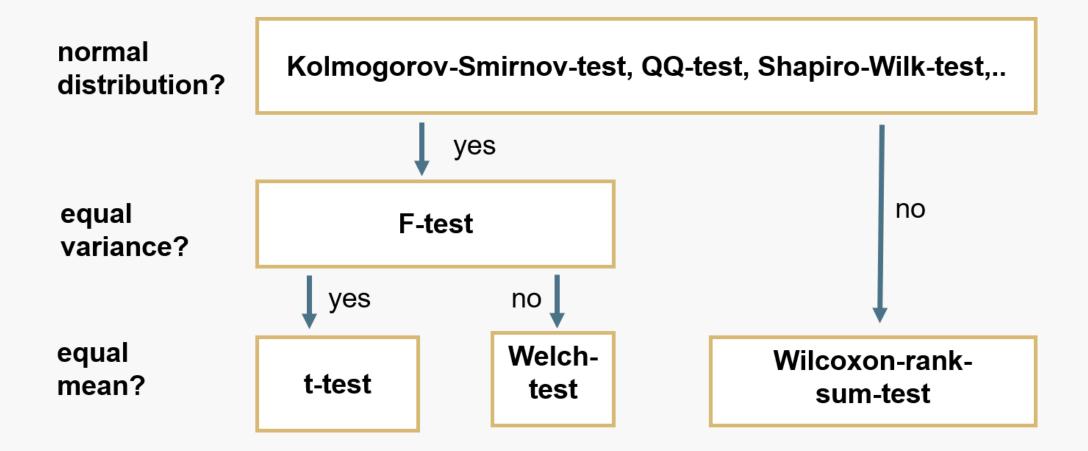
# Statistical tests

### Day 3 - Introduction to Data Analysis with R

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September 20, 2024

## Overview of tests



# Tests for normal distribution

## Test for normal distribution

There are various tests and the outcome might differ!

#### Shapiro-Wilk-Test

- How much does variance of observed data differ from normal distribution
- Specific test only for normal distribution
- High power, also for few data points

#### Visual tests: QQ-Plot

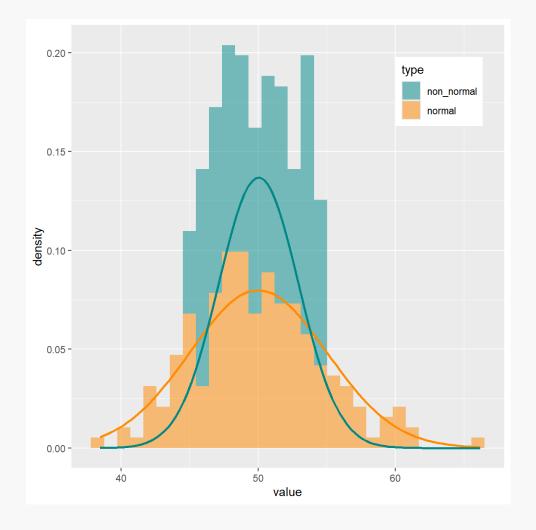
- Quantiles of observed data plotted against quantiles of normal distribution
- Scientist has to decide if normal or not

## The data

A tibble with two variables

- normal: 200 normally distributed values with mean 50 and standard deviation 5
- non\_normal: 200 uniformly distributed values between 45 and 55

#### mydata #> # A tibble: 200 × 2 #> normal non normal <dbl> <dbl> #> 54.9 47.2 #> #> 48.8 46.4 54.1 57.8 50.8 #> 50.4 50.6 49.0 58.6 49.5 52.3 52.1 #> 43.7 45.8 46.6 48.4 #> 47.8 51.8 10 #> # i 190 more rows



## Shapiro-Wilk-Test

#### $H_0$ : Data does not differ from a normal distribution

```
shapiro.test(mydata$normal)
#>
#> Shapiro-Wilk normality test
#>
#> data: mydata$normal
#> W = 0.99076, p-value = 0.2298
```

- W: test statistic
- ullet p-value: probability to observe the data if  $H_0$  was true

The data does not deviate significantly from a normal distribution (Shapiro-Wilk-Test, W = 0.991, p = 0.23).

```
shapiro.test(mydata$non_normal)
#>
#> Shapiro-Wilk normality test
#>
#> data: mydata$non_normal
#> W = 0.95114, p-value = 2.435e-06
```

