

Statistical tests

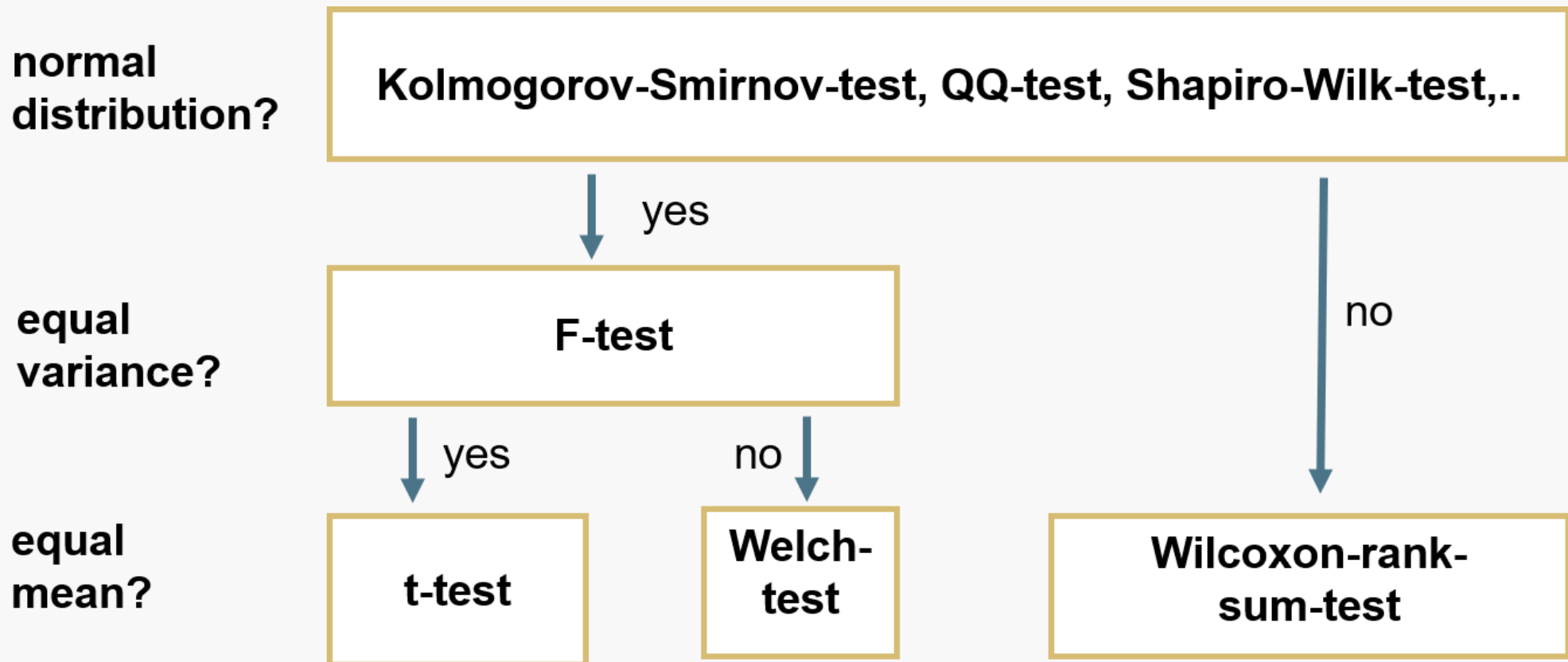
Day 3 - Introduction to Data Analysis with R

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Overview of tests



Please note the discussion going on about p-values as a basis for binary decisions. See e.g. [here](#) or [here](#) as a starting

Tests for normal distribution

Test for normal distribution

There are **various tests** and the outcome might differ!

Shapiro-Wilk-Test

- How much does variance of observed data differ from normal distribution
- Specific test only for normal distribution
- High power, also for few data points

Visual tests: QQ-Plot

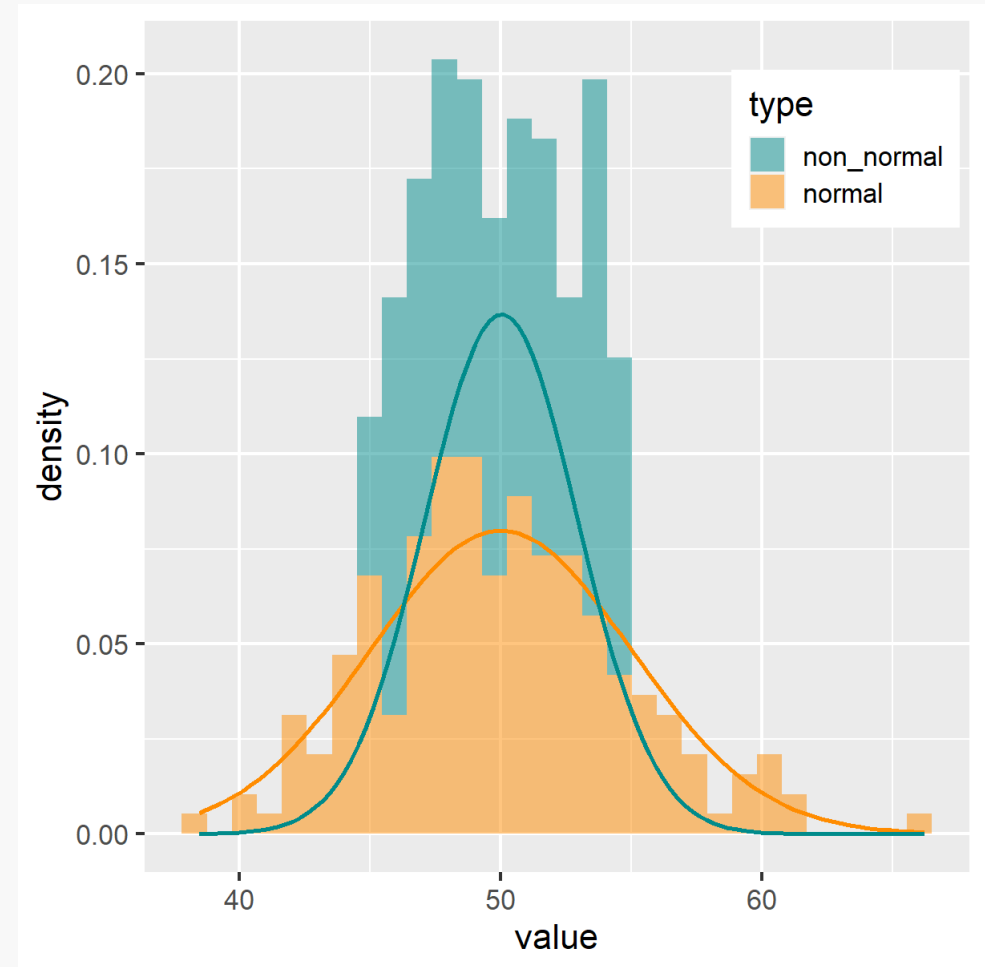
- Quantiles of observed data plotted against quantiles of normal distribution
- Scientist has to decide if normal or not

