more likely to relocate to cities with similar occupational compositions. I have also shown that within-occupation migration is more prevalent than across-occupation migration, consistent with the notion that people are more inclined to move to cities where they can find jobs in their current occupation. In the future, I hope to extend this model to include a housing market and unemployment which will allow up to explain housing prices in relatively low productivity cities as well as persistent unemployment in certain cities.

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8 Appendix

8.1 Derivations

City Choice Shares π_c : As discussed in Lind and Ramondo (2023), the choice shares can be expressed as:

$$\pi_c = \frac{Z_c^{-\theta} G_c}{G()}$$

I define $G()$ as the following, given the definition of T_{ck} and λ_k provided in the main text:

$$G(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \sum_k \left[\sum_c^N (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k} = \sum_k T_k \lambda_k^{1-\rho}$$

$G_c()$ is simply the derivative of $G()$ with respect to $Z_c^{-\theta}$.

$$\begin{aligned} \frac{\partial G()}{\partial Z_c^{-\theta}} &= \sum_k \frac{\partial}{\partial Z_c^{-\theta}} \left[\sum_c^N (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}} \right]^{1-\rho} \\ &= \sum_k \frac{\partial}{\partial Z_c^{-\theta}} \left[T_k^{\frac{1}{1-\rho}} \sum_c^N (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}} \right]^{1-\rho} \\ &= \sum_k T_k \left[(1-\rho) \lambda_k^{-\rho} \frac{\partial \lambda_k}{\partial Z_c^{-\theta}} \right] \\ &= \sum_k T_k \left[(1-\rho) \lambda_k^{-\rho} \left(\frac{1}{1-\rho} \right) t_{ck}^{\frac{1}{1-\rho}} (Z_c^{-\theta})^{\frac{\rho}{1-\rho}} \right] \\ &= (Z_c^{-\theta})^{\frac{\rho}{1-\rho}} \sum_k T_k t_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \end{aligned}$$

Putting these three terms together, I derive the choice shares:

$$\begin{aligned} \pi_c &= \frac{Z_c^{-\theta} G_c}{G()} \\ &= (Z_c^{-\theta})^{\frac{1}{1-\rho}} \left[\frac{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\sum_k T_k \lambda_k^{1-\rho}} \right] \end{aligned}$$

Own Occupation-Specific Elasticity: I wish to evaluate $\partial \ln \pi_c / \partial \ln t_{ck}$, under the assumption that $\partial \ln \lambda_k / \partial \ln t_{ck} = 0$. Notice this assumption yields the following:

$$\frac{\partial \ln \pi_c}{\partial \ln t_{ck}} \approx \frac{\partial \ln \pi_{ck}}{\partial \ln t_{ck}} - \frac{\partial \ln \phi_{ck}}{\partial \ln t_{ck}}$$

given the definitions of π_{ck} and ϕ_{ck} provided in the text.

Notice that this only leaves one term to evaluate if I take the logarithm of π_c and the derivative of this logarithm with respect to $\ln t_{ck}$:

$$\begin{aligned} \frac{\partial \ln \pi_c}{\partial \ln t_{ck}} &\approx \frac{\partial \ln [\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}]}{\partial \ln t_{ck}} \\ &= \left(\frac{\partial [\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}]}{\partial t_{ck}} \right) \left(\frac{t_{ck}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\ &= \left(\frac{1}{1-\rho} \right) \left(\frac{t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{t_{ck}} \right) \left(\frac{t_{ck}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\ &= \left(\frac{1}{1-\rho} \right) \left[\frac{t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right] \\ &= \frac{\phi_{ck}}{1-\rho} \end{aligned}$$

Cross-City Occupation-Specific Elasticity: I wish to evaluate $\partial \ln \pi_c / \partial \ln t_{c'k}$. Notice that this elasticity can be expressed as the following two terms:

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = t_{ck}^{\frac{1}{1-\rho}} T_k \left(\frac{\partial \lambda_k^{-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{ck}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) - T_k \left(\frac{\partial \lambda_k^{1-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{c'k}}{\sum_k T_k \lambda_k^{1-\rho}} \right)$$

