Q1

May 27, 2017

1 Implementing a Neural Network

In this exercise we will develop a neural network with fully-connected layers to perform classification, and test it out on the CIFAR-10 dataset.

```
In [22]: # A bit of setup

         import numpy as np
         import matplotlib.pyplot as plt

         %matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         plt.rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'

         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-
         %load_ext autoreload
         %autoreload 2

         def rel_error(x, y):
           """ returns relative error """
           return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
The autoreload extension is already loaded. To reload it, use:
  %reload_ext autoreload
```

The neural network parameters will be stored in a dictionary (`model` below), where the keys are the parameter names and the values are numpy arrays. Below, we initialize toy data and a toy model that we will use to verify your implementations.

```
In [23]: # Create some toy data to check your implementations
         input_size = 4
         hidden_size = 10
         num_classes = 3
         num_inputs = 5
```

```python
def init_toy_model():
  model = {}
  model['W1'] = np.linspace(-0.2, 0.6, num=input_size*hidden_size).reshape
  model['b1'] = np.linspace(-0.3, 0.7, num=hidden_size)
  model['W2'] = np.linspace(-0.4, 0.1, num=hidden_size*num_classes).reshap
  model['b2'] = np.linspace(-0.5, 0.9, num=num_classes)
  return model

def init_toy_data():
  X = np.linspace(-0.2, 0.5, num=num_inputs*input_size).reshape(num_inputs
  y = np.array([0, 1, 2, 2, 1])
  return X, y

model = init_toy_model()
X, y = init_toy_data()
```

2 Forward pass: compute scores

Open the file `cs231n/classifiers/neural_net.py` and look at the function `two_layer_net`. This function is very similar to the loss functions you have written for the SVM and Softmax exercises: It takes the data and weights and computes the class scores, the loss, and the gradients on the parameters.

Implement the first part of the forward pass which uses the weights and biases to compute the scores for all inputs.

In [24]:
```python
from cs231n.classifiers.neural_net import two_layer_net

scores = two_layer_net(X, model)
print scores
correct_scores = [[-0.5328368, 0.20031504, 0.93346689],
 [-0.59412164, 0.15498488, 0.9040914 ],
 [-0.67658362, 0.08978957, 0.85616275],
 [-0.77092643, 0.01339997, 0.79772637],
 [-0.89110401, -0.08754544, 0.71601312]]

# the difference should be very small. We get 3e-8
print 'Difference between your scores and correct scores:'
print np.sum(np.abs(scores - correct_scores))
```

```
[[-0.5328368   0.20031504  0.93346689]
 [-0.59412164  0.15498488  0.9040914 ]
 [-0.67658362  0.08978957  0.85616275]
 [-0.77092643  0.01339997  0.79772637]
 [-0.89110401 -0.08754544  0.71601312]]
Difference between your scores and correct scores:
3.84868227808e-08
```

3 Forward pass: compute loss

In the same function, implement the second part that computes the data and regularizaion loss.

In [25]:
```
reg = 0.1
loss, _ = two_layer_net(X, model, y, reg)
correct_loss = 1.38191946092

# should be very small, we get 5e-12
print 'Difference between your loss and correct loss:'
print np.sum(np.abs(loss - correct_loss))
```

```
Difference between your loss and correct loss:
4.67736960275e-12
```

4 Backward pass

Implement the rest of the function. This will compute the gradient of the loss with respect to the variables W1, b1, W2, and b2. Now that you (hopefully!) have a correctly implemented forward pass, you can debug your backward pass using a numeric gradient check:

In [28]:
```
from cs231n.gradient_check import eval_numerical_gradient

# Use numeric gradient checking to check your implementation of the backwa
# If your implementation is correct, the difference between the numeric ar
# analytic gradients should be less than 1e-8 for each of W1, W2, b1, and

loss, grads = two_layer_net(X, model, y, reg)

# these should all be less than 1e-8 or so
for param_name in grads:
  param_grad_num = eval_numerical_gradient(lambda W: two_layer_net(X, mode
  print '%s max relative error: %e' % (param_name, rel_error(param_grad_nu
```

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[[-0.17302699  0.05614786  0.11687913]
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[[-0.1730271   0.05614789  0.11687921]
 [ 0.02635449 -0.14425701  0.11790252]
 [ 0.02569743  0.05529996 -0.08099739]
 [ 0.02502761  0.05483428 -0.07986189]
 [ 0.02432509 -0.14566993  0.12134484]]
[[-0.17302703  0.05614805  0.11687898]
 [ 0.02635459 -0.1442568   0.11790221]
 [ 0.02569755  0.05530022 -0.08099778]
 [ 0.02502775  0.05483459 -0.07986235]
 [ 0.02432525 -0.14566956  0.12134431]]
[[-0.17302696  0.05614767  0.11687929]
 [ 0.02635468 -0.14425731  0.11790263]
 [ 0.02569767  0.05529959 -0.08099726]
 [ 0.02502788  0.05483384 -0.07986172]
 [ 0.0243254  -0.14567044  0.12134504]]
[[-0.17302707  0.0561477   0.11687936]
 [ 0.02635454 -0.14425726  0.11790272]
 [ 0.02569749  0.05529965 -0.08099713]
 [ 0.02502768  0.0548339  -0.07986158]
 [ 0.02432516 -0.14567037  0.12134521]]
[[-0.17302692  0.05614801  0.11687891]
 [ 0.02635474 -0.14425685  0.11790211]
 [ 0.02569773  0.05530016 -0.0809979 ]
```

