

City Location Choice and Household Productivity

Tan Sein Jone

1 Introduction

Cities capture a disproportionate amount of household location choices in the world. In 2018, 55% of the world's population lived in urban areas, and this is expected to increase to 68% by 2050. This is because of the benefits cities provide, such as access to jobs, amenities, and social networks. These benefits are often thought of as universal to all households, regardless of their occupation specific skills. However, the benefits of every city is clearly not the same for every household. An auto worker from Detroit will not view New York as an equivalent substitute for a city to live in as a finance worker from New York. Given the billions of dollars spent on place based policies, it is important for us to separate out this dimension of comparative advantage, where a city is able to provide higher levels of productivity for households working in specific occupations.

A city's comparative advantage exists in three dimensions. First, there is a city specific advantage which makes all occupations more productive in that city. This is due to the city's size, more specifically it's population which results in better amenities, more jobs, and a larger social network. Second, there is an occupation specific advantage which is universal across all cities. Some jobs are simply more productive than others and cities that specialize in that job will be observed as having a higher overall choice shares of households. Think cities that specialize in highly attractive occupations such as professional services. Finally, there is a city-occupation specific advantage. A city with a comparative advantage in this dimension may have specific policies that make it more attractive for a specific occupation such as tax breaks for mechanics in Chicago. One crucial distinction we need to make is between occupations and sectors. Sectors are broad categories of jobs such as manufacturing, services, and agriculture. Occupations are specific jobs such as mechanic and clerk. Cities can specialize in occupations by specializing in sectors that most intensely use that occupation.

In this paper, we propose a model of city location choices based on a class of models in the quantitative trade literature first proposed by Eaton and Kortum (2002). These models treat productivity as random draws from Fréchet distributions, allowing for a non zero production of goods which will help us to account for small cities. Redding (2016) applies this model to an urban setting by loading city heterogeneity onto

amenities, capturing the first dimension of comparative advantage. Both these models however rely on the independence assumption which treats that goods and cities are perfect substitutes for each other. Lind and Ramondo (2023) break this assumption by introducing a nested CES utility structure which allows for correlated draws of productivity within nests across countries. We will apply this structure to the urban setting by treating occupations as independent nests. This will allow us to capture substitution patterns where cities that have a similar occupational structure will be treated as better substitutes for each other. By doing this, we are able to capture the second and third dimensions of comparative advantage.

We start in the first section by adapting the model of Lind and Ramondo (2023) to the urban setting. Unlike their original paper where the nests are implied, we will explicitly model the nests as occupations. A few implications will result from this specification. First, we will be able to observe both overall city shares and city shares specific to each occupation. As well as city occupation compositions which can be used as a measure of similarity between cities. Second, using this data, we will derive elasticities for all three dimensions of comparative advantage, that being the city specific, occupation specific and city-occupation specific elasticities. While the last elasticity will serve as a sanity check for the direction of substitution. City and occupation elasticities will be used to verify our claim of unbalanced substitution patterns that favor similar cities. In other words, shocks to cities of a certain occupational composition will have larger effects of cities with similar compositions due to correlations in productivity draws.

In the second section, we will use data from the American Community Survey which has on the metropolitan area and occupational level to present some stylized facts about cities. We will then be presenting our estimation equations that will be used to recover our parameters. Once the model is calibrated, we will use it to run counterfactuals and simulate the effects of a policy at both the city and occupation level. This is where it is possible for us to evaluate the effectiveness of place based policies and also where we will make statements about how these policies should be designed to maximize their effectiveness.

2 Model

$$Y_{ck} = Z_{ck}$$

Consider a closed economy consisting of N cities and K occupations. Each city c employs households in occupation k to produce output Y_{ck} . We assume no trade costs between cities and that the price of the

good produced is freely traded and priced under perfect competition. The price index of city c is given by Φ_c and the wage of a household living in city c working in occupation k is given by $w_{ck} = \Phi_c Z_{ck}$ where Z_{ck} is the productivity of the household. We assume that when a household chooses to work in a particular occupation, they will be randomly allocated to a sector within a given city. A household has symmetric CES preferences over cities and occupations and will choose a city-occupation pair that maximizes their utility. We will assume that households are perfectly mobile across cities and that there are no fixed costs to moving. The productivity of a household within a given city-occupation is drawn from a Fréchet distribution. In Eaton and Kortum (2002), the Fréchet distribution is used to model productivity draws in a trade setting and has two main components. The shape parameter θ which determines the dispersion of draws across the distribution and reflects the heterogeneity of cities. θ will also determine the gains from city choices, ie how much households will gain from having more choices of cities to live in, which is analogous to gains from trade. The scale parameter T_{ck} is a level shifter that determines the absolute advantage of a city-occupation pair, reflecting its attractiveness. Our specification so far assumes independent draws of productivity across cities, the joint distribution of which is given by:

$$\begin{aligned} P[Z_1 < z_1, \dots, Z_N < z_N] &= \prod_c^N P[Z_c < z_c] \\ &= \exp \left\{ - \sum_c^N T_{ck} Z_c^{-\theta} \right\} \end{aligned}$$

