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Theorem. *A connected graph is Euler if and only if it is the union of “edge disjoint” cycles.*

Fleury's algorithm

1. Choose any vertex. $W_0 = v$
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