```
 [ 0.02502796  0.05483453 -0.07986249]
 [ 0.02432549 -0.14566964  0.12134415]]
[[-0.17302686  0.05614781  0.11687904]
 [ 0.02635481 -0.14425711  0.1179023 ]
 [ 0.02569781  0.05529984 -0.08099765]
 [ 0.02502806  0.05483414 -0.0798622 ]
 [ 0.02432559 -0.14567009  0.12134449]]
[[-0.17302712  0.0561479   0.11687922]
 [ 0.02635447 -0.144257    0.11790253]
 [ 0.02569741  0.05529997 -0.08099738]
 [ 0.02502758  0.05483429 -0.07986187]
 [ 0.02432506 -0.14566992  0.12134486]]
[[-0.17302703  0.05614809  0.11687895]
 [ 0.02635458 -0.14425676  0.11790218]
 [ 0.02569755  0.05530027 -0.08099782]
 [ 0.02502774  0.05483465 -0.07986239]
 [ 0.02432524 -0.1456695   0.12134426]]
[[-0.17302695  0.05614763  0.11687932]
 [ 0.02635469 -0.14425736  0.11790266]
 [ 0.02569768  0.05529954 -0.08099721]
 [ 0.02502789  0.05483378 -0.07986168]
 [ 0.02432541 -0.1456705   0.12134509]]
[[-0.17302708  0.05614767  0.11687941]
 [ 0.02635452 -0.1442573   0.11790278]
 [ 0.02569747  0.0552996  -0.08099708]
 [ 0.02502766  0.05483386 -0.07986152]
 [ 0.02432514 -0.14567042  0.12134528]]
[[-0.1730269   0.05614804  0.11687886]
 [ 0.02635475 -0.14425681  0.11790206]
 [ 0.02569775  0.05530021 -0.08099796]
 [ 0.02502798  0.05483457 -0.07986256]
 [ 0.02432551 -0.14566959  0.12134408]]
W2 max relative error: 1.401432e-09
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
 [ 0.02569761  0.0552999  -0.08099752]
 [ 0.02502782  0.05483422 -0.07986204]
 [ 0.02432532 -0.14567     0.12134468]]
[[-0.17302676  0.05614778  0.11687898]
 [ 0.02635487 -0.14425713  0.11790226]
 [ 0.02569783  0.05529983 -0.08099767]
 [ 0.02502804  0.05483415 -0.07986219]
 [ 0.02432554 -0.14567007  0.12134453]]
[[-0.17302723  0.05614793  0.11687929]
 [ 0.02635441 -0.14425698  0.11790257]
 [ 0.02569739  0.05529998 -0.08099736]
 [ 0.0250276   0.05483428 -0.07986189]
 [ 0.02432511 -0.14566994  0.12134483]]
```

```
[[-0.17302707  0.05614826  0.11687881]
 [ 0.02635456 -0.14425666  0.11790209]
 [ 0.02569754  0.05530031 -0.08099784]
 [ 0.02502775  0.05483461 -0.07986237]
 [ 0.02432526 -0.14566961  0.12134435]]
[[-0.17302692  0.05614745  0.11687946]
 [ 0.02635471 -0.14425746  0.11790275]
 [ 0.02569768  0.0552995  -0.08099719]
 [ 0.02502789  0.05483382 -0.07986171]
 [ 0.02432539 -0.1456704   0.12134501]]
[[-0.17302715  0.05614753  0.11687962]
 [ 0.02635448 -0.14425739  0.1179029 ]
 [ 0.02569746  0.05529958 -0.08099703]
 [ 0.02502767  0.05483389 -0.07986156]
 [ 0.02432518 -0.14567033  0.12134516]]
[[-0.17302683  0.05614819  0.11687865]
 [ 0.02635479 -0.14425673  0.11790194]
 [ 0.02569776  0.05530023 -0.080998  ]
 [ 0.02502797  0.05483455 -0.07986252]
 [ 0.02432547 -0.14566967  0.1213442 ]]
b2 max relative error: 7.311059e-11
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
 [ 0.02569761  0.0552999  -0.08099752]
 [ 0.02502782  0.05483422 -0.07986204]
 [ 0.02432532 -0.14567     0.12134468]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
 [ 0.02569761  0.0552999  -0.08099752]
 [ 0.02502782  0.05483422 -0.07986204]
 [ 0.02432532 -0.14567     0.12134468]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
 [ 0.02569761  0.0552999  -0.08099752]
 [ 0.02502782  0.05483422 -0.07986204]
 [ 0.02432532 -0.14567     0.12134468]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
 [ 0.02569761  0.0552999  -0.08099752]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
 [ 0.02569761  0.0552999  -0.08099752]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
```

