

Physics

Assignment - 2

Ques-1) Why should the function $\psi(x)$ be a single value everywhere?

Ans-1) The probability density of finding the particle, given by $P = \psi \psi^*$, ψ should be single value so that the probability has unique value everywhere.

Ques-2) What do you mean by a free particle?

Ans-2) Free particle is a particle on which no forces are acting such particle is characterised by definite momentum & energy.

Ques-3) Why should schrodinger equation have the 1st order time derivative.

Ans-3) To describe completely the wave function it is necessary to get the first order time derivative.

Ques-4) Can we represent a matter wave associated with the free particle by a wave function $\psi(x, t) = A \sin(kx - \omega t)$?

Ans-4) In this function $\psi(x, t) = A \sin(kx - \omega t)$ describe the free particle it must satisfy the one dimensional time dependent schrodinger wave equation.

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} = i\hbar \frac{\partial \psi}{\partial t}$$

After taking derivative, $LHS \neq RHS$. Hence, this function does not represent a matter wave.

Ques-5) Why can't a function $e^{i(kx - \omega t)}$ be used to represent a localised particle in quantum mechanics?

Ans-5) For localised particle ψ^* and ψ must depend on x .

$$\psi(x, t) = e^{i(kx - \omega t)}$$

$$P = \psi^* \psi$$

$$P = e^{-i(kx - \omega t)} \cdot e^{i(kx - \omega t)}$$

$$P = 1$$

But, here it is independent of x . So, it fails to represent the localised particle.

Ques-6) Is the Schrodinger equation valid for ~~real~~ realistic particle?

Ans-6) No, because we use the classical expression

$$E = \frac{p^2}{m} + V$$

for the derivation of schrodinger wave equation.

Ques-7) What are orthogonal wave function.

Ans-7) Two wave functions are said to be orthogonal if it satisfy the following condition:

$$\int_{-\infty}^{\infty} \psi_m^* \psi_n dx = 0$$

Ques-8) The mass of the particle appears in schrodinger's wave equation but its charge does not. both: charge & the mass effect the motion. why?

Ans- The Schrodinger equation describe the De-broglie waves associated with the particle. The De-broglie wavelength depends only on mass. Hence, the mass of the particle appears in schrodinger wave equation but its ~~length~~ charge does not.

Ques-9> Which operator is used for calculating the expectation value of momentum?

Ans-9>
$$P_x \rightarrow \cancel{-i\hbar \frac{\partial}{\partial x}} -i\hbar \frac{\partial}{\partial x}$$

$$P_y \rightarrow -\hbar \frac{\partial}{\partial y}$$

$$P_z \rightarrow -i\hbar \frac{\partial}{\partial z}$$

Ques-10> Which operator is used for calculating the expectation value of energy.

Ans-10>
$$E \rightarrow i\hbar \frac{\partial}{\partial t}$$