

## Exercise sheet 4

1. Design a non-deterministic finite state automaton over the alphabet  $\Sigma = \{0, 1\}$  that will recognize the following languages (try to design a deterministic one too to get a feel for how much easier it is to design a non-deterministic one).
  - a) Strings with the  $n$ th last character 0, for any natural number  $n$ .
  - b) Strings that begin with 01.
2. If  $w$  is a string, let  $w^*$  denote the string  $ww...w$ , i.e.  $w$  repeated any finite number of times. Design non-deterministic finite state automata to recognize the following languages over  $\Sigma := \{0, 1\}$ .
  - a) Strings of the form  $0^*$
  - b) Strings of the form  $11^*$
  - c) Strings of the form  $101(010)^*11$
3. If  $L_1$  and  $L_2$  are regular languages, design a non-deterministic finite state automaton that recognizes:
  - a)  $L_1 \cup L_2$
  - b)  $L_1 \circ L_2 := \{xy \mid x \in L_1, y \in L_2\}$  (i.e. the concatenation of a string from  $L_1$  with a string from  $L_2$ )
  - c)  $L_1^* := \{x_1x_2...x_n \mid x_i \in L_1\}$  (i.e. concatenation of finitely many strings from the language)
4. Prove that any language that can be recognized by a non-deterministic finite state automaton can also be recognized by a deterministic one. Therefore, a language is regular if and only if it can be recognized by a non-deterministic finite state automaton.
5. Prove that if a language,  $L$ , is regular then the language,  $L'$ , obtained by reversing every string of  $L$  is also regular.

**to be completed**