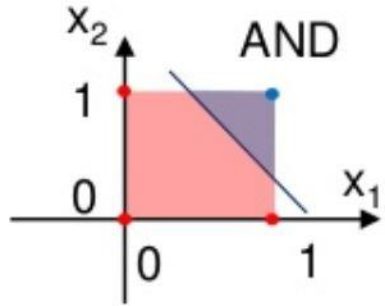
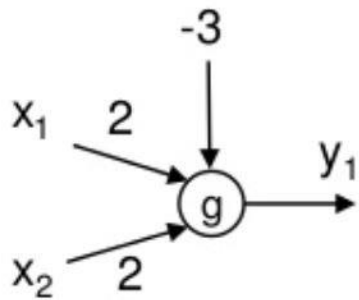




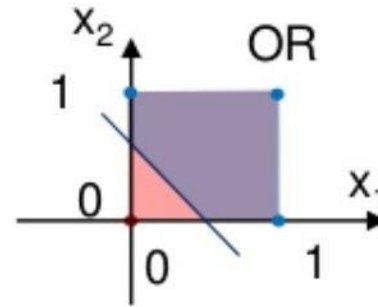
# Neural Network



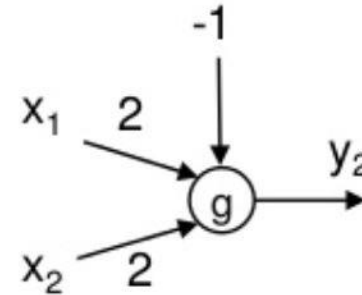
Input vector (x1,x2)	Class AND
(0,0)	0
(0,1)	0
(1,0)	0
(1,1)	1



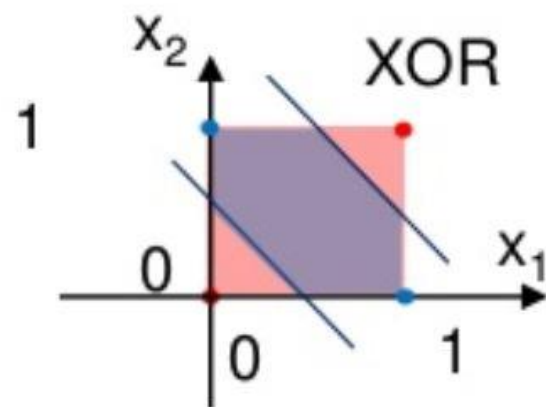
$$y_1 = g(\mathbf{w}^T \mathbf{x} + b) = u((2 \ 2) \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - 3)$$



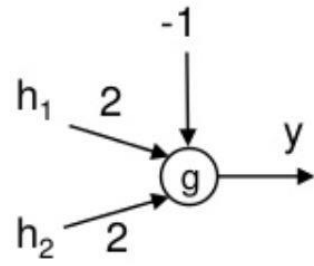
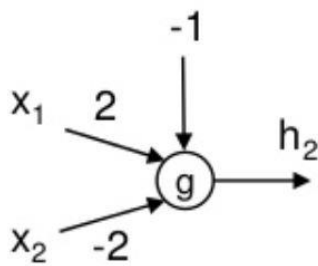
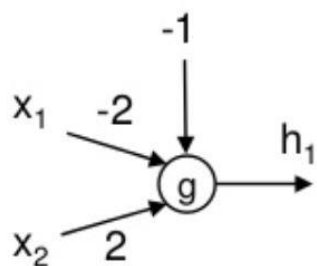
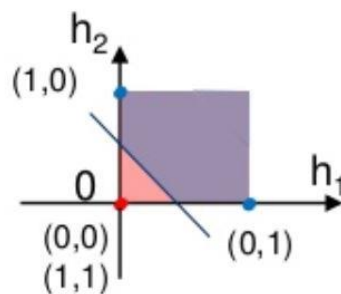
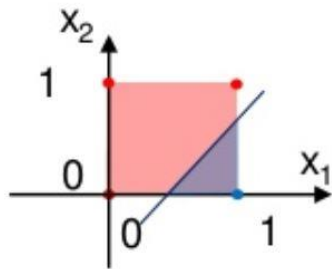
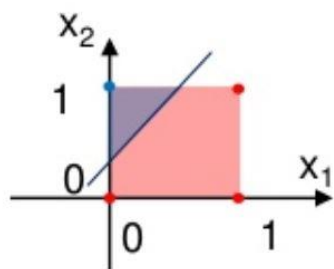
Input vector (x1,x2)	Class OR
(0,0)	0
(0,1)	1
(1,0)	1
(1,1)	1



$$y_2 = g(\mathbf{w}^T \mathbf{x} + b) = u((2 \ 2) \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - 1)$$



