Statistical tests

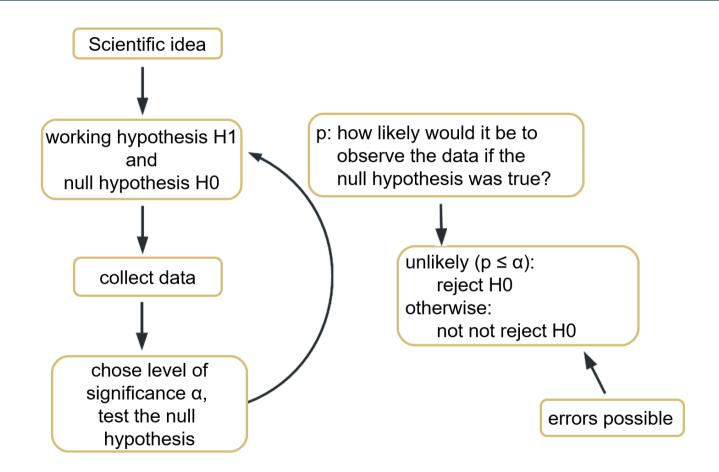
Introduction to R - Day 3

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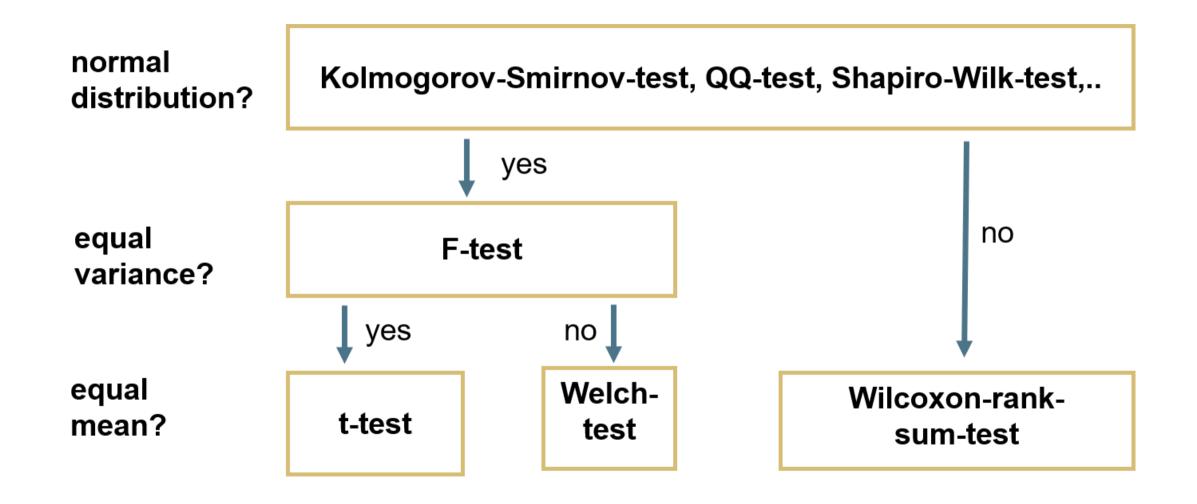
2021-08-01 (updated: 2023-02-25)

Classical approach in statistics



Please note the discussion going on about p-values as a basis for binary decisions. See e.g. here or here as a starting point

Overview of tests



Tests for normal distribution

Test for normal distribution

There are various tests and the outcome might differ!

Shapiro-Wilk-Test

- How much does variance of observed data differ from normal distribution.
- Specific test only for normal distribution
- High power, also for few data points

Visual tests: QQ-Plot

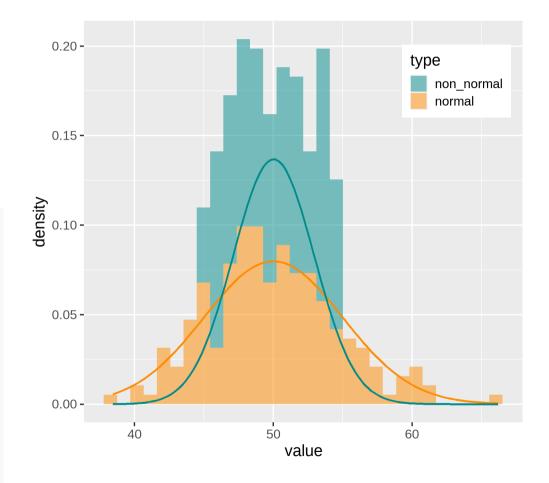
- Quantiles of observed data plotted against quantiles of normal distribution
- Scientist has to decide if normal or not