The data

Create a tibble with two variables

- `normal`: 200 normally distributed values with mean 50 and standard deviation 5
- `non_normal`: 200 uniformly distributed values between 45 and 55

```
1 set.seed(123)
2 mydata <- tibble(
3   normal = rnorm(
4     n = 200,
5     mean = 50,
6     sd = 5
7   ),
8   non_normal = runif(
9     n = 200,
10    min = 45,
11    max = 55
12  )
13 )
```



Shapiro-Wilk-Test

H_0 : Data does not differ from a normal distribution

```
1 shapiro.test(mydata$normal)
2 #>
3 #>  Shapiro-Wilk normality test
4 #>
5 #> data:  mydata$normal
6 #> W = 0.99076, p-value = 0.2298
```

- W: test statistic
- p-value: probability to observe the data if was true

The data does not deviate significantly from a normal distribution (Shapiro-Wilk-Test, $W = 0.991$, $p = 0.23$).

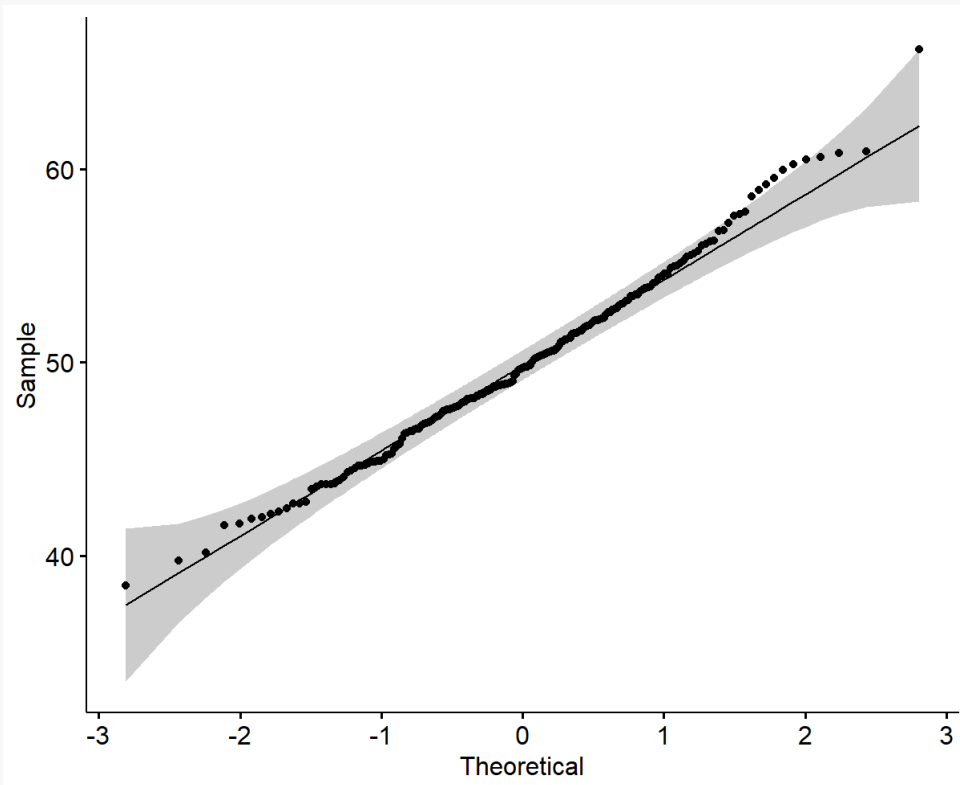
```
1 shapiro.test(mydata$non_normal)
2 #>
3 #>  Shapiro-Wilk normality test
4 #>
5 #> data:  mydata$non_normal
6 #> W = 0.95114, p-value = 2.435e-06
```

The data deviates significantly from a normal distribution (Shapiro-Wilk-Test, $W = 0.95$, $p < 0.001$).

