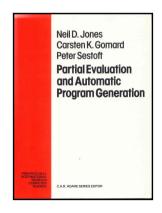
Parallel Functional Programming in Java 8

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Chalmers Tekniska Högskola Monday 2018-04-16

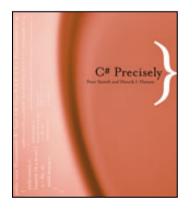
The speaker

- MSc 1988 computer science and mathematics and PhD 1991, DIKU, Copenhagen University
- KU, DTU, KVL and ITU; and Glasgow U, AT&T Bell Labs, Microsoft Research UK, Harvard University
- Programming languages, software development, ...
- Open source software
 - Moscow ML implementation, 1994...
 - C5 Generic Collection Library, with Niels Kokholm, 2006...
 - Funcalc spreadsheet implementation, 2014

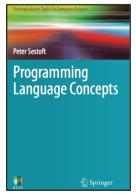


Java Precisely

(Compared to the property of t









2002, 2005, 2016

2004 & 2012

2007

2012, 2017

Plan

- Java 8 functional programming
 - Package java.util.function
 - Lambda expressions, method reference expressions
 - Functional interfaces, targeted function type
- Java 8 streams for bulk data
 - Package java.util.stream
- High-level parallel programming
 - Streams: primes, queens, van der Corput, ...
 - Array parallel prefix operations
 - Class java.util.Arrays static methods
- A multicore performance mystery

Materials

- Java Precisely 3rd edition, MIT Press 2016
 - § 11.13: Lambda expressions
 - § 11.14: Method reference expressions
 - § 23: Functional interfaces
 - § 24: Streams for bulk data
 - § 25: Class Optional<T>
- Book examples are called Example154.java etc
 - Get them from the book homepage http://www.itu.dk/people/sestoft/javaprecisely/

New in Java 8

- Lambda expressions(String s) -> s.length
- Method reference expressionsString::length
- Functional interfacesFunction<String,Integer>
- Streams for bulk data
 Stream<Integer> is = ss.map(String::length)
- Parallel streams
 is = ss.parallel().map(String::length)
- Parallel array operations
 Arrays.parallelSetAll(arr, i -> sin(i/PI/100.0))
 Arrays.parallelPrefix(arr, (x, y) -> x+y)

Functional programming in Java

- Immutable data instead of objects with state
- Recursion instead of loops
- Higher-order functions that either
 - take functions as argument
 - return functions as result

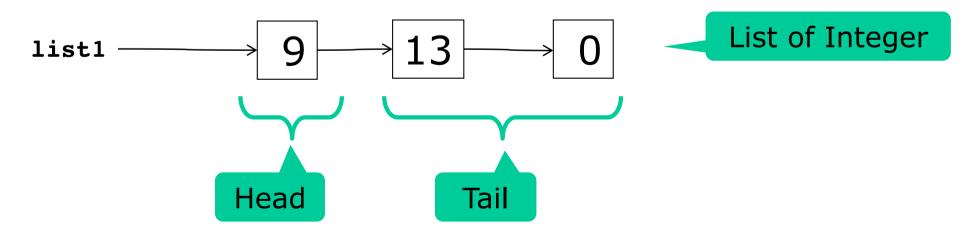
```
class FunList<T> {
    final Node<T> first;
    protected static class Node<U> {
        public final U item;
        public final Node<U> next;
        public Node (U item, Node<U> next) { ... }
    }
    ...
}
```

