Capabilities: Effects for Free

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Abstract. Object capabilities are increasingly used to reason informally about the properties of secure systems. Can capabilities also aid in *formal* reasoning? To answer this question, we examine a calculus that uses effects to capture resource use and extend it with a rule that captures the essence of capability-based reasoning. We demonstrate that capabilities provide a way to reason for free about effects: we can bound the effects of an expression based on the capabilities to which it has access. This reasoning is "free" in that it relies only on type-checking (not effect-checking); does not require the programmer to add effect annotations within the expression; nor does it require the expression to be analysed for its effects. Our result sheds light on the essence of what capabilities provide and suggests ways of integrating lightweight capability-based reasoning into languages.

1 Introduction

Capabilities have been recently gaining new attention as a promising mechanism for controlling access to resources, particularly in object-oriented languages and systems [15, 6, 5, 4]. A *capability* is an unforgeable token that can be used by its bearer to perform some operation on a resource [3]. In a *capability-safe* language, all resources must be accessed through object capabilities, and a resource-access capability must be obtained from an object that already has it: "only connectivity begets connectivity" [15]. For example, a logger component that provides a logging service would need to be initialised with an object capability providing the ability to append to the log file.

Capability-safe languages thus prohibit the *ambient authority* [16] that is present in non-capability-safe languages. An implementation of a logger in Java, for example, does not need to be initialised with a log file capability; it can simply import the appropriate file-access library and open the log file for appending by itself. But critically, a malicious implementation could also delete the log, read from another file, or exfiltrate logging information over the network. Other mechanisms such as sandboxing can be used to limit the effects of such malicious components, but recent work has found that Java's sandbox (for example) is difficult to use and is therefore often misused [2, 12].

In practice, reasoning about resource use in capability-based systems is mostly done informally. But if capabilities are useful for *informal* reasoning, shouldn't they also aid in *formal* reasoning? Recent work by Drossopoulou et. al. sheds some light on this question by presenting a logic that formalizes capability-based reasoning about trust

between objects [6]. Two other trains of work, rather than formalise capability-based reasoning itself, reason about how capabilities may be used. Dimoulas et al. developed a formalism for reasoning about which components may use a capability and which may influence (perhaps indirectly) the use of a capability [5]. Devriese et al. formulate an effect parametricity theorem that limits the effects of an object based on the capabilities it possesses, and then use logical relations to reason about capability use in higher-order settings [4]. Overall, this prior work presents new formal systems for reasoning about capability use, or reasoning about new properties using capabilities.

We are interested in a different question: can capabilities be used to enhance formal reasoning that is currently done without relying on capabilities? In other words, what value do capabilities add to existing formal reasoning approaches?

To answer this question, we decided to pick a simple and practical formal reasoning system, and see if capability-based reasoning could help. A natural choice for our investigation is effect systems [17]. Effect systems are a relatively simple formal reasoning approach, and keeping things simple will help to highlight the difference made by capabilities. Effects also have an intuitive link to capabilities: in a system that uses capabilities to protect resources, an expression can only have an effect on a resource if it is given a capability to do so.

One challenge to the wider adoption of effect systems is their annotation overhead [18]. Java's checked exception system, which is a kind of effect system, is often criticised for being cumbersome [8]. While effect inference can be used to reduce the annotations required [10], understanding error messages that arise through effect inference requires a detailed understanding of the internal structure of the code, not just its interface. Capabilities are a promising alternative for reducing the overhead of effect annotations, as suggested by the following example:

```
import log : String -> Unit with effect File.write
e
```

The code above, like the rest in this paper, is written in a capability-safe language supporting first-class, object-like modules, similar to Wyvern [9]. It should be read as the expression e declaring what capabilities it needs to execute. In this case, e must be passed a function of type $String \rightarrow Unit$, which incurs no more than the single File.write effect when invoked. This function is bound to the name log inside e, which is then evaluated.

If we were to evaluate e, what could we say about its effects on resources, such as the file system or network? Since we are in a capability-safe language, e has no ambient authority, so the only way it can have any effects is via the log function given to it. Since the log function is annotated as having no more than the File.write effect, this is an upper-bound on the effects of e. Note that we did not require anything of e, other than that it obeys the rules of a capability-safe language. In particular, we don't require it to have any effect annotations, and we don't need to analyse its structure, like an effect inference would have to do. Also note that e might be arbitrarily large, perhaps consisting of an entire program we have downloaded from a source we trust enough to write to a log, but not enough to access any other resources. Thus in this scenario, capabilities can be used to reason "for free" about the effects of a large body of code (e) based on a few annotations on the components it imports (log).

This example illustrates the central intuition of this paper: in a capability-safe setting, the effects of an unannotated expression can be bounded by the effects latent in the variables that are in scope. In the remainder of this paper, we formalise these ideas in a capability calculus (CC; section 2). Along the way we must generalise this intuitition to handle higher-order programs: what if log takes a higher-order argument? If e evaluates not to unit, but to a function, what can we say about its effects?