Input vector ( $x_1, x_2$ )	Class XOR
(0,0)	0
(0,1)	1
(1,0)	1
(1,1)	0

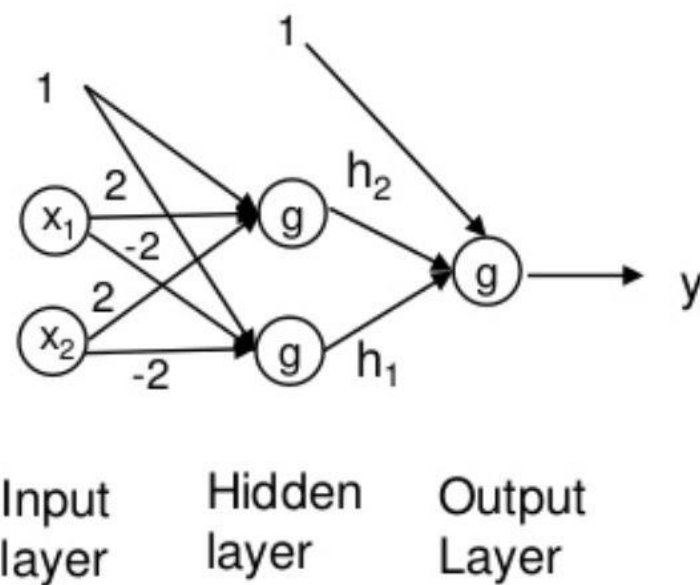
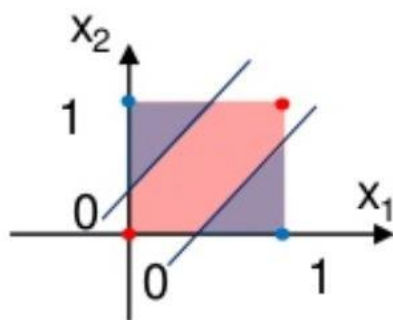


$$h_1 = g(\mathbf{w}_{11}^T \mathbf{x} + b_{11}) = u((-2 \ 2) \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - 1)$$

$$y = g(\mathbf{w}_2^T \mathbf{h} + b_2) = u((2 \ -2) \cdot \begin{pmatrix} h_1 \\ h_2 \end{pmatrix} + 1)$$

$$h_2 = g(\mathbf{w}_{12}^T \mathbf{x} + b_{12}) = u((2 \ -2) \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + 1)$$


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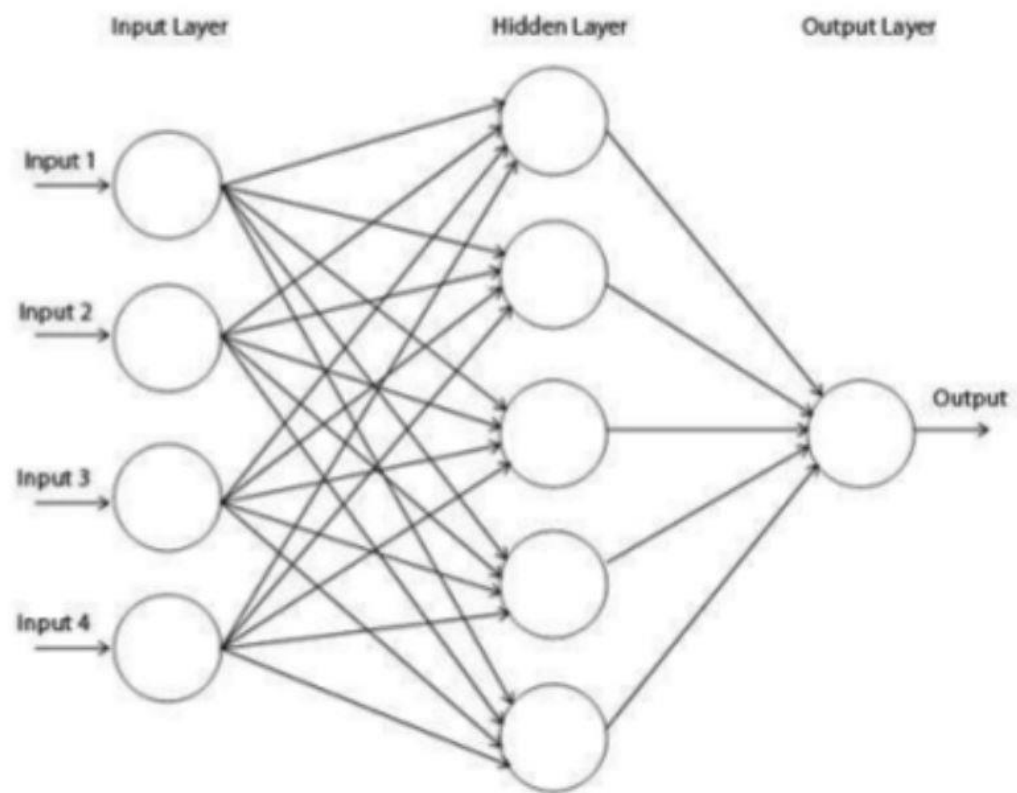
$$h_1 = g(\mathbf{w}_{11}^T \mathbf{x} + b_{11}) = u((-2 \ 2) \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} - 1)$$

$$h_2 = g(\mathbf{w}_{12}^T \mathbf{x} + b_{12}) = u((2 \ -2) \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + 1)$$