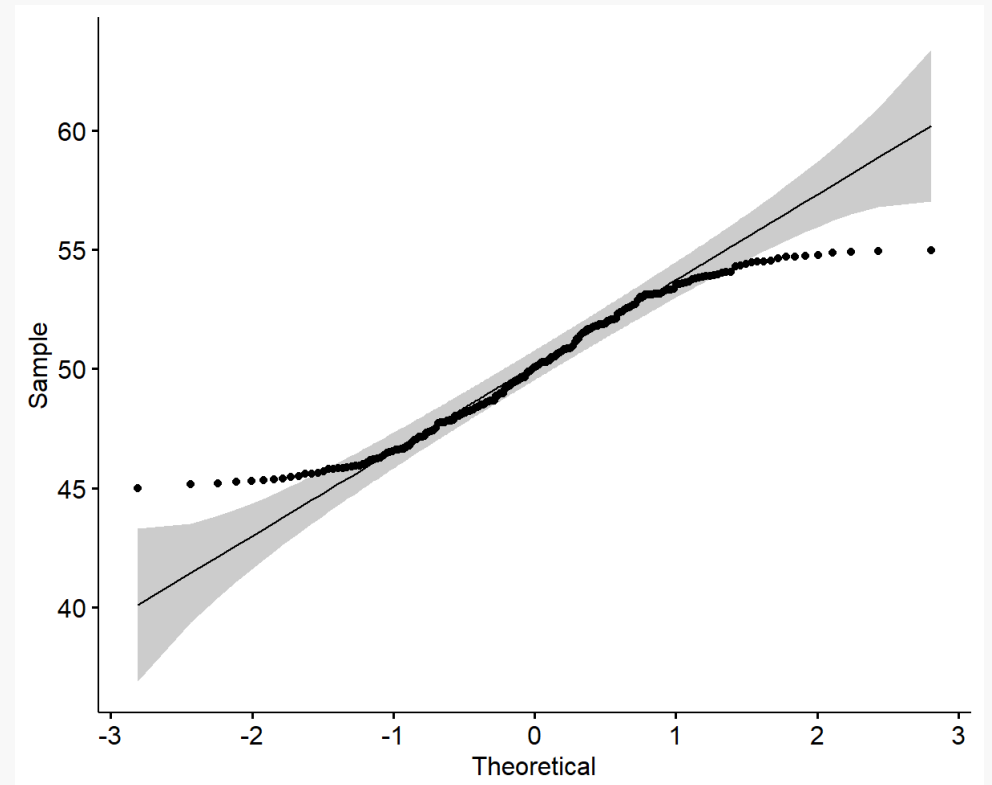
Visual test with QQ-Plot

Points should match the straight line. Small deviations are okay.

```
1 # ggplot(mydata, aes(sample = normal)) +  
2 #   stat_qq() + stat_qq_line()  
3 ggpubr::ggqqplot(mydata$normal)
```



```
1 # ggplot(mydata, aes(sample = non_normal)) +  
2 #   stat_qq() + stat_qq_line()  
3 ggpubr::ggqqplot(mydata$non_normal)
```



Tests for equal variance

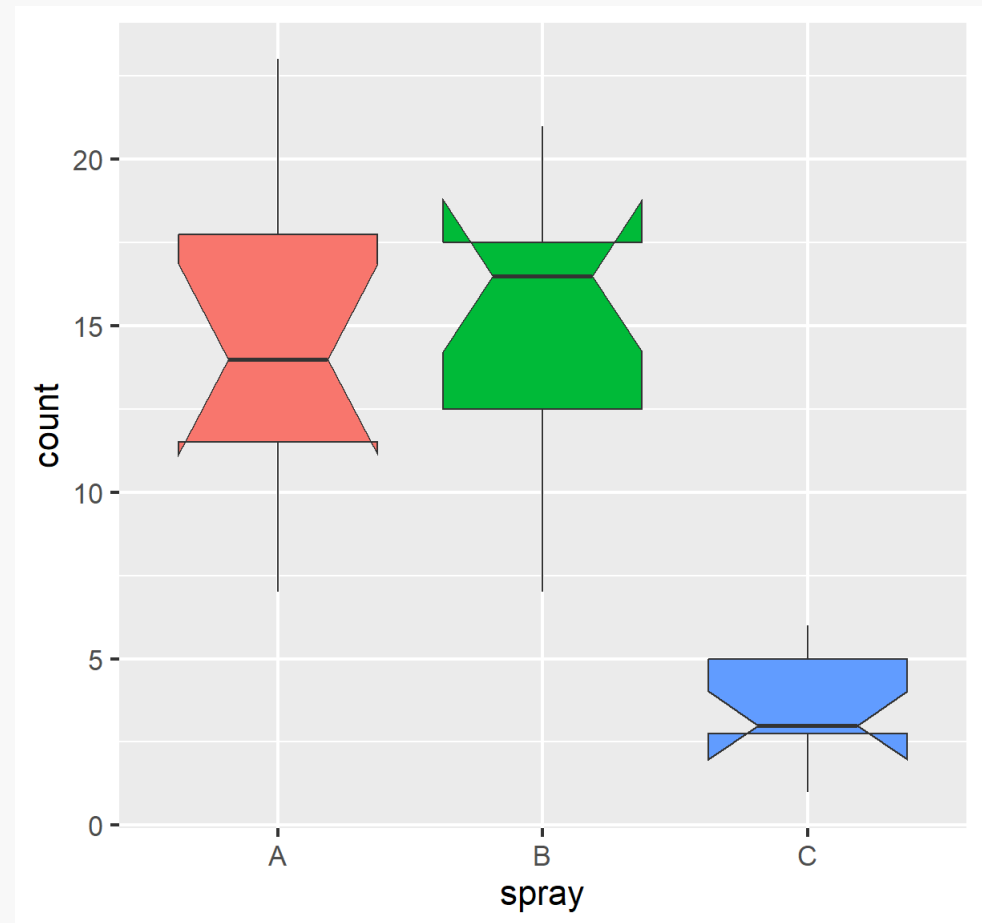
The data

Counts of insects in agricultural units treated with different insecticides.