Example154.java

Immutable data

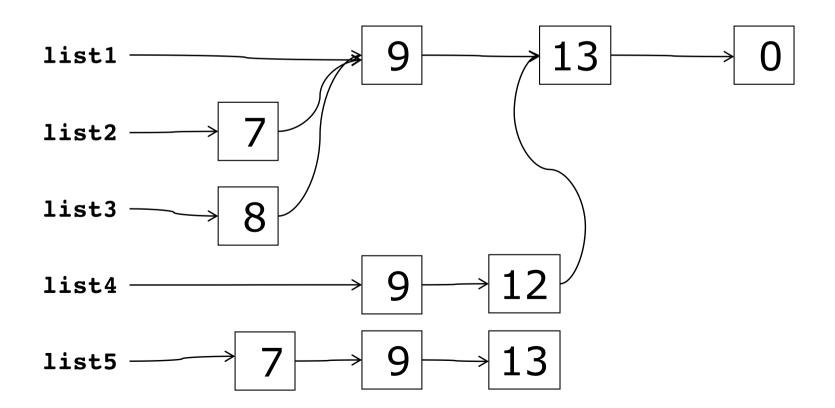
FunList<T>, linked lists of nodes

```
class FunList<T> {
  final Node<T> first;
  protected static class Node<U> {
    public final U item;
    public final Node<U> next;
    public Node(U item, Node<U> next) { ... }
}
```



Existing data do not change

```
FunList<Integer> empty = new FunList<>(null),
  list1 = cons(9, cons(13, cons(0, empty))),
  list2 = cons(7, list1),
  list3 = cons(8, list1),
  list4 = list1.insert(1, 12),
  list5 = list2.removeAt(3);
```



Recursion in insert

- "If i is zero, put item in a new node, and let its tail be the old list xs"
- "Otherwise, put the first element of xs in a new node, and let its tail be the result of inserting item in position i-1 of the tail of xs"

Immutable data: Bad and good

- Immutability leads to more allocation
 - Takes time and space
 - But modern garbage collectors are fast
- Immutable data can be safely shared
 - May actually reduce amount of allocation
- Immutable data are automatically threadsafe
 - No (other) thread can mess with it
 - And also due to visibility effects of final modifier



Lambda expressions 1

One argument lambda expressions:

```
Example64.java
Function<String,Integer>
  fsi1 = s -> Integer.parseInt(s)
                                    Function that takes a string s
... fsi1.apply("004711") ...
                                      and parses it as an integer
           Calling the function
                                                     Same, written
                                                      in other ways
Function<String,Integer>
  fsi2 = s -> { return Integer.parseInt(s);
```

Two-argument lambda expressions:

fsi3 = (String s) -> Integer.parseInt(s);

```
BiFunction<String,Integer,String>
  fsis1 = (s, i) -> s.substring(i, Math.min(i+3, s.length()));
```

Lambda expressions 2

Zero-argument lambda expression:

```
Example64.java
Supplier<String>
  now = () -> new java.util.Date().toString();
```

One-argument result-less lambda ("void"):

```
Consumer<String>
  show1 = s -> System.out.println(">>>" + s + "<<<");</pre>
Consumer<String>
  show2 = s -> { System.out.println(">>>" + s + "<<<");</pre>
```

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Method reference expressions

```
BiFunction<String,Integer,Character> charat
                                                               Example67.java
  = String::charAt;
                                  Same as (s,i) -> s.charAt(i)
System.out.println(charat.apply("ABCDEF", 1));
Function<String,Integer> parseint = Integer::parseInt;
                                    Same as fsi1, fs2 and fs3
Function<Integer,Character> hex1
  = "0123456789ABCDEF"::charAt;
                                     Conversion to hex digit
                                  Class and array constructors
Function<Integer,C> makeC = C::new;
Function<Integer,Double[]> make1DArray = Double[]::new
```

Targeted function type (TFT)

- A lambda expression or method reference expression does not have a type in itself
- Therefore must have a targeted function type
- Lambda or method reference must appear as
 - Assignment right hand side:

```
• Function<String,Integer> f = Integer::parseInt;
```

- Argument to call:

TFT

- stringList.map(Integer::parseInt)
- In a cast:

map's argument type is TFT

- (Function<String,Integer>)Integer::parseInt
- Argument to return statement: TFT
 - return Integer::parseInt;

Enclosing method's return type is TFT

Functions as arguments: map

```
public <U> FunList<U> map(Function<T,U> f) {
   return new FunList<U>(map(f, first));
}
static <T,U> Node<U> map(Function<T,U> f, Node<T> xs) {
   return xs == null ? null
      : new Node<U>(f.apply(xs.item), map(f, xs.next));
}
```

