## Exercise sheet 4

Set theory and Logic, MTH303

- 1. Prove that if X is a set, then so is its successor  $X^+$ .
- 2. Consider a subset A of  $\omega$ . Note that A is a family of sets. Prove that if  $\cup A = A$ , then  $A = \omega$
- 3. Recall the (recursive) definition of m+n, for  $m,n\in\omega$ . Prove that l+(m+n)=(l+m)+n for any  $l,m,n\in\omega$
- 4. Recall the (recursive) definition of m.n, for  $m,n\in\omega$ . Prove that l.(m.n)=(l.m).n for any  $l,m,n\in\omega$ . Also prove m.n=n.m
- 5. Prove that if m + a = n + a for some  $m, n, a \in \omega$ , then m = n.
- 6. Prove that if m.a = n.a for some  $m, n, a \in \omega$ , where  $a \neq 0$ , then m = n.