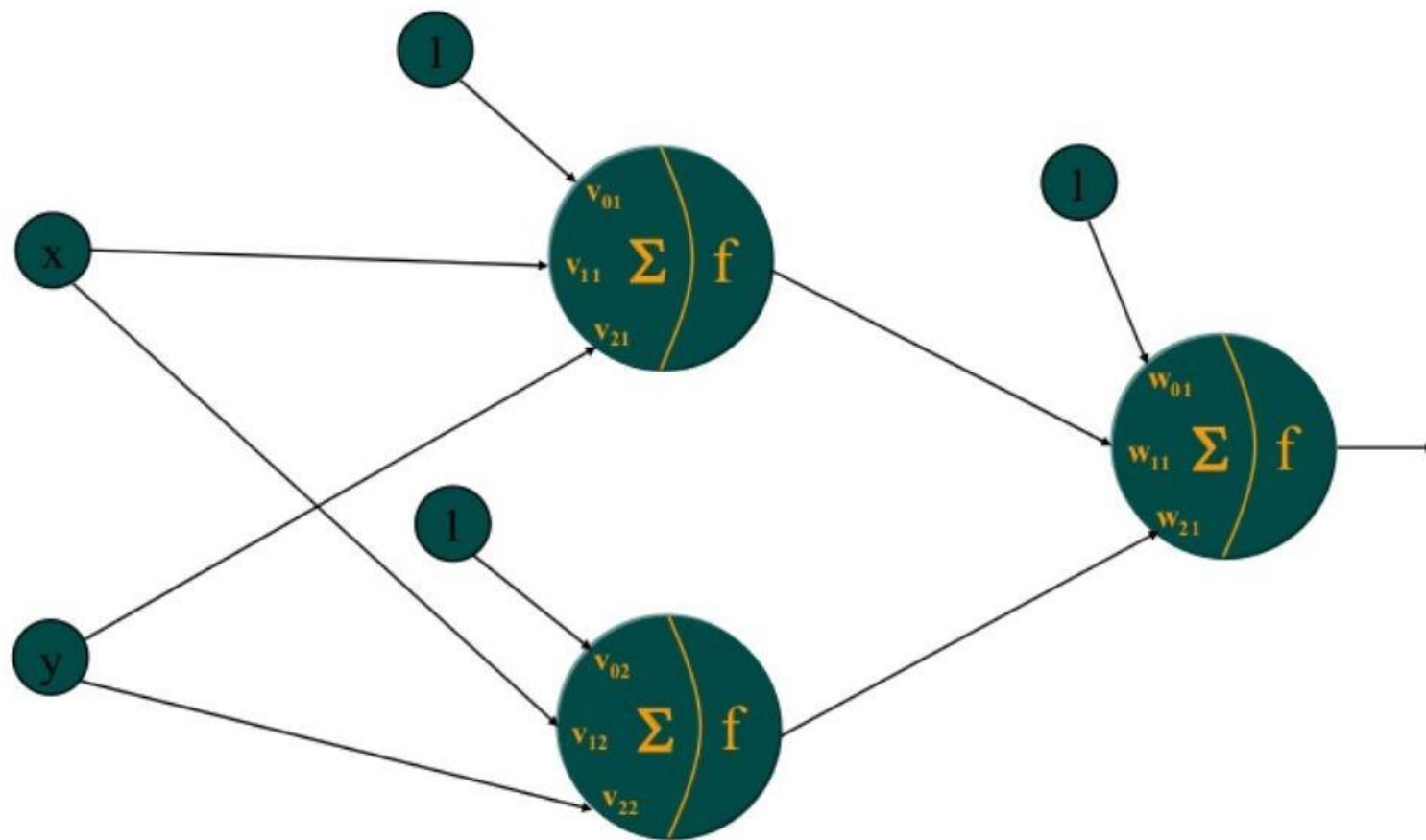
$$y = g(\mathbf{w}_2^T \mathbf{h} + b_2) = u((2 \ -2) \cdot \begin{pmatrix} h_1 \\ h_2 \end{pmatrix} + 1)$$

