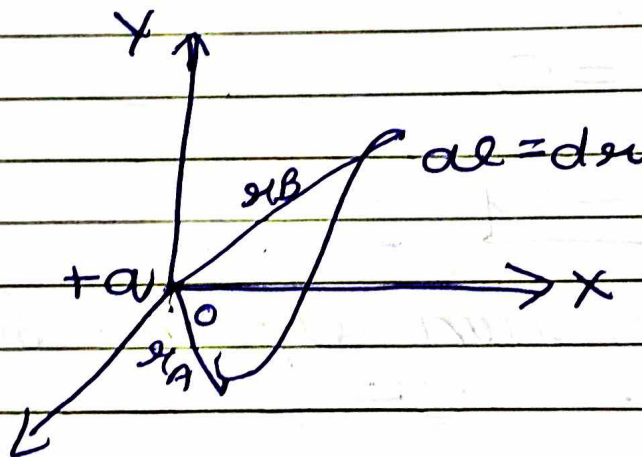


# Unit 5

## Chapter - 2

### # Curl of Electrostatic Field:

Consider a line element  $dl$  which is at a distance of  $r_A$  and  $r_B$  from the charge  $q$  situated at the origin.



Then the line integral of the electric field from  $A$  to  $B$  is given by

$$= \int_A^B \mathbf{E} \cdot d\mathbf{l} \quad \text{--- (1)}$$

Now, we know that

$$E = \frac{q}{4\pi\epsilon_0 r^2} \quad \text{--- (2)}$$

Put ② in ①.

$$= \int_A^B \frac{q}{4\pi\epsilon_0 r^2} dr.$$

$$= \int_{r_A}^{r_B} \frac{q}{4\pi\epsilon_0 r^2} dr$$

Line int of Elec. field =  $\frac{q}{4\pi\epsilon_0} \int_{r_A}^{r_B} \frac{1}{r^2} dr.$

$$= \frac{q}{4\pi\epsilon_0} \left[ -\frac{1}{r} \right]_{r_A}^{r_B}.$$

$$= \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{r_A} - \frac{1}{r_B} \right]$$

If  $r_A = r_B.$

$$\int_A^B E \cdot dr = \frac{q}{4\pi\epsilon_0} (0) = 0 \quad - (3)$$

Stokes Theorem:

$$\int_C \vec{A} \cdot d\vec{r} = \int_S (\vec{\nabla} \times \vec{A}) \cdot d\vec{S} \quad - (4)$$



~~Q~~  $\vec{\nabla} \times \vec{A} = \text{curl of } A.$

Put ① in ①

$$= \int_S (\vec{\nabla} \times \vec{E}) \cdot d\vec{s} \quad \text{--- ⑤}$$

Put ⑤ in ③.

$$\int_S \vec{E} \cdot d\vec{l} = \int_S (\vec{\nabla} \times \vec{E}) \cdot d\vec{s}$$

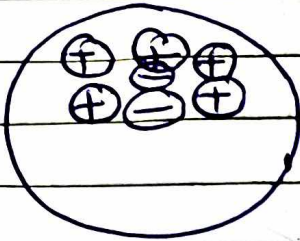
$$(\vec{\nabla} \times \vec{E}) \cdot d\vec{s} = 0$$

$$\boxed{\vec{\nabla} \times \vec{E} = 0}$$

curl of  $E = 0.$

## # Dielectrics

These are the materials which can't transmit electricity by itself.



Polar



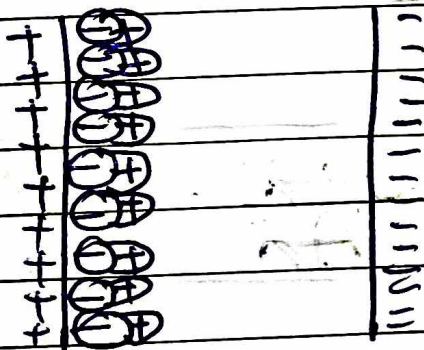
Di-polar

Two equal and opposite charges are separated by some distance is known as electric dipole.



