

# Linear Models

## Introduction to R - Day 3

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A little bit of theoretical background

# Linear models background

The data:

- Random sample of  $n$  data points ( $Y_i, X_{i1}, X_{i2}, \dots, X_{ip}, i = 1 \dots n$ )
  - $X_{i1}, X_{i2}, \dots, X_{ip}$  are  $p$  **independent predictor** variables
  - $Y_i$  is the **dependent** observation and **response variable**

Example

Data set of grassland productivity ( $Y_i$ ) depending on plant species richness ( $X_{i1}$ ) and the location/measurement site ( $X_{i2}$ ).

Aim of linear model:

- Do the predictors (species richness, location) have a significant effect on the response (grassland productivity)?

# Linear models background

The data:

- Random sample of n data points ( $Y_i, X_{i1}, X_{i2}, \dots, X_{ip}, i = 1\dots n$ )
  - $X_{i1}, X_{i2}, \dots, X_{ip}$  are p **independent predictor** variables
  - $Y_i$  is the **dependent** observation and **response variable**

The model:

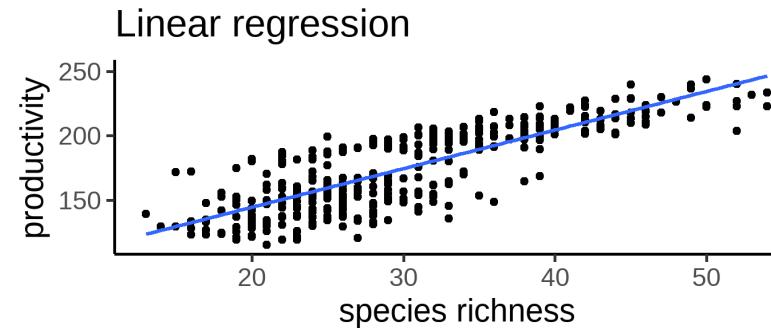
$$Y_i = \beta_0 + \beta_1 * X_{1,i} + \beta_2 * X_{2,i} + \epsilon$$

- $Y_i$  value of response variable
- $\beta_0, \beta_1, \beta_2$  model coefficients
- $X_{1,i}$  value of predictor  $X_1$
- $X_{2,i}$  value of predictor  $X_2$
- $\epsilon$  error term

# Linear models background

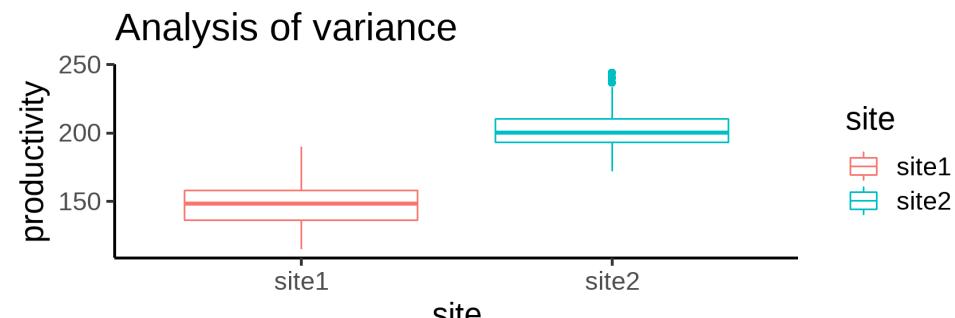
## Linear regression

- numerical response
- numerical predictor(s)



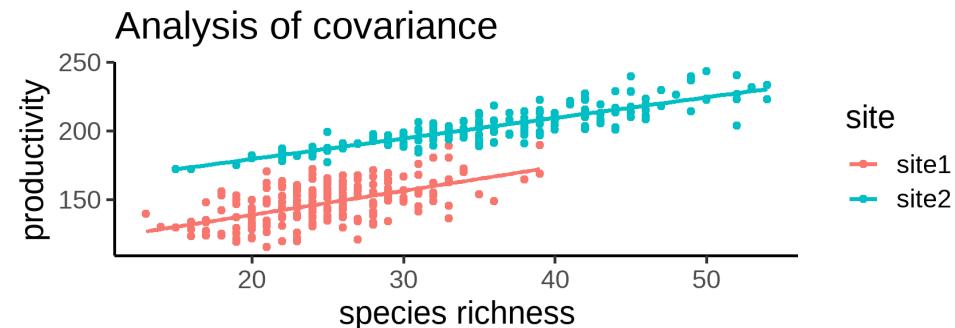
## Analysis of variance

- numerical response
- categorical predictor(s)



## Analysis of covariance

- numerical response
- numerical and categorical predictor(s)



# Linear models background

Linear relation with two predictors  $X_1$  and  $X_2$  ( $i = 1 \dots n$ )

Without interaction

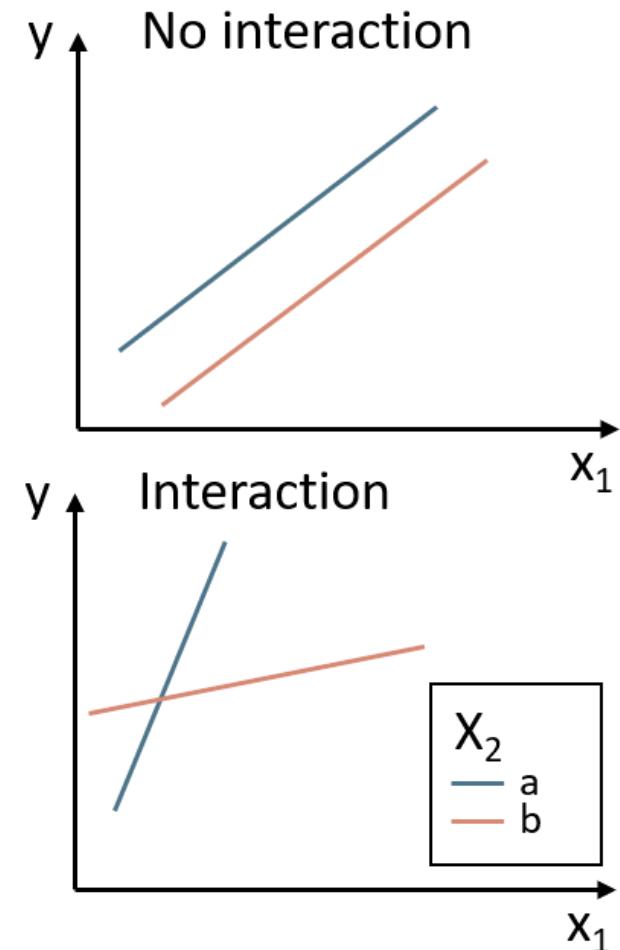
$$Y_i = \beta_0 + \beta_1 * X_{1,i} + \beta_2 * X_{2,i} + \epsilon$$

With interaction

$$Y_i = \beta_0 + \beta_1 * X_{1,i} + \beta_2 * X_{2,i} + \beta_3 * X_{1,i} * X_{2,i} + \epsilon$$

with

- $Y_i$  value of response variable
- $\beta_0, \beta_1, \beta_2$  model coefficients
- $X_{1,i}$  value of predictor  $X_1$
- $X_{2,i}$  value of predictor  $X_2$
- $\epsilon$  error term