```
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425706  0.11790242]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635463 -0.14425706  0.11790243]
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302699  0.05614786  0.11687913]
 [ 0.02635464 -0.14425705  0.11790241]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
[[-0.173027    0.05614785  0.11687915]
 [ 0.02635463 -0.14425706  0.11790243]
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302698  0.05614786  0.11687912]
 [ 0.02635464 -0.14425705  0.11790241]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
[[-0.173027    0.05614785  0.11687915]
 [ 0.02635463 -0.14425706  0.11790243]
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302698  0.05614786  0.11687912]
 [ 0.02635464 -0.14425705  0.11790241]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
[[-0.173027    0.05614785  0.11687915]
 [ 0.02635463 -0.14425706  0.11790243]
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302698  0.05614786  0.11687912]
 [ 0.02635464 -0.14425705  0.11790241]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
```

```
[[-0.173027    0.05614785  0.11687915]
 [ 0.02635463 -0.14425706  0.11790243]
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302698  0.05614786  0.11687912]
 [ 0.02635464 -0.14425705  0.11790241]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
[[-0.173027    0.05614785  0.11687915]
 [ 0.02635463 -0.14425706  0.11790243]
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302698  0.05614786  0.11687912]
 [ 0.02635464 -0.14425705  0.11790241]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
[[-0.173027    0.05614785  0.11687915]
 [ 0.02635463 -0.14425706  0.11790243]
 [ 0.0256976   0.0552999  -0.0809975 ]
 [ 0.02502781  0.05483421 -0.07986202]
 [ 0.02432532 -0.14567001  0.12134469]]
[[-0.17302698  0.05614786  0.11687912]
 [ 0.02635464 -0.14425705  0.11790241]
 [ 0.02569762  0.05529991 -0.08099753]
 [ 0.02502783  0.05483422 -0.07986205]
 [ 0.02432533 -0.14567     0.12134467]]
b1 max relative error: 2.746125e-08
```

5 Train the network

To train the network we will use SGD with Momentum. Last assignment you implemented vanilla SGD. You will now implement the momentum update and the RMSProp update. Open the file `classifier_trainer.py` and familiarze yourself with the `ClassifierTrainer` class. It performs optimization given an arbitrary cost function data, and model. By default it uses vanilla SGD, which we have already implemented for you. First, run the optimization below using Vanilla SGD:

```
In [29]: from cs231n.classifier_trainer import ClassifierTrainer

         model = init_toy_model()
         trainer = ClassifierTrainer()
         # call the trainer to optimize the loss
```

```
# Notice that we're using sample_batches=False, so we're performing Gradie
best_model, loss_history, _, _ = trainer.train(X, y, X, y,
                                               model, two_layer_net,
                                               reg=0.001,
                                               learning_rate=1e-1, momentum=
                                               update='sgd', sample_batches=
                                               num_epochs=100,
                                               verbose=False)
print 'Final loss with vanilla SGD: %f' % (loss_history[-1], )
```

```
starting iteration  0
starting iteration  10
starting iteration  20
starting iteration  30
starting iteration  40
starting iteration  50
starting iteration  60
starting iteration  70
starting iteration  80
starting iteration  90
Final loss with vanilla SGD: 0.940686
```

Now fill in the **momentum update** in the first missing code block inside the `train` function, and run the same optimization as above but with the momentum update. You should see a much better result in the final obtained loss:

```
In [30]: model = init_toy_model()
         trainer = ClassifierTrainer()
         # call the trainer to optimize the loss
         # Notice that we're using sample_batches=False, so we're performing Gradie
         best_model, loss_history, _, _ = trainer.train(X, y, X, y,
                                                        model, two_layer_net,
                                                        reg=0.001,
                                                        learning_rate=1e-1, momentum=
                                                        update='momentum', sample_bat
                                                        num_epochs=100,
                                                        verbose=False)
         correct_loss = 0.494394
         print 'Final loss with momentum SGD: %f. We get: %f' % (loss_history[-1],
```

```
starting iteration  0
starting iteration  10
starting iteration  20
starting iteration  30
starting iteration  40
starting iteration  50
starting iteration  60
starting iteration  70
```

```
starting iteration  80
starting iteration  90
Final loss with momentum SGD: 0.494394. We get: 0.494394
```

Now also implement the **RMSProp** update rule inside the `train` function and rerun the optimization:

```
In [38]: model = init_toy_model()
         trainer = ClassifierTrainer()
         # call the trainer to optimize the loss
         # Notice that we're using sample_batches=False, so we're performing Gradie
         best_model, loss_history, _, _ = trainer.train(X, y, X, y,
                                                  model, two_layer_net,
                                                  reg=0.001,
                                                  learning_rate=1e-1, momentum=
                                                  update='rmsprop', sample_batc
                                                  num_epochs=100,
                                                  verbose=False)
         correct_loss = 0.439368
         print 'Final loss with RMSProp: %f. We get: %f' % (loss_history[-1], corre
```

```
starting iteration  0
starting iteration  10
starting iteration  20
starting iteration  30
starting iteration  40
starting iteration  50
starting iteration  60
starting iteration  70
starting iteration  80
starting iteration  90
Final loss with RMSProp: 1.125201. We get: 0.439368
```

6 Load the data

Now that you have implemented a two-layer network that passes gradient checks, it's time to load up our favorite CIFAR-10 data so we can use it to train a classifier.