# Neural Networks

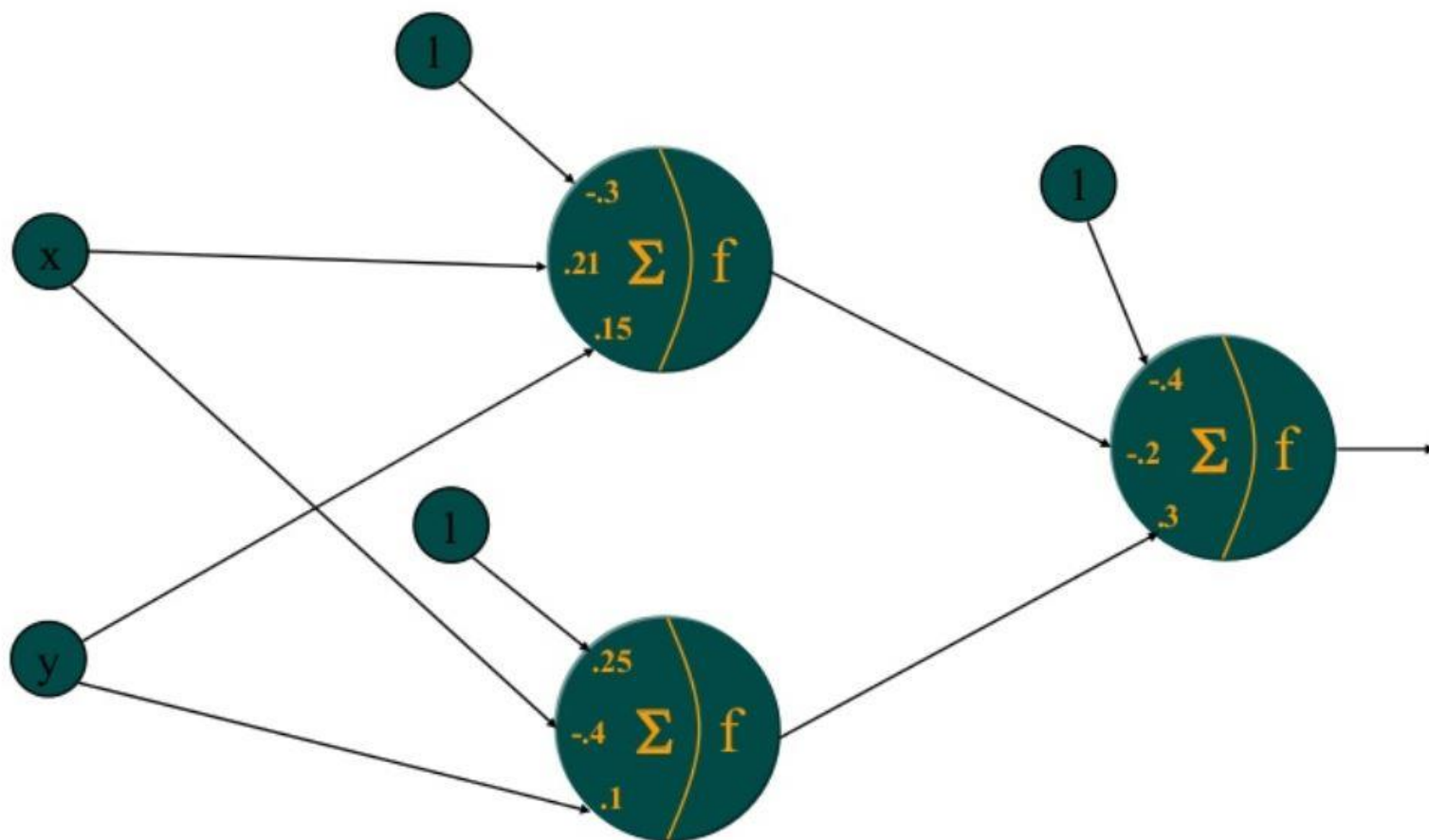
- A neural network is simply a composition of simple neurons into several layers.
- Each neuron simply computes a linear combination of its inputs, adds a bias and passes the result through an activation function  $g(x)$ .
- The network can contain one or more hidden layers. The outputs of these hidden layers can be thought of as a new representation of the data (new features).
- The final output is the target variable ( $y=f(x)$ )