Although the current resurgence of interest in capabilities is primarily focused on object-oriented languages, for simplicity our formal definitions build on a typed lambda calculus with a simple notion of capabilities and their operations. CC permits the nesting of unannotated code inside annotated code in a controlled, capability-safe manner using the import construct from above. This allows us to reason about unannotated code by inspecting what capabilities are passed into it from its annotated surroundings. We then show how CC can model practical situations, using it to encode a range of Wyvern-like programs. A more thorough discussion of how this is done is given in an accompanying technical report. [1].

2 Capability Calculus (CC)

Allowing a mix of annotated [with effects] and unannotated code helps reduce the cognitive overhead on developers, allowing them to rapidly prototype in the unannotated sublanguage and incrementally add annotations as they are needed. However, reasoning about unannotated code is difficult in general. Figure 1 demonstrates why: someMethod takes a function f as input and executes it, but the effects of f depend on its implementation. Without more information, there is no way to know what effects might be incurred by someMethod.

```
def someMethod(f: Unit → Unit):
   f()
```

Fig. 1. What effects can someMethod incur?

Consider another scenario, where a developer must decide whether or not to use the logger functor defined in Figure 2. This functor takes two capabilities as input, File and Socket³. It instantiates an object-like module which has access to these capabilities, and which has a single, unannotated log function that the developer may invoke. The type of this object-like module is Logger, which for brevity is assumed to be defined elsewhere.

```
module def logger(f:{File},s:{Socket}):Logger

def log(x: Unit): Unit

...
```

Fig. 2. In a capability-safe setting, logger can only exercise authority over the File and Socket capabilities given to it.

³ Note that the resource literal is File, while the type of the resource literal is {File}.

What effects will be incurred if Logger.log is invoked? One approach is to manually⁴ examine its source code, but this is tedious and error-prone. In many real-world situations, the source code may be obfuscated or unavailable. A capability-based argument can do better, since a Logger can only exercise what authority it is explicitly given. In this case, the logger functor must be given File and Socket, so an upper bound on the effects of the Logger it instantiates will be the set of all operations on those resources, {File.*, Socket.*}. Knowing the Logger could perform arbitrary reads and writes to File, or arbitrary communication with Socket, the developer decides this implementation cannot be trusted and does not use it.

This reasoning only required us to examine what code was passed into the unannotated \log function by its annotated surroundings. To model this situation in CC, we add a new import expression that selects what authority ε the unannotated code may exercise. In the above example, the expected least authority of Logger is $\{\text{File.append}\}$, so that is what the corresponding import would select. The type system can then check if the capabilities being passed into the unannotated code exceed its selected authority. If it accepts, then ε safely approximates the effects of the unannotated code. This is the key result: when unannotated code is nested inside annotated code, capability-safety enables us to make a safe inference about its effects by examining what capabilities are being passed in by the annotated code.

2.1 Grammar (CC)

The grammar of CC is split into rules for annotated code and analogous rules for unannotated code. To distinguish the two, we put a hat above annotated types, expressions, and contexts: \hat{e} , $\hat{\tau}$, and $\hat{\Gamma}$ are annotated, while e, τ , and Γ are unannotated. The rules for unannotated programs and their types are given in Figure 3. Unannotated types τ are built using \to and sets of resources $\{\bar{r}\}$. An unannotated context Γ maps variables to unannotated types.

Fig. 3. Unannotated programs and types in CC.

Rules for annotated programs and their types are in Figure 4. The first main difference is that the arrow type constructor now has a subscript ε , which is a set of effects that functions of that type may incur.

⁴ or automatically—but if the automation produces an unexpected result we must fall back to manual reasoning to understand why.

```
\begin{array}{llll} \hat{e} ::= & labeled \ exprs : & \hat{\tau} ::= & annotated \ types : \\ & | x & & | \{\bar{r}\} \\ & | \hat{v} & & | \hat{\tau} \rightarrow_{\varepsilon} \hat{\tau} \\ & | \hat{e} \hat{e} & & & | \hat{\tau} ::= & annotated \ type \ ctx : \\ & | \hat{e} \cdot \pi & & | \hat{\tau} ::= & annotated \ type \ ctx : \\ & | import(\varepsilon_s) \ x = \hat{e} \ in \ e & import & | \varnothing & & | \hat{\Gamma}, x : \hat{\tau} \\ & | \hat{\tau} ::= & labeled \ values : & | & | \hat{\tau} \cdot \pi \end{pmatrix} \\ \hat{v} ::= & labeled \ values : & | \varepsilon ::= & effects : \\ & | \lambda x : \hat{\tau} \cdot \hat{e} & | \{\bar{r} \cdot \pi\} & effect \ set \\ \end{array}
```

Fig. 4. Annotated programs and types in CC.

The other main difference is the new expression form, $import(\varepsilon_s)$ $x=\hat{e}$ in e, which models the points at which capabilities are passed from annotated code into unannotated code. e is the unannotated code, while \hat{e} is the capability being given to e; we call \hat{e} an import. Note this definition allows an import to be any kind of expression, not just a resource literal. For simplicity, we assume only one capability is being passed into e. \hat{e} is bound to the variable x inside e. ε_s is the maximum authority that e is allowed to exercise (its "selected authority"). As an example, suppose an unannotated Logger, which requires File, is expected to only append to a file, but has an implementation that writes. This would be modelled by the expression import(File.append) x= File in $\lambda y:$ Unit. x.write.