```
In [14]: from cs231n.data_utils import load_CIFAR10

         def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=100
             """
             Load the CIFAR-10 dataset from disk and perform preprocessing to prepa
             it for the two-layer neural net classifier. These are the same steps a
             we used for the SVM, but condensed to a single function.
             """
```

```
        # Load the raw CIFAR-10 data
        cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
        X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

        # Subsample the data
        mask = range(num_training, num_training + num_validation)
        X_val = X_train[mask]
        y_val = y_train[mask]
        mask = range(num_training)
        X_train = X_train[mask]
        y_train = y_train[mask]
        mask = range(num_test)
        X_test = X_test[mask]
        y_test = y_test[mask]

        # Normalize the data: subtract the mean image
        mean_image = np.mean(X_train, axis=0)
        X_train -= mean_image
        X_val -= mean_image
        X_test -= mean_image

        # Reshape data to rows
        X_train = X_train.reshape(num_training, -1)
        X_val = X_val.reshape(num_validation, -1)
        X_test = X_test.reshape(num_test, -1)

        return X_train, y_train, X_val, y_val, X_test, y_test


    # Invoke the above function to get our data.
    X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
    print 'Train data shape: ', X_train.shape
    print 'Train labels shape: ', y_train.shape
    print 'Validation data shape: ', X_val.shape
    print 'Validation labels shape: ', y_val.shape
    print 'Test data shape: ', X_test.shape
    print 'Test labels shape: ', y_test.shape
```

```
Train data shape:  (49000L, 3072L)
Train labels shape:  (49000L,)
Validation data shape:  (1000L, 3072L)
Validation labels shape:  (1000L,)
Test data shape:  (1000L, 3072L)
Test labels shape:  (1000L,)
```

7 Train a network

To train our network we will use SGD with momentum. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
In [18]: from cs231n.classifiers.neural_net import init_two_layer_model

         model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, n
         trainer = ClassifierTrainer()
         best_model, loss_history, train_acc, val_acc = trainer.train(X_train, y_tr
                                                       model, two_layer_net,
                                                       num_epochs=5, reg=1.0,
                                                       momentum=0.9, learning_rate_d
                                                       learning_rate=1e-5, verbose=T
```

```
starting iteration  0
Finished epoch 0 / 5: cost 2.302593, train: 0.078000, val 0.072000, lr 1.000000e-05
starting iteration  10
starting iteration  20
starting iteration  30
starting iteration  40
starting iteration  50
starting iteration  60
starting iteration  70
starting iteration  80
starting iteration  90
starting iteration  100
starting iteration  110
starting iteration  120
starting iteration  130
starting iteration  140
starting iteration  150
starting iteration  160
starting iteration  170
starting iteration  180
starting iteration  190
starting iteration  200
starting iteration  210
starting iteration  220
starting iteration  230
starting iteration  240
starting iteration  250
starting iteration  260
starting iteration  270
starting iteration  280
starting iteration  290
starting iteration  300
```

```
starting iteration  310
starting iteration  320
starting iteration  330
starting iteration  340
starting iteration  350
starting iteration  360
starting iteration  370
starting iteration  380
starting iteration  390
starting iteration  400
starting iteration  410
starting iteration  420
starting iteration  430
starting iteration  440
starting iteration  450
starting iteration  460
starting iteration  470
starting iteration  480
Finished epoch 1 / 5: cost 2.288314, train: 0.161000, val 0.177000, lr 9.500000e-06
starting iteration  490
starting iteration  500
starting iteration  510
starting iteration  520
starting iteration  530
starting iteration  540
starting iteration  550
starting iteration  560
starting iteration  570
starting iteration  580
starting iteration  590
starting iteration  600
starting iteration  610
starting iteration  620
starting iteration  630
starting iteration  640
starting iteration  650
starting iteration  660
starting iteration  670
starting iteration  680
starting iteration  690
starting iteration  700
starting iteration  710
starting iteration  720
starting iteration  730
starting iteration  740
starting iteration  750
starting iteration  760
starting iteration  770
```

```
starting iteration  780
starting iteration  790
starting iteration  800
starting iteration  810
starting iteration  820
starting iteration  830
starting iteration  840
starting iteration  850
starting iteration  860
starting iteration  870
starting iteration  880
starting iteration  890
starting iteration  900
starting iteration  910
starting iteration  920
starting iteration  930
starting iteration  940
starting iteration  950
starting iteration  960
starting iteration  970
Finished epoch 2 / 5: cost 2.098012, train: 0.264000, val 0.245000, lr 9.025000e-06
starting iteration  980
starting iteration  990
starting iteration  1000
starting iteration  1010
starting iteration  1020
starting iteration  1030
starting iteration  1040
starting iteration  1050
starting iteration  1060
starting iteration  1070
starting iteration  1080
starting iteration  1090
starting iteration  1100
starting iteration  1110
starting iteration  1120
starting iteration  1130
starting iteration  1140
starting iteration  1150
starting iteration  1160
starting iteration  1170
starting iteration  1180
starting iteration  1190
starting iteration  1200
starting iteration  1210
starting iteration  1220
starting iteration  1230
starting iteration  1240
```

```
starting iteration  1250
starting iteration  1260
starting iteration  1270
starting iteration  1280
starting iteration  1290
starting iteration  1300
starting iteration  1310
starting iteration  1320
starting iteration  1330
starting iteration  1340
starting iteration  1350
starting iteration  1360
starting iteration  1370
starting iteration  1380
starting iteration  1390
starting iteration  1400
starting iteration  1410
starting iteration  1420
starting iteration  1430
starting iteration  1440
starting iteration  1450
starting iteration  1460
Finished epoch 3 / 5: cost 1.948069, train: 0.313000, val 0.298000, lr 8.573750e-0
starting iteration  1470
starting iteration  1480
starting iteration  1490
starting iteration  1500
starting iteration  1510
starting iteration  1520
starting iteration  1530
starting iteration  1540
starting iteration  1550
starting iteration  1560
starting iteration  1570
starting iteration  1580
starting iteration  1590
starting iteration  1600
starting iteration  1610
starting iteration  1620
starting iteration  1630
starting iteration  1640
starting iteration  1650
starting iteration  1660
starting iteration  1670
starting iteration  1680
starting iteration  1690
starting iteration  1700
starting iteration  1710
```

```
starting iteration  1720
starting iteration  1730
starting iteration  1740
starting iteration  1750
starting iteration  1760
starting iteration  1770
starting iteration  1780
starting iteration  1790
starting iteration  1800
starting iteration  1810
starting iteration  1820
starting iteration  1830
starting iteration  1840
starting iteration  1850
starting iteration  1860
starting iteration  1870
starting iteration  1880
starting iteration  1890
starting iteration  1900
starting iteration  1910
starting iteration  1920
starting iteration  1930
starting iteration  1940
starting iteration  1950
Finished epoch 4 / 5: cost 1.862223, train: 0.342000, val 0.337000, lr 8.145063e-06
starting iteration  1960
starting iteration  1970
starting iteration  1980
starting iteration  1990
starting iteration  2000
starting iteration  2010
starting iteration  2020
starting iteration  2030
starting iteration  2040
starting iteration  2050
starting iteration  2060
starting iteration  2070
starting iteration  2080
starting iteration  2090
starting iteration  2100
starting iteration  2110
starting iteration  2120
starting iteration  2130
starting iteration  2140
starting iteration  2150
starting iteration  2160
starting iteration  2170
starting iteration  2180
```

```
starting iteration  2190
starting iteration  2200
starting iteration  2210
starting iteration  2220
starting iteration  2230
starting iteration  2240
starting iteration  2250
starting iteration  2260
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starting iteration  2390
starting iteration  2400
starting iteration  2410
starting iteration  2420
starting iteration  2430
starting iteration  2440
Finished epoch 5 / 5: cost 1.701112, train: 0.343000, val 0.367000, lr 7.737809e-06
finished optimization. best validation accuracy: 0.367000
```

