## Exercise sheet 1

Set theory and Logic, MTH303

- 1. Use truth tables to prove that the following are tautologies:
  - (a)  $P \to (Q \to P)$
  - (b)  $(P \to (Q \to R)) \to ((P \to Q) \to [P \to R])$
  - (c)  $(\neg P \rightarrow \neg Q) \rightarrow (Q \rightarrow P)$
- 2. Show that the first FL axiom, along with modus ponens, allows you to show:  $p, q \vdash p$ .
- 3. Show that the second FL axiom, along with modus ponens, allows you to show:  $p \to q, q \to r, p \vdash r$
- 4. Show that the third FL axiom, along with modus ponens, allows you to show:  $\neg q \rightarrow \neg p, p \vdash q$  (Does this remind you of proving by considering the contrapositive?)