- Function map encodes general behavior
 - Transform each list element to make a new list
 - Argument f expresses the specific transformation
- Same effect as OO "template method pattern"

Calling map

7 9 13

```
FunList<Double> list8 = list5.map(i -> 2.5 * i);
```

17.5 22.5 32.5

```
FunList<Boolean> list9 = list5.map(i -> i < 10);</pre>
```

true true false

Functions as arguments: reduce

```
static <T,U> U reduce(U x0, BiFunction<U,T,U> op, Node<T> xs) {
  return xs == null ? x0
  : reduce(op.apply(x0, xs.item), op, xs.next);
}
```

```
• Example: list.reduce(0, (x,y) -> x+y)
= 0+x1+...+xn
```

Example 154. java

Calling reduce

```
17.5 22.5 32.5
                                                                       Exam<mark>ple15</mark>4.java
double sum = list8.reduce(0.0, (res, item) -> res + item)
                                                         72.5
double product = list8.reduce(1.0, (res, item) -> res * item);
                                                         12796.875
boolean allBig
       = list8.reduce(true, (res, item) -> res && item > 10);
                                                         true
```

Tail recursion and loops

```
static <T,U> U reduce(U x0, BiFunction<U,T,U> op, Node<T> xs) {
   return xs == null ? x0
   : reduce(op.apply(x0, xs.item), op, xs.next);
}
Tail call
```

- A call that is the func's last action is a tail call
- A tail-recursive func can be replaced by a loop

```
static <T,U> U reduce(U x0, BiFunction<U,T,U> op, Node<T> xs) {
   while (xs != null) {
      x0 = op.apply(x0, xs.item);
      xs = xs.next;
   }
   return x0;
}
Loop version
of reduce
```

The Java compiler does not do that automatically

Java 8 functional interfaces

• A functional interface has exactly one abstract

method

```
interface Function<T,R> {
  R apply(T x);
}
```

```
Type of functions from T to R
```

```
C#: Func<T,R>
```

```
F#: T -> R
```

```
interface Consumer<T> {
  void accept(T x);
}
```

```
Type of functions from T to void
```

```
C#: Action<T>
```

F#: T -> unit

Java Precisely page 125

(Too) many functional interfaces

Interface	Sec.	Function Type	Single Abstract Method Signature	
		One-Argument Functions and Predicates		
Function <t,r></t,r>	23.5	T -> R	R apply(T)	
UnaryOperator <t></t>	23.6	T -> T	T apply(T)	
Predicate <t></t>	23.7	T -> boolean	boolean test(T)	
Consumer <t></t>	23.8	T -> void	void accept(T)	
Supplier <t></t>	23.9	void -> T	T get()	
Runnable		void -> void	void run()	
		Two-Argument Functions and Predicates		
BiFunction <t,u,r></t,u,r>	23.10	T * U -> R	R apply(T, U)	
BinaryOperator <t></t>	23.11	T * T -> T	T apply(T, T)	
BiPredicate <t,u></t,u>	23.7	T * U -> boolean	boolean test(T, U)	
BiConsumer <t,u></t,u>	23.8	T * U -> void	void accept (T, U)	
Primitive-Type Specialized Versions of the Generic Functional Interfaces				
DoubleToIntFunction	23.5	double -> int	int applyAsInt(double)	
DoubleToLongFunction	23.5	double -> long	long applyAsLong(double)	
IntToDoubleFunction	23.5	int -> double	double applyAsDouble(int)	
IntToLongFunction	23.5	int -> long	long applyAsLong(int)	
LongToDoubleFunction	23.5	long -> double	double applyAsDouble(long)	
LongToIntFunction	23.5	long -> int	int applyAsInt(long)	
DoubleFunction <r></r>	23.5	double -> R	R apply(double)	
IntFunction <r></r>	23.5	int -> R	R apply(int)	
LongFunction <r></r>	23.5	long -> R	R apply(long)	
ToDoubleFunction <t></t>	23.5	T -> double	double applyAsDouble(T)	
ToIntFunction <t></t>	23.5	T -> int	int applyAsInt(T)	
ToLongFunction <t></t>	23.5	T -> long	long applyAsLong(T)	
ToDoubleBiFunction <t,u></t,u>	23.10	T * U -> double	double applyAsDouble(T, U)	
ToIntBiFunction <t,u></t,u>	23.10	T * U -> int	int applyAsInt(T, U)	
ToLongBiFunction <t,u></t,u>	23.10	T * U -> long	long applyAsLong(T, U)	
DoubleUnaryOperator	23.6	double -> double	double applyAsDouble(double)	
IntUnaryOperator	23.6	int -> int	int applyAsInt(int)	
LongUnaryOperator	23.6	long -> long	long applyAsLong(long)	
DoubleBinaryOperator	23.11	double * double -> double	double applyAsDouble (double, double)	
IntBinaryOperator	23.11	int * int -> int	int applyAsInt(int, int)	
LongBinaryOperator	23.11	long * long -> long	long applyAsLong(long, long)	
DoublePredicate	23.7	double -> boolean	boolean test (double)	
IntPredicate	23.7	int -> boolean	boolean test(int)	
LongPredicate	23.7	long -> boolean	boolean test(long)	
DoubleConsumer	23.8	double -> void	void accept (double)	
IntConsumer	23.8	int -> void	void accept(int)	
LongConsumer	23.8	long -> void	void accept (long)	
ObjDoubleConsumer <t></t>	23.8	T * double -> void	void accept (T, double)	
ObjIntConsumer <t></t>	23.8	T * int -> void	void accept(T, int)	
ObjLongConsumer <t></t>	23.8	T * long -> void	void accept (T, long)	
BooleanSupplier	23.9	void -> boolean	boolean getAsBoolean()	
DoubleSupplier	23.9	void -> double	double getAsDouble()	
IntSupplier	23.9	void -> double	int getAsInt()	
LongSupplier	23.9	void -> long	long getAsLong()	
Longouppiloi	23.7	void -> Tong	Total decuational()	

```
interface IntFunction<R> {
   R apply(int x);
}
```