This result implies that the choice shares of households for a given city is equal to the probability of households choosing that city. So far, we have stuck with the the base EK specification with the only modification being the mapping of productivity onto wages rather than prices which allows us to obtain city choice shares. We will now abandon the independence assumption and introduce a structure that allows for correlated draws across cities.

$$P[Z_1 < z_1, \dots, Z_N < z_N] = \exp \left\{ - \left(\sum_c^N (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}} \right)^{1-\rho} \right\}$$

Notice with this structure that the shape of the distribution is no longer purely determined by θ but also by the correlation parameter ρ . Where the distribution of productivity within a given occupation decreases as

ρ increases. Meaning that within a given occupation, the higher correlation will result in cities being more similar with each other in terms of productivity. When $\rho = 0$, the distribution reduces down to the original joint distribution with the shape being purely determined by θ and where draws are independent. As $\rho \rightarrow 1$, the draws become perfectly correlated and the productivity is identical across all cities.

2.1 Cross Nested CES

$$P[Z_1(\nu) < z, \dots, Z_N(\nu) < z] = \exp \left\{ - \sum_k^K \left[\sum_c^N (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k} \right\} \quad (1)$$

We will assume that productivity is distributed max stable multivariate Fréchet with T_{ck} being the scale parameter for city c and occupation k . $\theta > 0$ is the shape parameter that determines the dispersion of draws across the distribution and ρ_k is the occupation specific correlation parameter. As in Lind and Ramondo (2023), we adopt a cross nested CES structure with a correlational structure within independent occupational nests. This has the characteristic of distributions not purely determined by θ but also by the correlation parameter. This is because the correlation parameter determines the degree of correlation between draws of productivity across cities.

In order to identify the three dimensions of comparative advantage, we will be separating out the scale parameter into three components where $T_{ck} = T_c T_k t_{ck}$. T_c is the city specific scale parameter which captures the attractiveness of a city, shifting the distribution of all productivity draws within that city upwards. T_k is the occupation specific scale parameter which is common across all cities, this captures the effect that any occupation has across all cities. t_{ck} is the city-occupation specific scale parameter which captures the effect of a city on a specific occupation. This will give us the final dimension of comparative advantage.

$$Z = \max_c \left\{ \frac{Z_c}{\Phi_c} \right\} \quad (2)$$

A household's schedule of productivity is characterized by a vector of draws from different Fréchet distributions for each city occupation pair. The realized productivity a household has in city c is the occupation that maximizes the productivity has in the city. Unlike sequential games where households might pick a city before picking an occupation, we assume that households pick both simultaneously. A way to contextualize

this is to think of households as already having an ideal occupation in mind when picking a city, hence $Z_c = \max_k \{Z_{ck}\}$. This productivity is then scaled by the price index of a city to reflect how high prices reduces the purchasing power of the household within that city, hence making it less attractive.

2.2 Equilibrium

$$G(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \sum_k^K T_k \left[\sum_c^N (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k} \quad (3)$$

We first define $Z_c^{-\theta} = (\gamma w_c)^{-\theta} T_c$ and $\gamma = \Gamma(\frac{\theta+1-\rho_k}{\theta})^{\frac{1}{1-\rho_k}}$. Given our definition of $Z_c^{-\theta}$, T_c will be absorbed within $Z_c^{-\theta}$, giving us the correlation function $G(Z_1^{-\theta}, \dots, Z_N^{-\theta})$ as defined in equation 3.

$$\pi_c = \frac{Z_c^{-\theta} G_c(Z_1^{-\theta}, \dots, Z_N^{-\theta})}{G(Z_1^{-\theta}, \dots, Z_N^{-\theta})}$$

Where $G_c(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \partial G(Z_1^{-\theta}, \dots, Z_N^{-\theta}) / \partial Z_c^{-\theta}$. The expression above gives us the city specific choice shares of households across all occupations. In order to evaluate the expression, we make the simplifying assumption that the correlation parameter is the same across all occupations $\rho_k = \rho$.

$$\lambda_k = \sum_c^N (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}}$$

We introduce the above expression which measures the appeal of occupation k . Given that the expression does not include T_k , it does not capture the attractiveness of occupation k . Instead the expression captures the extent to which a given occupation k exhibits city-specific productivities which are correlated with aggregate city-level attractiveness. The following definitions will be useful in simplifying the expression for city shares.

$$\pi_{ck} = \frac{Z_c^{-\theta} G_c^k(Z_1^{-\theta}, \dots, Z_N^{-\theta})}{G^k(Z_1^{-\theta}, \dots, Z_N^{-\theta})}$$

To obtain occupation specific choice shares, we can evaluate the derivative for city shares at the occupation level. More specifically, rather than $G(Z_1^{-\theta}, \dots, Z_N^{-\theta})$, we will be evaluating $G^k(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \sum_c^N (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}}$. This will give us the following:

$$\pi_{ck} = \frac{(t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}}}{\lambda_k} \quad (4)$$