# Goodness of fit linear model

Model residuals

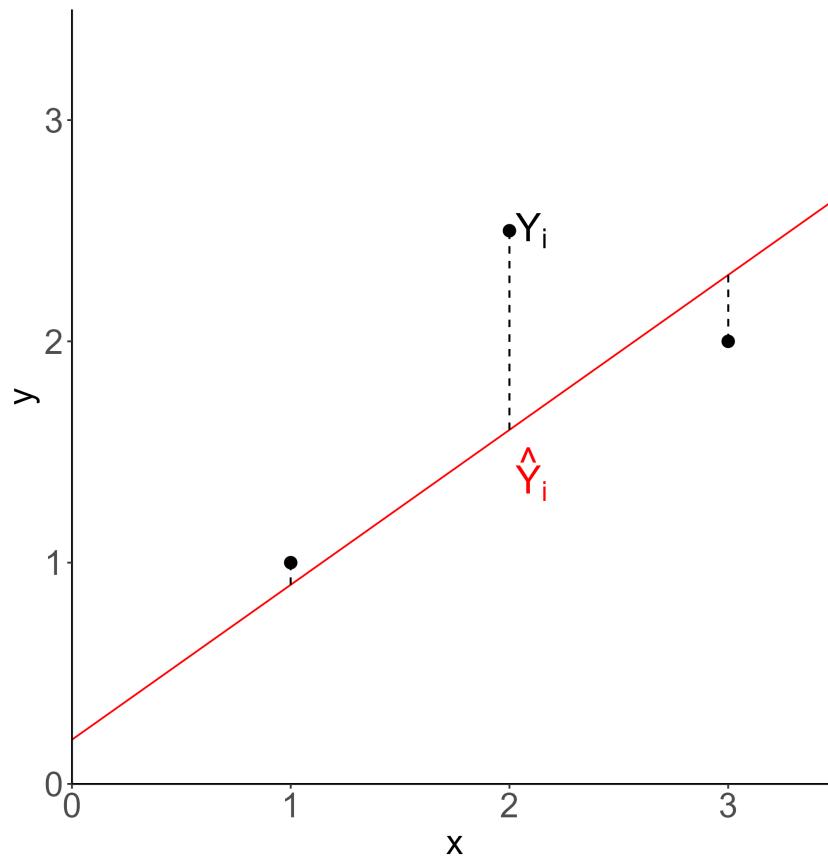
$$Y_i - \hat{Y}_i$$

Residual sum of squares (RSS)

$$RSS = \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

Aim of the model fitting:

Find the model coefficients that lead to the lowest sum of squares.



# Assumptions for linear models

Finding the model estimates that lead to the lowest residual sum of squares works only if:

- 1) Residuals are normally distributed
- 2) Residual variance is constant
- 3) No strong outliers

This has to be checked for every linear model!

If assumptions are not fulfilled, a different model approach has to be chosen.

# How to fit linear models in

# The data

We use productivity data from grassland sites.

The data set is called `prod` and has 3 variables: site, productivity and richness (species richness):

```
prod
```

```
## # A tibble: 400 x 3
##   site   richness productivity
##   <fct>    <dbl>        <dbl>
## 1 site1      23        122.
## 2 site1      26        158.
## 3 site1      24        165
## 4 site1      25        165.
## # ... with 396 more rows
```

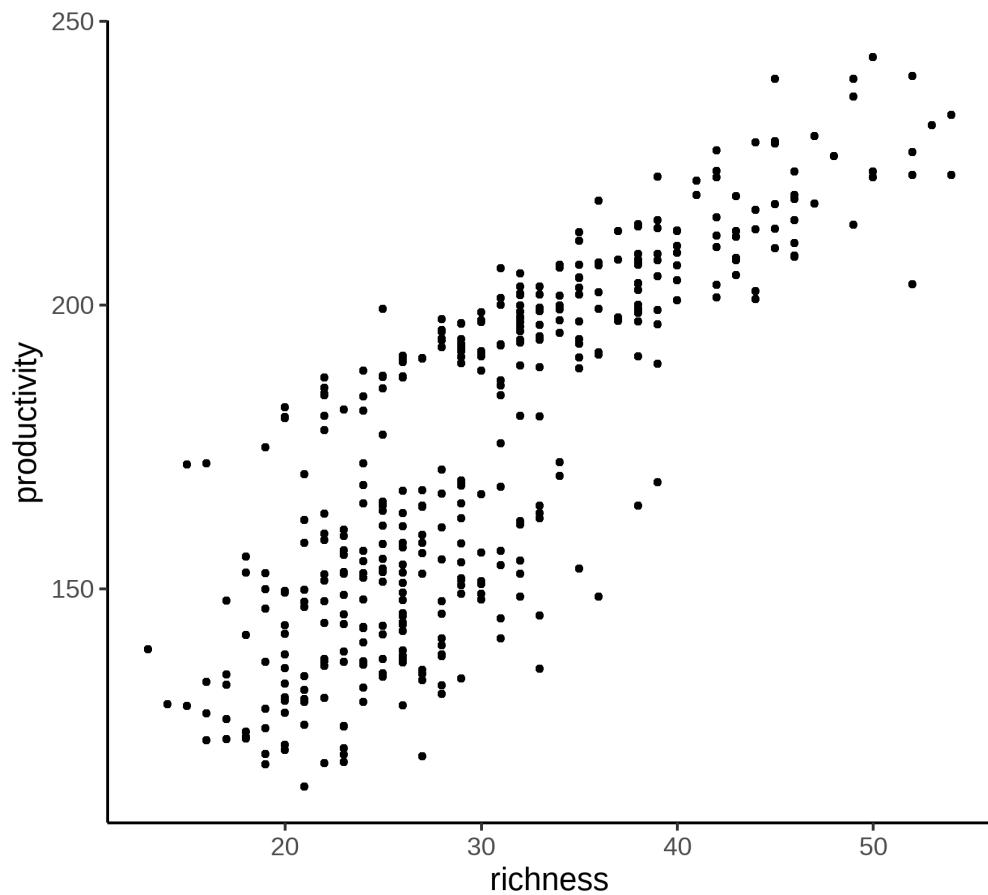
The variable site is a factor with two levels: site1 and site2

```
levels(prod$site) # get all levels of the factor
## [1] "site1" "site2"
```

# Linear regression in

# Linear regression in R

$H_1$ : Species richness has an effect on productivity



# Linear regression in R

Use the `lm` function to fit a linear model in R.

The general structure of the function call is like this:

```
lm ( formula = Y ~ X, data = dat )
```

with

- `Y` being the response variable
- `X` being the predictor(s)
- `dat` being the name of the data

Multiple predictors can be added with `+` and `:` depending on interaction:

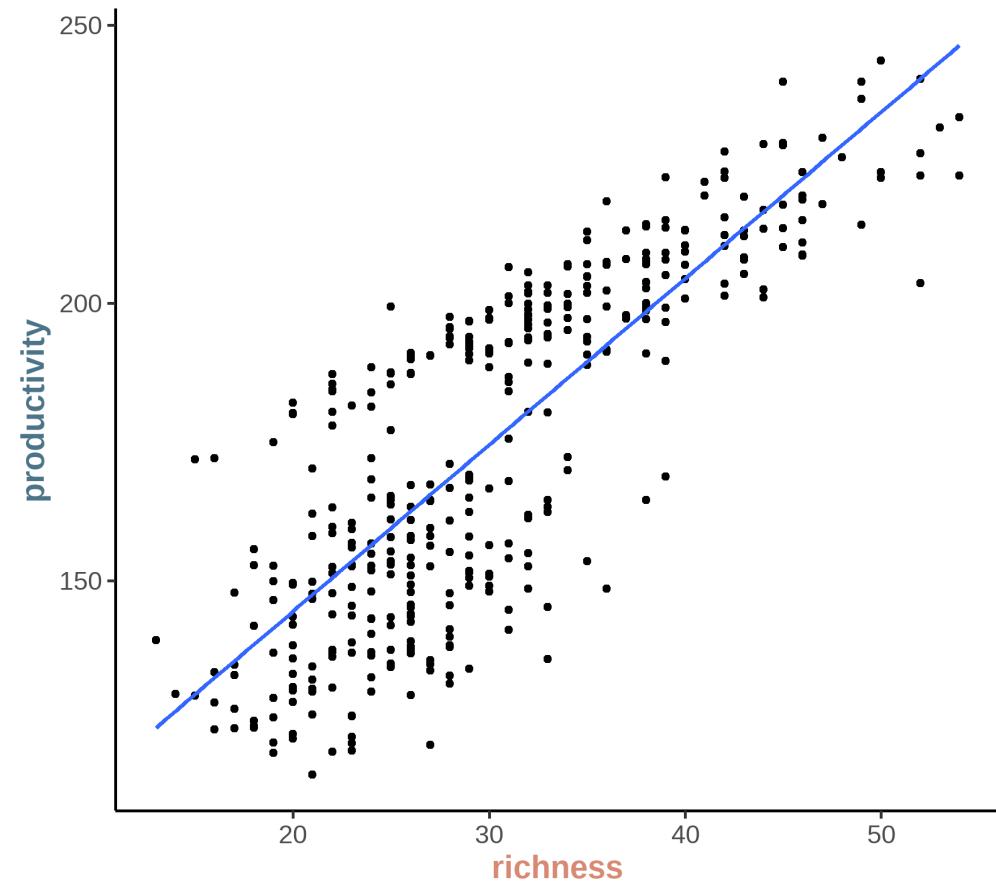
- `Y ~ x1 + x2` tests effects without interaction
- `Y ~ x1 + x2 + x1:x2` tests single effects and interaction between `x1` and `x2`

# Linear regression in R

Let's fit a linear model to test our hypothesis

```
lm ( formula = Y ~ X, data = dat )
```

```
prod_lm <- lm(productivity ~ richness,  
                 data = prod)
```



# Linear regression in R

Is the effect of richness on productivity significant?