Use instead of Function<Integer,R> to avoid (un)boxing

Primitive-type specialized interfaces

Primitive-type specialized interfaces for int, double, and long

```
interface Function<T,R> {
   R apply(T x);
}

interface IntFunction<R> {
   R apply(int x);
}

Why
both?

What difference?
```

```
Function<Integer,String> f1 = i -> "#" + i;
IntFunction<String> f2 = i -> "#" + i;
```

- Calling **f1.apply(i)** will box **i** as Integer
 - Allocating object in heap, takes time and memory
- Calling f2.apply(i) avoids boxing, is faster
- Purely a matter of performance

Functions that return functions

Conversion of n to English numeral, cases

```
n < 20 : one, two, ..., nineteen
n < 100: twenty-three, ...

n>=100: two hundred forty-three, ...
n>=1000: three thousand two hundred forty-three...
n >= 1 million: ... million ...
n >= 1 billion: ... billion ...
```

Functions that return functions

Using the general higher-order function

Converting to English numerals:

toEnglish(2147483647)

```
two billion one hundred forty-seven million four hundred eighty-three thousand six hundred forty-seven
```

Streams for bulk data

- Stream<T> is a finite or infinite sequence of T
 - Possibly lazily generated
 - Possibly parallel
- Stream methods
 - map, flatMap, reduce, filter, ...
 - These take functions as arguments
 - Can be combined into pipelines
 - Java optimizes (and parallelizes) the pipelines well
- Similar to
 - Java Iterators, but very different implementation
 - The extension methods underlying .NET Ling

Some stream operations

- Stream<Integer> s = Stream.of(2, 3, 5)
- s.filter(p) = the x where p.test(x) holds s.filter(x -> x%2==0) gives 2
- s.map(f) = results of f.apply(x) for x in s s.map(x -> 3*x) gives 6, 9, 15
- s.flatMap(f) = a flattening of the streams created by f.apply(x) for x in s

```
s.flatMap(x \rightarrow Stream.of(x,x+1)) gives 2,3,3,4,5,6
```