Observe that import is the only way to mix annotated and unannotated code, because it is the only situation in which we can say something interesting about the unannotated code. For the rest of our discussion on CC, we will only be interested in unannotated code when it is encapsulated by an import expression.

One of the requirements of capability safety is that there be no ambient authority. This requirement is met by forbidding resource literals r from being used directly inside an import statement (they can still be passed in as a capability via the import's binding variable x). We could enforce this syntactically, by removing r from the language of unannotated expressions, but we choose to do it instead using the typing rule for import, given below.

2.2 Semantics (CC)

Reductions are defined on annotated expressions. The notation $\hat{e} \longrightarrow \hat{e}' \mid \varepsilon'$ means that \hat{e} is being reduced to \hat{e}' in a single step, incurring the set of effects ε' . The rules for CC are natural extensions of the simply-typed lambda calculus. Apart from the rules for import, we omit them for brevity.

If unannotated code e is wrapped inside annotated code $\operatorname{import}(\varepsilon_s) x = \hat{e}$ in e, we transform it into annotated code by recursively annotating its parts with ε_s . In practice, it is meaningful to execute purely unannotated code, but our only interest is when that code is wrapped inside an import expression, so we do not bother to give rules for it. There are two rules for reducing import expressions, given in Figure 5. E-IMPORT1 reduces the capability being imported. When it has been reduced to a value, E-IMPORT2

first annotates e with its selected authority ε — this is $\mathtt{annot}(e,\varepsilon)$ — and then substitutes the import \hat{v} for its name x in e — this is $\lceil \hat{v}/x \rceil \mathtt{annot}(e,\varepsilon)$.

$$\begin{split} \widehat{e} &\longrightarrow \widehat{e} \mid \varepsilon \end{split} \\ &\frac{\widehat{e} \longrightarrow \widehat{e}' \mid \varepsilon'}{\text{import}(\varepsilon_s) \ x = \widehat{e} \ \text{in} \ e \longrightarrow \text{import}(\varepsilon_s) \ x = \widehat{e}' \ \text{in} \ e \mid \varepsilon'} \ \ (\text{E-IMPORT1}) \\ \\ &\frac{\text{import}(\varepsilon_s) \ x = \widehat{v} \ \text{in} \ e \longrightarrow [\widehat{v}/x] \text{annot}(e, \varepsilon_s) \mid \varnothing} \end{split}$$

Fig. 5. New single-step reductions in CC.

 $\mathtt{annot}(e,\varepsilon)$ produces the expression obtained by recursively annotating the parts of e with the set of effects $\varepsilon.$ A definition is given in Figure 6. There are versions of annot defined for expressions and types. Later we shall need to annotate contexts, so the definition is given here. It is worth mentioning that annot operates on a purely syntatic level — nothing prevents us from annotating a program with something unsafe, so any use of annot must be justified.

```
\begin{split} & \operatorname{annot} :: e \times \varepsilon \to \hat{e} \\ & \operatorname{annot}(r, \_) = r \\ & \operatorname{annot}(\lambda x : \tau_1.e, \varepsilon) = \lambda x : \operatorname{annot}(\tau_1, \varepsilon).\operatorname{annot}(e, \varepsilon) \\ & \operatorname{annot}(e_1 e_2, \varepsilon) = \operatorname{annot}(e_1, \varepsilon) \operatorname{annot}(e_2, \varepsilon) \\ & \operatorname{annot}(e_1.\pi, \varepsilon) = \operatorname{annot}(e_1, \varepsilon).\pi \\ \\ & \operatorname{annot} :: \tau \times \varepsilon \to \hat{\tau} \\ & \operatorname{annot}(\{\bar{r}\}, \_) = \{\bar{r}\} \\ & \operatorname{annot}(\tau_1 \to \tau_2, \varepsilon) = \operatorname{annot}(\tau_1, \varepsilon) \to_\varepsilon \operatorname{annot}(\tau_2, \varepsilon). \\ \\ & \operatorname{annot} :: \Gamma \times \varepsilon \to \hat{\Gamma} \\ & \operatorname{annot}(\varnothing, \_) = \varnothing \\ & \operatorname{annot}(\Gamma, x : \tau, \varepsilon) = \operatorname{annot}(\Gamma, \varepsilon), x : \operatorname{annot}(\tau, \varepsilon) \end{split}
```

Fig. 6. Definition of annot.

2.3 Static Rules (CC)

A term can be annotated or unannotated, so we need to be able to recognise when either is well-typed. We do not reason about the effects of unannotated code directly, so judgements about them have the form $\Gamma \vdash e : \tau$. Subtyping judgements have the form $\tau <: \tau$. A summary of the rules for unannotated judgements is given in Figure 7.

