

HW2

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Q1

Existing			
A	B	C	D
15	6	9	10

Current state:

Available			
A	B	C	D
6	3	5	4

Alloc				
	A	B	C	D
P ₀	2	0	2	1
P ₁	0	1	1	1
P ₂	4	1	0	2
P ₃	1	0	0	1
P ₄	1	1	0	0
P ₅	1	0	1	1

Max				
	A	B	C	D
P ₀	9	5	5	5
P ₁	2	2	3	3
P ₂	7	5	4	4
P ₃	3	3	3	2
P ₄	5	2	2	1
P ₅	4	4	4	4

	Need			
	A	B	C	D
P ₀	7	5	3	4
P ₁	2	1	2	2
P ₂	3	4	4	2
P ₃	2	3	3	1
P ₄	4	1	2	1
P ₅	3	4	3	3

with available (6, 3, 5, 4), we can give the needed (2, 3, 3, 1) to P₃. After P₃ finishes our available becomes (7, 3, 5, 5). with that (2, 1, 2, 2) can be allocated for P₁ and after P₁ finishes our available becomes (7, 4, 6, 6). Then needed resources (3, 4) can be given to P₂ after P₂ finishes available becomes (11, 5, 6, 8) with this P₀ can be given (7, 5, 3, 4) & available becomes (13, 5, 8, 9) then P₄ can run & finish & available becomes (14, 6, 8, 9) finally P₅ can run & finish and available becomes (15, 6, 9, 10) so state is safe

P₃ → P₁ → P₂ → P₀ → P₄ → P₅

(6, 3, 5, 4) → (7, 3, 5, 5) → (7, 4, 6, 6) → (11, 5, 6, 8) → (13, 5, 8, 9) →
→ (14, 6, 8, 9) → (15, 6, 9, 10)

if P_5 requests (3, 2, 3, 3) assume that we allowed it according to Banker's algorithm. Available & Need matrix become

Available			
A	3	C	0
3	1	2	1

	Need			
P_0	7	5	3	4
P_1	2	1	2	2
P_2	3	4	4	2
P_3	2	3	3	1
P_4	4	1	2	1
P_5	0	2	0	0

in this state

none of the processes can suffice their needs completely in order

to finish & release the helded resources. So if P_5 given (3, 2, 3, 3), deadlock occurs - thus according to Banker's Algorithm this request should not be granted in order to avoid deadlock.

Q2

a) if there is no TLB, our EAT formula is

$$EAT = 2 * (150ns) = 300ns$$

since without TLB, we have to access for page table & data/instruction. Thus 2 memory access

b) with TLB our EAT is

$$EAT = ((1 * 150ns + 10ns) * \frac{85}{100}) + (2 * 150ns + 10ns) * \frac{15}{100}$$

$$= \frac{160 * 85}{100} ns + \frac{310 * 15}{100} ns = (136 + 46.5)ns = 182.5ns$$

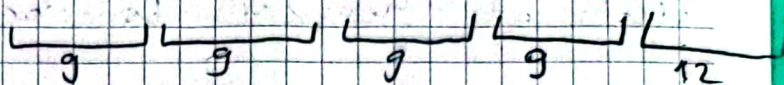
c) if 2 lvl pagm used, without TLB we would need 3 memory accesses for each (1 for each lvl & 1 for data) so;

$$c-a) EAT = 3 * 150ns = 450ns$$

$$c-b) EAT = \underbrace{(1 * 150ns + 10ns) * \frac{85}{100}}_{136ns} + \underbrace{(3 * 150ns + 10ns) * \frac{15}{100}}_{69ns} = 205ns$$

Q3

a) virtual address



physical address is also 48 bits. We know that the offset of the virtual & physical addresses are the same. thus

$$48 - 12 = \underline{36} \text{ bits are used as a frame number in a PTE}$$

b)

page sizes are $2^{12} = 4 \text{ KB} = 4096 \text{ bytes}$

and 4^{th} level table contains $2^9 = 512$ entries so

4^{th} level table can map $2^9 \cdot 2^{12} = 2^{21} = \underline{2 \text{ MB}}$

since each entry is 8 bytes every table is $2^9 \cdot 2^3 = \underline{4 \text{ KB}}$

also 1 entry maps 4 KB from $2^{40} \rightarrow$ offset.