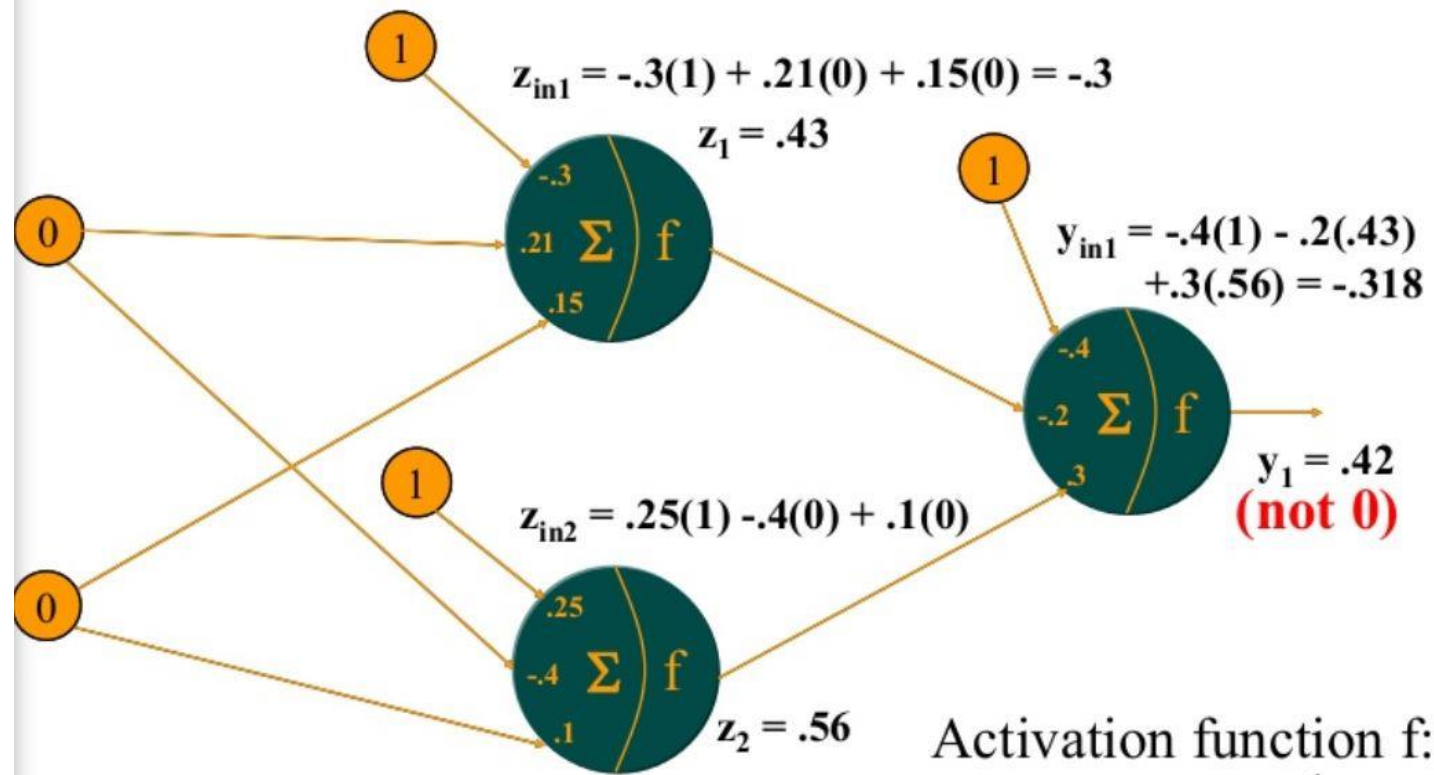


Example:





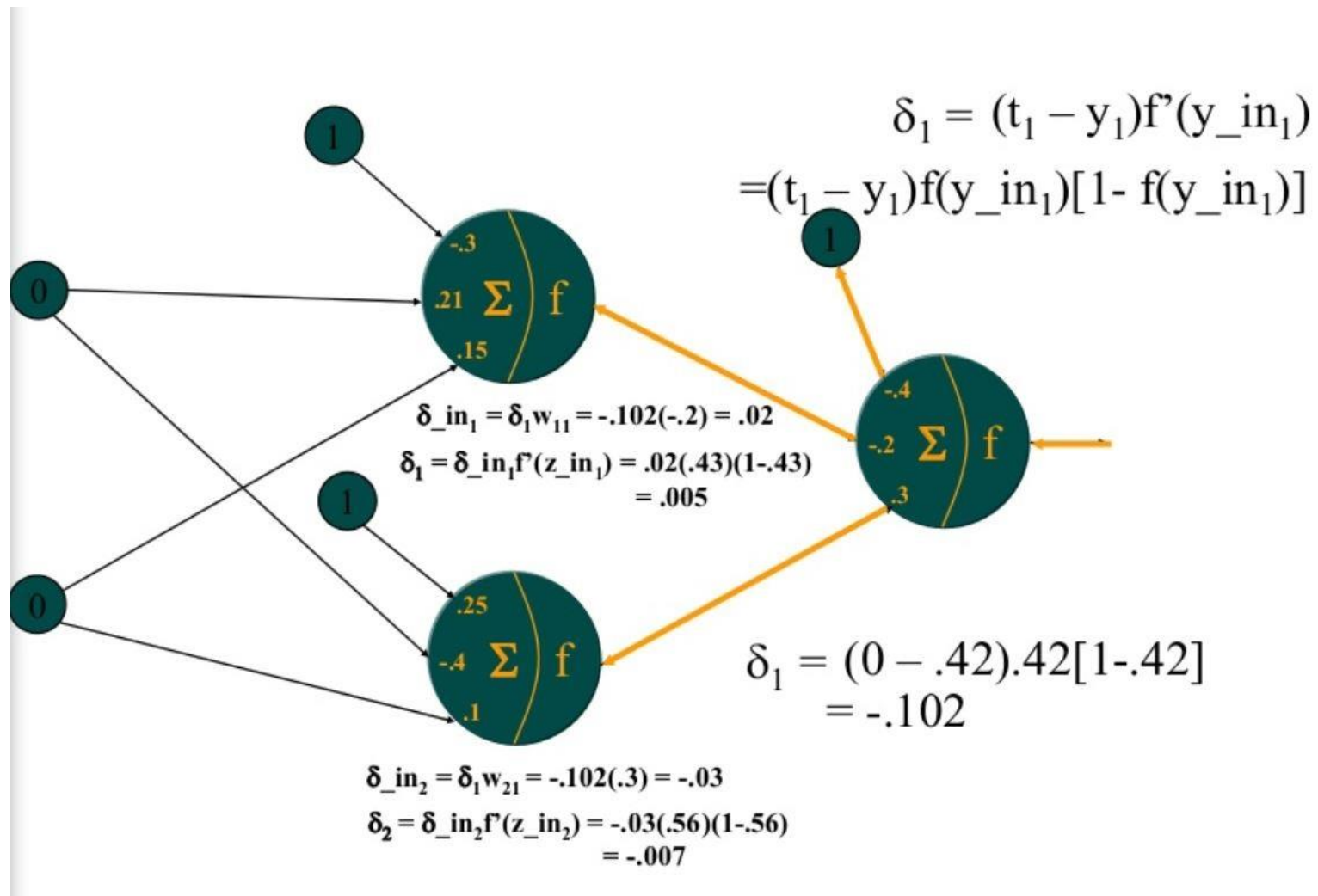




Training Case: (0 0 0)

Activation function f:

$$f(x) = \frac{1}{1 + e^{-x}}$$

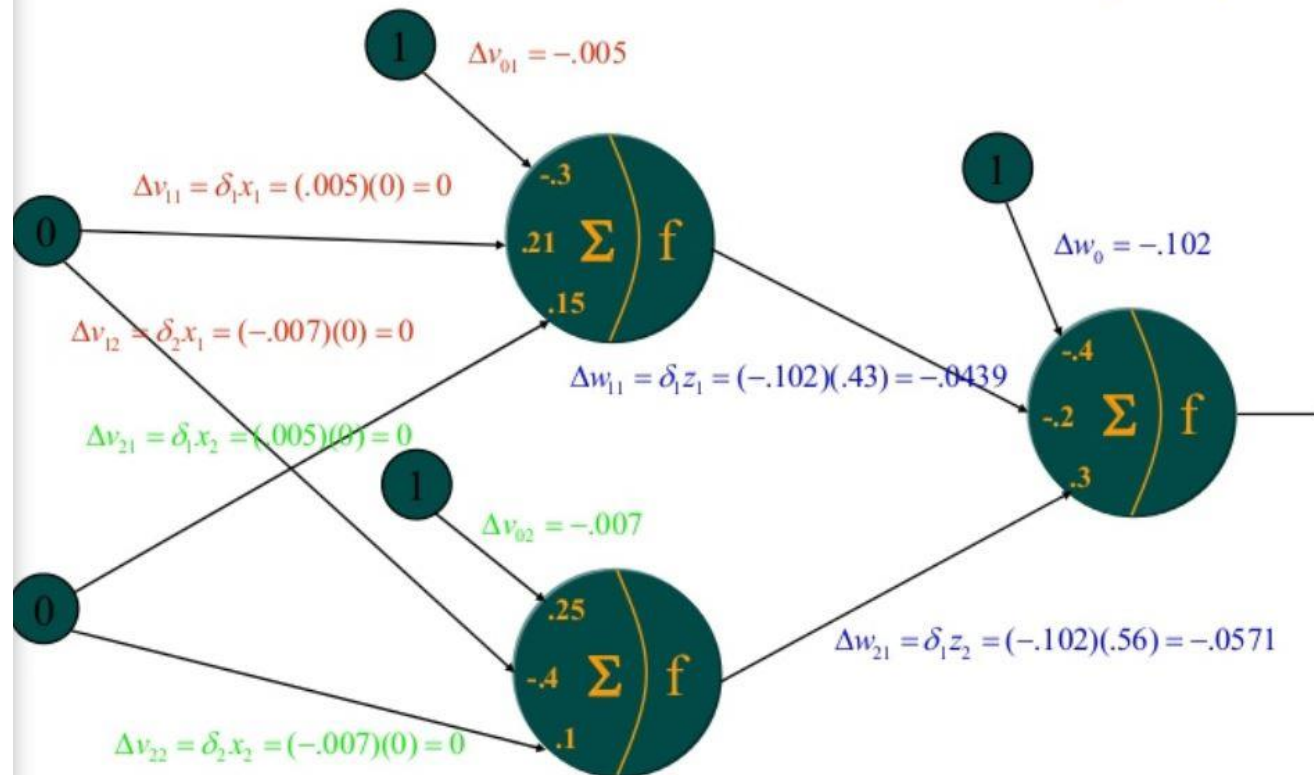


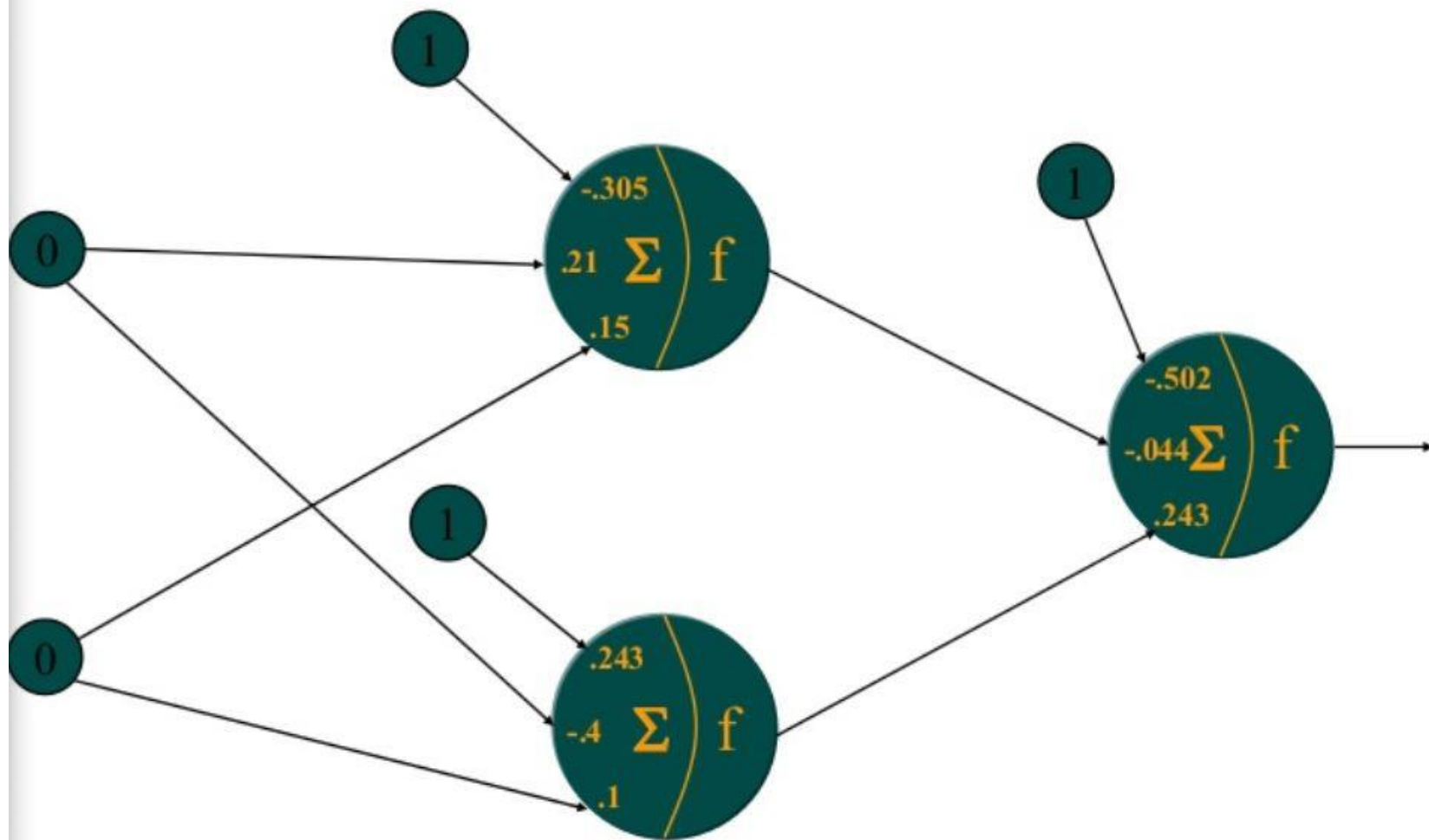
$$\Delta v_{ij} = \alpha \delta_j x_i \quad j = 1, 2$$