The annotated static rules are effectively the same only involving the annotated expressions. The interesting rule is ε -IMPORT, given in Figure 16, which gives the type

$$\Gamma \vdash e : \tau$$

$$\frac{\Gamma, x : \tau_1 \vdash e : \tau_2}{\Gamma, x : \tau \vdash x : \tau} \quad \text{(T-VAR)} \qquad \frac{\Gamma, x : \tau_1 \vdash e : \tau_2}{\Gamma, x : \tau_1 \vdash e : \tau_2} \quad \text{(T-Abs)}$$

$$\frac{\Gamma \vdash e_1 : \tau_2 \to \tau_3 \quad \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash e_1 \; e_2 : \tau_3} \quad \text{(T-APP)} \qquad \frac{\Gamma \vdash e : \{\bar{r}\}}{\Gamma \vdash e . \pi : \text{Unit}} \quad \text{(T-OperCall)}$$

$$\tau <: \tau$$

$$\frac{\tau_1' <: \tau_1 \quad \tau_2 <: \tau_2'}{\tau_1 \rightarrow \tau_2 <: \tau_1' \rightarrow \tau_2'} \text{ (S-ARROW)} \qquad \frac{\{\bar{r}_1\} \subseteq \{\bar{r}_2\}}{\{\bar{r}_1\} <: \{\bar{r}_2\}} \text{ (S-RESOURCES)}$$

Fig. 7. (Sub)typing judgements for the unannotated sublanguage of CC

and approximate effects of an import expression. This is the only way to reason about what effects might be incurred by some unannotated code.

The rule is complicated, so to explain it we shall start with a simplified version and spend the rest of this section building up to the final version of ε -IMPORT.

To begin, typing $\operatorname{import}(\varepsilon_s)$ $x=\hat{e}$ in e in a context $\hat{\Gamma}$ requires us to know that the import \hat{e} is well-typed, so we add the premise $\hat{\Gamma}\vdash\hat{e}:\hat{\tau}$ with ε_1 . Since $x=\hat{e}$ is an import, it can be used throughout e. We do not want e to exercise authority it hasn't explicitly selected, so whatever capabilities it uses must be selected by the import expression; therefore, we require that e can be typechecked using only the binding $x:\hat{\tau}$. There is a problem though: e is unannotated and $\hat{\tau}$ is annotated, and there is no rule for typechecking unannotated code in an annotated context. To get around this, we define a function erase in Figure 8 which removes the annotations from a type. We then add $x:\operatorname{erase}(\hat{\tau})\vdash e:\tau$ as a premise.

```
erase :: \hat{\tau} \to \tau
 \begin{split} & \texttt{erase}(\{\bar{r}\}) = \{\bar{r}\} \\ & \texttt{erase}(\hat{\tau}_1 \to_{\varepsilon} \hat{\tau}_2) = \texttt{erase}(\hat{\tau}_1) \to \texttt{erase}(\hat{\tau}_2) \end{split}   \begin{aligned} & \textbf{Fig. 8. Definition of erase.} \end{aligned}
```

Note that, since the environment Γ for e has only one binding (for x), it cannot contain any bindings of resource literals—and the rule T-RESOURCE requires a binding in the environment in order to type a resource literal in an expression. Typing e in the restricted environment given by import thus prohibits ambient authority.

The first version of ε -IMPORT is given in Figure 9. Since $\mathrm{import}(\varepsilon_s)\,x=\hat{v}$ in $e\longrightarrow [\hat{v}/x]\mathrm{annot}(e,\varepsilon_s)$ by E-IMPORT2, the ascribed type is $\mathrm{annot}(\tau,\varepsilon)$, which is the type of the unannotated code, annotated with its selected authority ε_s . The effects of the import are $\varepsilon_1 \cup \varepsilon_s$ — the former comes from reducing the imported capability, which happens before the body of the import is annotated and executed, and the latter contains all the effects which the unannotated code might incur.

At the moment there is no relation between the selected authority ε and those effects captured by the imported capability \hat{e} . Consider $\hat{e}' = \mathtt{import}(\varnothing) \, x = \mathtt{File in x.write}$,

```
8 A. Craig et al. \frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad x : \texttt{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\Gamma} \vdash \texttt{import}(\varepsilon_s) \ x = \hat{e} \text{ in } e : \texttt{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon_s \cup \varepsilon_1} \ (\varepsilon\text{-IMPORT1-BAD})
```

Fig. 9. A first (incorrect) rule for type-and-effect checking import expressions.

which imports a File and writes to it, but declares its authority as \varnothing . According to ε -IMPORT1, $\vdash \hat{e}'$: Unit with \varnothing , but this is clearly wrong since \hat{e}' writes to File. An import should only be well-typed if the capability being imported only captures effects contained in the unannotated code's selected authority ε . In this case, File captures $\{\text{File.*}\}$, which is not contained in the selected authority \varnothing , so it should be rejected for that reason. To this end we define a function effects, which collects the set of effects that an annotated type captures. A first (but not yet correct) definition is given in Figure 10. We can then add the premise effects($\hat{\tau}$) $\subseteq \varepsilon_s$ to require that any imported capability must not capture authority beyond that selected in ε_s . The updated rule is given in Figure 11.

```
\begin{split} \text{effects} &:: \hat{\tau} \to \varepsilon \\ &\quad \text{effects}(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \varPi\} \\ &\quad \text{effects}(\hat{\tau}_1 \to_\varepsilon \hat{\tau}_2) = \text{effects}(\hat{\tau}_1) \cup \varepsilon \cup \text{effects}(\hat{\tau}_2) \end{split}
```