It will be useful to first define the derivative of λ_k with respect to myvariable of interest, $t_{c'k}$:

$$\frac{\partial \lambda_k}{\partial t_{c'k}} = \left(\frac{1}{1-\rho} \right) \left(\frac{1}{t_{c'k}} \right) [t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}$$

I can now use chain rule in order to evaluate my elasticity of interest. The first term becomes the following:

$$\begin{aligned}
t_{ck}^{\frac{1}{1-\rho}} T_k \left(\frac{\partial \lambda_k^{-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{c'k}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) &= t_{ck}^{\frac{1}{1-\rho}} T_k (-\rho) (\lambda_k^{-\rho-1}) \left(\frac{1}{1-\rho} \right) \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\
&= - \left(\frac{\rho}{1-\rho} \right) \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\lambda_k} \right) \left(\frac{t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\
&= - \left(\frac{\rho}{1-\rho} \right) \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\lambda_k} \right) \phi_{ck} \\
&= - \left(\frac{\rho}{1-\rho} \right) \pi_{c'k} \phi_{ck}
\end{aligned}$$

The second term can be derived in the following way:

$$\begin{aligned}
-T_k \left(\frac{\partial \lambda_k^{1-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{c'k}}{\sum_k T_k \lambda_k^{1-\rho}} \right) &= -T_k (\lambda_k^{-\rho}) [t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}} \left(\frac{1}{\sum_k T_k \lambda_k^{1-\rho}} \right) \\
&= - \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\lambda_k} \right) \left(\frac{T_k \lambda_k^{1-\rho}}{\sum_k T_k \lambda_k^{1-\rho}} \right) \\
&= -\pi_{c'k} \omega_k
\end{aligned}$$

Putting these together, I derive the cross-city occupation-specific elasticity as the following:

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = -\pi_{c'k} \left[\omega_k + \left(\frac{\rho}{1-\rho} \right) \phi_{ck} \right]$$

Notice that this is equivalent to the following, given the identity linking π_c , π_{ck} , ϕ_{ck} , and ω_k .

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = -\pi_{c'k} \phi_{ck} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \quad (12)$$

Cross-City Aggregate Elasticity: I wish to evaluate $\partial \ln \pi_c / \partial \ln T_{c'}$. Notice that:

$$\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} = \left(\frac{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\partial T_{c'}} \right) \left(\frac{T_{c'}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) - \left(\frac{\partial \sum_k T_k \lambda_k^{1-\rho}}{\partial T_{c'}} \right) \left(\frac{T_{c'}}{\sum_k T_k \lambda_k^{1-\rho}} \right)$$

Notice also that:

$$\frac{\partial \lambda_k}{\partial T_{c'}} = \left(\frac{1}{1-\rho} \right) \left(\frac{[t_{ck}(Z_c^{-\theta})]^{\frac{1}{1-\rho}}}{T_{c'}} \right)$$

I can therefore solve for this cross-derivative as the following:

$$\begin{aligned} \frac{\partial \ln \pi_c}{\partial \ln T_{c'}} &= \sum_k \left[- \left(\frac{\rho}{1-\rho} \right) \phi_{ck} \pi_{c'k} \right] + \sum_k \left[- \omega_k \pi_{c'k} \right] \\ &= - \sum_k \pi_{c'k} \left[\omega_k + \left(\frac{\rho}{1-\rho} \right) \phi_{ck} \right] \end{aligned}$$

8.2 Regression Tables

8.2.1 First Stage Shift Share Regression

<i>Dependent variable: wage</i>	
	(1)
sim_wage	0.523*** (0.037)
Observations	19280
R^2	0.881
Adjusted R^2	0.863
Residual Std. Error	0.198 (df=16799)
F Statistic	3696120.683*** (df=2480; 16799)
<i>Note:</i> *p<0.1; **p<0.05; ***p<0.01	