Compare treatments A, B and C:

Create subsets before: count variable for each treatment as a vector

```
1 TreatA <- filter(  
2   InsectSprays,  
3   spray == "A")$count  
4 TreatB <- filter(  
5   InsectSprays,  
6   spray == "B")$count  
7 TreatC <- filter(  
8   InsectSprays,  
9   spray == "C")$count
```



Test for equal variance

First, test for normal distribution!

F-Test

- Normal distribution of groups
- Calculates ratio of variances (if equal, ratio = 1)
- p: How likely is ratio if variances were equal?

Levene test

- Non-normal distribution of groups
- Compare difference between data sets with difference within data sets

Test for equal variances

If we want to compare variances between treatments A, B and C, we first test for normal distribution

```
1 shapiro.test(TreatA)
2 #>
3 #>  Shapiro-Wilk normality test
4 #>
5 #> data:  TreatA
6 #> W = 0.95757, p-value = 0.7487
7 shapiro.test(TreatB)
8 #>
9 #>  Shapiro-Wilk normality test
10 #>
11 #> data:  TreatB
12 #> W = 0.95031, p-value = 0.6415
13 shapiro.test(TreatC)
14 #>
15 #>  Shapiro-Wilk normality test
16 #>
17 #> data:  TreatC
18 #> W = 0.92128, p-value = 0.2967
```

Result: All 3 treatments are normally distributed.

F-Test

: Variances do not differ between groups

```
1 var.test(TreatA, TreatB)
2 #>
3 #>  F test to compare two variances
4 #>
5 #> data:  TreatA and TreatB
6 #> F = 1.2209, num df = 11, denom df = 11, p-value = 0.7464
7 #> alternative hypothesis: true ratio of variances is not equal to 1
8 #> 95 percent confidence interval:
9 #>  0.3514784 4.2411442
10 #> sample estimates:
11 #> ratio of variances
12 #>          1.22093
```

- F: test statistics, ratio of variances (if $F = 1$, variances are equal)
- df: degrees of freedom of both groups
- p-value: how likely is it to observe the data if was true?

Result: The variances of sprays A and B do not differ significantly (F-Test, $= 1.22$, $p = 0.75$)

F-Test

: Variances do not differ between groups

```
1 var.test(TreatA, TreatC)
2 #>
3 #>  F test to compare two variances
4 #>
5 #> data:  TreatA and TreatC
6 #> F = 7.4242, num df = 11, denom df = 11, p-value = 0.002435
7 #> alternative hypothesis: true ratio of variances is not equal to 1
8 #> 95 percent confidence interval:
9 #>    2.137273 25.789584
10 #> sample estimates:
11 #> ratio of variances
12 #>           7.424242
```

Result: The variances of sprays A and C differ significantly (F-Test, = 7.42, p = 0.002)

Test for equal means

Test for equal means

t-test

- Normal distribution AND equal variance
- Compares if mean values are within range of standard error of each other
- p : how likely is the difference if the means were equal

Welch-Test

- Normal distribution but unequal variance
- Corrected t-test

Wilcoxon rank sum test

- Non-normal distribution and unequal variance
- Compares rank sums of the data
- Non-parametric

t-test

: The samples do not differ in their mean

Treatment A and B: **normally distributed** and **equal variance**

```
1  t.test(TreatA, TreatB, var.equal = TRUE)
2  #>
3  #>  Two Sample t-test
4  #>
5  #> data:  TreatA and TreatB
6  #> t = -0.45352, df = 22, p-value = 0.6546
7  #> alternative hypothesis: true difference in means is not equal to 0
8  #> 95 percent confidence interval:
9  #>  -4.643994  2.977327
10 #> sample estimates:
11 #> mean of x mean of y
12 #>  14.50000  15.33333
```

- t: test statistics ($t = 0$ means equal means)
- df: degrees of freedom of t-statistics
- p-value: how likely is it to observe the data if was true?

Result: The means of spray A and B don't differ significantly ($t = -0.45$, $df = 22$, $p = 0.66$)

Welch-Test

: The samples do not differ in their mean

Treatment A and C: **normally distributed** and **non-equal variance**

```
1  t.test(TreatA, TreatC, var.equal = FALSE)
2  #>
3  #>  Welch Two Sample t-test
4  #>
5  #> data:  TreatA and TreatC
6  #> t = 7.5798, df = 13.91, p-value = 2.655e-06
7  #> alternative hypothesis: true difference in means is not equal to 0
8  #> 95 percent confidence interval:
9  #>    7.885546 14.114454
10 #> sample estimates:
11 #> mean of x mean of y
12 #>    14.5    3.5
```

Result: The means of spray A and C do differ significantly ($t = 7.58$, $df = 13.9$, $p < 0.001$)

Wilcoxon-rank-sum Test

: The samples do not differ in their mean

We don't need the Wilcoxon test to compare treatment A and B, but for the sake of an example:

```
1 wilcox.test(TreatA, TreatB)
2 #>
3 #> Wilcoxon rank sum test with continuity correction
4 #>
5 #> data: TreatA and TreatB
6 #> W = 62, p-value = 0.5812
7 #> alternative hypothesis: true location shift is not equal to 0
```

Result: The means of spray A and B do not differ significantly ($W = 62$, $p = 0.58$)

Paired values

Are there pairs of data points?

Example: samples of invertebrates across various rivers before and after sewage plants.

