## Exercise sheet 9

- Design a Turing machine to add two numbers in binary. More specifically, givan an input of the form 101+10, the tape should finally have 101+10=111 written on it. You could try to do this on a multi-tape Turing machine since any one can always then build a single tape one that will simulate it.
- 2. Show that if we allow a Turing machine's head to stay where it is, i.e. the set of possible directions for the head are  $\{L, R, S\}$ , then any computation that it can perform, can also be performed by an ordinary Turing machine.
- 3. Show that this language is undecidable:

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\{\langle T \rangle \mid T \text{ is a Turing machine that outputs } 1011\}
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4. Show that this language and its complement are both undecidable:

$$\{\langle T_1, T_2 \rangle \mid T_1, T_2 \text{ are Turing machines and } L(T_1) = L(T_2)\}$$

- 5. Prove that the set of C programs (over the obvious alphabet) that run the printer is undecidable.
- 6. Exercise 5.16 from the third edition of Sipser's book (6.28 from the second edition) on Rice's theorem.