Or in other words

Does the model with richness as predictor significantly reduce the residual sum of squares?

## Hypothesis testing using F-Tests

Compare the complex model with a simple model that does not contain the predictor

$H_0$ : The error variance in the simple model is not significantly higher than in the more complex model

- $H_0$  accepted: simplification was justified → use simple model without predictor
- $H_0$  rejected: simplification reduced explanatory power → use complex model with predictor

# Linear regression in R

## Hypothesis testing using F-Tests in R

$H_0$ : The error variance in the simple model is not significantly higher than in the more complex model

`drop1` deletes single terms from the model and performs an F-test:

```
drop1(prod_lm, test = "F")
## Single term deletions
##
## Model:
## productivity ~ richness
##           Df Sum of Sq    RSS    AIC F value    Pr(>F)
## <none>          132779 2326.0
## richness  1     254119 386899 2751.8   761.71 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Result: Reject  $H_0 \rightarrow$  Richness increases productivity ( $F_{1,398} = 761.71, p < 0.001$ )

# Extracting the coefficients

Look at model coefficients using the model `summary`

```
summary(prod_lm)
##
## Call:
## lm(formula = productivity ~ richness, data = prod)
##
## Residuals:
##     Min      1Q  Median      3Q     Max 
## -47.593 -13.683   0.029  13.970  42.295 
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 84.6982    3.3987  24.92   <2e-16 ***
## richness    2.9938    0.1085  27.60   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 18.27 on 398 degrees of freedom
## Multiple R-squared:  0.6568,    Adjusted R-squared:  0.6559 
## F-statistic: 761.7 on 1 and 398 DF,  p-value: < 2.2e-16
```

# Summary table

```
summary(prod_lm)
##
## Call:
## lm(formula = productivity ~ richness, data = prod)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -47.593 -13.683   0.029  13.970  42.295
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 84.6982    3.3987  24.92 <2e-16 ***
## richness    2.9938    0.1085  27.60 <2e-16 ***
## ---
## Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 18.27 on 398 degrees of freedom
## Multiple R-squared:  0.6568,   Adjusted R-squared:  0.6559
## F-statistic: 761.7 on 1 and 398 DF,  p-value: < 2.2e-16
```

Calculated model

Distribution of residuals (errors)

# Summary table

```
summary(prod_lm)
##
## Call:
## lm(formula = productivity ~ richness, data = prod)
## Model coefficients:
## 1. Intercept = 84.7
## 2. Slope = 3
## -47.593 -13.683   Median 0.029 18.970   Max 42.295
## 
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 84.6982   3.3987  24.92 <2e-16 ***
## richness    2.9938   0.1085  27.60 <2e-16 ***
## ---
## Signif. codes:  0 '****' 0.001 '***' 0.01 '**' 0.05 '*' 0.1 '.' 1
## 
## Residual standard error: 18.27 on 398 degrees of freedom
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# Summary table

```
summary(prod_lm)
##
## Call:
## lm(formula = productivity ~ richness, data = prod)
##
## Residuals:
##     Min      1Q  Median      3Q     Max 
## -47.593 -13.683   0.029  13.970  42.295 
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 84.6982    3.3987  24.92   <2e-16 ***
## richness    2.9938    0.1085  27.60   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 18.27 on 398 degrees of freedom
## Multiple R-squared:  0.6568, Adjusted R-squared:  0.6559 
## F-statistic: 761.7 on 1 and 398 DF, p-value: < 2.2e-16
```

t-statistics: ratio of coefficients to their standard error

# Summary table

```
summary(prod_lm)
##
## Call:
## lm(formula = productivity ~ richness, data = prod)
##
## Residuals:
##     Min      1Q  Median      3Q     Max 
## -47.593 -13.683   0.029  13.970  42.295 
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 84.6982    3.3987  24.92   <2e-16 ***
## richness    2.9938    0.1085  27.60   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.01 '**' 0.05 '*' 0.1 '.' 1
## 
## Coefficient of determination R2
## 
## Residual standard error: 18.27 on 398 degrees of freedom
## Multiple R-squared:  0.6568, Adjusted R-squared:  0.6559 
## F-statistic: 761.7 on 1 and 398 DF, p-value: < 2.2e-16
```

# Test model assumptions

Test model assumptions to make sure that:

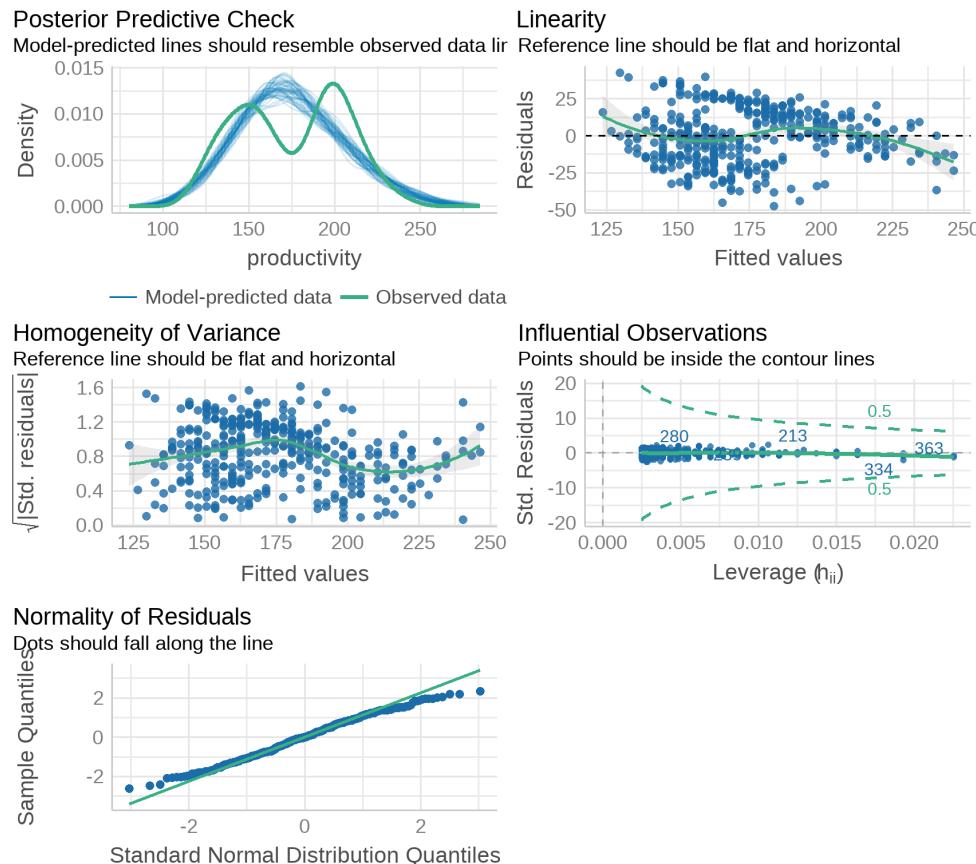
- 1) Residuals are normally distributed
- 2) Variance is constant (homogeneous)
- 3) There are no strong outliers or very influential observations