So $2 \text{ MB} = 0x200000$ from starting at $0x000 \dots 0$

for every $0x200000$, we need another 4^{th} lvl table

our 16 MB of virtual memory starts at $0x300000$

so 1 MB mapped with 256 entries in one 4^{th} lvl table
 $[0x300000 - 0x400000]$

and 1 MB mapped with 256 entries in one 4^{th} lvl table
 $[0x500000 - 0x600000]$ half of the entries used

between $[0x400000 - 0x800000]$, 2 4^{th} lvl used with

both containing 512 used entries. In total 4 table to 4^{th} lvl

For 3^{rd} lvl

$0x300000 \rightarrow$	$0's \quad 0011 \quad 0000 \quad 0000$	} 4 entries used inside the 1 3^{rd} lvl page for the 2^{nd} & 1^{st} lvl's
$0x400000 \rightarrow$	$0's \quad 0100 \quad \dots \dots$	
$0x600000 \rightarrow$	$0's \quad 0111 \quad \dots \dots$	
$0x800000 \rightarrow$	$0's \quad 1000 \quad \dots \dots$	

1st 2nd 3rd 4th lvl page used so

$$1 + 1 + 1 + 4 = 7 \text{ pagetable total}$$

$$7 \times 4 \text{ KB} = 28 \text{ KB needed}$$

c) In contrast to part b, all the starting addresses starts at the 2MB boundary. By keeping that in mind;

- 128KB is much less than 2MB so 1 4th lvl page table is enough. Also, only $128KB / 4KB = 32$ entry is used.

- for data segment we need $2^{31} / 2^{21} = 2^{10}$ 4th lvl page since $2^{10} > 2^9$, 1 3rd lvl is not enough we need 2.

data \rightarrow 0x 8 0000 0000
 $=$ $\begin{array}{|c|c|c|c|} \hline 0's & 1000 & 0000 & 0000 & 0000 & 0000 \\ \hline 1^{st} & 2^{nd} & 3^{rd} & 4^{th} & & \end{array}$ Offset

code \rightarrow 0x 1000 0000
 $=$ $\begin{array}{|c|c|c|c|} \hline 0's & 0001 & 0000 & 0000 & 0000 \\ \hline 1^{st} & 2^{nd} & 3^{rd} & 4^{th} & \end{array}$ Offset

stack \rightarrow 0x F 00000 0000
 $=$ $\begin{array}{|c|c|c|c|} \hline 0's & 1111 & 0000 & 0000 & 0000 & 0000 & 0000 & 0000 \\ \hline 1^{st} & 2^{nd} & 3^{rd} & 4^{th} & & & & \end{array}$ Offset

as seen for the stack, we need different 2nd lvl page. Since it is 4MB. it needs $2^{22} / 2^{21} = 2$ 4th lvl page in summary.

code: 1 first, 1 second, 1 third, 1 fourth

data: same, same, 2 third, 2¹⁰ fourth

stack: same, 1 second, 1 third, 2 fourth

$$1 + 2 + 4 + (2^{10} + 3) = (10 + 2^{10}) \text{ page table,}$$

$$(10 + 2^{10}) 4KB \text{ needed} \approx 4MB$$

Q4

underlined one is the victim pointer

2: 2(1)
 4: 2(1) 4(1)
 1: 2(1) 4(1) 1(1)
 3: 3(1) 4(0) 1(0)
 4: 3(1) 4(1) 1(0)

6: 3(0) 6(1) 1(0)
 3: 3(1) 6(1) 1(0)
 6: 3(1) 6(1) 1(0)
 1: 3(1) 6(1) 1(1)
 2: 3(0) 6(0) 2(1)

1: 1(1) 6(0) 2(0)
 5: 1(1) 5(1) 2(0)
 2: 1(1) 5(1) 2(1)
 5: 1(1) 5(1) 2(1)
 4: 1(0) 5(0) 4(1)