The data

Create a tibble with two variables

- normal: 200 normally distributed values with mean 50 and standard deviation 5
- non_normal: 200 uniformly distributed values between 45 and 55

```
set.seed(123)
mydata <- tibble(
  normal = rnorm(
    n = 200,
    mean = 50,
    sd = 5
),
  non_normal = runif(
    n = 200,
    min = 45,
    max = 55
)
)</pre>
```



Shapiro-Wilk-Test

 H_0 : Data does not differ from a normal distribution

```
shapiro.test(mydata$normal)
##
## Shapiro-Wilk normality test
##
## data: mydata$normal
## W = 0.99076, p-value = 0.2298
```

- W: test statistic
- ullet p-value: probability to observe the data if H_0 was true

The data does not deviate significantly from a normal distribution (Shapiro-Wilk-Test, W = 0.991, p = 0.23).

```
shapiro.test(mydata$non_normal)
##
## Shapiro-Wilk normality test
##
## data: mydata$non_normal
## W = 0.95114, p-value = 2.435e-06
```

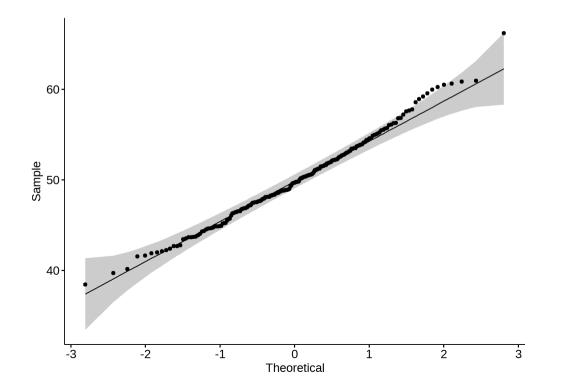
The data deviates significantly from a normal distribution (Shapiro-Wilk-Test, W = 0.95, p < 0.001).

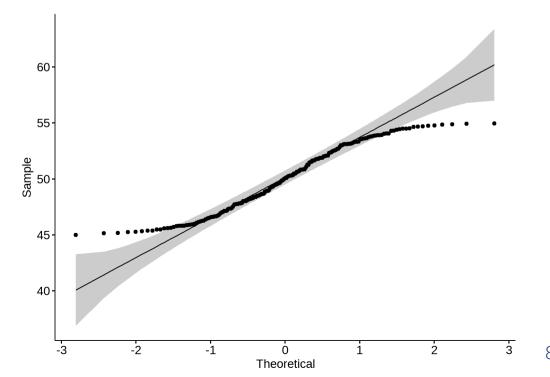
Visual test with QQ-Plot

Points should match the straight line. Small deviations are okay.

```
# ggplot(mydata, aes(sample = normal)) +
# stat_qq() + stat_qq_line()
ggpubr::ggqqplot(mydata$normal)
```

```
# ggplot(mydata, aes(sample = non_normal)) +
# stat_qq() + stat_qq_line()
ggpubr::ggqqplot(mydata$non_normal)
```





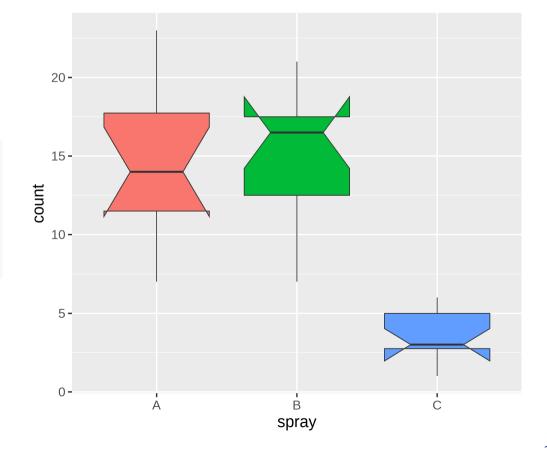
Tests for equal variance

The data

Counts of insects in agricultural units treated with different insecticides.