- s.findAny() = some element of s, if any, or else the absent Option<T> value
 - s.findAny() gives 2 or 3 or 5
- s.reduce(x0, op) = x0\$s0\$...\$sn if we write
 op.apply(x,y) as x\$y

```
s.reduce(1, (x,y)->x*y) gives 1*2*3*5 = 30
```

Similar functions are everywhere

- Java stream map is called
 - map in Haskell, Scala, F#, Clojure
 - Select in C#
- Java stream flatMap is called
 - concatMap in Haskell
 - flatMap in Scala
 - collect in F#
 - SelectMany in C#
 - mapcat in Clojure
- Java reduce is a special (assoc. op.) case of
 - fold1 in Haskell
 - foldLeft in Scala
 - fold in F#
 - Aggregate in C#
 - reduce in Clojure

Counting primes on Java 8 streams

Our old standard Java for loop:

```
int count = 0;
for (int i=0; i<range; i++)
  if (isPrime(i))
    count++;</pre>
```

Classical efficient imperative loop

Sequential Java 8 stream:

```
IntStream.range(0, range)
.filter(i -> isPrime(i))
.count()
```

Pure functional programming ...

Parallel Java 8 stream:

```
IntStream.range(0, range)
.parallel()
.filter(i -> isPrime(i))
.count()
```

... and thus parallelizable and thread-safe

Performance results (!!)

Counting the primes in 0 ...99,999

Method	Intel i7 (ms)	AMD Opteron (ms)
Sequential for-loop	9.9	40.5
Sequential stream	9.9	40.8
Parallel stream	2.8	1.7
Best thread-parallel	3.0	4.9
Best task-parallel	2.6	1.9

- Functional streams give the simplest solution
- Nearly as fast as tasks and threads, or faster:
 - Intel i7 (4 cores) speed-up: 3.6 x
 - AMD Opteron (32 cores) speed-up: 24.2 x
 - ARM Cortex-A7 (RP 2B) (4 cores) speed-up: 3.5 x
- The future is parallel and functional ☺

Side-effect freedom

From the java.util.stream package docs:

Side-effects

Side-effects in behavioral parameters to stream operations are, in general, discouraged, as they can often lead to unwitting violations of the statelessness requirement, as well as other thread-safety hazards.

This means "catastrophic"

- Java compiler (type system) cannot enforce side-effect freedom
- Java runtime cannot detect it

Creating streams 1

Explicitly or from array, collection or map:

```
IntStream is = IntStream.of(2, 3, 5, 7, 11, 13);
String[] a = { "Hoover", "Roosevelt", ...};
Stream<String> presidents = Arrays.stream(a);
Collection<String> coll = ...;
Stream<String> countries = coll.stream();
Map<String,Integer> phoneNumbers = ...;
Stream<Map.Entry<String,Integer>> phones
  = phoneNumbers.entrySet().stream();
```

Finite, ordered, sequential, lazily generated

:xample164.jav

Creating streams 2

- Useful special-case streams:
- IntStream.range(0, 10_000)
- random.ints(5_000)
- bufferedReader.lines()
- bitset.stream()
- Functional iterators for infinite streams
- Imperative generators for infinite streams
- StreamBuilder<T>: eager, only finite streams

Creating streams 3: generators

• Generating 0, 1, 2, 3, ...

Functional

```
Example16<mark>5.jav</mark>a
IntStream nats1 = IntStream.iterate(0, x -> x+1);
              Most efficient (!!),
                                                Object
              and parallelizable
                                              imperative
IntStream nats2 = IntStream.generate(new IntSupplier() {
  private int next = 0;
  public int getAsInt() { return next++; }
});
```

Imperative, using final array for mutable state

```
final int[] next = { 0 };
IntStream nats3 = IntStream.generate(() -> next[0]++);
```

Example 182. java

Creating streams 4: StreamBuilder

Convert own linked IntList to an IntStream

```
class IntList {
 public final int item;
 public final IntList next;
  public static IntStream stream(IntList xs) {
    IntStream.Builder sb = IntStream.builder();
    while (xs != null) {
      sb.accept(xs.item);
      xs = xs.next;
    return sb.build();
```

- Eager: no stream element output until end
- Finite: does not work on cyclic or infinite lists