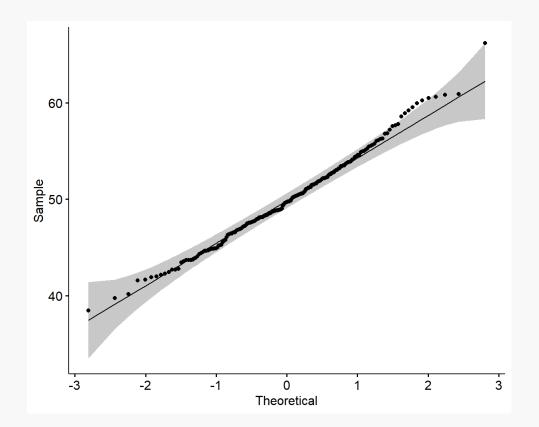
The data deviates significantly from a normal distribution (Shapiro-Wilk-Test, W = 0.95, p < 0.001).

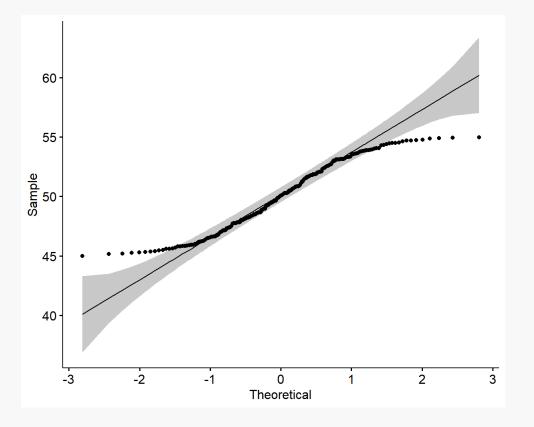
## Visual test with QQ-Plot

Points should match the straight line. Small deviations are okay.

```
# ggplot(
# mydata,
# aes(sample = normal)
# ) +
# stat_qq() +
# stat_qq_line()
ggpubr::ggqqplot(mydata$normal)
```

```
# ggplot(
# mydata,
# aes(sample = non_normal)
# ) +
# stat_qq() +
# stat_qq_line()
ggpubr::ggqqplot(mydata$non_normal)
```





# Tests for equal variance

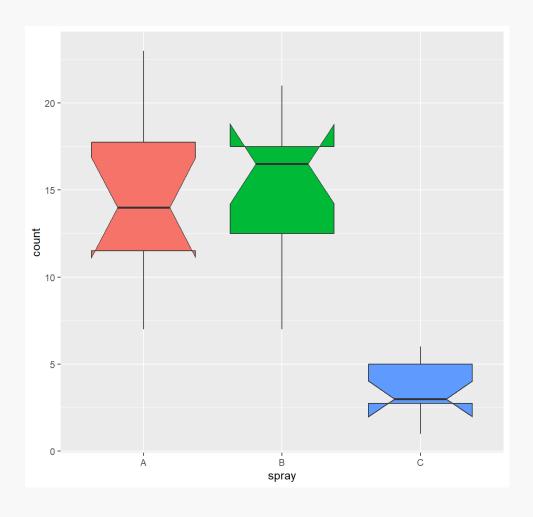
## The data

Counts of insects in agricultural units treated with different insecticides.

Compare treatments A, B and C:

Create subsets before: count variable for each treatment as a vector

```
TreatA <- filter(
   InsectSprays,
   spray == "A") $count
TreatB <- filter(
   InsectSprays,
   spray == "B") $count
TreatC <- filter(
   InsectSprays,
   spray == "C") $count</pre>
```



## Test for equal variance

First, test for normal distribution!

#### F-Test

- Normal distribution of groups
- Calculates ratio of variances (if equal, ratio = 1)
- p: How likely is ratio if variances were equal?

#### Levene test

- Non-normal distribution of groups
- Compare difference between data sets with difference within data sets

## Test for equal variance

First, test for normal distribution

```
shapiro.test(TreatA)
#>
#>
   Shapiro-Wilk normality test
#>
#> data: TreatA
\#> W = 0.95757, p-value = 0.7487
shapiro.test(TreatB)
#>
#>
   Shapiro-Wilk normality test
#>
#> data: TreatB
\#> W = 0.95031, p-value = 0.6415
shapiro.test(TreatC)
#>
#>
   Shapiro-Wilk normality test
#>
#> data: TreatC
\#> W = 0.92128, p-value = 0.2967
```

Result: All 3 treatments are normally distributed.