Moving forward, it will be convenient for us to provide the following definitions. First, we define ϕ_{ck} as the comparative advantage of city c in occupation k . This can be interpreted as an occupation's within city choice shares. As such ϕ_{ck} will be between 0 and 1. We define this formally as:

$$\phi_{ck} \equiv \frac{t_{ck}^{\frac{1}{1-\rho_k}} T_k \lambda_k^{-\rho_k}}{\sum_k t_{ck}^{\frac{1}{1-\rho_k}} T_k \lambda_k^{-\rho_k}} \quad (5)$$

Second, we define an occupation specific choice share which takes into account both the size of each occupation, as measured by productivity T_k , and the extent to which individual city-occupation productivities are correlated with overall city attractiveness. This is defined as the following expression:

$$\omega_k \equiv \frac{T_k \lambda_k^{1-\rho_k}}{\sum_k T_k \lambda_k^{1-\rho_k}} \quad (6)$$

From the perspective of discrete choice demand models, ω_k can be interpreted as the "market share" of occupation k . This is because it captures the extent to which the productivity of occupation k is correlated with overall city attractiveness. The expression is normalized by the sum of all ω_k to ensure that the sum of all market shares is equal to 1.

$$\frac{\pi_{ck}}{\pi_c} \equiv \frac{\phi_{ck}}{\omega_k} \quad (7)$$

The expression above tells us the extent to which a given occupation k is concentrated in city c above and beyond the predicted concentration, given the size of the city π_c is equivalent to the within-city choice share in occupation k divided by the aggregate choice share of that occupation.

$$\pi_c = \sum_k^K \frac{(Z_c^{-\theta} t_{ck})^{\frac{1}{1-\rho}}}{\lambda_k} \frac{T_k \lambda_k^{1-\rho}}{\sum_k^K T_k \lambda_k^{1-\rho}}$$

$$\pi_c = \sum_k^K \pi_{ck} \omega_k \quad (8)$$

By using our definitions, we arrive at the above expression for city shares, which is now the sum of all occupation specific shares weighted by the market share of each occupation.

2.3 City-Occupation Elasticities

We now turn to the city-occupation derivatives: city c 's own technology elasticity and cross technology elasticity with respect to another city c' . This derivative will be approximated by assuming that each city is small, and therefore $\partial \ln \lambda_k / \partial \ln t_{ck} \approx 0$. That is, the aggregate "price index" associated with location choice in occupation k is not affected by a marginal change in the productivity of a given city-occupation pair. We then obtain the following for the own technology shock:

$$\frac{\partial \ln \pi_{ck}}{\partial \ln t_{ck}} \approx \phi_{ck} \left(\frac{1}{1-\rho} \right) \quad (9)$$

This elasticity is positive and increasing in a city's comparative advantage in occupation k . The intuition

is that a city that is more attractive for occupation k will see a larger increase in the choice share of that occupation in response to a marginal increase in the productivity of that occupation. The more specialized the city is in that occupation, the larger the effect of a productivity shock in that occupation. As $\rho \rightarrow 1$, the elasticity approaches infinity, as within any given occupation, if they become more correlated, cities within that given occupation become perfect substitutes for each other.

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = -\pi_{c'} \phi_{ck} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \quad (10)$$

Turning our attention to the cross city technology elasticity, we see that the first term captures the CES element of consumer choice. As the city c' increases in size and becomes increasingly competitive in that occupation, any shocks to this city-occupation pair will have an increasingly negative effects on all other cities.

How much the other cities will be affected is captured by the second term which captures the unbalanced substitution patterns. If a city is relatively concentrated in occupation k , then the affects of a shock in that given occupation will be felt more severely, this is shown by the ratio π_{ck}/π_c . Notice also that if $\rho = 0$, this elasticity simplified to the standard CES elasticity. As $\rho \rightarrow 1$, the elasticity approaches infinity and the correlated choices start to dominate.

2.4 Aggregate Elasticities

We now consider the elasticity of city shares with respect to aggregate city technology shocks T_c and aggregate occupation shocks T_k . Beginning with the former, if we assume again that each cit is small and that $\partial \ln \lambda_k / \partial \ln T_c \approx 0$, we get the following for a city's own technology shock:

$$\frac{\partial \ln \pi_c}{\partial \ln T_c} \approx \frac{1}{1-\rho}$$

This is simply the summation of city-occupation elasticities which was derived in expression 9. And given that by definition $\sum_k^K \phi_{ck} = 1$, we get the following derivations:

$$\begin{aligned}
\frac{\partial \ln \pi_c}{\partial \ln T_c} &= \sum_k \frac{\partial \ln \pi_c}{\partial \ln t_{ck}} \\
&= \sum_k \phi_{ck} \left(\frac{1}{1-\rho} \right) \\
&= \left(\frac{1}{1-\rho} \right) \sum_k \phi_{ck} = \frac{1}{1-\rho}
\end{aligned}$$