Streams for backtracking

- Generate all n-permutations of 0, 1, ..., n-1
 - Eg [2,1,0], [1,2,0], [2,0,1], [0,2,1], [0,1,2], [1,0,2]

Set of numbers not yet used

An incomplete permutation

```
public static Stream<IntList> perms(BitSet todo, IntList tail) {
  if (todo.isEmpty())
    return Stream.of(tail);
  else
    return todo.stream().boxed()
    .flatMap(r -> perms(minus(todo, r), new IntList(r, tail)));
}
```

```
public static Stream<IntList> perms(int n) {
   BitSet todo = new BitSet(n); todo.flip(0, n);
   return perms(todo, null);
}
```

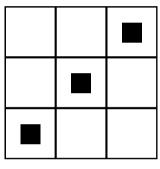
{ 0, ..., n-1 }

Empty permutation []

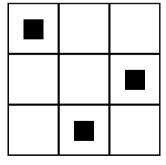
A closer look at generation for n=3

```
(\{0,1,2\},[])
 (\{1,2\},[0])
   (\{2\}, [1,0])
       (\{\}, [2,1,0])
                        Output to stream
   (\{1\}, [2,0])
       (\{\}, [1,2,0])
                        Output to stream
 (\{0,2\},[1])
   ({2}, [0,1])
       (\{\}, [2,0,1])
                       Output to stream
   ({0}, [2,1])
       (\{\}, [0,2,1])
                        Output to stream
 (\{0,1\},[2])
```

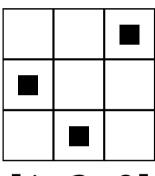
A permutation is a rook (tårn) placement on a chessboard



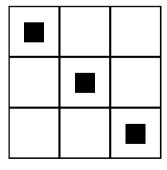
[2, 1, 0]



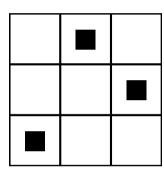
[0, 2, 1]



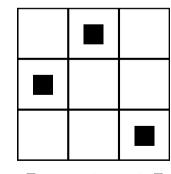
[1, 2, 0]



[0, 1, 2]



[2, 0, 1]



[1, 0, 2]

Solutions to the n-queens problem

- For queens, just take diagonals into account:
 - consider only r that are safe for the partial solution

```
public static Stream<IntList> queens(BitSet todo, IntList tail)
  if (todo.isEmpty())
                                        Diagonal
    return Stream.of(tail);
  else
                                         check
    return todo.stream()
      .filter(r -> safe(r, tail)).boxed()
      .flatMap(r -> queens(minus(todo, r), new IntList(r, tail))
         public static boolean safe(int mid, IntList tail) {
           return safe(mid+1, mid-1, tail);
                                                               .parallel()
         public static boolean safe(int d1, int d2, IntList tail) {
           return tail==null || d1!=tail.item && d2!=tail.item && safe(d1+1, d2-1, tail.next);
```

- Simple, and parallelizable for free, 3.5 x faster
- Solve or generate sudokus: much the same

Versatility of streams

- Many uses of a stream of solutions
 - Print the number of solutions
 System.out.println(queens(8).count());
 - Print all solutions
 queens(8).forEach(System.out::println);
 - Print an arbitrary solution (if there is one)
 System.out.println(queens(8).findAny());
 - Print the 20 first solutions
 queens(8).limit(20).forEach(System.out::println);
- Much harder in an imperative version
- Separation of concerns (Dijkstra): production of solutions versus consumption of solutions

Example174.java

Streams for quasi-infinite sequences

- van der Corput numbers
 - 1/2, 1/4, 3/4, 1/8, 5/8, 3/8, 7/8, 1/16, ...
 - Dense and uniform in interval [0, 1]
 - For simulation and finance, Black-Scholes options
- Trick: v d Corput numbers as base-2 fractions
 0.1, 0.01, 0.11, 0.001, 0.101, 0.011, 0.111 ...
 are bit-reversals of 1, 2, 3, 4, 5, 6, 7, ... in binary

```
public static DoubleStream vanDerCorput() {
   return IntStream.range(1, 31).asDoubleStream()
        .flatMap(b -> bitReversedRange((int)b));
}

private static DoubleStream bitReversedRange(int b) {
   final long bp = Math.round(Math.pow(2, b));
   return LongStream.range(bp/2, bp)
        .mapToDouble(i -> (double)(bitReverse((int)i) >>> (32-b)) / bp);
}
```