Fig. 10. A first (incorrect) definition of effects.

```
\frac{\hat{\varGamma} \vdash \hat{e} : \hat{\tau} \; \mathtt{with} \; \varepsilon_1 \quad x : \mathtt{erase}(\hat{\tau}) \vdash e : \tau \quad \mathtt{effects}(\hat{\tau}) \subseteq \varepsilon_s}{\hat{\varGamma} \vdash \mathtt{import}(\varepsilon_s) \; x = \hat{e} \; \mathtt{in} \; e : \mathtt{annot}(\tau, \varepsilon_s) \; \mathtt{with} \; \varepsilon \cup \varepsilon_1} \; (\varepsilon\text{-IMPORT2-BAD})
```

Fig. 11. A second (still incorrect) rule for type-and-effect checking import expressions.

The counterexample from before is now rejected by ε -IMPORT2, but there are still issues: the annotations on one import can be broken by another import. To illustrate, consider Figure 12 where two⁵ capabilities are imported. This program imports a function go which, when given a Unit \to_{\varnothing} Unit function with no effects, will execute it. The other import is File. The unannotated code creates a Unit \to Unit function which writes to File and passes it to go, which subsequently incurs File.write.

In the world of annotated code it is not possible to pass a file-writing function to go, but because the judgement $x: \mathtt{erase}(\hat{\tau}) \vdash e: \tau$ discards the annotations on go, and since the file-writing function has type $\mathtt{unit} \to \mathtt{unit}$, the unannotated world accepts it. The approximation is actually safe at the top-level, because the import selects $\{\mathtt{File.*}\}$, which contains $\mathtt{File.write} \longrightarrow \mathtt{but}$ it contains code that violates the type signature of go. We want to prevent this.

If go had the type $Unit \rightarrow_{\{File.write\}} Unit$ the above example would be safe, but a modified version where a file-reading function is passed to go would have the same issue. go is only safe when it expects every effect that the unannotated code might pass

⁵ Our formalisation only permits a single capability to be imported, but this discussion leads to a generalisation needed for the rules to be safe when multiple capabilities can be imported. In any case, importing multiple capabilities can be handled with an encoding of pairs.

```
import({File.*})
go = \lambdax: Unit \rightarrow_{\varnothing} Unit. x unit
f = File
in
go (\lambday: Unit. f.write)
```

Fig. 12. Permitting multiple imports will break ε -IMPORT2.

to it: if go had the type Unit $\rightarrow_{\{\text{File.*}\}}$ Unit, then the unannotated code cannot pass it a capability with an effect it isn't already expecting, so the annotation on go cannot be violated. Therefore, we require imported capabilities to have authority to incur the effects in ε . To achieve greater control in how we say this, the definition of effects is split into two separate functions called effects and ho-effects. The latter is for higher-order effects, i.e. the effects that are not captured within a function, but rather are possible because of what it is passed as an argument. If values of $\hat{\tau}$ possess a capability that can be used to incur the effect $r.\pi$, then $r.\pi \in \text{effects}(\hat{\tau})$. If values of $\hat{\tau}$ can incur an effect $r.\pi$, but need to be given the capability (as a function argument) by someone else in order to do it, then $r.\pi \in \text{ho-effects}(\hat{\tau})$. Definitions are given in Figure 13.

```
\begin{split} \text{effects} &:: \hat{\tau} \to \varepsilon \\ &\quad \text{effects}(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \varPi\} \\ &\quad \text{effects}(\hat{\tau}_1 \to_\varepsilon \hat{\tau}_2) = \text{ho-effects}(\hat{\tau}_1) \cup \varepsilon \cup \text{effects}(\hat{\tau}_2) \end{split} \text{ho-effects} &:: \hat{\tau} \to \varepsilon \\ &\quad \text{ho-effects}(\{\bar{r}\}) = \varnothing \\ &\quad \text{ho-effects}(\hat{\tau}_1 \to_\varepsilon \hat{\tau}_2) = \text{effects}(\hat{\tau}_1) \cup \text{ho-effects}(\hat{\tau}_2) \end{split} \textbf{Fig. 13. Effect functions (corrected)}.
```

Both effects and ho-effects are mutually recursive, with base cases for resource types. Any effect can be directly incurred by a resource on itself, hence $\mathsf{effects}(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$. A resource cannot be used to indirectly invoke some other effect, so ho-effects($\{\bar{r}\}$) = \varnothing . The mutual recursion echoes the subtyping rule for functions. Recall that functions are contravariant in their input type and covariant in their output; likewise, both functions recurse on the input-type using the other function, and recurse on the output-type using the same function.