The result tells us that if $\rho = 0$ and there's no correlation between occupations, then the elasticity is simply 1. We get a similar story when deriving the cross city technology elasticity. Using the same assumption, we arrive at the result:

$$\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} = -\pi_{c'} \left[\sum_k \phi_{c'k} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \right] \quad (11)$$

Similarly, this is simply the sum over all city-occupation elasticities derived in expression 10. This is shown in the following derivation:

$$\begin{aligned}
\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} &= \sum_k \frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} \\
&= \sum_k \left[-\pi_{c'} \phi_{ck} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \right] \\
&= -\pi_{c'} \left[\sum_k \phi_{c'k} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \right]
\end{aligned}$$

The interpretation of this elasticity is the same as expression 10. The first term captures the CES element of consumer choice and the second term captures the unbalanced substitution patterns, with ρ governing the strength of this unbalanced substitution. Now we simply sum over all occupations to get the aggregate elasticities.

Lastly, we derive the elasticity of city shares with respect to aggregate occupation shocks T_k . This is fairly straightforward as we can simply evaluate the following:

$$\begin{aligned}\frac{\partial \ln \pi_c}{\partial \ln T_k} &= \left(\frac{\partial \phi_{ck}}{\partial T_k} \right) \left(\frac{T_k}{\phi_{ck}} \right) - \left(\frac{\partial \omega_k}{\partial T_k} \right) \left(\frac{T_k}{\omega_k} \right) \\ &= \phi_{ck} - \omega_k\end{aligned}$$

By using the identity in expression 7, we can rewrite the elasticity as the following:

$$\frac{\partial \ln \pi_c}{\partial \ln T_k} = \omega_k \left[\frac{\pi_{ck}}{\pi_c} - 1 \right] \quad (12)$$

You should first notice that the second term in brackets can be either positive or negative depending on the city's relative concentration in that occupation. If the city is relatively concentrated and $\pi_{ck}/\pi_c > 1$, then the city will face a positive shock. If the city is relatively less concentrated and $\pi_{ck}/\pi_c < 1$, then the city will face a negative shock. We can think of this as certain occupations start to become more attractive, cities that are less concentrated in that occupation will face a negative shock as households start to move to cities that are more concentrated in that occupation. This second term is scaled by the market share of that occupation, ω_k , which is simply the market share of that occupation across all cities.

3 Estimation Strategy

3.1 Within-Occupation Migration

Notice that for us to estimate our shifters, we have to first recover our ρ parameter. To do so, we exploit a variation in city-occupation shares over time. Consider the following equation at the city-occupation-year level. From expression 4, we can get the following:

$$\ln \pi_{ck} = \frac{1}{1-\rho} \ln t_{ckt} - \frac{1}{1-\rho} \ln Z_{ct}^{-\theta} - \ln \lambda_{kt}$$

Now we assume the following relationship productivity and wages at the city-occupation level: $t_{ckt} = w_{ckt} \eta_{ckt}$. Where w_{ckt} are wages paid and η_{ckt} is productivity. This will give us the following model:

$$\ln \pi_{ckt} = \left(\frac{1}{1 - \rho} \right) \ln w_{ckt} + \delta_{ct} + \delta_{kt} + \eta_{ckt}$$

With some abuse of notation, we have defined $\eta_{ckt} = \ln \eta_{ckt}$. We now take differences over time to eliminate level shifts.

$$\Delta_t \ln \pi_{ckt} = \left(\frac{1}{1 - \rho} \right) \Delta_t \ln w_{ckt} + \delta_{ct} + \delta_{kt} + \Delta_t \eta_{ckt}$$

We can estimate this equation by regressing wages on city occupation shares and using city and occupation fixed effects at the city-occupation level for every year with δ_{ct} being city fixed effects and δ_{kt} being occupation fixed effects. Given that $\hat{\rho} \in (0, 1)$, we will end up with the restriction $\hat{\beta} \in [1, +\infty)$.

With this regression, we are testing whether migration decisions are primarily within occupations rather than across occupations. If the correlation parameter is close to 1, then migration decisions are purely within occupations. Notice that as $\hat{\rho}$ increases, $\hat{\beta}$ increases. From this perspective, we can interpret ρ as governing within-occupation migration and θ as governing across-occupation migration.

$$Y_{st} = A_{st} \prod_k^K Q_{kst}^{\gamma_{ks}}$$

One concern with the initial specification is the endogeneity of wages with the error term, more explicitly $cov[w_{ckt}, \eta_{ckt}] \neq 0$. In order to instrument for the change in wages, we will use a shift share in which we make use of sectors. Here, we define a Cobb-Douglas structure of production where the intensity of occupation k in sector s is given by γ_{ks} such that $\sum_k^K \gamma_{ks} = 1$. We will use the shift share of occupation k in sector s as an instrument for the change in wages. A_{st} will be the total factor productivity of sector s in year t . This will give us the following first stage regression:

$$\Delta_t \ln w_{ckt}^{IV} = \sum_s^S \gamma_{ks} \bar{\phi}_{cs} \Delta_t \ln A_{st}$$

where $\bar{\phi}_{cs}$ is the share of occupation k in sector s in city c . We will then use the predicted values of $\Delta_t \ln w_{ckt}^{IV}$ as our instrument in the second stage regression.

