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Assignment-I

Ques-1 Which law indicates the absence of Magnetic Monopoles?

→ The Maxwell's Gauss law in Magnetostatics indicates the absence of Magnetic Monopoles.

It can be mathematically represented as

$$\nabla \cdot \mathbf{B} = 0$$

Ques-2 changing electric field induces the magnetic field. Write mathematical relation to this effect.

→ The Maxwell's third equation of Faraday's law of electromagnetic induction shows the relation between electric field and magnetic field. It can be mathematically written as

$$\nabla \times \mathbf{E} = - \frac{\partial \mathbf{B}}{\partial t}$$

Ques-3 Which Maxwell's equation are coupled together?

→ The Faraday's law and Ampere Maxwell law are dynamically coupled equations forming the core of electromagnetic wave theory.

1. Faraday's law of induction:

$$\nabla \times \mathbf{E} = - \frac{\partial \mathbf{B}}{\partial t}$$

2. Ampere Maxwell law:

$$\nabla \times \mathbf{B} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t}$$

Ques- Write the characteristics of EM waves?

→ Characteristics of EM waves:

1. Transverse Nature.

- 2.) Travel at the speed of light (in vacuum) $c = 3 \times 10^8$
- 3.) Gauss Energy and Momentum:

$$\text{Energy} = \frac{1}{2} \left(\epsilon_0 E^2 + \frac{B^2}{\mu_0} \right)$$
- 4.) EM waves consists of \vec{E} and \vec{B} oscillating perpendicular to wave propagation of wave.
- 5.) Oscillation of \vec{E} and \vec{B} occurs in same phase.
- 6.) Which Maxwell equation remains unchanged under all condition?

→ The second Maxwell equation, Gauss law in magnetism remains unchanged under all conditions. It states:

$$\nabla \cdot \vec{B} = 0$$

7.) What is plane electromagnetic wave?

→ A plane EM wave is a type of EM wave in which electric field (E) and Magnetic field (B) oscillate perpendicular to each other and to the direction of wave propagation.

8.) When do Maxwell's equations become uncoupled and with what consequences?

→ Maxwell's equations become uncoupled in regions where there is no free charges ($\rho = 0$) and no free currents ($J = 0$), such as in free space or vacuum.

The equations for free space will be

$$\nabla^2 \vec{E} = \mu_0 \epsilon_0 \frac{\partial^2 \vec{E}}{\partial t^2} \quad \text{--- (1)}$$

$$\nabla^2 \vec{H} = \mu_0 \epsilon_0 \frac{\partial^2 \vec{H}}{\partial t^2} \quad \text{(2)}$$

Consequences of Uncoupling!

The Maxwell's equations will not depend on each other as there is no free electrons and no current ($J=0$) in free space.

Ques-8) The light is generally characterised by electric vector although it also possess Magnetic vector. Explain?

→ In light, electric field dominate over magnetic field vector. Light, as it goes through a medium which has small probability to interact with magnetic field component with medium and mainly, so, electric field components predominate.

Ques-9) What is plane polarised EM wave?

→ The light wave that has vibrations occurring only in one plane is called plane polarised or EM waves.

Ques-10) Which relation indicates EM waves are related to speed of light?

→ The relation which indicates EM waves are related to speed of light

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = 3 \times 10^8 \text{ m/s}$$

$$\nabla^2 \phi = \frac{1}{c^2} \frac{\partial^2 \psi}{\partial t^2}$$