We can check that by looking at diagnostic plots

```
# install.packages("performance")
performance::check_model(prod_lm)
```

# Test model assumptions

```
performance::check_model(prod_lm)
```



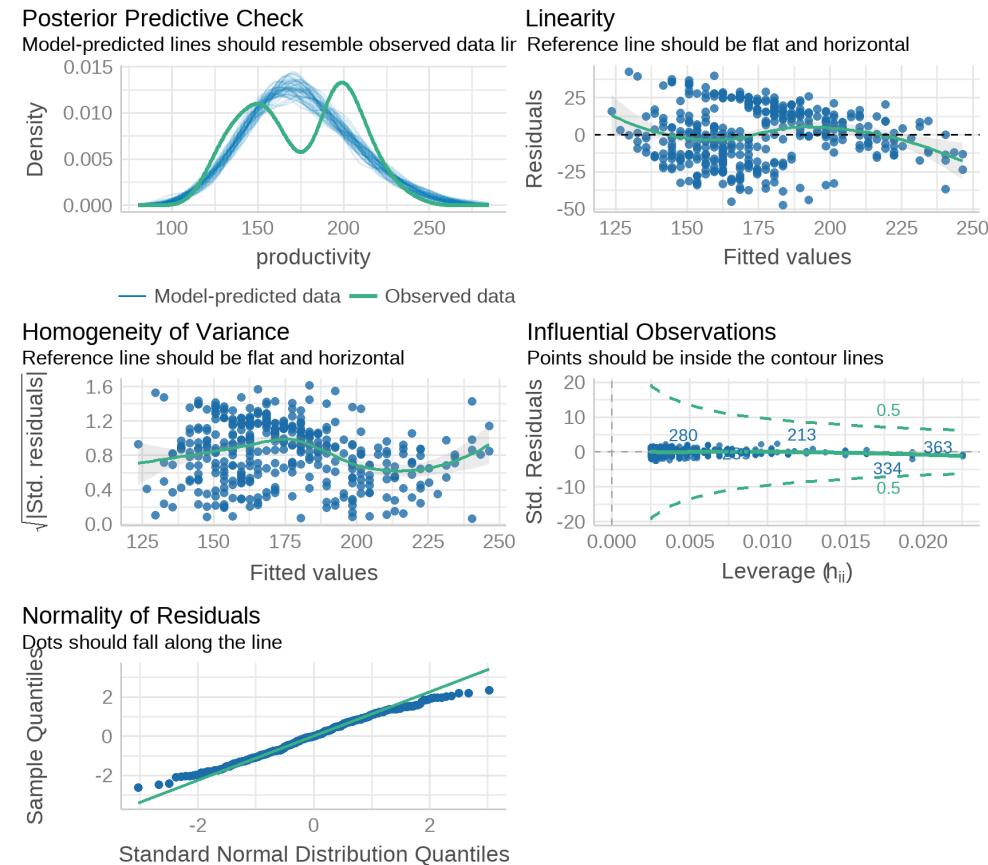
# Test model assumptions

Check the assumptions

- Residuals are normally distributed ✓
- Variance is constant (homogeneous) ✓
- There are no strong outliers or very influential observations ✓

Checking diagnostic plots needs some experience

- Real life data (almost) never perfectly fit the assumptions
- Linear models are to some extent robust against violations of the assumptions



# Plot the model

## Option 1

Add the regression line directly as a ggplot layer

Use `geom_smooth()` to add the model directly:

```
ggplot(prod, aes(x = richness, y =  
productivity)) +  
  geom_point() +  
  geom_smooth(method = "lm", se = FALSE)
```

# Plot the model

## Option 2

Extract coefficients (slope + intercept) of the model and add the regression line

```
# These are the coefficients of the lm  
prod_lm$coefficients  
## (Intercept) richness  
## 84.698163 2.993774
```

```
intercept <- prod_lm$coefficients[1]  
slope <- prod_lm$coefficients[2]
```

# Plot the model

## Option 2

Extract coefficients (slope + intercept) of the model and add the regression line

```
intercept <- prod_lm$coefficients[1]
slope <- prod_lm$coefficients[2]
```

Add a line defined by slope and intercept using

`geom_abline()`:

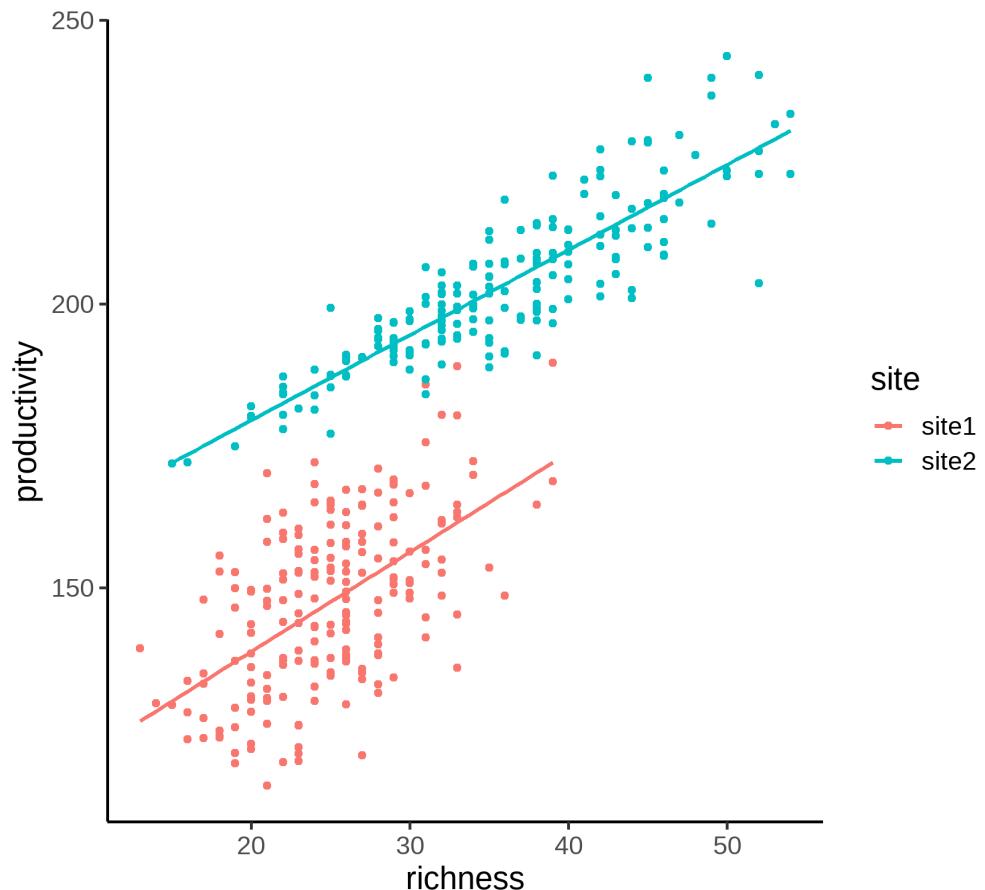
```
ggplot(prod, aes(x=richness, y=productivity)) +
  geom_point() +
  geom_abline(slope = slope,
              intercept = intercept)
```

# Analysis of covariance

# Analysis of covariance

One categorical and one numerical predictor variable

Two possible models:



# Analysis of covariance

Fit the model with `lm`

## Without interaction

Species richness has an effect on productivity and there is a difference between sites.

```
prod_lm2a <- lm(productivity ~ richness + site, data = prod)
```

## With interaction

Species richness has an effect on productivity and the effect differs between sites.

```
prod_lm2b <- lm(productivity ~ richness + site + richness:site, data = prod)
```

# Analysis of covariance

Are the effects significant?