$$\Delta_t \ln \pi_{ckt} = \left(\frac{1}{1 - \rho} \right) \Delta_t \ln w_{ckt}^{IV} + \delta_{ct} + \delta_{kt} + \Delta_t \eta_{ckt}$$

3.2 Across Occupation Migration

Given that we've identified ρ , we can now proceed to estimate our shape parameter θ and in the process recover all our scale parameters. We start with occupation market shares ω_k in expression 6. By taking relative shares, we get the following:

$$\frac{\omega_{kt}}{\omega_{k't}} = \frac{T_{kt} \lambda_{kt}^{1-\rho}}{T_{k't} \lambda_{k't}^{1-\rho}}$$

Subject to normalization to some base occupation year, we can estimate $T_{kt} \lambda_{kt}^{1-\rho} \forall (k, t)$. We can then use this to recover the denominator in ω_k and get $\sum_k T_{kt} \lambda_{kt}^{1-\rho} \forall t$. This will be useful in recovering our city and city occupation specific scale parameters. Now consider the city-occupation shares from expression 4 taken in logs and transformed into a form with fixed effects:

$$\begin{aligned} \ln \pi_{ckt} &= \frac{1}{1 - \rho} \ln t_{ckt} - \frac{1}{1 - \rho} \ln Z_{ct}^{-\theta} - \ln \lambda_{kt} \\ &= \hat{\epsilon}_{ckt} + \hat{\delta}_{ct} + \hat{\delta}_{kt} \end{aligned}$$

such that,

$$\hat{\lambda}_{kt} = \exp(-\hat{\delta}_{kt})$$

$$\hat{t}_{ckt} = \exp((1 - \rho)\hat{\epsilon}_{ckt})$$

We can then use the estimated $\hat{\lambda}_{kt}$ to recover our occupation specific scale parameters:

$$\hat{T}_{kt} = \frac{\sum_k^K \widehat{T_{kt} \lambda_{kt}^{1-\rho}}}{\hat{\lambda}_{kt}^{1-\rho}}$$

Now we need some way for us to recover productivity in order to estimate the shape parameter θ . Consider the following modification to city shares using our recovered parameters:

$$\begin{aligned} \tilde{\pi}_{ct} &= \pi_{ct} \frac{\sum_k^K T_{kt} \lambda_{kt}^{-\rho}}{\sum_k^K t_{ckt}^{\frac{1}{1-\rho}} T_{kt} \lambda_{kt}^{1-\rho}} \\ &= Z_{ct}^{-\frac{\theta}{1-\rho}} \end{aligned}$$

We now take logs and difference the equation to eliminate the level shift. Recalling our definition of $Z_c^{-\theta} = (\gamma w_c)^{-\theta} T_c$, we get the following estimation equation:

$$\Delta_t \ln \hat{\pi}_{ct} = \hat{\beta} \Delta_t \ln w_{ct} + \Delta_t \hat{\eta}_{ct}$$

The differencing will eliminate γ , which is constant over time, leaving us with a regression of changes in wages and city fixed effects over time on changes in city shares. The coefficient $\hat{\beta}$ will be our estimate of $-\theta/(1 - \rho)$, which when rearranged gives us $\hat{\theta} = -\hat{\beta}(1 - \hat{\rho})$. Note the relationship between θ and ρ is such that as ρ increases, θ decreases. This indicates that as the strength of within occupation migration increases, the across occupation migration becomes less important, reinforcing our interpretation of ρ as governing

within-occupation migration and θ as governing across-occupation migration.

$$\hat{T}_{ct} = \exp((1 - \rho)\hat{\eta}_{ct})$$

Using this regression, we also recover city level shifters from fixed effects estimates.

4 Empirical Results

4.1 Data

We will be using data from the American Community Survey (ACS) which is a survey conducted by the US Census Bureau. The ACS is a survey that collects data on the metropolitan area and occupational level. We will be using data from 2010 to 2022. The ACS provides data on the household level, detailing wages, metropolitan area, occupation and sector of employment based on NAICS codes. This will be used to construct our share data π_c , π_{ck} , ω_k , ϕ_{ck} and ϕ_{cs} as well as obtain wage data w_{ckt} . We will also be using data from the Bureau of Labour Statistics to obtain total factor productivity data at the sector level A_{st} .