1: 1(1) 5(0) 4(0)
 2: 1(0) 2(1) 4(0)
 4: 1(0) 2(1) 4(1)
 3: 3(1) 2(1) 4(0)

Fault

F
F
F
F

F

F

F
F

F

F

F
F

11F

optimal:

Reference string:

2 4 1 3 4 6 3 6 1 2 1 5 2 5 4 1 2 4 3

2 2 2 3 3 3 3 3 3 3 3 5 5 5 4 4 4 4
 4 4 4 4 6 6 6 6 2 2 2 2 2 2 2 2 2
 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1

F F F F F F F F F F F F F F F

9 Fault.

Q5

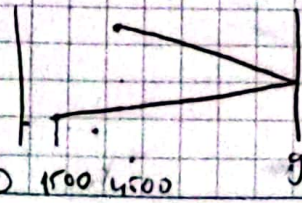
FCTS: 5200 - 4500 = 700
 5200 - 2000 = 3200
 9500 - 2000 = 7500
 9500 - 4300 = 5200
 4300 - 1500 = 2800
 5100 - 1500 = 3600
 3600 - 5100 = 4500
 9600 - 4000 = 5600
 4600 - 4000 = 600

$\Sigma = 33700$

SCAN: Ordered (ascending)

1500, 2000, 4000, 4300, [4500 >], 4600, 5100, 5200, 9500

it will;



go to 9999 while serving requests then it will move to other side again while serving. It stops at 1500 so

$(9999 - 4500) + (9999 - 1500) = 13998$

SSTF: It chooses the closest one.

initially it is at 4500 >>

it will choose: 4300, 4000, 4600, 5100, 5200, 2000, 1500, 9500, 9600
in this order:

so the total: $200 + 300 + 600 + 500 + 100 + 3200 + 500 + 8000 + 100$
 $= 13500$

Q.6

a)

$4\text{KB} / 30\text{MB/s} = 0.130\text{ms}$. This is the transfer time for 4KB. Avg rotational latency is: $((1/(3600/60))\text{s})/2 = 0.083\text{s} = 83\text{ms}$. Then total time to transfer 4KB is $83 + 4 + 0.130 = 87.13\text{ms} = T$. Number of disk I/Os per second $= 1/T = 11$. Throughput: 0.042MB/s

b)

$512 \times 4\text{KB} / 30 = 0.04\text{seconds} = 40\text{ms}$. Time for one I/O $= 83 + 4 + 40 = 127\text{ms} = T$. Number of disk I/Os per second $= 1/T = 7$. Throughput $= 7 \times 4 \times 512 / 1024 = 14\text{MB/s}$

Q.7

a) In an index we can store $4\text{KB}/8 = 512$ pointers. Total file size is: $10 + 512 + 512^2 + 512^3 \approx 2^{27}$ blocks. That makes:

$2^{27} \cdot 2^{12} = 2^{39}$ Bytes. This max file size supported is $\approx 512\text{GB}$

b) A leaf index block can map $2^9 \cdot 2^{12} = 2^{21} = 2\text{MB}$ of file data. For 8GB, we need $2^{33} / 2^{21} = 2^{12} = 4096$ leaf index blocks. Thus we have to use one single leaf index block and for the remaining second level index block. $4096 - 1 = 4095$ second level index blocks.

c) (i) $2^{15} / 2^{12} = 8$. It is in the file block P. Hence the respective block is pointed directly by the node. Thus we need 1 access

(ii) $2^{23} = 8\text{MB}$. Since a single index block can map $2\text{MB} = 2^9 \cdot 2^{12}$

$8\text{MB} / 2\text{MB} = 4$. So we need to access the first-level index block of the two-lvl index, then a second-lvl index block and then the data block so we need 3 disk accesses

(iii) $2^{32} = 4\text{GB}$, since three-lvl index structure can map $2^{14} \cdot (2^9)^3 = 2^{27} \cdot 2^{12} = 2^{39}$ we have to access first-lvl, second-lvl, third-lvl pointers so, 4 access