$$P = q \cdot 2r$$

## Polarization of Dielectrics

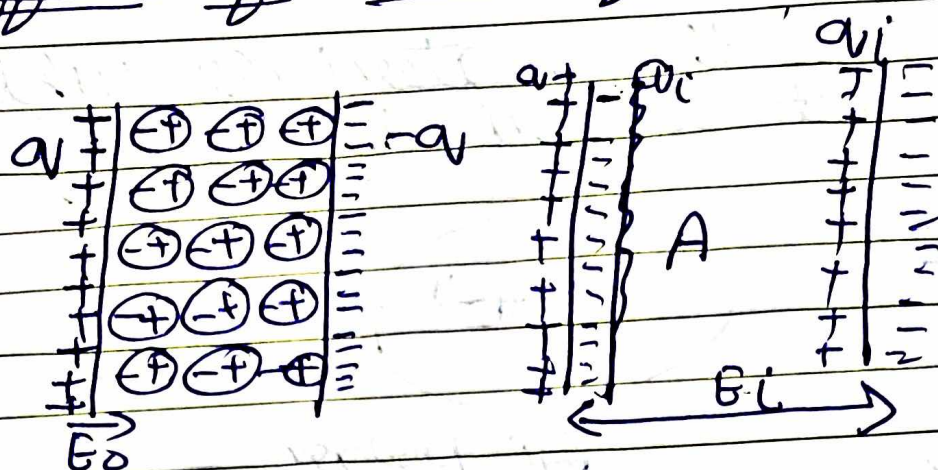


$$\vec{P} = \epsilon_0 \alpha \vec{E}$$

$$\vec{P} = n \vec{p}$$



# # Effect of electric field on Dielectrics.



## Resultant Electric field:

$$E = E_0 - E_i$$

$$\boxed{\begin{matrix} E_0 & K \\ E = & \end{matrix}}$$

$$\sigma = \frac{q}{A}$$

$$\sigma_i = \frac{q_i}{A}$$

$$\boxed{\vec{P} = \frac{p}{\text{volume}} = \frac{q_i d}{A d} = \frac{q_i}{A} = \sigma_i}$$

$$\begin{matrix} P \propto E \\ \boxed{P = \epsilon_0 X E} \end{matrix}$$

$X =$  Dielectric acceptability.

$$\boxed{E_0 = \frac{\sigma}{\epsilon_0}}$$

$$\boxed{E_i = \frac{\sigma_i}{\epsilon_0}}$$

$$E = \frac{\sigma}{\epsilon_0} - \frac{\sigma_i}{\epsilon_0}$$

$$E = E_0 - \frac{\sigma_i}{\epsilon_0}$$

$$E = E_0 - \frac{P}{\epsilon_0}$$

$$E = E_0 - \frac{\epsilon_0 \times E_0}{\epsilon_0}$$

$$E = E_0 - X E_0$$

$$E = E_0 (1 - X)$$

$$\frac{E}{E_0} = (1 - X)$$

$$\frac{1}{K} = 1 - X$$

$$E_0 = E + X E$$

$$\frac{E_0}{E} = 1 + X$$

$$K = 1 + X$$



# # Gauss Law in Dielectrics:



Acc. to Gauss Law.

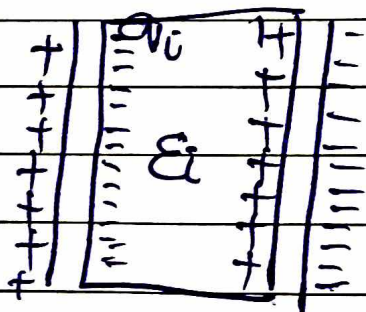
$$\vec{E}_0 = \vec{E}$$

$$\int \vec{E}_0 \cdot d\vec{s} = \frac{q}{\epsilon_0}$$

$$E_0 \int ds = \frac{q}{\epsilon_0}$$

$$E_0 A = \frac{q}{\epsilon_0}$$

$$E_0 = \frac{q}{\epsilon_0 A} \quad \text{--- (1)}$$



$$E = E_0 - E_i$$

$$\int \vec{E} \cdot d\vec{s} = \left( \frac{q - q_i}{\epsilon_0} \right)$$

$$EA = \frac{(q - q_i)}{\epsilon_0}$$

$$EA = \frac{(q - q_i)}{\epsilon_0 A}$$

$$E = \frac{qV}{\epsilon_0 A} - \frac{q_i}{A \epsilon_0} \quad - (2)$$

$$E = \frac{E_0}{K} \quad - (3)$$

Put (3) in (1)

$$E = \frac{qV}{\epsilon_0 K} \quad - (4)$$

Put (4) in (2)

$$\frac{qV}{A \epsilon_0 K} = \frac{qV}{\epsilon_0 A} - \frac{q_i}{A \epsilon_0}$$

$$\frac{qV}{K} = (q - q_i) \quad - (5)$$

Comparing (5) & (6)

$$\int \vec{E} \cdot \hat{n} ds = \frac{q}{K \epsilon_0}$$

$$\boxed{K \int \vec{E} \cdot \hat{n} ds = \frac{q}{\epsilon_0}}$$



\* Electric Displacement Vector:

$$\frac{Q}{\epsilon_0 A} = E + \frac{Q_i}{\epsilon_0 A}$$

$$\frac{Q_i}{A} = P$$

$$\frac{Q}{\epsilon_0 A} = E + \frac{P}{\epsilon_0}$$

$$\frac{Q}{A} = \epsilon_0 E + P$$

$$\frac{Q}{A} = \mathcal{D}$$

$$\boxed{\mathcal{D} = \epsilon_0 E + P}$$