Compare treatments A, B and C:

 Create subsets before: count variable for each treatment as a vector



Test for equal variance

First, test for normal distribution!

F-Test

- Normal distribution of groups
- Calculates ratio of variances (if equal, ratio = 1)
- p: How likely is ratio if variances were equal?

Levene test

- Non-normal distribution of groups
- Compare difference between data sets with difference within data sets

Test for equal variances

If we want to compare variances between treatments A, B and C, we first test for normal distribution

```
shapiro.test(TreatA)
     Shapiro-Wilk normality test
## data: TreatA
\#\#\ W = 0.95757, p-value = 0.7487
shapiro.test(TreatB)
##
      Shapiro-Wilk normality test
## data: TreatB
## W = 0.95031, p-value = 0.6415
shapiro.test(TreatC)
       Shapiro-Wilk normality test
## data: TreatC
\#\#\ W = 0.92128, p-value = 0.2967
```

Result: All 3 treatments are normally distributed.

F-Test

H_0 : Variances do not differ between groups

```
var.test(TreatA, TreatB)
##
## F test to compare two variances
##
## data: TreatA and TreatB
## F = 1.2209, num df = 11, denom df = 11, p-value = 0.7464
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 0.3514784 4.2411442
## sample estimates:
## ratio of variances
## 1.22093
```

- F: test statistics, ratio of variances (if F = 1, variances are equal)
- df: degrees of freedom of both groups
- ullet p-value: how likely is it to observe the data if H_0 was true?

Result: The variances of sprays A and B do not differ significantly (F-Test, $F_{11,11}$ = 1.22, p = 0.75)

F-Test

H_0 : Variances do not differ between groups

```
var.test(TreatA, TreatC)
##
## F test to compare two variances
##
## data: TreatA and TreatC
## F = 7.4242, num df = 11, denom df = 11, p-value = 0.002435
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 2.137273 25.789584
## sample estimates:
## ratio of variances
## 7.424242
```

Result: The variances of sprays A and C differ significantly (F-Test, $F_{11,11}$ = 7.42, p = 0.002)

Test for equal means

Test for equal means

t-test

- Normal distribution AND equal variance
- Compares if mean values are within range of standard error of each other
- p: how likely is the difference if the means were equal

Welch-Test

- Normal distribution but unequal variance
- Corrected t-test

Wilcoxon rank sum test

- Non-normal distribution and unequal variance
- Compares rank sums of the data
- Non-parametric



t-test

 H_0 : The samples do not differ in their mean

Treatment A and B: normally distributed and equal variance

```
t.test(TreatA, TreatB, var.equal = TRUE)
##

## Two Sample t-test
##

## data: TreatA and TreatB
## t = -0.45352, df = 22, p-value = 0.6546
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -4.643994 2.977327
## sample estimates:
## mean of x mean of y
## 14.50000 15.333333
```

- t: test statistics (t = 0 means equal means)
- df: degrees of freedom of t-statistics
- ullet p-value: how likely is it to observe the data if H_0 was true?

Result: The means of spray A and B do not differ significantly (t = -0.45, df = 22, p = 0.66)

Welch-Test

 H_0 : The samples do not differ in their mean

Treatment A and C: normally distributed and non-equal variance

```
t.test(TreatA, TreatC, var.equal = FALSE)
##
## Welch Two Sample t-test
##
## data: TreatA and TreatC
## t = 7.5798, df = 13.91, p-value = 2.655e-06
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 7.885546 14.114454
## sample estimates:
## mean of x mean of y
## 14.5 3.5
```

Result: The means of spray A and C do differ significantly (t = 7.58, df = 13.9, p < 0.001)

Wilcoxon-rank-sum Test

 H_0 : The samples do not differ in their mean

We don't need the Wilcoxon test to compare treatment A and B, but for the sake of an example:

```
wilcox.test(TreatA, TreatB)
##
## Wilcoxon rank sum test with continuity correction
##
## data: TreatA and TreatB
## W = 62, p-value = 0.5812
## alternative hypothesis: true location shift is not equal to 0
```

Result: The means of spray A and B do not differ significantly (W = 62, p = 0.58)

Paired values

Are there pairs of data points?

