

# Part 1: overview

- Principal Component Analysis (PCA)
- Partial Least Squares (PLS)
- Two-way Orthogonal PLS (O2PLS)
  - Population model
  - Multi-omics data integration
- Post-hoc analyses using external databases



# Introduction

- We have seen PCA and PLS
- Looked at them from an algorithmic point of view
- What is the underlying population model?
  - What are the random variables, and what are the parameters?



# Population model for PCA

$$x = tW^{\top} + e$$

- $t$  are scores (the PCs)
- $W$  are weights (or loadings), parameters
- $e$  are residuals
- Parameters are estimated such that the variance of  $Xw$  is maximized



# Population model for PLS

$$x = tW^{\top} + e$$

$$y = uC^{\top} + f$$

$$u = tB + h$$

- $t$  and  $u$  are latent (hidden) scores (the joint PCs)
- $w$  and  $c$  are weights (or loadings), parameters
- The relation between  $x$  and  $y$  is fully captured by  $t$  and  $u$ , via the third relation
- Parameters are estimated such that the covariance between  $Xw$  and  $Yc$  is maximized



# Interpretation of the model

$$\begin{aligned}x &= tW^{\top} + e \\y &= uC^{\top} + f \\u &= tB + h\end{aligned}$$

- $x$  and  $y$  are two datasets, say genetic and metabolomic data
- $t$  and  $u$  are latent variables underlying these data
- These latent variables vary, and through  $W$  and  $C$  cause variation in the two datasets
- In the above context,  $t$  and  $u$  could be methylation/glycomic pathways
- Then,  $W$  and  $C$  would tell us which CpGs and glycans are involved



# Omics-specific variation

- PCA models the variance of  $X$  (or  $Y$ )
- PLS models the covariance
- Suppose both sources are present, independently
  - E.g. some pathways connect CpGs and glycans
  - Other pathways are there for self-maintenance
- Capture both parts at the same time
- Need to extend the PLS model



## O2PLS model and data-specific parts

$$\begin{aligned}x &= tW^{\top} + t_s W_s^{\top} + e \\y &= uC^{\top} + u_s C_s^{\top} + f \\u &= tB + h\end{aligned}$$

- $x$  and  $y$  are two datasets, say genetic and metabolomic data
- In addition to the PLS joint weights and scores, we have **specific** weights and scores
- The relation between  $x$  and  $y$  is still fully captured by  $t$  and  $u$



# Estimating the O2PLS components

- Three step estimation
  - First estimate several PLS components, they will contain both joint and specific parts
  - From that, estimate specific parts only and subtract
  - Finally, estimate again PLS on the “corrected” data
- Implemented and on CRAN: *OmicPLS*
  - Obtain loadings with: *loadings*
  - Obtain scores with: *scores*





# Number of components

- Until now, we did not mention how to find out the number of components needed
- For PCA, this number is the number of PCs
- For PLS, this is the number of joint PCs
- For O2PLS, this is
  - The number of joint PCs
  - And the number of X-specific components
  - And Y-specific components
- Standard way is to do cross-validation (not covered now)



## O2PLS: summary

- For given datasets  $X$  and  $Y$ , we want to inspect their relation
- Want to capture data-specific parts as well
- O2PLS estimates joint and specific parts, consisting of weights and scores
- One can interpret or plot the weights and scores to understand which features/samples are most important



# Exercises

- Load the Down Syndrome data and run PCA to obtain the first principal component of the glycans
  - `svd(glycomics, nu=0, nv=1)$v`
- Now run *o2m* using both methylation and glycomics data and obtain the first joint principal component
  - `fit <- o2m(methylation, glycomics, 4, 2, 6)`
  - `loadings(fit, "Yj", subset=1)`
- Compare the two loading vectors



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