1 Virtual Machine Abstract Syntax

Notation: overbar means a list of elements, as in Java

2 Standard prelude

```
type Int
def +(i:Int):Int
def -(i:Int):Int
def *(i:Int):Int
def /(i:Int):Int
```

3 Virtual Machine Typing Rules

$$\frac{\Gamma \vdash e : \tau}{\Gamma \vdash e : \tau} \qquad \frac{\Gamma \vdash d : \sigma \quad \Gamma, \sigma \vdash S : \tau}{\Gamma \vdash d : STMT} \qquad \frac{x : \tau \in \Gamma}{\Gamma \vdash x : \tau} \qquad (\text{T-VAR})$$

$$\frac{\Gamma \mid x : \tau \vdash \overline{d} : unfold_{\Gamma}(\tau)}{\Gamma \vdash \text{new } x : \tau \ \{\overline{d}\} : \tau} \qquad (\text{T-NEW})$$

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \text{def } m(x : \tau_2) : \tau \in unfold_{\Gamma}(\tau_1) \quad \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash e_1.m(e_2) : \tau} \qquad (\text{T-Invk})$$

$$\frac{\Gamma \vdash e : \tau' \quad \text{val } f : \tau \in unfold_{\Gamma}(\tau')}{\Gamma \vdash e.f : \tau} \qquad (\text{T-Field})$$

$$\frac{\Gamma \vdash e : \tau' \quad \text{val } f : \tau \in unfold_{\Gamma}(\tau')}{\Gamma \vdash e.f : \tau} \qquad (\text{T-Field})$$

Technically Γ is a list of σ , but we often write $x : \tau$ for val $x : \tau$.

$$\Gamma \mid x : \tau \vdash d : \sigma$$

$$\frac{\Gamma, x : \tau \vdash \overline{\tau} \ \textit{wf} \quad \Gamma, \ \overline{y : \tau} \vdash e : \tau_2}{\Gamma \mid x : \tau \vdash \mathsf{def} \ m(\overline{y : \tau}) : \tau_2 = e \ : \ \mathsf{def} \ m(\overline{y : \tau}) : \tau_2} \ (\text{T-Def})$$

$$\frac{\Gamma \vdash e : \tau}{\Gamma \mid x : \tau \vdash \mathtt{val} \ f = e \ : \ \mathtt{val} \ f : \tau} \ (\text{T-VAL})$$

$$\frac{\Gamma, x : \tau \vdash \mathsf{type}\ L = \tau\ \mathit{wf}}{\Gamma \mid x : \tau \vdash \mathsf{type}\ L = \tau : \mathsf{type}\ L = \tau}\ (\mathsf{T-Type})$$

$$unfold_{\Gamma}(\tau) = \overline{\sigma}$$

$$\overline{\mathit{unfold}_{\Gamma}(\mathtt{Unit})} = ullet$$

$$\frac{\mathsf{type}\ L = \tau \in \Gamma \quad \mathit{unfold}_{\Gamma}(\tau) = \overline{\sigma}}{\mathit{unfold}_{\Gamma}(L) = \overline{\sigma}}$$

$$\frac{unfold_{\Gamma}(\beta) = \overline{\sigma}}{unfold_{\Gamma}(\beta\{\overline{\sigma'}\}) = \overline{\sigma} \leftarrow \overline{\sigma'}}$$

Note: $\overline{\sigma} \leftarrow \overline{\sigma'}$ means that we append the two lists, except that when the same symbol is defined in both $\overline{\sigma}$ and $\overline{\sigma'}$, we include only the (overriding) definition in $\overline{\sigma'}$.

Now, finally, type and declaration type well-formedness rules: $\Gamma \vdash \tau \ wf$

$$\overline{\Gamma \vdash \mathtt{Unit} \ wf}$$

$$\frac{\mathit{unfold}_{\Gamma}(L) = \overline{\sigma}}{\Gamma \vdash L \ \mathit{wf}}$$

$$\frac{\Gamma \vdash \beta \ wf \quad \Gamma \vdash \overline{\sigma'} \ wf}{\Gamma \vdash \beta \{\overline{\sigma'}\} \ wf}$$

$$\Gamma \vdash \sigma \ \textit{wf}$$

$$\frac{\Gamma \vdash \overline{y} : \overline{\tau} \ \textit{wf} \quad \Gamma \vdash \tau_2 \ \textit{wf}}{\Gamma \vdash \mathsf{def} \ m(\overline{y} : \overline{\tau}) : \tau_2 \ \textit{wf}}$$

$$\frac{\Gamma \vdash \tau \ wf}{\Gamma \vdash \mathtt{val} \ f : \tau \ wf}$$

$$\frac{\Gamma, \mathtt{type}\ L = \tau \vdash \tau\ \mathit{wf}}{\Gamma \vdash \mathtt{type}\ L = \tau\ \mathit{wf}}$$