Example: samples of invertebrates across various rivers before and after sewage plants.

- For each plant, there is a pair of data points (before and after the plant)
- Question: Is the change (before-after) significant

Use paired = TRUE in the test.

```
t.test(TreatA, TreatB, var.equal = TRUE, paired = TRUE)
t.test(TreatA, TreatB, var.equal = FALSE, paired = TRUE)
wilcox.test(TreatA, TreatB, paired = TRUE)
```

Careful: your treatment vector both have to have the same order

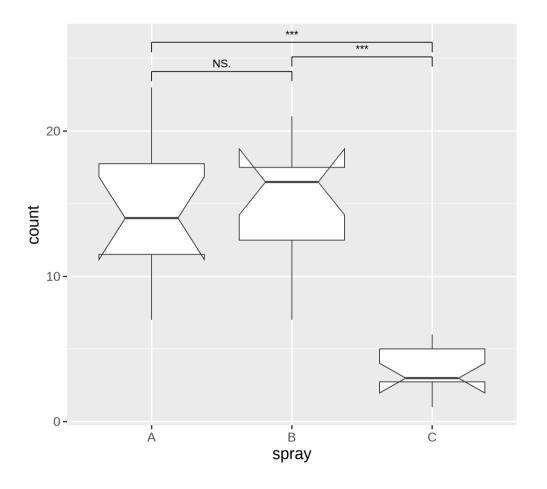
Plot test results with ggsignif

The <code>ggsignif</code> package offers a <code>geom_signif()</code> layer that can be added to a ggplot to annotate significance levels

```
# install.packages("ggsignif")
library(ggsignif)
```

Plot test results with geom_signif()

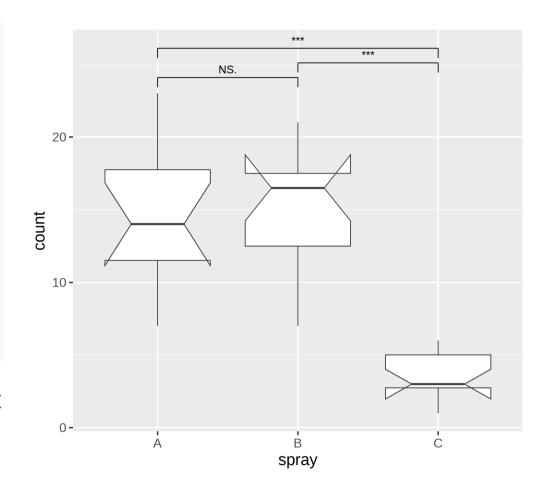
• By default, a Wilcoxon test is performed



Plot test results with geom_signif()

```
ggplot(InsectSprays,
       aes(x = spray, y = count)) +
  geom\ boxplot(notch = TRUE) +
 geom signif(
    comparisons = list(
      c("A", "B"),
     c("B", "C"),
      c("A", "C")
    test = "t.test",
   test.args = list(
     var.equal = TRUE
    map signif level = TRUE,
    y position = c(23, 24, 25)
```

- Specify a specific test with the test argument
- Additional arguments can be passed as a list with the test.args argument
- Look at ?geom signif for more options

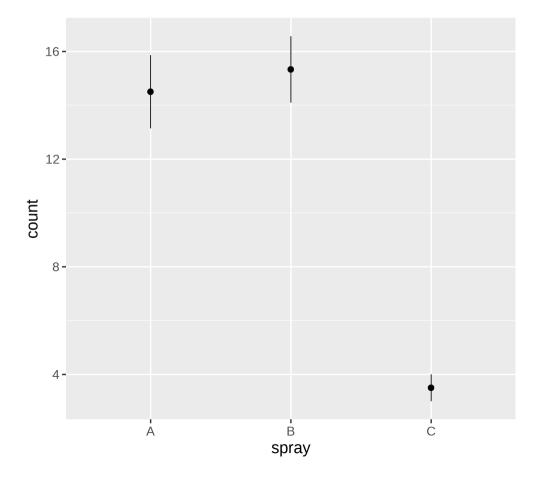


Plot mean +- se using stat_summary

Another way to plot the results is to plot mean and standard error of the mean:

```
ggplot(
   InsectSprays,
   aes(x = spray, y = count)
) +
   stat_summary()
```