- For each plant, there is a pair of data points (before and after the plant)
- Question: Is the change (before-after) significant

Use `paired = TRUE` in the test.

```
1 t.test(TreatA, TreatB, var.equal = TRUE, paired = TRUE)
2 t.test(TreatA, TreatB, var.equal = FALSE, paired = TRUE)
3 wilcox.test(TreatA, TreatB, paired = TRUE)
```

Careful: your treatment vector both have to have the same order

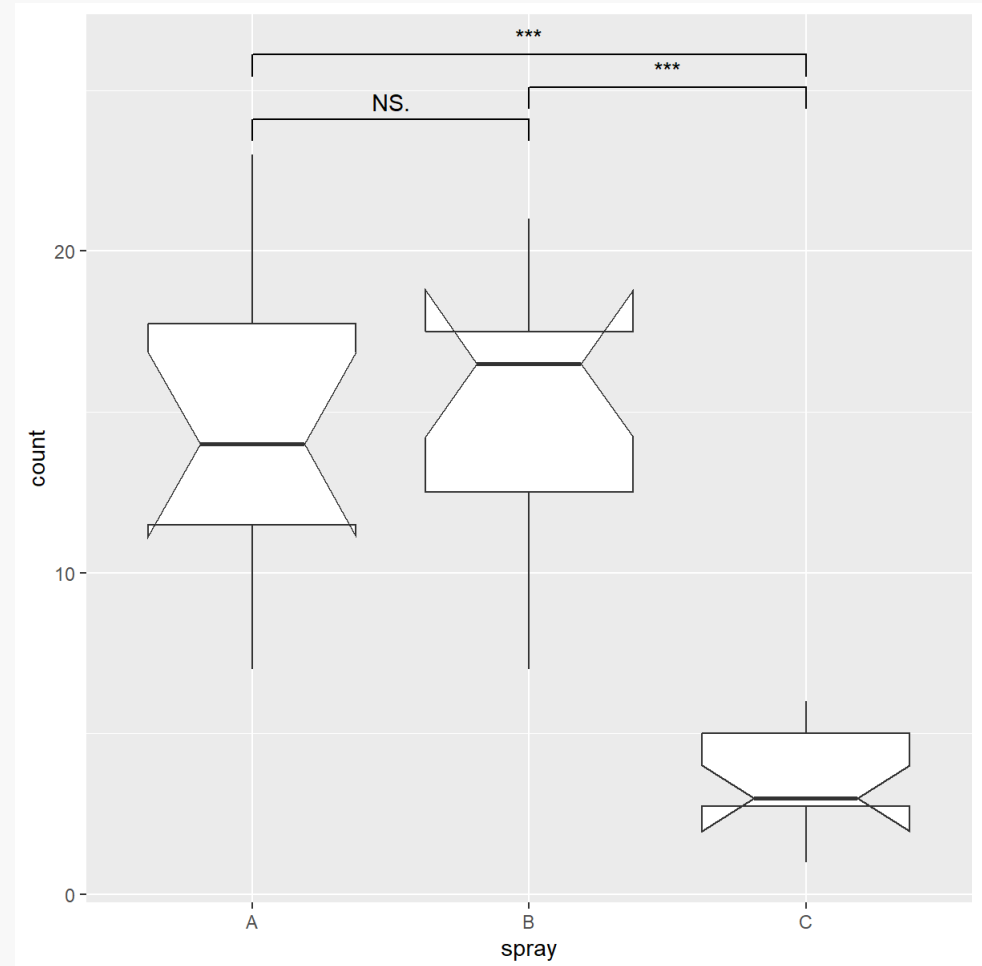
Plot test results with **ggsignif**

The **ggsignif** package offers a `geom_signif()` layer that can be added to a ggplot to annotate significance levels

```
1 # install.packages("ggsignif")  
2 library(ggsignif)
```

Plot test results with `geom_signif()`

```
1 ggplot(  
2   InsectSprays,  
3   aes(x = spray, y = count)  
4 ) +  
5   geom_boxplot(notch = TRUE) +  
6   geom_signif(  
7     comparisons = list(  
8       c("A", "B"),  
9       c("B", "C"),  
10      c("A", "C")  
11   ),  
12   map_signif_level = TRUE,  
13   y_position = c(23, 24, 25)  
14 )
```