8 Debug the training

With the default parameters we provided above, you should get a validation accuracy of about 0.37 on the validation set. This isn't very good.

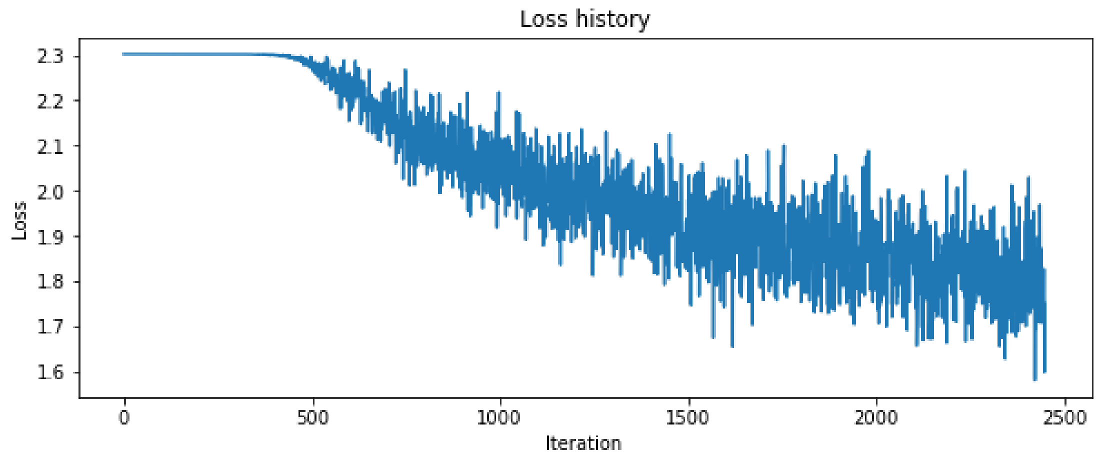
One strategy for getting insight into what's wrong is to plot the loss function and the accuracies on the training and validation sets during optimization.