#### F-Test

#### $H_0$ : Variances do not differ between groups

```
var.test(TreatA, TreatB)
#>
#> F test to compare two variances
#>
#> data: TreatA and TreatB
#> F = 1.2209, num df = 11, denom df = 11, p-value = 0.7464
#> alternative hypothesis: true ratio of variances is not equal to 1
#> 95 percent confidence interval:
#> 0.3514784 4.2411442
#> sample estimates:
#> ratio of variances
#> 1.22093
```

- F: test statistics, ratio of variances (if F = 1, variances are equal)
- df: degrees of freedom of both groups
- ullet p-value: how likely is it to observe the data if  $H_0$  was true?

Variances of sprays A & B don't differ significantly (F-Test,  $F_{11,11}=1.22$ , p = 0.75)

#### F-Test

#### $H_0$ : Variances do not differ between groups

```
var.test(TreatA, TreatC)
#>
#> F test to compare two variances
#>
#> data: TreatA and TreatC
#> F = 7.4242, num df = 11, denom df = 11, p-value = 0.002435
#> alternative hypothesis: true ratio of variances is not equal to 1
#> 95 percent confidence interval:
#> 2.137273 25.789584
#> sample estimates:
#> ratio of variances
#> 7.424242
```

Variances of sprays A & C differ significantly (F-Test,  $F_{11,11} = 7.42$ , p = 0.002)

# Test for equal means

## Test for equal means

#### t-test

- Normal distribution AND equal variance
- Compares if mean values are within range of standard error of each other
- p: how likely is the difference if the means were equal

#### Welch-Test

- Normal distribution but unequal variance
- Corrected t-test

#### Wilcoxon rank sum test

- Non-normal distribution and unequal variance
- Compares rank sums of the data
- Non-parametric

#### t-test

 $H_0$ : The samples do not differ in their mean

Treatment A and B: normally distributed and equal variance

```
t.test(TreatA, TreatB, var.equal = TRUE)
#>
#> Two Sample t-test
#>
#> data: TreatA and TreatB
#> t = -0.45352, df = 22, p-value = 0.6546
#> alternative hypothesis: true difference in means is not equal to 0
#> 95 percent confidence interval:
#> -4.643994 2.977327
#> sample estimates:
#> mean of x mean of y
#> 14.50000 15.333333
```

- t: test statistics (t = 0 means equal means)
- df: degrees of freedom of t-statistics
- ullet p-value: how likely is it to observe the data if  $H_0$  was true?

#### t-test

 $H_0$ : The samples do not differ in their mean

Treatment A and B: normally distributed and equal variance

```
t.test(TreatA, TreatB, var.equal = TRUE)
#>
#> Two Sample t-test
#>
#> data: TreatA and TreatB
#> t = -0.45352, df = 22, p-value = 0.6546
#> alternative hypothesis: true difference in means is not equal to 0
#> 95 percent confidence interval:
#> -4.643994 2.977327
#> sample estimates:
#> mean of x mean of y
#> 14.50000 15.333333
```

**Result:** The means of spray A and B don't differ significantly (t = -0.45, df = 22, p = 0.66)

### Welch-Test

 $H_0$ : The samples do not differ in their mean

Treatment A and C: normally distributed and non-equal variance

```
t.test(TreatA, TreatC, var.equal = FALSE)
#>
#> Welch Two Sample t-test
#>
#> data: TreatA and TreatC
#> t = 7.5798, df = 13.91, p-value = 2.655e-06
#> alternative hypothesis: true difference in means is not equal to 0
#> 95 percent confidence interval:
#> 7.885546 14.114454
#> sample estimates:
#> mean of x mean of y
#> 14.5 3.5
```

**Result**: The means of spray A and C do differ significantly (t = 7.58, df = 13.9, p < 0.001)

## Wilcoxon-rank-sum Test

 $H_0$ : The samples do not differ in their mean

We don't need the Wilcoxon test to compare treatment A and B, but for the sake of an example:

```
wilcox.test(TreatA, TreatB)
#>
#> Wilcoxon rank sum test with continuity correction
#>
#> data: TreatA and TreatB
#> W = 62, p-value = 0.5812
#> alternative hypothesis: true location shift is not equal to 0
```

**Result**: The means of spray A and B do not differ significantly (W = 62, p = 0.58)

### Paired values

Are there pairs of data points?