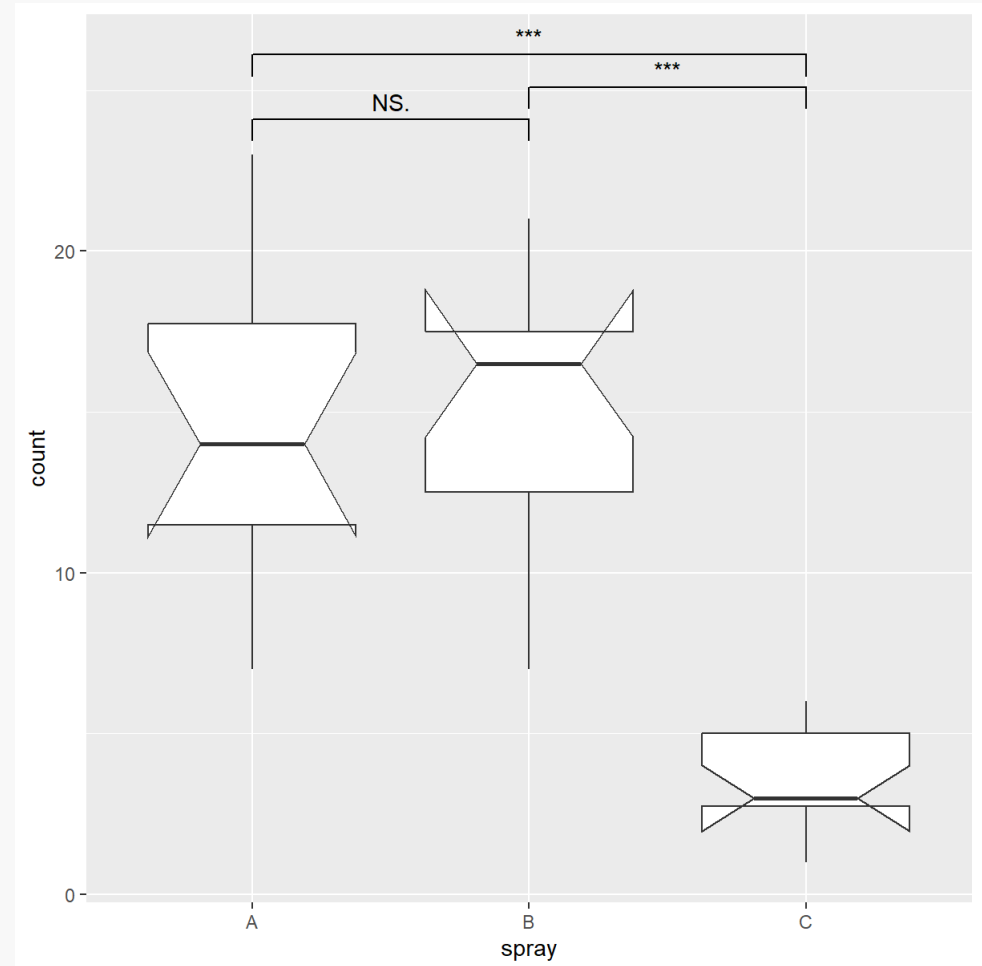


- By default, a Wilcoxon test is performed

Plot test results with `geom_signif()`

```
1 ggplot(  
2   InsectSprays,  
3   aes(x = spray, y = count)  
4 ) +  
5   geom_boxplot(notch = TRUE) +  
6   geom_signif(  
7     comparisons = list(  
8       c("A", "B"),  
9       c("B", "C"),  
10      c("A", "C")  
11   ),  
12   test = "t.test",  
13   test.args = list(  
14     var.equal = TRUE  
15   ),  
16   map_signif_level = TRUE,  
17   y_position = c(23, 24, 25)  
18 )
```

- `test`: run specific test
- `test.args`: pass additional arguments in a list
- `?geom_signif` for more options

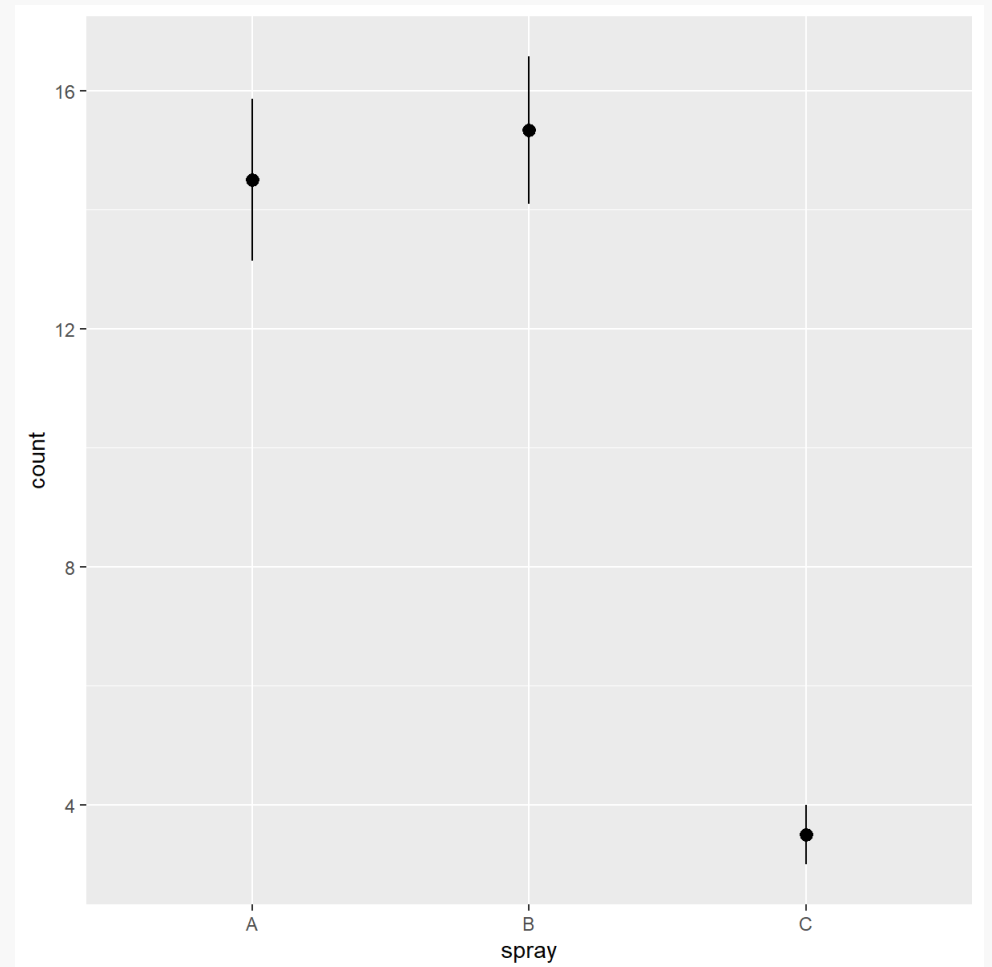


Plot mean \pm se using `stat_summary`

Another way to plot the results is to plot mean and standard error of the mean:

```
1 ggplot(  
2   InsectSprays,  
3   aes(x = spray, y = count)  
4 ) +  
5   stat_summary()
```

- By default `stat_summary` adds mean and standard error of the mean as pointrange