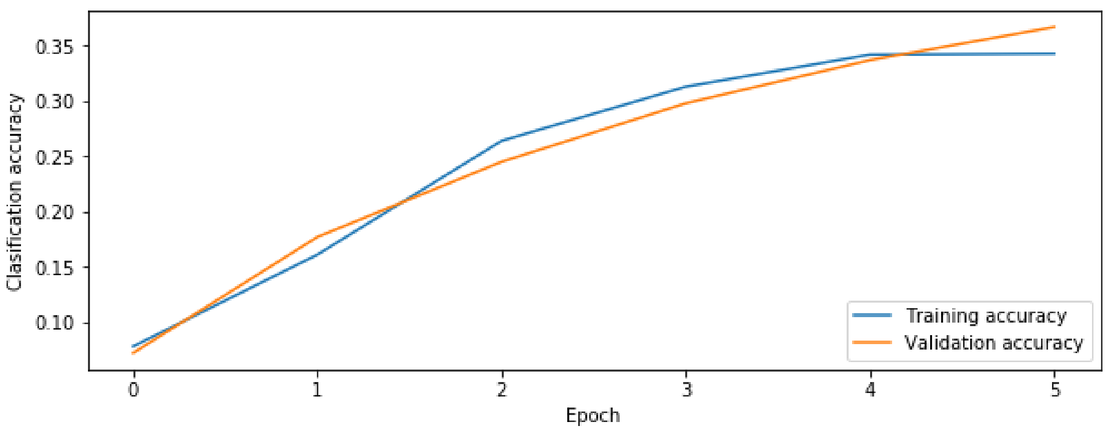
Another strategy is to visualize the weights that were learned in the first layer of the network. In most neural networks trained on visual data, the first layer weights typically show some visible structure when visualized.

In [19]:
```
# Plot the loss function and train / validation accuracies
plt.subplot(2, 1, 1)
plt.plot(loss_history)
plt.title('Loss history')
plt.xlabel('Iteration')
plt.ylabel('Loss')
```

```
    plt.subplot(2, 1, 2)
    plt.plot(train_acc)
    plt.plot(val_acc)
    plt.legend(['Training accuracy', 'Validation accuracy'], loc='lower right'
    plt.xlabel('Epoch')
    plt.ylabel('Clasification accuracy')
```

Out[19]: <matplotlib.text.Text at 0x80eccc0>



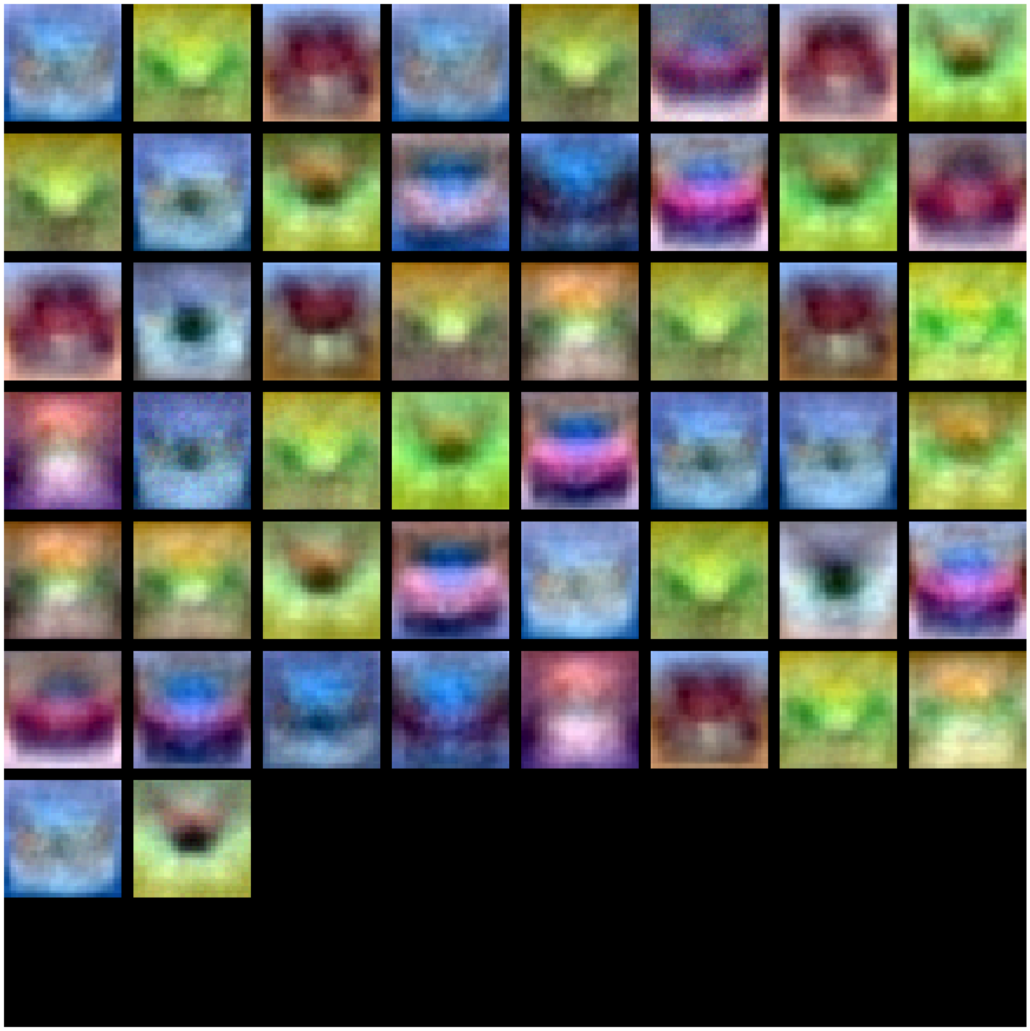


In [20]:
```
from cs231n.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(model):
    plt.imshow(visualize_grid(model['W1'].T.reshape(-1, 32, 32, 3), paddir
    plt.gca().axis('off')
    plt.show()

show_net_weights(model)
```



9 Tune your hyperparameters

What's wrong?. Looking at the visualizations above, we see that the loss is decreasing more or less linearly, which seems to suggest that the learning rate may be too low. Moreover, there is no gap between the training and validation accuracy, suggesting that the model we used has low capacity, and that we should increase its size. On the other hand, with a very large model we would expect to see more overfitting, which would manifest itself as a very large gap between the training and validation accuracy.