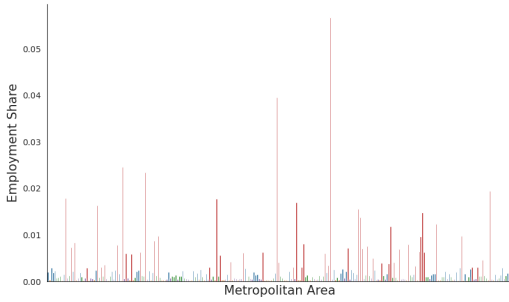


Figure 1: City Employment Share

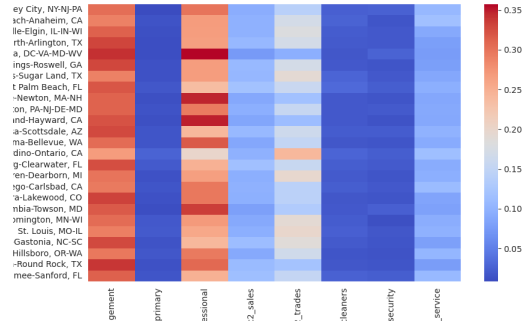


Figure 2: Occupation Shares by Cities

From the data in figure 1, we see that a few metropolitan areas own a disproportionate share of employment which illustrates the size effects of cities to attract employment and households. Intuitively, we should expect these cities to be very different from each other in terms of their specialization, otherwise we would expect the largest city with a particular composition to dominate in the share of households. When zooming into the compositions of the top 25 cities however, we see a different story. In figure 2, we see that the top 25 cities

are very similar with each other in terms of their specialization. With all cities specializing in occupations like management and professional services. This indicates to us that the occupation shifter will play a large role in determining the attractiveness of a city.

References

- EATON, J. AND S. S. KORTUM (2002): “Technology, Geography, and Trade,” *Econometrica*, 70, 1741–1779.
- LIND, N. AND N. RAMONDO (2023): “Trade with Correlation,” *American Economic Review*, 113, 317–53.
- REDDING, S. J. (2016): “Goods trade, factor mobility and welfare,” *Journal of International Economics*, 101, 148–167.

5 Appendix

5.1 Derivations

City Choice Shares π_c : As discussed in Lind and Ramondo (2023), the choice shares can be expressed as:

$$\pi_c = \frac{Z_c^{-\theta} G_c}{G()}$$

We define $G()$ as the following, given the definition of T_{ck} and λ_k provided in the main text:

$$G(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \sum_k \left[\sum_c (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k} = \sum_k T_k \lambda_k^{1-\rho}$$

$G_c()$ is simply the derivative of $G()$ with respect to $Z_c^{-\theta}$.

$$\begin{aligned} \frac{\partial G()}{\partial Z_c^{-\theta}} &= \sum_k \frac{\partial}{\partial Z_c^{-\theta}} \left[\sum_c (T_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k} \\ &= \sum_k \frac{\partial}{\partial Z_c^{-\theta}} \left[T_k^{\frac{1}{1-\rho}} \sum_c (t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}} \right]^{1-\rho} \\ &= \sum_k T_k \left[(1-\rho) \lambda_k^{-\rho} \frac{\partial \lambda_k}{\partial Z_c^{-\theta}} \right] \\ &= \sum_k T_k \left[(1-\rho) \lambda_k^{-\rho} \left(\frac{1}{1-\rho} \right) t_{ck}^{\frac{1}{1-\rho}} (Z_c^{-\theta})^{\frac{\rho}{1-\rho}} \right] \\ &= (Z_c^{-\theta})^{\frac{\rho}{1-\rho}} \sum_k T_k t_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \end{aligned}$$

Putting these three terms together, we derive the choice shares:

$$\begin{aligned} \pi_c &= \frac{Z_c^{-\theta} G_c}{G()} \\ &= (Z_c^{-\theta})^{\frac{1}{1-\rho}} \left[\frac{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\sum_k T_k \lambda_k^{1-\rho}} \right] \end{aligned}$$

Own Occupation-Specific Elasticity: We wish to evaluate $\partial \ln \pi_c / \partial \ln t_{ck}$, under the assumption that $\partial \ln \lambda_k / \partial \ln t_{ck} = 0$. Notice this assumption yields the following:

$$\frac{\partial \ln \pi_c}{\partial \ln t_{ck}} \approx \frac{\partial \ln \pi_{ck}}{\partial \ln t_{ck}} - \frac{\partial \ln \phi_{ck}}{\partial \ln t_{ck}}$$

given the definitions of π_{ck} and ϕ_{ck} provided in the text.