8.2.2 City and Occupation Shifter Estimations

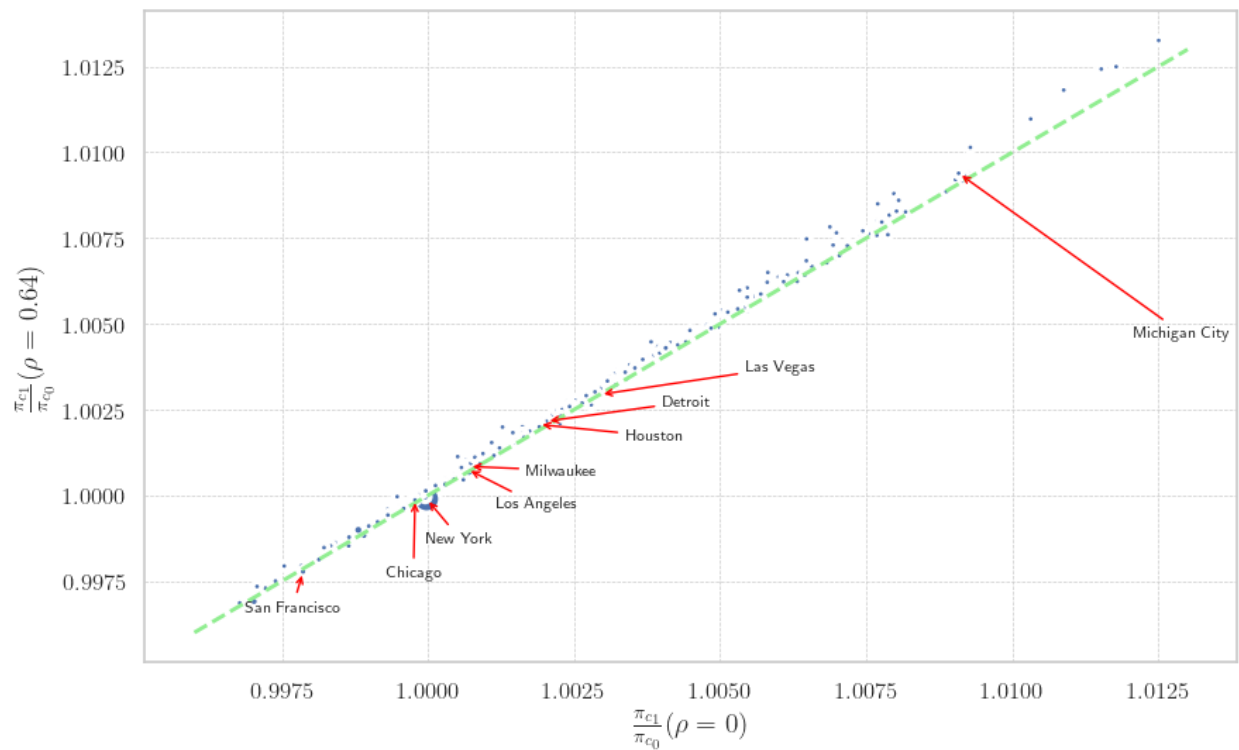
Table 2: Estimations for T_c and T_k for 2019

(A) Occupation Shifters		(B) Top City Shifters	
Occupation	Occupation Shifter	City	City Shifter
Management	0.849566	New York-Newark-Jersey City	3.029541
Professional	0.743607	Los Angeles-Long Beach-Anaheim	2.645708
Trades	0.610380	Chicago-Naperville-Elgin	2.333439
Service	0.344887	Dallas-Fort Worth-Arlington	2.158189
Sales	0.318461	Houston-The Woodlands-Sugar Land	2.093633
Cleaners	0.090246	Philadelphia-Camden-Wilmington	2.028458
Primary	0.066206	Washington-Arlington-Alexandria	2.007037
Security	0.066183	Atlanta-Sandy Springs-Roswell	2.001475

Note: Occupation and city shifters are not directly comparable. Recall that occupations are scaled only by ρ while occupations are scaled by ρ and θ . Comparisons should only be relative and be made within each table.

8.3 Figures

Figure 5: Relative Change in City Shares Following A Shock in Management ($\rho = 0$ vs $\rho = 0.64$)



Note: π_{c0} is the share of households in city c before the negative shock of 5% to Management occupations, and π_{c1} is the share of households in city c after the shock. The size of each plot represents the size of each city before the shock. Both the x and y axis do not start from 1, some cities experience a decrease in the shares of households and some experience an increase.