



Forward Pass

$$Yp = W * X + b$$

$$Loss = 1/n \sum 1/2(Yp - Y)^2$$

Backward Pass

$$L = \frac{1}{2}(Yp - Y)^2 = \frac{1}{2}((Yp)^2 - 2YpY + Y^2) = (Yp)^2/2 - YpY + Y^2/2$$

$$\frac{\partial L}{\partial Yp} = Yp - Y$$

$$\frac{\partial L}{\partial W} = \frac{\partial L}{\partial Yp} * \frac{\partial Yp}{\partial W} \qquad \text{and} \qquad \frac{\partial Yp}{\partial W} = X$$

$$\text{so} \quad \frac{\partial L}{\partial W} = \frac{1}{n} \sum (Yp - Y) * X$$