• By default stat_summary adds mean and standard error of the mean as pointrange

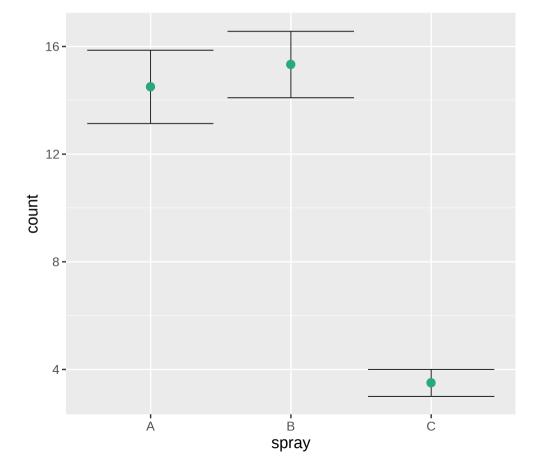


Plot mean +- se using stat summary

Another way to plot the results is to plot mean and standard error of the mean:

```
ggplot(InsectSprays, aes(x = spray, y = count))
+
    stat_summary(
        fun.data = mean_se,
        geom = "errorbar"
) +
    stat_summary(
        fun.y = mean,
        geom = "point",
        color = "#28a87d",
        size = 4
)
```

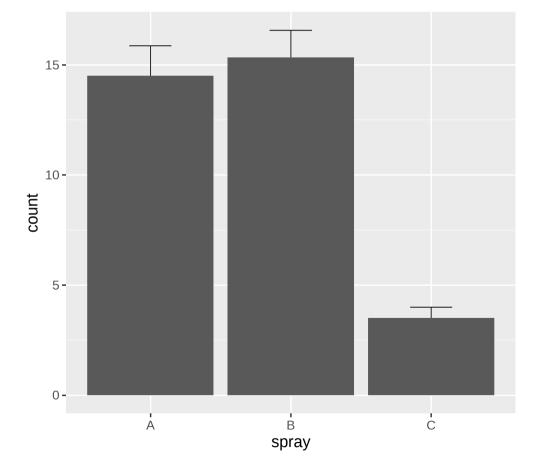
- Inside stat_summary, you can define function used to calculate the summary
 - o fun.data for errorbars
 - fun.y for point values (e.g. mean)
- Define the geom that represents the summary



Plot mean +- se using stat_summary

Another way to plot the results is to plot mean and standard error of the mean:

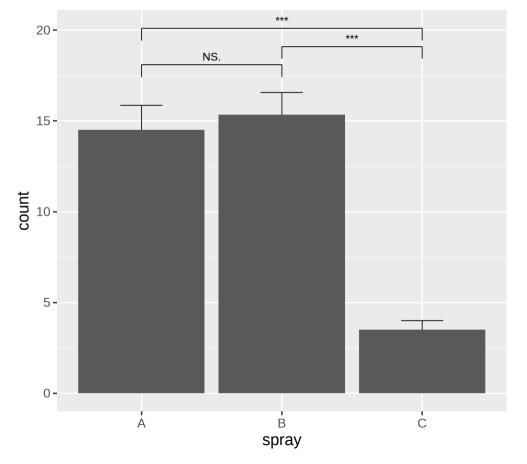
```
ggplot(InsectSprays, aes(x = spray, y = count))
+
    stat_summary(
        fun.data = mean_se,
        geom = "errorbar",
        width = 0.3
) +
    stat_summary(
        fun.y = mean,
        geom = "bar",
        size = 4
)
```



Plot mean +- se using stat summary

Just like before, you can also add a geom signif to a barplot:

```
qqplot(InsectSprays, aes(x = spray, y = count))
  stat summary(
    fun.data = mean se,
    geom = "errorbar",
    width = 0.3
  stat summary(
    fun.y = mean
    geom = "bar"
  ggsignif::geom signif(
    comparisons = list(
      c("A", "B"),
      c("B", "C"),
      c("A", "C")
    test = "t.test",
   map signif level = TRUE,
    y position = c(17, 18, 19)
```



Now you

Task 1: Statistical tests (45 min)

Find the task description here