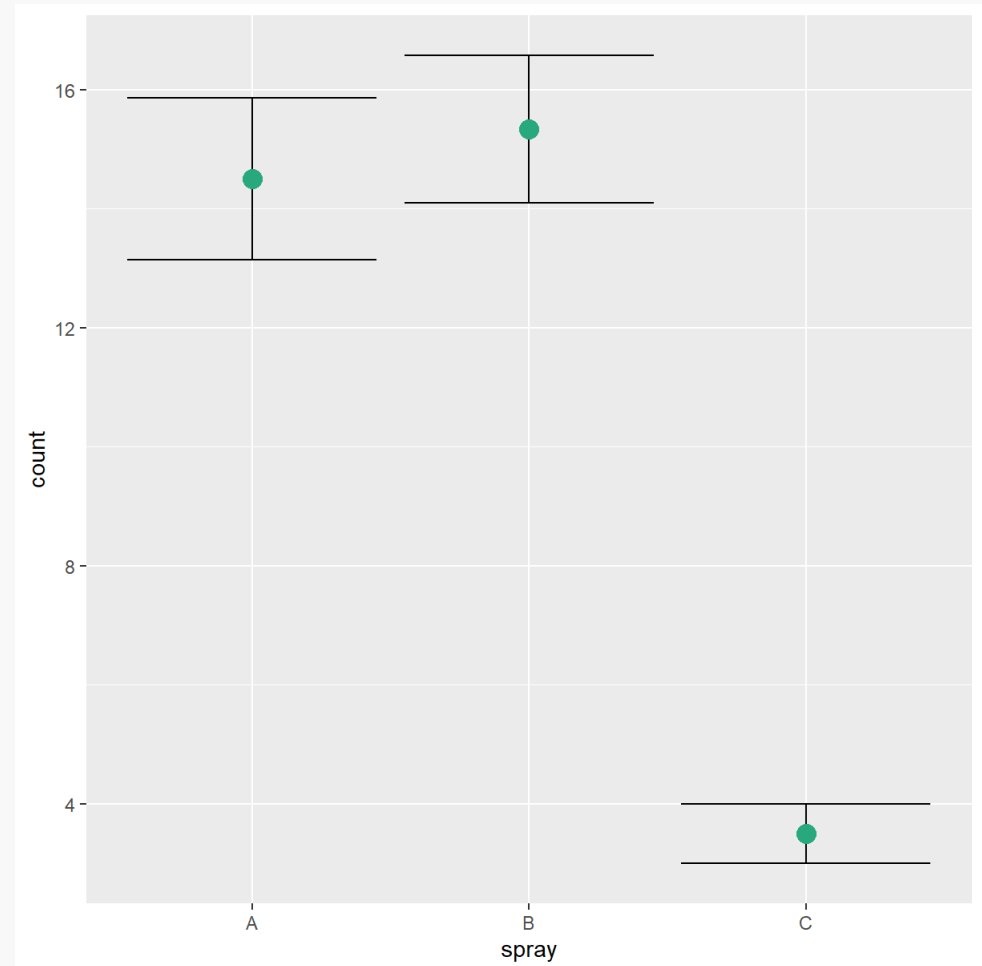


Plot mean \pm se using `stat_summary`

Another way to plot the results is to plot mean and standard error of the mean:

```
1 ggplot(  
2   InsectSprays,  
3   aes(x = spray, y = count)  
4 ) +  
5   stat_summary(  
6     fun.data = mean_se,  
7     geom = "errorbar"  
8   ) +  
9   stat_summary(  
10    fun.y = mean,  
11    geom = "point",  
12    color = "#28a7d",  
13    size = 4  
14  )
```

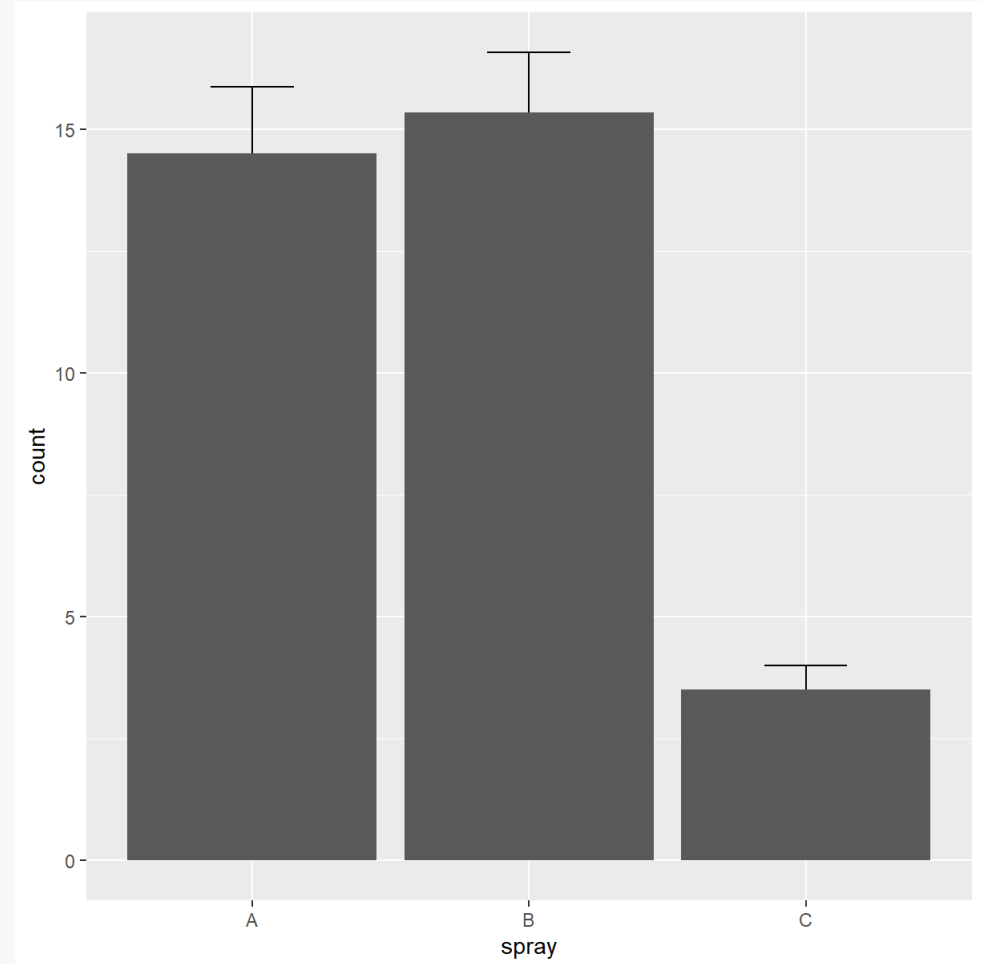
- Inside `stat_summary`, define summary function
 - `fun.data` for errorbars, `fun.y` for points (e.g. mean)
- Define the geom that represents the summary