## Without interaction

```
drop1(prod_lm2a, test = "F") # no interaction
## Single term deletions
##
## Model:
## productivity ~ richness + site
##           Df Sum of Sq    RSS    AIC F value    Pr(>F)
## <none>            40064 1848.7
## richness   1     42908  82973 2137.9  425.18 < 2.2e-16 ***
## site       1     92715 132779 2326.0  918.72 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Both, the removal of site and richness significantly increase the model's RSS → both site and richness are significant predictors

# Analysis of covariance

Are the effects significant?

With interaction

```
drop1(prod_lm2b, test = "F") # interaction
## Single term deletions
##
## Model:
## productivity ~ richness + site + richness:site
##           Df Sum of Sq   RSS   AIC F value Pr(>F)
## <none>            39850 1848.6
## richness:site     1    214.53 40064 1848.7  2.1319 0.1451
```

The removal of the interaction does not significantly increase the model's RSS → the interaction is not significant and the simpler model without interaction is just as good in predicting productivity.

# Extracting model coefficients

```
summary(prod_lm2a)
##
## Call:
## lm(formula = productivity ~ richness + site, data = prod)
##
## Residuals:
##       Min     1Q Median     3Q    Max
## -30.1743 -6.2895 -0.0352  5.6955 28.9276
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 108.36550   2.02582  53.49 <2e-16 ***
## richness     1.56699   0.07599  20.62 <2e-16 ***
## sitesite2    38.78575   1.27962  30.31 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.05 on 397 degrees of freedom
## Multiple R-squared:  0.8964,    Adjusted R-squared:  0.8959 
## F-statistic: 1718 on 2 and 397 DF,  p-value: < 2.2e-16
```

# Extracting model coefficients

Call:

```
lm(formula = productivity ~ richness + site, data = prod)
```

Residuals:

Min	1Q	Median
-30.1743	-6.2895	-0.0352

Intercept site1 = 108.4

Slope = 1.6

Intercept site2 = 108.4 + 38.8

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	108.36550	2.02582	53.49	<2e-16	***
richness	1.56699	0.07599	20.62	<2e-16	***
sitesite2	38.78575	1.27962	30.31	<2e-16	***
---					

Signif. codes: 0 ‘\*\*\*’ 0.001 ‘\*\*’ 0.01 ‘\*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 10.05 on 397 degrees of freedom

Multiple R-squared: 0.8964, Adjusted R-squared: 0.8959

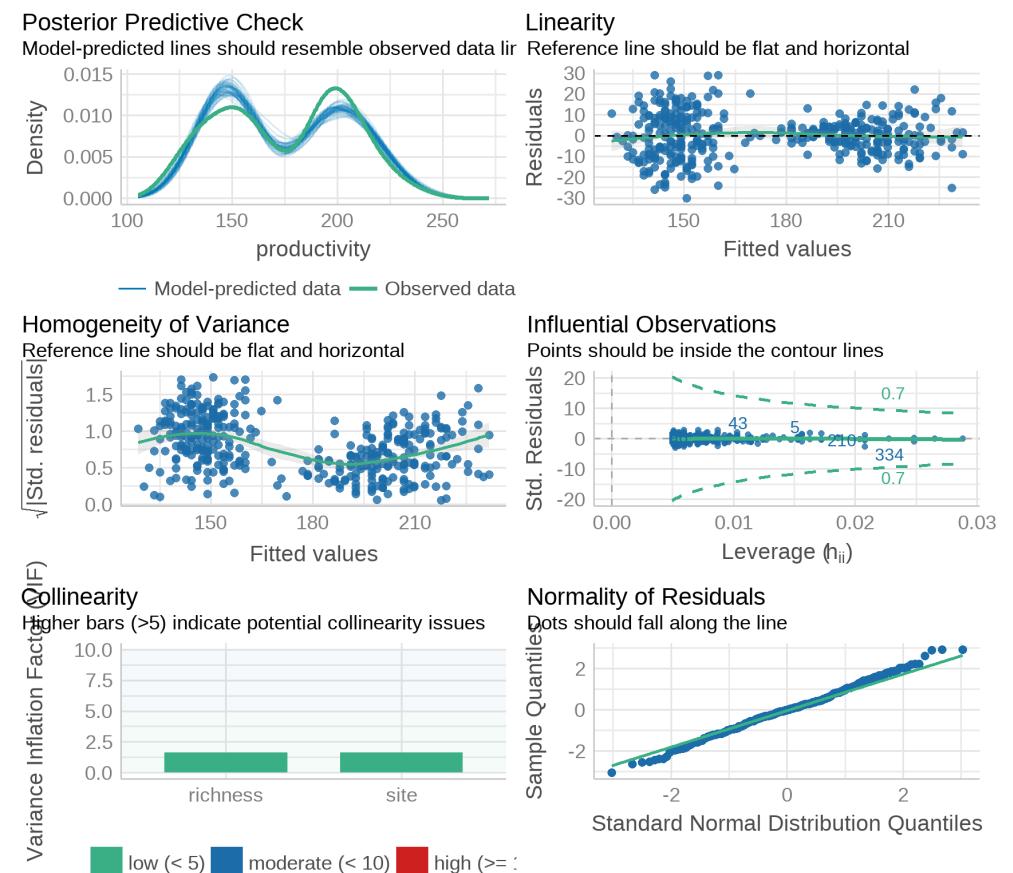
F-statistic: 1718 on 2 and 397 DF, p-value: < 2.2e-16

# Test model assumptions

Check the assumptions

- Residuals are normally distributed ✓
- Variance is constant (homogeneous) ✓
- There are no strong outliers or very influential observations ✓

```
performance::check_model(prod_lm2a)
```



# Plot the model

If we want to be precise, we could not use `geom_smooth()` for this model because it plots the full model with interaction between the predictors

```
ggplot(prod, aes(x = richness,  
                  y = productivity,  
                  color = site)) +  
  geom_point() +  
  geom_smooth(method = "lm")
```

This plot is not 100% appropriate if the model you present is without interaction

# Plot the model

Extract coefficients and add regression line

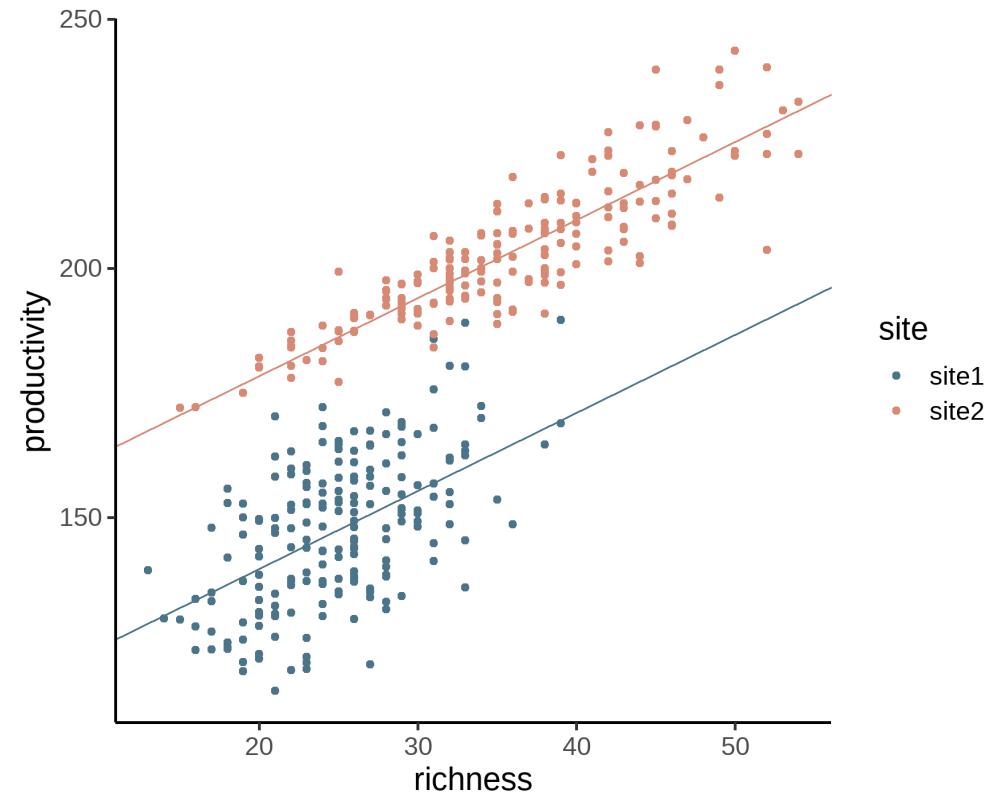
```
# these are the model coefficients
prod_lm2a$coefficients
## (Intercept)    richness   sitesite2
## 108.365497     1.566994   38.785753
```