In light of these new definitions, we still require $\operatorname{effects}(\hat{\tau}) \subseteq \varepsilon_s$ — unannotated code must select any effect its capabilities can incur — but we add a new premise $\varepsilon_s \subseteq \operatorname{ho-effects}(\hat{\tau})$, stipulating that imported capabilities must know about every effect they could be given by the unannotated code (which is at most ε). The counterexample from Figure 12 is now rejected, because $\operatorname{ho-effects}((\operatorname{Unit} \to_\varnothing \operatorname{Unit}) \to_\varnothing \operatorname{Unit}) = \varnothing$, but $\{\operatorname{File.*}\} \not\subseteq \varnothing$. However, this is still not sufficient! Consider $\varepsilon_s \subseteq \operatorname{ho-effects}(\hat{\tau}_1 \to_{\varepsilon'} \hat{\tau}_2)$. We want every higher-order capability involved to be expecting ε_s . Expanding the definition of $\operatorname{ho-effects}$, this is the same as $\varepsilon_s \subseteq \operatorname{effects}(\hat{\tau}_1) \cup \operatorname{ho-effects}(\hat{\tau}_2)$. Let $r.\pi \in \varepsilon_s$ and suppose $r.\pi \in \operatorname{effects}(\hat{\tau}_1)$, but $r.\pi \notin \operatorname{ho-effects}(\hat{\tau}_2)$. Then $\varepsilon_s \subseteq \operatorname{effects}(\hat{\tau}_1) \cup \operatorname{ho-effects}(\hat{\tau}_2)$ is still true, but $\hat{\tau}_2$ is not expecting $r.\pi$. Unannotated code could then violate the annotations on $\hat{\tau}_2$ by passing it a capability for $r.\pi$, using the same trickery as before. The cause of the issue is that $\subseteq \operatorname{does}$ not distribute over \cup . We want a relation like $\varepsilon_s \subseteq \operatorname{effects}(\hat{\tau}_1) \cup \operatorname{ho-effects}(\hat{\tau}_2)$, which

also implies $\varepsilon_s \subseteq \mathtt{effects}(\hat{\tau}_1)$ and $\varepsilon_s \subseteq \mathtt{effects}(\hat{\tau}_2)$. Figure 14 defines this: safe is a distributive version of $\varepsilon_s \subseteq \mathtt{effects}(\hat{\tau})$ and ho-safe is a distributive version of $\varepsilon_s \subseteq \mathtt{ho-effects}(\hat{\tau})$.

$$\begin{array}{l} \boxed{ \begin{array}{l} \operatorname{safe}(\hat{\tau},\varepsilon) \\ \\ \end{array}} \\ \frac{\operatorname{safe}(\{\bar{r}\},\varepsilon)}{\operatorname{safe}(\{\bar{r}\},\varepsilon)} \text{ (SAFE-RESOURCE)} & \frac{\varepsilon \subseteq \varepsilon' \quad \operatorname{ho-safe}(\hat{\tau}_1,\varepsilon) \quad \operatorname{safe}(\hat{\tau}_2,\varepsilon)}{\operatorname{safe}(\hat{\tau}_1 \to_{\varepsilon'} \hat{\tau}_2,\varepsilon)} \text{ (SAFE-ARROW)} \\ \\ \frac{\operatorname{ho-safe}(\hat{\tau},\varepsilon)}{\operatorname{ho-safe}(\{\bar{r}\},\varepsilon)} \text{ (HOSAFE-RESOURCE)} & \frac{\operatorname{safe}(\hat{\tau}_1,\varepsilon) \quad \operatorname{ho-safe}(\hat{\tau}_2,\varepsilon)}{\operatorname{ho-safe}(\hat{\tau}_1 \to_{\varepsilon'} \hat{\tau}_2,\varepsilon)} \text{ (HOSAFE-ARROW)} \\ \end{array}$$

Fig. 14. Safety judgements in CC.

```
\begin{split} \hat{\varGamma} \vdash \hat{e} : \hat{\tau} \; \text{with} \; \varepsilon_1 & \quad \text{effects}(\hat{\tau}) \subseteq \varepsilon_s \\ \frac{\text{ho-safe}(\hat{\tau}, \varepsilon_s) \quad x : \text{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\varGamma} \vdash \text{import}(\varepsilon_s) \; x = \hat{e} \; \text{in} \; e : \text{annot}(\tau, \varepsilon_s) \; \text{with} \; \varepsilon \cup \varepsilon_1} \end{split} \; (\varepsilon\text{-IMPORT3-BAD})
```

Fig. 15. A third (still incorrect) rule for type-and-effect checking import expressions.