Collectors: aggregation of streams

- To format an IntList as string "[2, 3, 5, 7]"
 - Convert the list to an IntStream
 - Convert each element to get Stream<String>
 - Use a predefined Collector to build final result

```
public static String toString(IntList xs) {
   StringBuilder sb = new StringBuilder();
   sb.append("[");
   boolean first = true;
   while (xs != null) {
      if (!first)
            sb.append(", ");
      first = false;
      sb.append(xs.item);
      xs = xs.next;
   }
   return sb.append("]").toString();
}
```

The alternative "direct" solution requires care and cleverness

Java 8 stream properties

- Some stream dimensions
 - Finite vs infinite
 - Lazily generated (by iterate, generate, ...)
 vs eagerly generated (stream builders)
 - Ordered (map, filter, limit ... preserve element order) vs unordered
 - Sequential (all elements processed on one thread)
 vs parallel
- Java streams
 - can be lazily generated, like Haskell lists
 - but are use-once, unlike Haskell lists
 - reduces risk of space leaks
 - limits expressiveness, harder to compute average ...

How are Java streams implemented?

Spliterators

```
interface Spliterator<T> {
  long estimateSize();
  void forEachRemaining(Consumer<T> action);
  boolean tryAdvance(Consumer<T> action);
  void Spliterator<T> trySplit();
}
```

Many method calls (well inlined/fused by the JIT)

Parallelization

- Divide stream into chunks using trysplit
- Process each chunk in a task (Haskell "spark")
- Run on thread pool using work-stealing queues
- ... thus similar to Haskell parBuffer/parListChunk

Example25.java

Parallel (functional) array operations

- Simulating random motion on a line
 - Take n random steps of length at most [-1, +1]:

- Compute the positions at end of each step: a[0], a[0]+a[1], a[0]+a[1]+a[2], ...

```
Arrays.parallelPrefix(a, (x,y) -> x+y);
```

NB: Updates array a

- Find the maximal absolute distance from start:

- A lot done, fast, without loops or assignments
 - Just arrays and streams and functions

Array and streams and parallel ...

Associative array aggregation

```
Arrays.parallelPrefix(a, (x,y) -> x+y);
```

- Such operations can be parallelized well
 - So-called prefix scans (Blelloch 1990)
- Streams and arrays complement each other
- Streams: lazy, possibly infinite, non-materialized, use-once, parallel pipelines
- Array: eager, always finite, materialized, use-many-times, parallel prefix scans

Some problems with Java streams

- Streams are use-once & have other restrictions
 - Probably to permit easy parallelization
- Hard to create lazy finite streams
 - Probably to allow high-performance implementation
- Difficult to control resource consumption
- A single side-effect may mess all up completely
- Sometimes .parallel() hurts performance a lot
 - See exercise
 - And strange behavior, in parallel + limit in Sudoku generator
- Laziness in Java is subtle, easily goes wrong:

2P

A multicore performance mystery

K-means clustering 2P: Assign – Update –
 Assign – Update … till convergence

```
Pseudocode
while (!converged) {
                                                                           TestKMeansSolution.java
  let taskCount parallel tasks do {
                                                     Assign
    final int from = \ldots, to = \ldots;
    for (int pi=from; pi<to; pi++)</pre>
      myCluster[pi] = closest(points[pi], clusters);
  let taskCount parallel tasks do {
                                                     Update
    final int from = \dots, to = \dots;
    for (int pi=from; pi<to; pi++)</pre>
      myCluster[pi].addToMean(points[pi]);
                                                             Imperative
```

- Assign: writes a point to myCluster[pi]
- Update: calls addToMean on myCluster[pi]

A multicore performance mystery

- "Improved" version 2Q:
 - call addToMean directly on point
 - instead of first writing it to myCluster array

```
while (!converged) {
   let taskCount parallel tasks do {
     final int from = ..., to = ...;
     for (int pi=from; pi<to; pi++)
        closest(points[pi], clusters).addToMean(points[pi]);
   }
   ...
}</pre>
```

Performance of k-means clustering

- Sequential: as you would expect, 5% speedup
- Parallel: surprisingly bad!