```
slope <- prod_lm2a$coefficients[2]
intercept1 <- prod_lm2a$coefficients[1]
intercept2 <- prod_lm2a$coefficients[1] + prod_lm2a$coefficients[3]
```

# Plot the model

Extract coefficients and add regression line

```
ggplot(prod, aes(x = richness,
                  y = productivity,
                  color = site)) +
  geom_point() +
  scale_color_manual(
    values = c("#4C7488", "#D78974")) +
  geom_abline(
    slope = slope,
    intercept = intercept1,
    color = "#4C7488"
  ) +
  geom_abline(
    slope = slope,
    intercept = intercept2,
    color = "#D78974"
  )
```



# Plot the model

## Option 2: Use the `predict()` function

```
# step 1: create some data to predict from
pred_data <- tidyverse::expand_grid(
  richness = min(prod$richness) : max(prod$richness),
  site = c("site1", "site2")
)
```

```
## # A tibble: 84 x 2
##   richness site
##       <int> <chr>
## 1        13 site1
## 2        13 site2
## 3        14 site1
## # ... with 81 more rows
```

- `tidyverse::expand_grid` returns a tibble with all combinations of site and richness given as input
  - The `tidyverse` package is part of the tidyverse
- The column names of the tibble that you create in this step have to correspond to the predictor names in the linear model

# Plot the model

## Option 2: Use the `predict()` function

```
# step 1: create some data to predict from
pred_data <- tidyverse::expand_grid(
  richness = min(prod$richness) : max(prod$richness),
  site = c("site1", "site2")
)
```

```
# step2: predict productivity values from pred_data
predictions <- predict(prod_lm2a, newdata = pred_data)
```

- `predict` uses the `prod_lm2a` model and the data produced with `expand_grid` to predict productivity values for each combination of site and richness.

# Plot the model

## Option 2: Use the `predict()` function

```
# step 1: create some data to predict from
pred_data <- tidyverse::expand_grid(
  richness = min(prod$richness) : max(prod$richness),
  site = c("site1", "site2")
)
```

```
# step 2: predict productivity values from pred_data
predictions <- predict(prod_lm2a, newdata = pred_data)
```

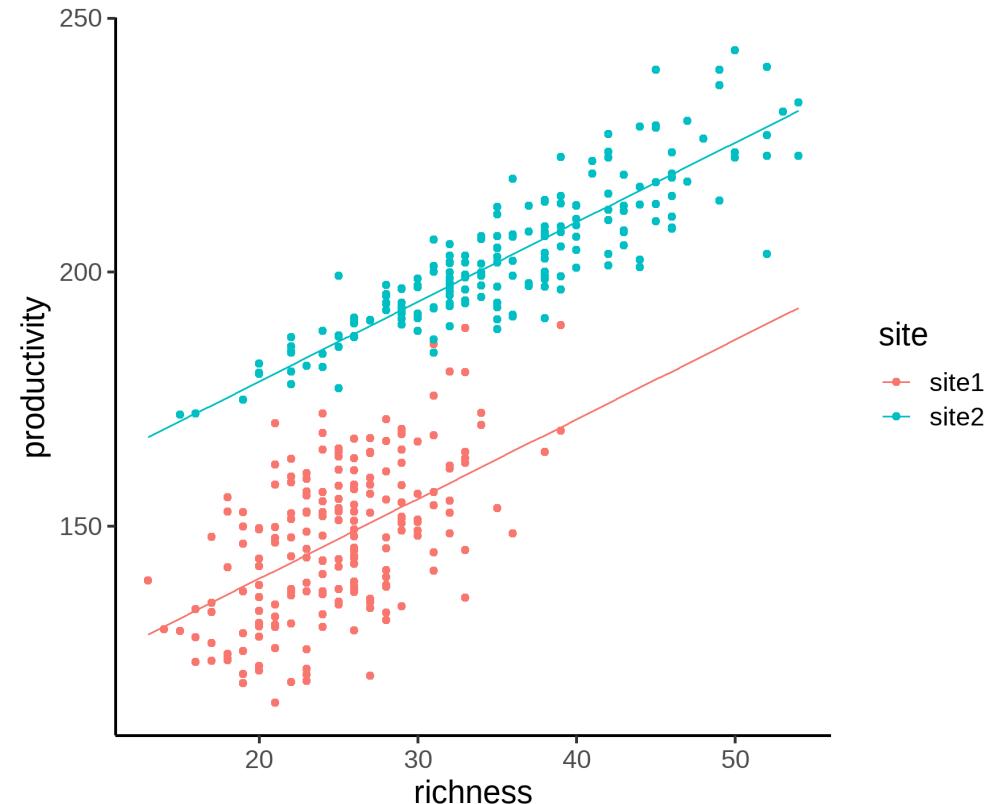
```
# step 3: add predictions to the tibble
pred_data$productivity <- predictions
```

# Plot the model

## Option 2: Use the `predict()` function

Add a new `geom_*` layer to the plot from the prediction data:

```
# step 4: Add predictions with geom_line
ggplot(prod, aes(x = richness,
                  y = productivity,
                  color = site)) +
  geom_point() +
  geom_line(data = pred_data)
```



- The aesthetic mapping is inherited from the top level `ggplot` call to the `geom_line`

# Plot the model

## Option 2: Use the `predict()` function

### Summary of general workflow

- **Step 1:** Use `expand_grid` to create a tibble with values for all predictor variables (the columns have to have the exact same name as the original data)
- **Step 2:** Use `predict` to predict response variable with the model using input predictor values from tibble in step 1
- **Step 3:** Add predictions as column to the tibble from step 1
- **Step 4:** Add predictions to the plot using a new `geom_line()` layer based on the tibble from step 3

# Analysis of variance (Anova)

# Anova

Only categorical predictors.

Example: Data set `chickwts` about the weight of chickens fed with different diets.

```
chickwts  
## # A tibble: 71 x 2  
##   weight feed  
##   <dbl> <fct>  
## 1    179 horsebean  
## 2    160 horsebean  
## 3    136 horsebean  
## 4    227 horsebean  
## # ... with 67 more rows
```

# Anova

$H_1$ : The diet has an effect on the weight of chicken.

Fit a linear model with `lm` and test the significance of the predictor:

```
lm_chicken <- lm(weight ~ feed, data = chickwts)
drop1(lm_chicken, test = "F")
## Single term deletions
##
## Model:
## weight ~ feed
##      Df Sum of Sq    RSS    AIC F value    Pr(>F)
## <none>          195556 574.39
## feed     5     231129 426685 619.78  15.365 5.936e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Removing the predictor `feed` from the model significantly increases the RSS → The model with `feed` explains the data better than the model without `feed`, so the effect of `feed` on the chicken weight is significant.