An amended version of ε -IMPORT is given in Figure 15. It contains a new premise ho-safe $(\hat{\tau}, \varepsilon_s)$ which formalises the notion that every capability which could be given to a value of $\hat{\tau}$ — or any of its constituent pieces — must be expecting the effects ε_s it might be given by the unannotated code. The premises so far restrict what authority can be selected by unannotated code, but what about authority passed as a function argument? Consider the example $\hat{e} = \text{import}(\varnothing) \ x = \text{unit in } \lambda f : \text{File. f.write.}$ The unannotated code selects no capabilities and returns a function which, when given File, incurs File.write. This satisfies the premises in ε -IMPORT3, but its annotated type is $\{\text{File}\} \to_{\varnothing} \text{Unit: not good!}$

Suppose the unannotated code defines a function f, which gets annotated with ε_s to produce $\mathrm{annot}(f,\varepsilon_s)$. Suppose $\mathrm{annot}(f,\varepsilon_s)$ is invoked at a later point in the annotated world and incurs the effect $r.\pi$. What is the source of $r.\pi$? If $r.\pi$ was selected by the import expression surrounding f, it is safe for $\mathrm{annot}(f,\varepsilon_s)$ to incur this effect. Otherwise, $\mathrm{annot}(f,\varepsilon_s)$ may have been passed an argument which can be used to incur $r.\pi$, in which case $r.\pi$ is a higher-order effect of $\mathrm{annot}(f,\varepsilon_s)$. If the argument is a function, then $r.\pi \in \varepsilon_s$ by the soundness of our calculus (or it would not typecheck). If the argument is a resource r, then $\mathrm{annot}(f,\varepsilon_s)$ may exercise $r.\pi$ without declaring it — this is the case we do not yet account for.

We want ε_s to contain every effect captured by resources passed into annot (f, ε_s) as arguments. We can do this by inspecting the (unannotated) type of f for resource sets. For example, if the unannotated type is $\{\text{File}\} \to \text{Unit}$, then we need $\{\text{File}.*\}$

```
\mathtt{effects}(\hat{\tau}) \cup \mathtt{ho\text{-effects}}(\mathtt{annot}(\tau,\varnothing)) \subseteq \varepsilon_s
\frac{\hat{\varGamma} \vdash \hat{e} : \hat{\tau} \; \mathtt{with} \; \varepsilon_1 \quad \; \mathtt{ho\text{-safe}}(\hat{\tau}, \varepsilon_s) \quad \; x : \mathtt{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\varGamma} \vdash \mathtt{import}(\varepsilon_s) \; x = \hat{e} \; \mathtt{in} \; e : \mathtt{annot}(\tau, \varepsilon_s) \; \mathtt{with} \; \varepsilon_s \cup \varepsilon_1} \quad (\varepsilon\text{-IMPORT})
```

Fig. 16. The final rule for typing imports.

in ε_s . To do this, we add a new premise ho-effects (annot (τ,\varnothing)) $\subseteq \varepsilon_s$. ho-effects is only defined on annotated types, so we first annotate τ with \varnothing . We are only inspecting the resources passed into f as arguments, so the annotations are not relevant – annotating τ with \varnothing is therefore a good choice. We can now handle the example from before. The unannotated code types via the judgement x: Unit $\vdash \lambda f$: {File}. f.write: $\{\text{File}\} \rightarrow \text{Unit.} \text{ Its higher-order effects are ho-effects}(\text{annot}(\{\text{File}\} \rightarrow \text{Unit.}\varnothing)) =$ $\{File.*\}$, but $\{File.*\} \not\subseteq \emptyset$, so the example is safely rejected.

The final version of ε -IMPORT is given in Figure 16. With it, we can now model the example from the beginning of this section, where the Logger selects the File capability and exposes an unannotated function \log with type Unit \rightarrow Unit and implementation e. The expected least authority of Logger is {File.append}, so its corresponding import expression would be import(File.append) $f = \text{File in } \lambda x$: Unit. e. The imported capability is f = File, and $\text{effects}(\{\text{File}\}) = \{\text{File.*}\} \not\subseteq$ {File.append}, so this example is safely rejected: Logger.log has authority to do anything with File, and its implementation e might be violating its stipulated least authority {File.append}.

2.4. Soundness (CC) Only annotated programs can be reduced and have their effects approximated, so the soundness theorem only applies to annotated judgements. Its statement is given below.

Theorem 1 (CC Single-step Soundness). If $\hat{\Gamma} \vdash \hat{e}_A : \hat{\tau}_A$ with ε_A and \hat{e}_A is not a value, then $\hat{e}_A \longrightarrow \hat{e}_B \mid \varepsilon$, where $\hat{\Gamma} \vdash \hat{e}_B : \hat{\tau}_B$ with ε_B and $\hat{\tau}_B <: \hat{\tau}_A$ and $\varepsilon_B \cup \varepsilon \subseteq \varepsilon_A$, for some $\hat{e}_B, \varepsilon, \hat{\tau}_B, \varepsilon_B$.

Due to small page limit we refer the interested readers to the Technical Report with complete proofs including multi-step soundness for the system presented here [1].

Applications

In this section we show how the capability-based design of CC can assist in reasoning about the effects and behaviour of a program. We present several scenarios which demonstrate unsafe behaviour or a particular developer story. This takes the form of writing a Wyvern program, translating it to CC using the techniques of the previous section, and then explaining how the rules of CC apply. In discussing these, we hope to illustrate where the rules of CC may arise in practice, and convince the reader that they adequately capture the intuitive properties of capability-safe languages like Wyvern.

