City Location Choice and Houehold Productivity

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- 2. Background
- 3. Model
- 4. Preliminary Results
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- 1. Cities

Agglomoration

- According to the world bank, 56% of the world's population live in cities.
 - This is expected to increase to 70% by 2050.

• People choose to live in cities in spite of problems such as congestion and high rents.

- This is because of the benifits cities offer.
 - Households, better work opportunities and better amenities.
 - Businesses, better access to services and a larger market.

Trivial Solution

• If cities are identical and size determines the magnitude of agglomoration benifits, then all households would choose to live in the same city.

- Cities are obviously not homogenous.
 - Toronto is not the same as Vancouver.

• Why do people choose to live in the cities they do?

Research Question

- What will happen to city populations when there's a shock to the economy?
 - What will the migration patterns look like?

- How substitutable are cities?
 - How do households choose between cities?

- With city heterogeneity, can we break the independence of irrelevant alternatives (IIA) assumption in spacial econ?
 - Cities are not directly substitutable for each other.

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Eaton and Kortum (2002)

- Ricardian Model of Trade
 - Countries should perfectly specialize in the production of goods they have a comparative advantage in.

- Probabalistic draws of Productivity
 - Draw from a Frechet distribution.
 - For a variety of goods, what is the probability you can produce below a certain price?

- Result
 - Non zero production of all goods in all countries.

Redding (2016)

• Quatitative Spacial Model

• Take EK and applied to to an urban/spacial setting.

• Wages are determined by productivities.

• Wages and amenities determine location choice shares.

Lind and Ramondo (2023)

• Trade with Correlation

- Preferences
 - \bullet EK has CES preferences where goods are perfectly substitutable.
 - Lind and Ramondo proposed a cross nested CES structure in order to break IIA.
 - A Lamborghini is not the same as a Toyota.

• Better suited substitution patterns in trade.

This Paper

• Apply this new framework that allows for correlation to Redding's QSM.

• QSM currently loads city heterogeneity entirely onto amenities.

• This paper will attempt to explain some of that variation.

- 3. Model

Setup

• N cities indexed by c.

• K occupations indexed by k.

• A continuim of household types $\nu \in [0, 1]$.

Setup

• Output is entirely determined by productivity.

- Wages are determined by productivity and a city specific price index.
 - The price index will be set to 1 in the baseline model.

- Utility is entirely determined by wages.
 - A housheold maximizes utility by choosing the city that maximizes their wage.

Productivity

• Every household tyoe in every city occupation pair draws a productivity from this Frechet distribution.

$$P[Z_{ck} < z] = exp[(T_{ck}^* z^{-\theta})^{\frac{1}{1-\rho_k}}]$$
 (1)

- T_{ck} is the city occupation specific productivity scale parameter.
 - This represents a city's absolute advantage in that occupation.
- $H_k(\nu)$ is the household type occupation specific productivity scale parameter.
- \bullet θ is the Frechet shape parameter.
- ρ_k is the occupation correlation parameter.

Correlation Function

• These productivities have a correlation structure.

$$G(Z_1^{-\theta}, \dots, Z_N^{-\theta}) = \sum_k \left[\sum_c^N (T_{ck}^* Z_c^{-\theta})^{\frac{1}{1-\rho_k}} \right]^{1-\rho_k}$$
 (2)

- Cities have correlated draws based on occupations.
- T_{ck}^{\star} is what we get when we intergrate over all household types.

Choice Shares

$$\pi_c = \frac{Z_c^{-\theta} G_c(Z_1^{-\theta}, \dots, Z_N^{-\theta})}{G(Z_1^{-\theta}, \dots, Z_N^{-\theta})}$$
(3)

$$\pi_c = \frac{T_c^* Z_c^{-\theta}}{\sum_c^N T_c^* Z_c^{-\theta}} \tag{4}$$

• Choice shares are dependent on productivity shares and city specifc shifters.

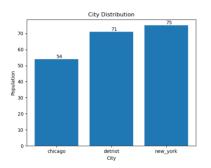
Preliminary Results \bullet 00

- 4. Preliminary Results

Setup

- 3 cities
 - Chicago, Detriot and New York.
 - Chicago and Detriot specialise in trades with Chicago having an absolute advantage.
 - New York specialises in services.

Simulation Results



City Distribution

91

90

91

90

13

Chicago detriot new_york

Figure: Initial Distribution of Populations

Figure: Post Detriot Shock

- 5. To Do List

To Do List

• Estimation equation for parameters.

• Obtain wage and emplyment for American cities.

- Run counterfacutals.
 - China shock.