# Extracting model coefficients

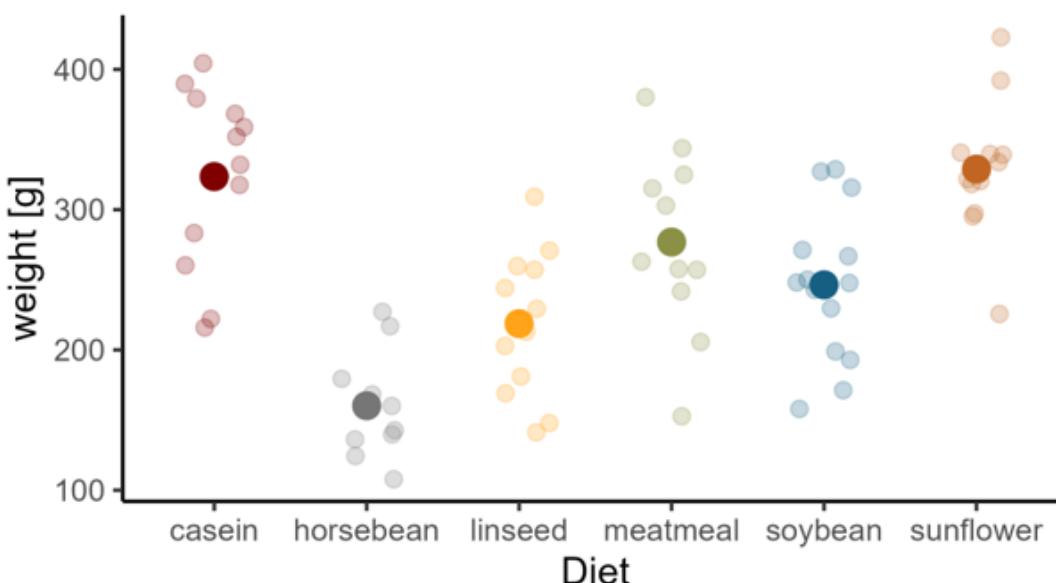
```
summary(lm_chicken)
##
## Call:
## lm(formula = weight ~ feed, data = chickwts)
##
## Residuals:
##       Min        1Q    Median        3Q       Max
## -123.909 -34.413     1.571   38.170  103.091
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 323.583   15.834  20.436 < 2e-16 ***
## feedhorsebean -163.383   23.485 -6.957 2.07e-09 ***
## feedlinseed   -104.833   22.393 -4.682 1.49e-05 ***
## feedmeatmeal   -46.674   22.896 -2.039 0.045567 *
## feedsoybean    -77.155   21.578 -3.576 0.000665 ***
## feedsunflower      5.333   22.393   0.238 0.812495
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 54.85 on 65 degrees of freedom
## Multiple R-squared:  0.5417,    Adjusted R-squared:  0.5064
## F-statistic: 15.36 on 5 and 65 DF,  p-value: 5.936e-10
```

# Extracting model coefficients

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	323.583	15.834	20.436	< 2e-16	***
feedhorsebean	-163.383	23.485	-6.957	2.07e-09	***
feedlinseed	-104.833	22.393	-4.682	1.49e-05	***
feedmeatmeal	-46.674	22.896	-2.039	0.045567	*
feedsoybean	-77.155	21.578	-3.576	0.000665	***
feedsunflower	5.333	22.393	0.238	0.812495	

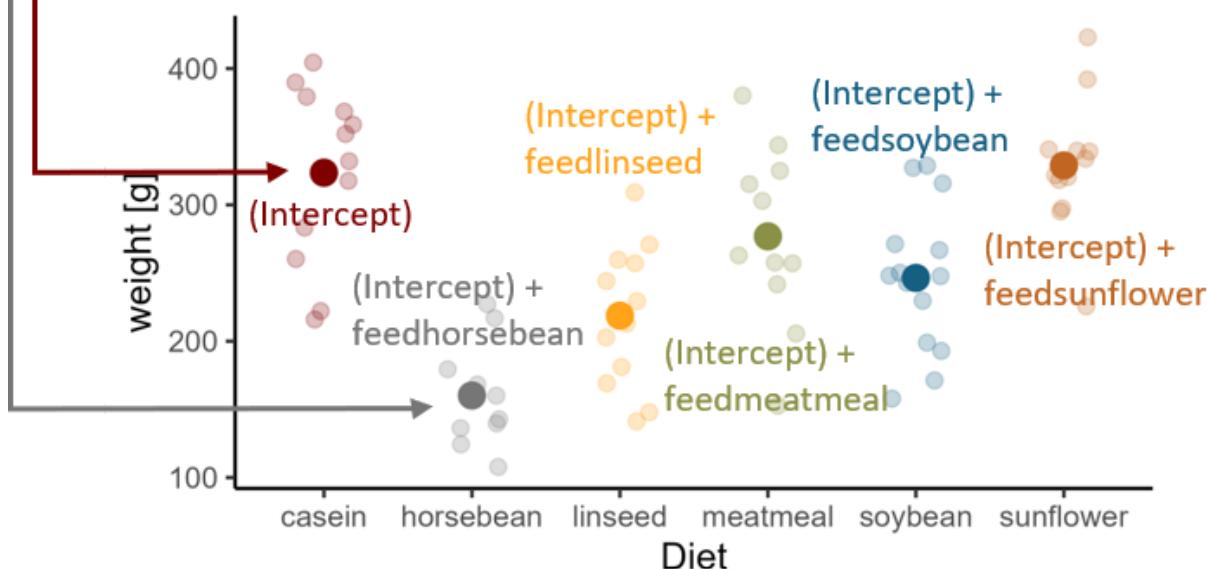
---



# Extracting model coefficients

Coefficients:

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---				

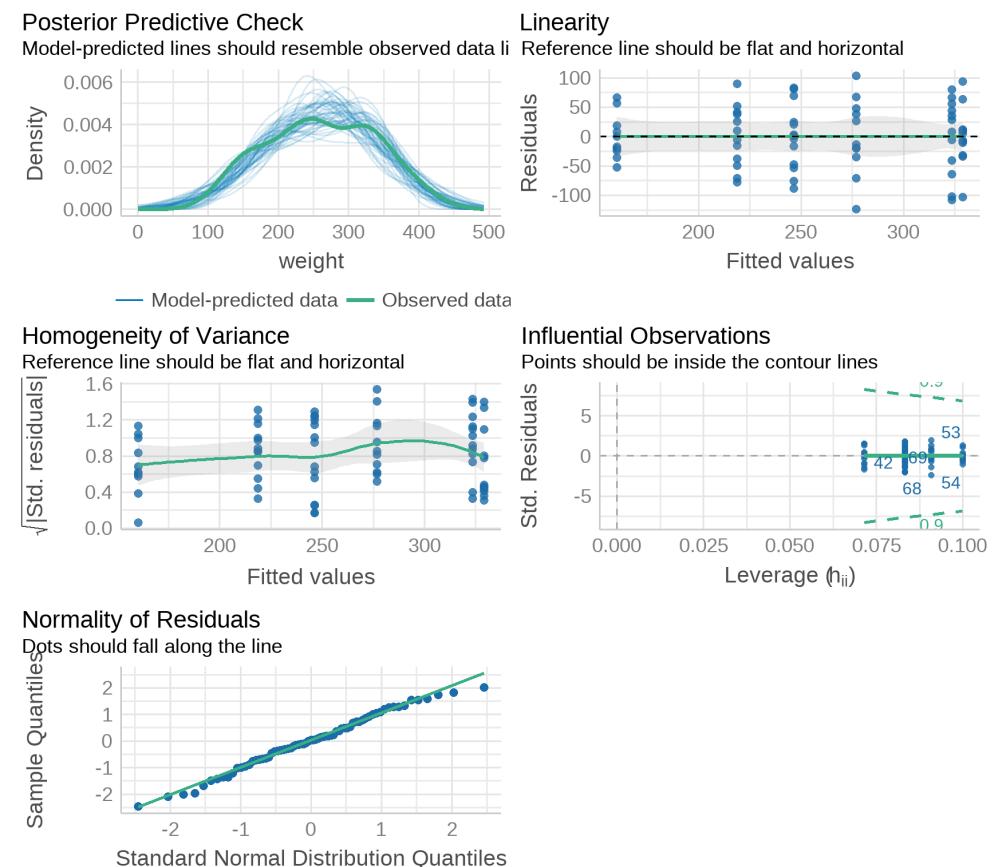


# Test model assumptions

Check the assumptions

- Residuals are normally distributed ✓
- Variance is constant (homogeneous) ✓
- There are no strong outliers or very influential observations ✓