**Example:** samples of invertebrates across various rivers before and after sewage plants.

- For each plant, there is a pair of data points (before and after the plant)
- Question: Is the change (before-after) significant

Use paired = TRUE in the test.

```
t.test(TreatA, TreatB, var.equal = TRUE, paired = TRUE)
t.test(TreatA, TreatB, var.equal = FALSE, paired = TRUE)
wilcox.test(TreatA, TreatB, paired = TRUE)
```

Careful: your treatment vector both have to have the same order

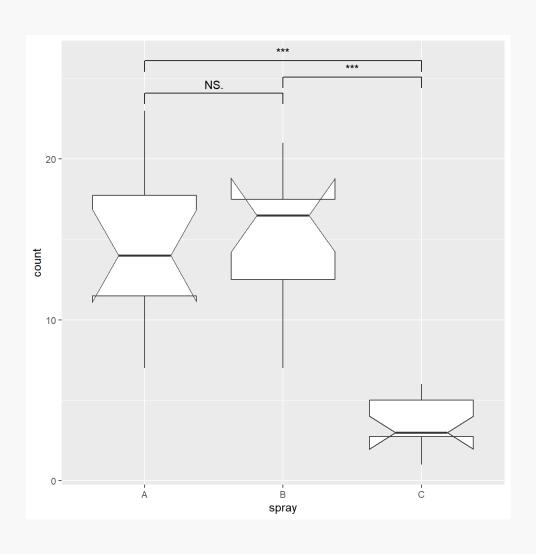
## Plot test results with ggsignif

The **ggsignif** package offers a **geom\_signif()** layer that can be added to a ggplot to annotate significance levels

```
# install.packages("ggsignif")
library(ggsignif)
```

# Plot test results with geom\_signif()

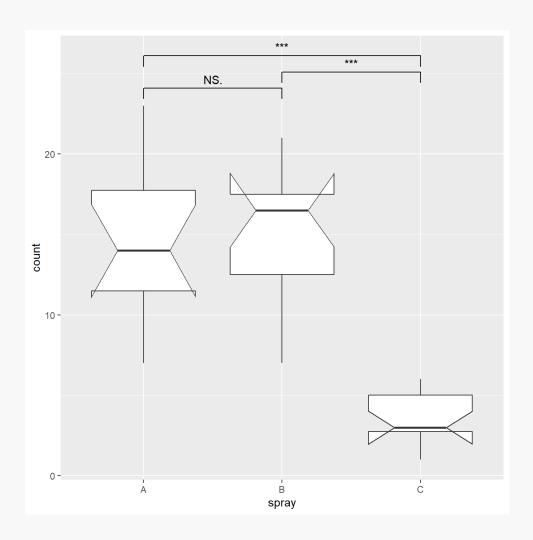
```
gaplot (
     InsectSprays,
     aes (x = spray, y = count)
     geom boxplot(notch = TRUE) +
     geom signif(
       comparisons = list(
         c("A", "B"),
         c("B", "C"),
         c("A", "C")
10
11
12
       map signif level = TRUE,
       y position = c(23, 24, 25)
13
14
```



By default, a Wilcoxon test is performed

## Plot test results with geom\_signif()

```
1 ggplot(
     InsectSprays,
    aes (x = spray, y = count)
 4
     geom boxplot(notch = TRUE) +
    geom signif(
       comparisons = list(
         c("A", "B"),
         c("B", "C"),
         c("A", "C")
10
11
12
   test = "t.test",
13
      test.args = list(
14
       var.equal = TRUE
15
16
       map signif level = TRUE,
17
       y position = c(23, 24, 25)
18
```

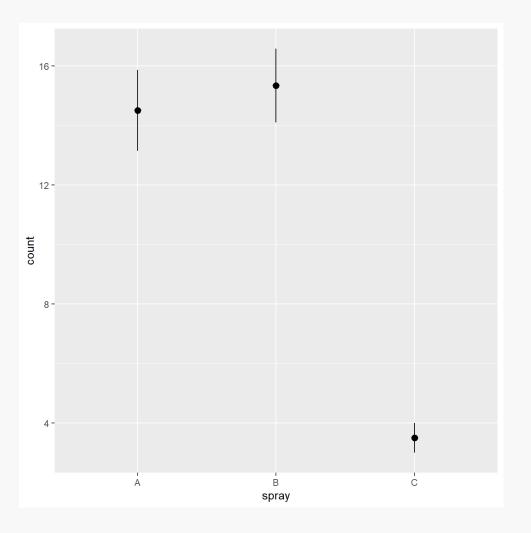


- test: run specific test
- test.args: pass additional arguments in a list
- ?geom\_signif for more options

Another way to plot the results is to plot mean and standard error of the mean:

```
1 ggplot(
2   InsectSprays,
3   aes(x = spray, y = count)
4 ) +
5   stat_summary()
```