$$\Delta v_{0j} = \alpha \delta_j$$

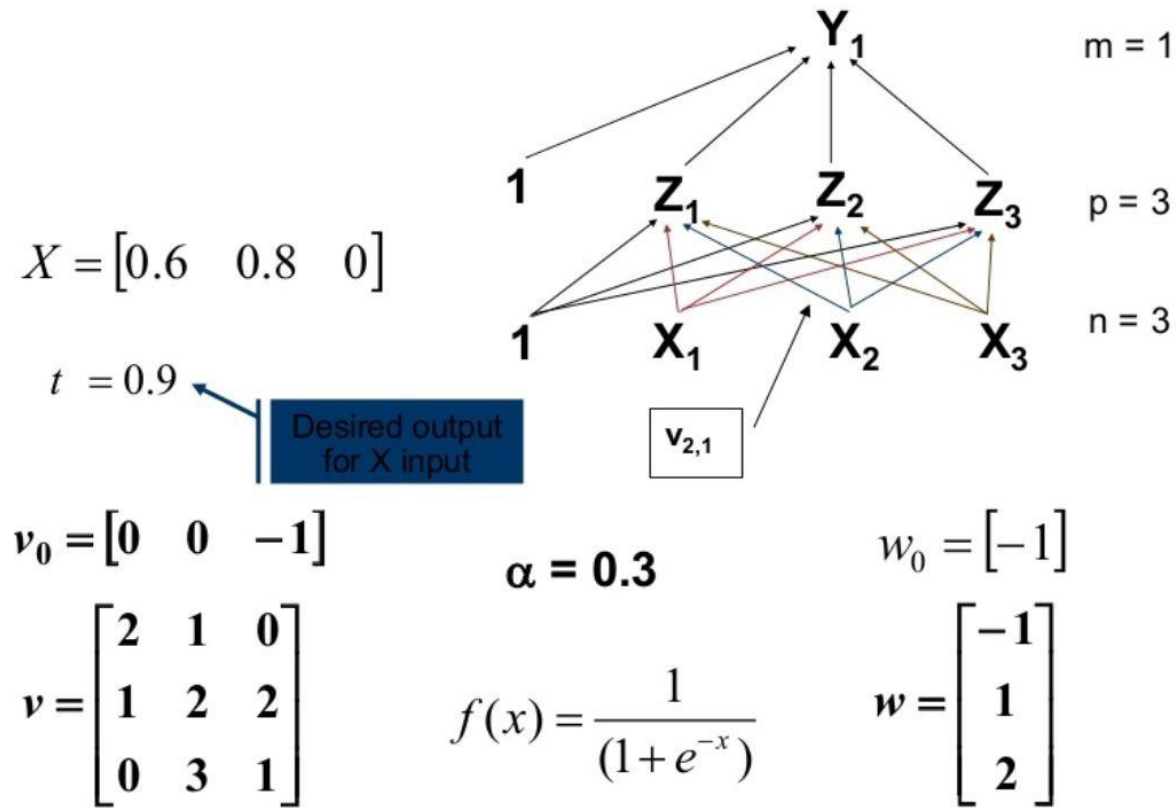
$$\Delta w_{j1} = \alpha \delta_1 z_j \quad j = 1, 2$$

$$\Delta w_0 = \alpha \delta_1$$



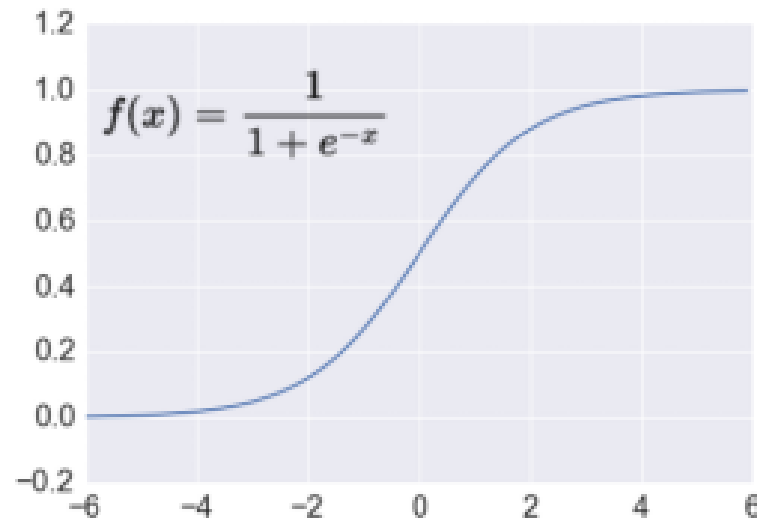


# Example

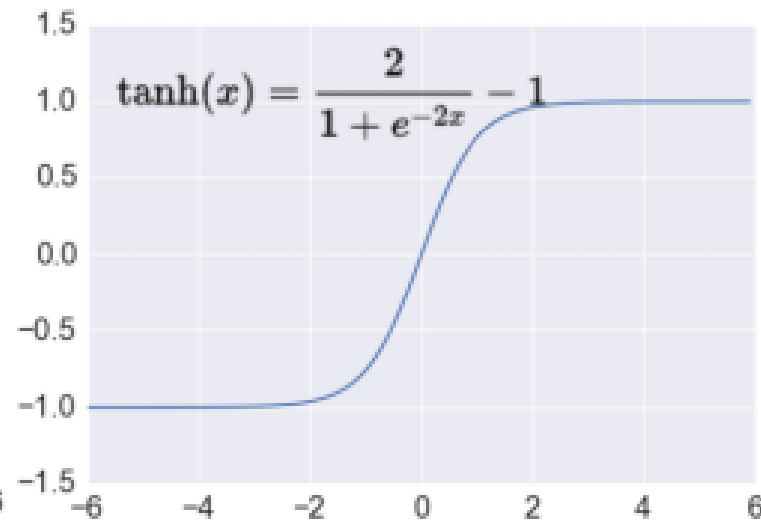


# Activation Functions

Sigmoid



TanH



ReLU