Notice that this only leaves one term to evaluate if we take the logarithm of π_c and the derivative of this logarithm with respect to $\ln t_{ck}$:

$$\begin{aligned} \frac{\partial \ln \pi_c}{\partial \ln t_{ck}} &\approx \frac{\partial \ln [\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}]}{\partial \ln t_{ck}} \\ &= \left(\frac{\partial [\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}]}{\partial t_{ck}} \right) \left(\frac{t_{ck}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\ &= \left(\frac{1}{1-\rho} \right) \left(\frac{t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{t_{ck}} \right) \left(\frac{t_{ck}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\ &= \left(\frac{1}{1-\rho} \right) \left[\frac{t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right] \\ &= \frac{\phi_{ck}}{1-\rho} \end{aligned}$$

Cross-City Occupation-Specific Elasticity: We wish to evaluate $\partial \ln \pi_c / \partial \ln t_{c'k}$. Notice that this elasticity can be expressed as the following two terms:

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = t_{ck}^{\frac{1}{1-\rho}} T_k \left(\frac{\partial \lambda_k^{-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{c'k}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) - T_k \left(\frac{\partial \lambda_k^{1-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{c'k}}{\sum_k T_k \lambda_k^{1-\rho}} \right)$$

It will be useful to first define the derivative of λ_k with respect to our variable of interest, $t_{c'k}$:

$$\frac{\partial \lambda_k}{\partial t_{c'k}} = \left(\frac{1}{1-\rho} \right) \left(\frac{1}{t_{c'k}} \right) [t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}$$

We can now use chain rule in order to evaluate our elasticity of interest. The first term becomes the following:

$$\begin{aligned}
t_{ck}^{\frac{1}{1-\rho}} T_k \left(\frac{\partial \lambda_k^{-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{c'k}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) &= t_{ck}^{\frac{1}{1-\rho}} T_k (-\rho) (\lambda_k^{-\rho-1}) \left(\frac{1}{1-\rho} \right) \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\
&= - \left(\frac{\rho}{1-\rho} \right) \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\lambda_k} \right) \left(\frac{t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) \\
&= - \left(\frac{\rho}{1-\rho} \right) \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\lambda_k} \right) \phi_{ck} \\
&= - \left(\frac{\rho}{1-\rho} \right) \pi_{c'k} \phi_{ck}
\end{aligned}$$

The second term can be derived in the following way:

$$\begin{aligned}
-T_k \left(\frac{\partial \lambda_k^{1-\rho}}{\partial t_{c'k}} \right) \left(\frac{t_{c'k}}{\sum_k T_k \lambda_k^{1-\rho}} \right) &= -T_k (\lambda_k^{-\rho}) [t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}} \left(\frac{1}{\sum_k T_k \lambda_k^{1-\rho}} \right) \\
&= - \left(\frac{[t_{c'k} (Z_{c'}^{-\theta})]^{\frac{1}{1-\rho}}}{\lambda_k} \right) \left(\frac{T_k \lambda_k^{1-\rho}}{\sum_k T_k \lambda_k^{1-\rho}} \right) \\
&= -\pi_{c'k} \omega_k
\end{aligned}$$

Putting these together, we derive the cross-city occupation-specific elasticity as the following:

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = -\pi_{c'k} \left[\omega_k + \left(\frac{\rho}{1-\rho} \right) \phi_{ck} \right]$$

Notice that this is equivalent to the following, given the identity linking π_c , π_{ck} , ϕ_{ck} , and ω_k .

$$\frac{\partial \ln \pi_c}{\partial \ln t_{c'k}} = -\pi_{c'k} \phi_{ck} \left[1 + \left(\frac{\rho}{1-\rho} \right) \left(\frac{\pi_{ck}}{\pi_c} \right) \right] \quad (13)$$

Cross-City Aggregate Elasticity: We wish to evaluate $\partial \ln \pi_c / \partial \ln T_{c'}$. Notice that:

$$\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} = \left(\frac{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}}{\partial T_{c'}} \right) \left(\frac{T_{c'}}{\sum_k t_{ck}^{\frac{1}{1-\rho}} T_k \lambda_k^{-\rho}} \right) - \left(\frac{\partial \sum_k T_k \lambda_k^{1-\rho}}{\partial T_{c'}} \right) \left(\frac{T_{c'}}{\sum_k T_k \lambda_k^{1-\rho}} \right)$$

Notice also that:

$$\frac{\partial \lambda_k}{\partial T_{c'}} = \left(\frac{1}{1-\rho} \right) \left(\frac{[t_{ck}(Z_c^{-\theta})]^{\frac{1}{1-\rho}}}{T_{c'}} \right)$$

We can therefore solve for this cross-derivative as the following:

$$\begin{aligned} \frac{\partial \ln \pi_c}{\partial \ln T_{c'}} &= \sum_k \left[- \left(\frac{\rho}{1-\rho} \right) \phi_{ck} \pi_{c'k} \right] + \sum_k \left[- \omega_k \pi_{c'k} \right] \\ &= - \sum_k \pi_{c'k} \left[\omega_k + \left(\frac{\rho}{1-\rho} \right) \phi_{ck} \right] \end{aligned}$$

5.2 Cross City Elasticity

$$\ln \pi_c = \frac{1}{1-\rho} \ln Z_c^{-\theta} + \ln \left(\sum_k (T_c T_k t_{ck})^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \right) - \ln \left(\sum_k \lambda_k^{1-\rho} \right)$$

$$\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} = \frac{\partial \left(\sum_k (T_c T_k t_{ck})^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \right)}{\partial T_{c'}} \frac{T_{c'}}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} - \frac{\partial \left(\sum_k \lambda_k^{1-\rho} \right)}{\partial T_{c'}} \frac{T_{c'}}{\sum_k \lambda_k^{1-\rho}}$$