Tuning. Tuning the hyperparameters and developing intuition for how they affect the final performance is a large part of using Neural Networks, so we want you to get a lot of practice. Below, you should experiment with different values of the various hyperparameters, including hidden layer size, learning rate, numer of training epochs, and regularization strength. You might also consider tuning the momentum and learning rate decay parameters, but you should be able to get good performance using the default values.

Approximate results. You should be aim to achieve a classification accuracy of greater than 50% on the validation set. Our best network gets over 56% on the validation set.

Experiment: You goal in this exercise is to get as good of a result on CIFAR-10 as you can, with a fully-connected Neural Network. For every 1% above 56% on the Test set we will award you with one extra bonus point. Feel free implement your own techniques (e.g. PCA to reduce dimensionality, or adding dropout, or adding features to the solver, etc.).

```
In [66]: best_model = None # store the best model into this

         ####################################################################
         # TODO: Tune hyperparameters using the validation set. Store your best tra
         # model in best_model.
         #
         # To help debug your network, it may help to use visualizations similar to
         # ones we used above; these visualizations will have significant qualitati
         # differences from the ones we saw above for the poorly tuned network.
         #
         # Tweaking hyperparameters by hand can be fun, but you might find it usefu
         # write code to sweep through possible combinations of hyperparameters
         # automatically like we did on the previous assignment.
         ####################################################################
         model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, n
         trainer = ClassifierTrainer()
         best_model, loss_history, train_acc, val_acc = trainer.train(X_train, y_tr
                                                  model, two_layer_net,
                                                  num_epochs=28, reg=1.1,
                                                  momentum=0.9, learning_rate_d
                                                  learning_rate=1.5e-4, verbose
         ####################################################################
         #                          END OF YOUR CODE
         ####################################################################
```

```
starting iteration  0
Finished epoch 0 / 28: cost 2.302593, train: 0.113000, val 0.100000, lr 1.500000e-0
starting iteration  10
starting iteration  20
starting iteration  30
starting iteration  40
starting iteration  50
starting iteration  60
starting iteration  70
starting iteration  80
starting iteration  90
starting iteration  100
starting iteration  110
starting iteration  120
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starting iteration  130
starting iteration  140
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starting iteration  200
starting iteration  210
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starting iteration  380
starting iteration  390
starting iteration  400
starting iteration  410
starting iteration  420
starting iteration  430
starting iteration  440
starting iteration  450
starting iteration  460
starting iteration  470
starting iteration  480
Finished epoch 1 / 28: cost 1.580177, train: 0.447000, val 0.420000, lr 1.350000e-0
starting iteration  490
starting iteration  500
starting iteration  510
starting iteration  520
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starting iteration  580
starting iteration  590
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starting iteration  890
starting iteration  900
starting iteration  910
starting iteration  920
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starting iteration  940
starting iteration  950
starting iteration  960
starting iteration  970
Finished epoch 2 / 28: cost 1.780223, train: 0.469000, val 0.452000, lr 1.215000e-0
starting iteration  980
starting iteration  990
starting iteration  1000
starting iteration  1010
starting iteration  1020
starting iteration  1030
starting iteration  1040
starting iteration  1050
starting iteration  1060
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starting iteration  1100
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starting iteration  1460
Finished epoch 3 / 28: cost 1.824917, train: 0.476000, val 0.461000, lr 1.093500e-0
starting iteration  1470
starting iteration  1480
starting iteration  1490
starting iteration  1500
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starting iteration  1530
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starting iteration  1920
starting iteration  1930
starting iteration  1940
starting iteration  1950
Finished epoch 4 / 28: cost 1.774068, train: 0.491000, val 0.449000, lr 9.841500e-0
starting iteration  1960
starting iteration  1970
starting iteration  1980
starting iteration  1990
starting iteration  2000
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starting iteration  2010
starting iteration  2020
starting iteration  2030
starting iteration  2040
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starting iteration  2080
starting iteration  2090
starting iteration  2100
starting iteration  2110
starting iteration  2120
starting iteration  2130
starting iteration  2140
starting iteration  2150
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Finished epoch 5 / 28: cost 1.826170, train: 0.485000, val 0.465000, lr 8.857350e-0
starting iteration  2450
starting iteration  2460
starting iteration  2470
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Finished epoch 6 / 28: cost 1.667484, train: 0.508000, val 0.488000, lr 7.971615e-0
starting iteration  2940
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Finished epoch 7 / 28: cost 1.393923, train: 0.478000, val 0.481000, lr 7.174453e-0
starting iteration  3430
starting iteration  3440
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starting iteration  3900
starting iteration  3910