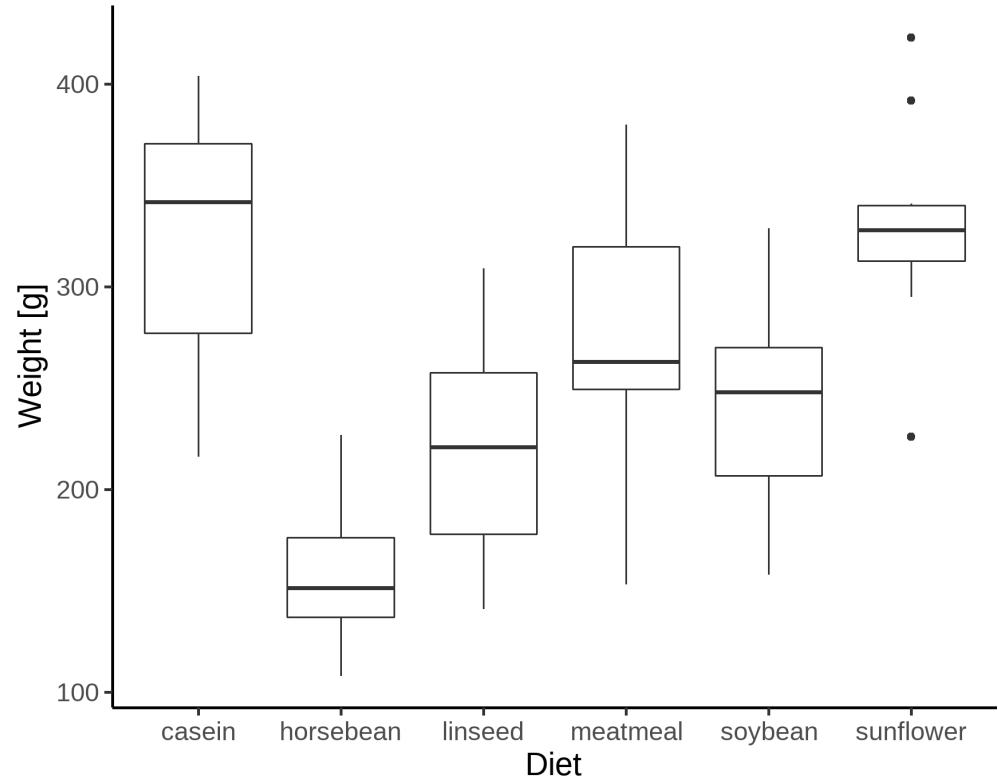
```
performance::check_model(lm_chicken)
```



# Plot results

Plot anova results e.g. in a boxplot:

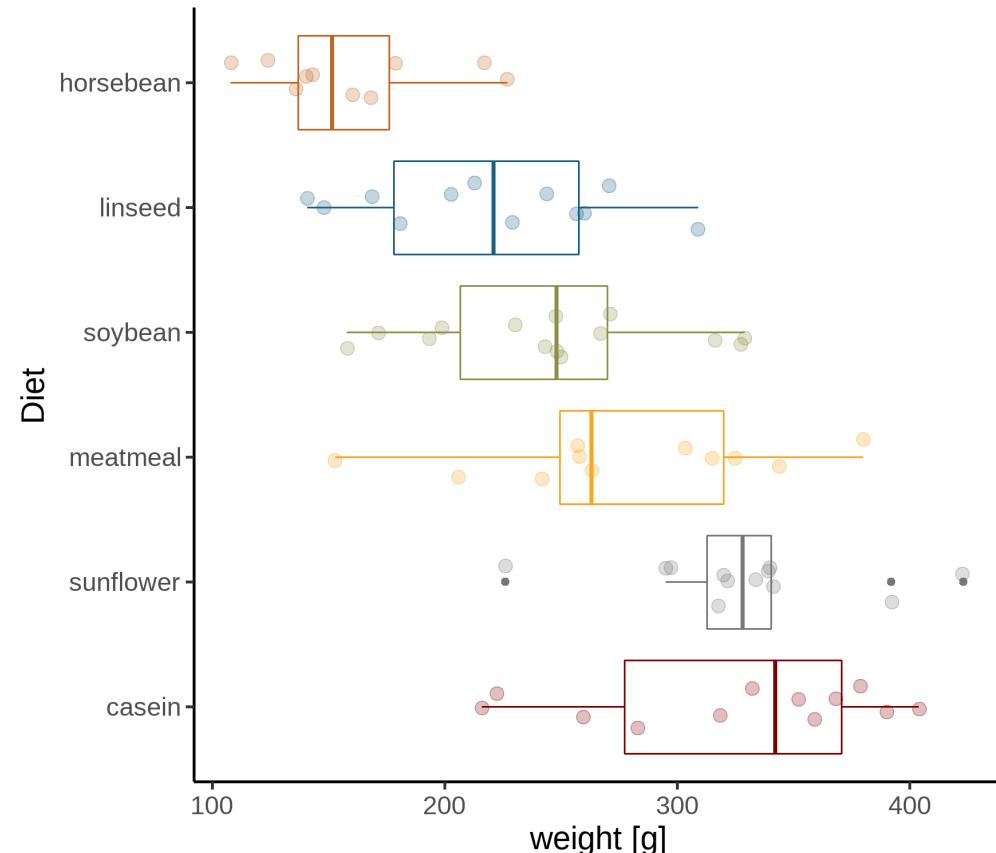
```
ggplot(chickwts, aes(feed, weight)) +  
  geom_boxplot() +  
  labs(x = "Diet", y= "Weight [g]")
```



# Plot results

If you want a slightly nicer box plot, you could do something like this:

```
chickwts %>%
  mutate(feed = as.factor(feed)) %>%
  mutate(feed = fct_reorder(feed, -weight)) %>%
  ggplot(aes(
    x = feed,
    y = weight,
    color = feed
  )) +
  geom_boxplot() +
  geom_point(
    size = 3, alpha = 0.25,
    position = position_jitter(width = 0.2,
    seed = 0)
  ) +
  coord_flip() +
  ggsci::scale_color_uchicago() +
  labs(y = "weight [g]", x = "Diet") +
  theme(legend.position = "none")
```



# Linear models step by step

Step 1: Explore the data with plots

Step 2: Write down a **question/hypothesis** and think of the **model** to test it

Step 3: Fit the linear model using the `lm` function:

```
lm(formula = Y ~ x1 + x2 + x1:x2, data = dat)
```

- Use `+` for additive effects and `:` for interactions between predictors

Step 4: Check model **assumptions** by looking at the diagnostic plots

```
performance::check_model(mod)
```

- Normally distributed residuals
- Constant variance
- No strong outliers / influential data points

# Linear models step by step

Step 5: Check significant variables by conducting F-tests with `drop1`

```
drop1(mod, test = "F")
```

- If the removal of a variable significantly increases the RSS of the model, the predictor is significant

Step 6: Check effect size e.g. in the `summary` table

```
summary(mod)
```

- Extract coefficients from the model with `mod$coefficients`

Step 7: Plot model

- Regression: regression line and scatterplot
- Analysis of covariance: regression lines and scatter plot
- Analysis of variance: boxplots, barplot, mean + sem or similar

# Options for model plotting

## Option 1: `geom_smooth(method = "lm")`

- Plots a regression line with all interactions between variables
  - only use it if this is what you want to plot

## Option 2: extract coefficients and use `geom_abline()`

- Extract slopes and intercepts from the model
  - `mod$coefficients`
- Add a `geom_abline` layer to your plot
  - `geom_abline(slope = your_slope, intercept = your_intercept)`

# Options for model plotting

## Option 3: Use `predict` function

- This is the most flexible plotting option
- Step 1: Create a new tibble with data to predict from
  - Column names have to be same as predictors of linear model
  - Use e.g. `tidyverse::expand_grid()` to create variable combinations
- Step 2: Predict the response for all value combinations from step 1

```
predict(mod, newdata = pred_data)
```

- Step 3: Add predicted response to tibble from step 1
- Step 4: Add a `geom_line` layer with the new data to your plot

```
ggplot(orig_dat, aes(x = some_x, y = some_y, color = some_col)) +  
  geom_point() +  
  geom_line(data = pred_data)
```

Now you

Task 2: Linear models with the penugin data set

Find the task description [here](#)