Consider the derivative of λ_k with respect to $T_{c'}$:

$$\begin{aligned} \frac{\partial \lambda_k}{\partial T_{c'}} &= T_k^{\frac{1}{1-\rho}} \left(\frac{1}{1-\rho} \right) T_{c'}^{\frac{1}{1-\rho}-1} t_{c'k}^{\frac{1}{1-\rho}} (Z_c^{-\theta})^{\frac{\rho}{1-\rho}} \\ &= \frac{1}{1-\rho} \frac{1}{T_{c'}} (T_{c'k} Z_c^{-\theta})^{\frac{1}{1-\rho}} \end{aligned}$$

Consider the first term in the derivative:

$$\begin{aligned} \frac{\partial \left(\sum_k (T_c T_k t_{ck})^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \right)}{\partial T_{c'}} \frac{T_{c'}}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} &= \frac{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho-1} \left(\frac{1}{1-\rho} \right) \frac{1}{T_{c'}} T_{c'k}^{\frac{1}{1-\rho}} (Z_c^{-\theta})^{\frac{1}{1-\rho}}}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} \times T_{c'} \\ &= -\frac{\rho}{1-\rho} \frac{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \pi_{c'k}}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} \end{aligned}$$

Now consider the second term in the derivative:

$$\begin{aligned} -\frac{\partial \left(\sum_k \lambda_k^{1-\rho} \right)}{\partial T_{c'}} \frac{T_{c'}}{\sum_k \lambda_k^{1-\rho}} &= -\frac{-\sum_k \rho \lambda_k^{-\rho-1} \left(\frac{1}{1-\rho} \right) \frac{1}{T_{c'}} (T_{c'k} Z_c^{-\theta})^{\frac{1}{1-\rho}}}{\sum_k \lambda_k^{-\theta}} \times T_{c'} \\ &= \frac{\rho}{1-\rho} \frac{\sum_k \lambda_k^{-\rho} \pi_{c'k}}{\sum_k \lambda_k^{-\rho}} \end{aligned}$$

This will give us:

$$\frac{\partial \ln \pi_c}{\partial \ln T_{c'}} = \frac{\rho}{1-\rho} \left[\frac{\sum_k \lambda_k^{-\rho} \pi_{c'k}}{\sum_k \lambda_k^{-\rho}} - \frac{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \pi_{c'k}}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} \right]$$

5.3 Technology Elasticity

$$\frac{\partial \ln \pi_c}{\partial \ln T_k} = \frac{\partial \left(\sum_k (T_c T_k t_{ck})^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \right)}{\partial T_k} \frac{T_k}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} - \frac{\partial \left(\sum_k \lambda_k^{1-\rho} \right)}{\partial T_k} \frac{T_k}{\sum_k \lambda_k^{1-\rho}}$$

Consider the derivative of λ_k with respect to T_k :

$$\begin{aligned}
\frac{\partial \lambda_k}{\partial T_k} &= \frac{1}{1-\rho} T_k^{\frac{1}{1-\rho}-1} \sum_k (T_c t_{ck} Z_c^{-\theta})^{\frac{1}{1-\rho}} \\
&= \frac{1}{1-\rho} \frac{1}{T_k} \lambda_k
\end{aligned}$$

Consider the first term in the derivative:

$$\begin{aligned}
\frac{\partial \left(\sum_k (T_c T_k t_{ck})^{\frac{1}{1-\rho}} \lambda_k^{-\rho} \right)}{\partial T_k} \frac{T_k}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} &= \frac{T_k^{\frac{1}{1-\rho}} (T_c t_{ck})^{\frac{1}{1-\rho}} (-\rho) \lambda_k^{-\rho-1} \left(\frac{1}{1-\rho} \right) \frac{1}{T_k} \lambda_k + \lambda_k^{-\rho} \left(\frac{1}{1-\rho} \right) \frac{1}{T_k} T_{ck}^{\frac{1}{1-\rho}}}{\sum_k T_{ck}^{\frac{1}{1-\rho}} \lambda_k^{-\rho}} \\
&= \phi_{ck}
\end{aligned}$$

Consider the second term in the derivative:

$$\begin{aligned}
-\frac{\partial \left(\sum_k \lambda_k^{1-\rho} \right)}{\partial T_k} \frac{T_k}{\sum_k \lambda_k^{1-\rho}} &= -\frac{(1-\rho) \lambda_k^{-\rho} \left(\frac{1}{1-\rho} \right) \frac{1}{T_k} \lambda_k}{\sum_k \lambda_k^{1-\rho}} \times T_k \\
&= -\omega_k
\end{aligned}$$

This will give us:

$$\frac{\partial \ln \pi_c}{\partial \ln T_k} = \phi_{ck} - \omega_k$$