Finished epoch 8 / 28: cost 1.638118, train: 0.506000, val 0.493000, lr 6.457008e-0
starting iteration  3920
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starting iteration  4370
starting iteration  4380
starting iteration  4390
starting iteration  4400
Finished epoch 9 / 28: cost 1.621459, train: 0.520000, val 0.497000, lr 5.811307e-0
starting iteration  4410
starting iteration  4420
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Finished epoch 10 / 28: cost 1.510799, train: 0.511000, val 0.493000, lr 5.230177e-
starting iteration  4900
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Finished epoch 11 / 28: cost 1.511887, train: 0.521000, val 0.492000, lr 4.707159e-
starting iteration  5390
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Finished epoch 12 / 28: cost 1.623313, train: 0.547000, val 0.506000, lr 4.236443e-
starting iteration  5880
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starting iteration  6360
Finished epoch 13 / 28: cost 1.601677, train: 0.536000, val 0.503000, lr 3.812799e-
starting iteration  6370
starting iteration  6380
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Finished epoch 14 / 28: cost 1.623268, train: 0.539000, val 0.511000, lr 3.431519e-
starting iteration  6860
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Finished epoch 15 / 28: cost 1.421311, train: 0.528000, val 0.494000, lr 3.088367e-
starting iteration  7350
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Finished epoch 16 / 28: cost 1.560554, train: 0.557000, val 0.510000, lr 2.779530e-
starting iteration  7840
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starting iteration  8320
Finished epoch 17 / 28: cost 1.511056, train: 0.555000, val 0.504000, lr 2.501577e-
starting iteration  8330
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starting iteration  8490
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Finished epoch 18 / 28: cost 1.428990, train: 0.523000, val 0.512000, lr 2.251420e-
starting iteration  8820
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starting iteration  9240
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starting iteration  9280
starting iteration  9290
starting iteration  9300
Finished epoch 19 / 28: cost 1.434726, train: 0.550000, val 0.513000, lr 2.026278e-
starting iteration  9310
starting iteration  9320
starting iteration  9330
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starting iteration  9730
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starting iteration  9780
starting iteration  9790
Finished epoch 20 / 28: cost 1.494886, train: 0.537000, val 0.522000, lr 1.823650e-
starting iteration  9800
starting iteration  9810
starting iteration  9820
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starting iteration  9980
starting iteration  9990
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starting iteration  10220
starting iteration  10230
starting iteration  10240
starting iteration  10250
starting iteration  10260
starting iteration  10270
starting iteration  10280
Finished epoch 21 / 28: cost 1.456008, train: 0.579000, val 0.505000, lr 1.641285e-
starting iteration  10290
starting iteration  10300
starting iteration  10310
starting iteration  10320
starting iteration  10330
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starting iteration  10370
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starting iteration  10760
starting iteration  10770
Finished epoch 22 / 28: cost 1.557188, train: 0.558000, val 0.524000, lr 1.477156e-
starting iteration  10780
starting iteration  10790
starting iteration  10800
starting iteration  10810
starting iteration  10820
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starting iteration  11180
starting iteration  11190
starting iteration  11200
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starting iteration  11220
starting iteration  11230
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starting iteration  11260
Finished epoch 23 / 28: cost 1.485863, train: 0.561000, val 0.519000, lr 1.329441e-
starting iteration  11270
starting iteration  11280
starting iteration  11290
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Finished epoch 24 / 28: cost 1.357398, train: 0.545000, val 0.508000, lr 1.196497e-
starting iteration  11760
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starting iteration  12210
starting iteration  12220
starting iteration  12230
starting iteration  12240
Finished epoch 25 / 28: cost 1.380623, train: 0.574000, val 0.525000, lr 1.076847e-
starting iteration  12250
starting iteration  12260
starting iteration  12270
starting iteration  12280
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starting iteration  12730
Finished epoch 26 / 28: cost 1.298217, train: 0.559000, val 0.521000, lr 9.691623e-
starting iteration  12740
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starting iteration  13150
starting iteration  13160
starting iteration  13170
starting iteration  13180
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starting iteration  13200
starting iteration  13210
starting iteration  13220
Finished epoch 27 / 28: cost 1.460846, train: 0.579000, val 0.512000, lr 8.722461e-
starting iteration  13230
starting iteration  13240
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starting iteration  13270
starting iteration  13280
starting iteration  13290
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starting iteration  13300
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starting iteration  13670
starting iteration  13680
starting iteration  13690
starting iteration  13700
starting iteration  13710
Finished epoch 28 / 28: cost 1.371728, train: 0.566000, val 0.523000, lr 7.850214e-
finished optimization. best validation accuracy: 0.525000
```

```
In [ ]: # visualize the weights
        show_net_weights(best_model)
```

10 Run on the test set

When you are done experimenting, you should evaluate your final trained network on the test set.

We will give you extra bonus point for every 1% of accuracy above 56%.

```
In [65]: scores_test = two_layer_net(X_test, best_model)
         print 'Test accuracy: ', np.mean(np.argmax(scores_test, axis=1) == y_test)
```

```
Test accuracy:  0.507
```

```
In [ ]:
```