	2P	2Q	2Q/2P	
Sequential	4.240	4.019	0.95	Bad
4-core parallel	1.310	2.234	1.70	
24-core parallel	0.852	6.587	7.70	Very
Time in seconds for 200,	bad			

Q: WHY is the "improved" code slower?

A: Cache invalidation and false sharing

The Point and Cluster classes

```
class Point {
  public final double x, y;
}
```

```
static class Cluster extends ClusterBase {
  private volatile Point mean;
  private double sumx, sumy;
  private int count;
  public synchronized void addToMean(Point p) {
    sumx += p.x;
    sumy += p.y;
    count++;
  }
  ...
}
```

mean sum	sumy	count
----------	------	-------

Cluster object layout (maybe)

KMeans 2P

- Assignment step
 - Reads each Cluster's mean field 200,000 times
 - Writes only myCluster array segments, separately
 - Takes no locks at all
- Update step
 - Calls addToMean 200,000 times
 - Writes the 81 clusters' sumx, sumy, count fields
 200,000 times in total
 - Takes Cluster object locks 200,000 times

KMeans 2Q

- Unified loop
 - Reads each Cluster's mean field 200,000 times
 - Calls addToMean 200,000 times and writes the sumx, sumy, count fields 200,000 times in total
 - Takes Cluster object locks 200,000 times
- Problem in 2Q:
 - mean reads are mixed with sumx, sumy, ... writes
 - The writes invalidate the cached mean field
 - The 200,000 mean field reads become slower
 - False sharing: mean and sumx on same cache line
 - (A problem on Intel i7, not on 20 x slower ARM A7)
- See http://www.itu.dk/people/sestoft/papers/cpucache-20170319.pdf

Parallel streams to the rescue, 3P 3P

```
while (!converged) {
  final Cluster[] clustersLocal = clusters;
  Map<Cluster, List<Point>> groups =
                                                                    Assign
    Arrays.stream(points).parallel()
          .collect(Collectors.groupingBy(p -> closest(p,clustersLocal)));
  clusters = groups.entrySet().stream().parallel()
    .map(kv -> new Cluster(kv.getKey().getMean(), kv.getValue()))
    .toArray(Cluster[]::new);
  Cluster[] newClusters =
                                                                   Update
    Arrays.stream(clusters).parallel()
          .map(Cluster::computeMean).toArray(Cluster[]::new);
  converged = Arrays.equals(clusters, newClusters);
  clusters = newClusters;
                                                                 Functional
```

	2P	2Q	3P
Sequential	4.240	4.019	5.353
4-core parallel i7	1.310	2.234	1.350
24-core parallel Xeon	0.852	6.587	0.553

Time in seconds for 200,000 points, 81 clusters, 1/8/48 tasks, 108 iterations

Exercise: Streams & floating-point sum

Compute series sum: for N=999,999,999

$$\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{N}$$

For-loop, forwards summation

```
double sum = 0.0;
for (int i=1; i<N; i++)
  sum += 1.0/i;</pre>
```

For-loop, backwards summation

Different results!

```
double sum = 0.0;
for (int i=1; i<N; i++)
  sum += 1.0/(N-i);</pre>
```

- Could make a DoubleStream, and use .sum()
- Or *parallel* DoubleStream and .sum()

Different results?

This week

Reading

- Java Precisely 3rd ed. § 11.13, 11.14, 23, 24, 25
- Optional:
 - http://www.itu.dk/people/sestoft/papers/benchmarking.pdf
 - http://www.itu.dk/people/sestoft/papers/cpucache-20170319.pdf

Exercises

- Extend immutable list class with functional programming; use parallel array operations; use streams of words and streams of numbers
- Alternatively: Make a faster and more scalable kmeans clustering implementation, if possible, in any language