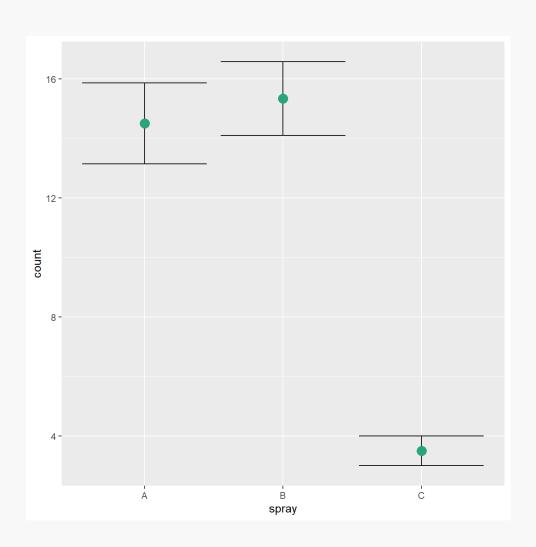
 By default stat\_summary adds mean and standard error of the mean as pointrange



Another way to plot the results is to plot mean and standard error of the mean:

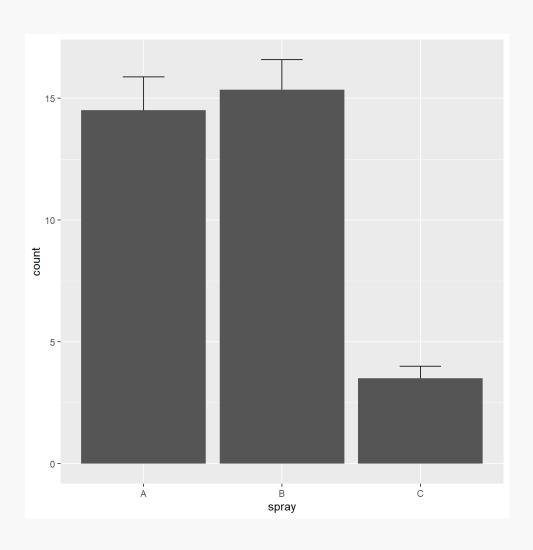
```
ggplot (
     InsectSprays,
    aes(x = spray, y = count)
     stat summary (
       fun.data = mean se,
       geom = "errorbar"
     stat summary (
10
    fun.y = mean,
    geom = "point",
11
12
   color = "#28a87d",
13
    size = 4
14
```

- Inside stat\_summary, define summary function
  - fun.data for errorbars, fun.y for points (e.g. mean)



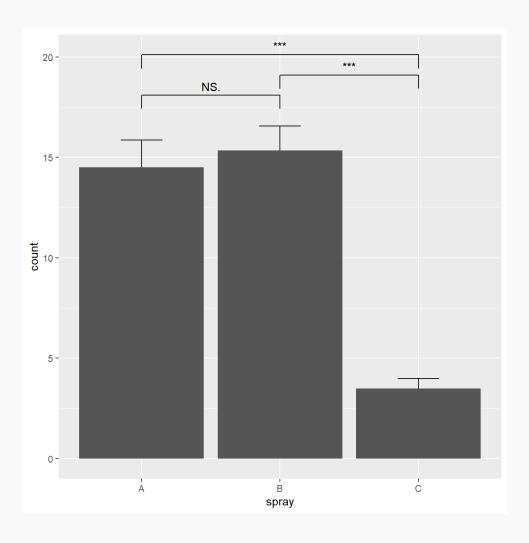
Another way to plot the results is to plot mean and standard error of the mean:

```
gaplot (
    InsectSprays,
   aes (x = spray, y = count)
    stat summary(
    fun.data = mean se,
   geom = "errorbar",
    width = 0.3
10
    stat summary (
11
  fun.y = mean,
  geom = "bar",
12
13 size = 4
14
```



Just like before, you can also add a **geom\_signif** to a barplot:

```
1 ggplot(
     InsectSprays,
    aes(x = spray, y = count)
    stat summary(
    fun.data = mean se,
    geom = "errorbar",
    width = 0.3
    ) +
10
    stat summary(
11
   fun.y = mean,
12
    geom = "bar"
13
14
     ggsignif::geom signif(
15
       comparisons = list(
16
       c("A", "B"),
        c("B", "C"),
17
      c("A", "C")
18
19
       ),
```



# Now you

Task 1 (45) min)

Statistical tests

Find the task description here