Plot mean \pm se using `stat_summary`

Another way to plot the results is to plot mean and standard error of the mean:

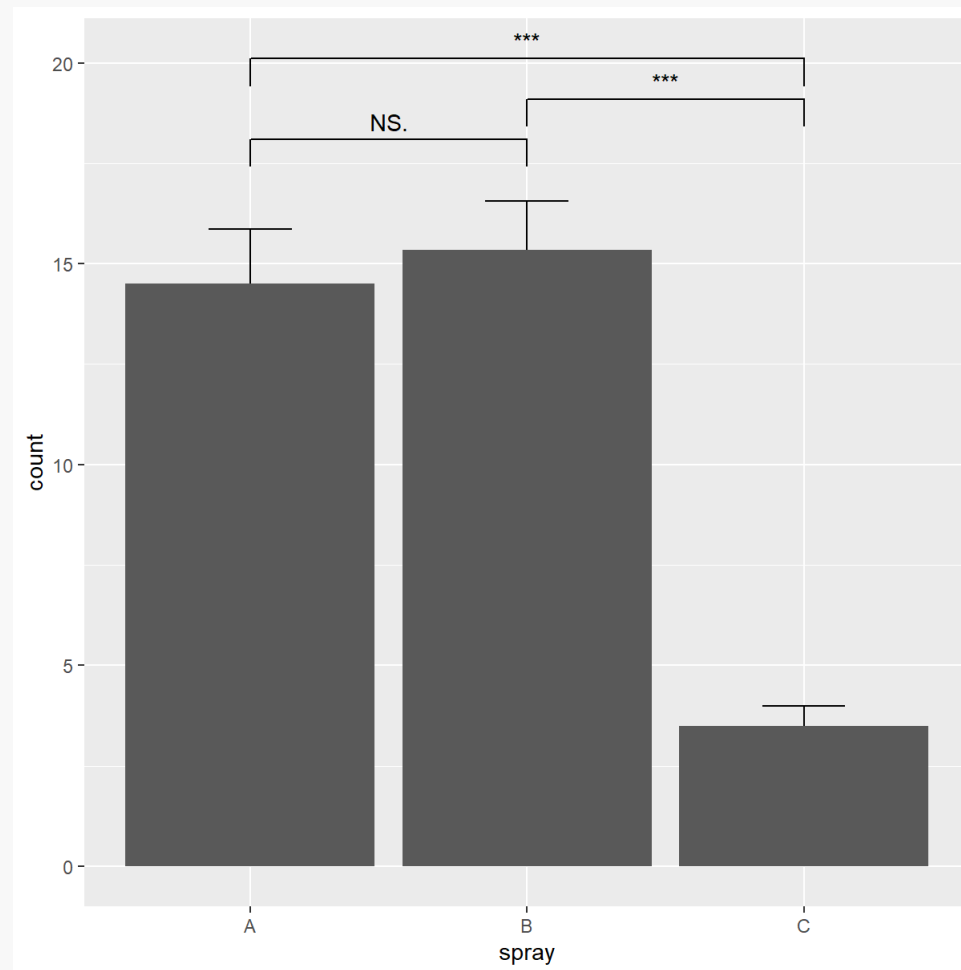
```
1 ggplot(  
2   InsectSprays,  
3   aes(x = spray, y = count)  
4 ) +  
5   stat_summary(  
6     fun.data = mean_se,  
7     geom = "errorbar",  
8     width = 0.3  
9   ) +  
10  stat_summary(  
11    fun.y = mean,  
12    geom = "bar",  
13    size = 4  
14  )
```



Plot mean \pm se using `stat_summary`

Just like before, you can also add a `geom_signif` to a barplot:

```
1 ggplot(  
2   InsectSprays,  
3   aes(x = spray, y = count)  
4 ) +  
5   stat_summary(  
6     fun.data = mean_se,  
7     geom = "errorbar",  
8     width = 0.3  
9   ) +  
10  stat_summary(  
11    fun.y = mean,  
12    geom = "bar"  
13  ) +  
14  ggsignif::geom_signif(  
15    comparisons = list(  
16      c("A", "B"),  
17      c("B", "C"),  
18      c("A", "C")  
19    ),  
20    test = "t.test",  
21    map_signif_level = TRUE,  
22    y_position = c(17, 18, 19)  
23  )
```



Now you

Task 1 (45) min)

Statistical tests

Find the task description [here](#)