3.1 Unannotated Client There is a single primitive capability File. A logger module possessing this capability exposes a function log which incurs File.write when executed. The client module, possessing the logger module, exposes a functino run which invokes logger.log, incurring File.write. While logger has been annotated, client has not — if client.run is executed, what effects might it have? Code for this example is given below.

```
module def logger(f: {File}):Logger
  def log(): Unit with {File.append} =
    f.append(''message logged'')
  module def client (logger: Logger)
2
  def run(): Unit =
  logger.log()
  require File
  instantiate logger(File)
  instantiate client(logger)
4
  client.run()
```

The translation is given below. It first creates two functions, MakeLogger and MakeClient, which instantiate the logger and client modules. Lines 1-3 define MakeLogger. When given a File, it returns a function representing logger.log. Lines 5-8 define MakeClient. When given a Logger, it returns a function representing client.run. Lines 10-15 define MakeMain which returns a function which, when executed, instantiates all other modules and invokes the code in the body of Main. Program execution begins on line 16, where Main is given the initial capabilities: just File in this case.

```
let MakeLogger =
      (\lambdaf: File.
2
        \lambdax: Unit. f.append) in
   let MakeClient =
      (\lambdalogger: Unit \rightarrow_{\{\text{File.append}\}} Unit.
         import(File.append) l = logger in
           \lambdax: Unit. 1 unit) in
   let MakeMain =
10
      (\lambdaf: File.
11
           let loggerModule = MakeLogger f in
12
           let clientModule = MakeClient loggerModule in
13
           clientModule unit) in
14
15
   MakeMain File
```

The interesting part is on line 7 where the unannotated code selects {File.append} as its authority. This is exactly the effects of the logger, i.e. $effects(Unit \rightarrow_{\{File.append\}})$ Unit) = {File.append}. The code also satisfies the higher-order safety predicates, and the body of the import expression typechecks in the empty context. Therefore, the unannotated code typechecks by ε -IMPORT with approximate effects {File.append}.

3.2 Unannotated Library
The next example inverts the roles of the last scenario: now, the annotated client wants to use the unannotated logger. logger captures File and exposes a single function log which incurs the File.append effect. client has a function run which executes logger.log, incurring its effects. client.run is annotated with \emptyset , so the implementation of logger.log violates its interface.

```
module def logger(f: {File}): Logger

def log(): Unit =
    f.append(``message logged'')

module def client(logger: Logger)

def run(): Unit with {File.append} =
    logger.log()

require File

instantiate logger(File)
instantiate client(logger)

client.run()
```

The translation is given below. On lines 3-4, the unannotated code is wrapped in an import expression selecting $\{\text{File.append}\}$ as its authority. The implementation of logger actually abides by this selected authority, but it has the authority to perform any operation on File, so it could, in general, invoke any of them. ε -IMPORT rejects this example because the imported capability has the type $\{\text{File}\}$ and $\text{effects}(\{\text{File}\}) = \{\text{File.*}\} \not\subseteq \{\text{File.append}\}$.

```
let MakeLogger =
      (\lambdaf: File.
        import (File.append) f = f in
           \lambda x: Unit. f.append) in
   let MakeClient =
      (\lambdalogger: Logger.
        \lambda x: Unit. logger unit) in
   let MakeMain =
10
      (\lambdaf: File.
11
        let loggerModule = MakeLogger f in
12
        let clientModule = MakeClient loggerModule in
13
        clientModule unit) in
14
15
  MakeMain File
```

The only way for this to typecheck would be to annotate client.run as having every effect on File. This demonstrates how the effect-system of CC approximates unannotated code: it simply considers it as having every effect which could be incurred on those resources in scope, which here is File.*.

3.3 Higher-Order Effects

Here Main gains its functionality from a plugin. Plugins might be written by third-parties, in which case we may not be able to view their source code, but still want to

reason about the authority they exercise. In this example, plugin has access to a File capability, but its interface does not permit it to perform any operations on File. It tries to subvert this by wrapping the capability inside a function and passing it to malicious, which invokes File.read in a higher-order manner in an unannotated context.

```
module malicious

def log(f: Unit → Unit): Unit
    f()

module plugin
import malicious

def run(f: {File}): Unit with Ø
malicious.log(λx:Unit. f.read)

require File
import plugin

plugin.run(File)
```

This example shows how higher-order effects can obfuscate potential security risks. On line 3 of malicious, the argument to log has type Unit \rightarrow Unit. The body of log types with the T-rules, which do not approximate effects. It is not clear from inspecting the unannotated code that a File.read will be incurred. To realise this requires one to examine the source code of both plugin and malicious.

A translation is given below. On lines 2-3, the malicious code selects its authority as \varnothing , to be consistent with the annotation on plugin.run. This example is rejected by ε -IMPORT. When the unannotated code is annotated with \varnothing , it has type {File} \to_{\varnothing} Unit. The higher-order effects of this type are File.*, which is not contained in the selected authority \varnothing — hence, ε -IMPORT safely rejects the program.

```
let malicious =  (import(\emptyset) \text{ y=unit in} \\ \lambda f \text{: Unit } \rightarrow \text{ Unit. } f()) \text{ in} 

let plugin =  (\lambda f \text{: } \{\text{File}\} \text{.} \\ \text{malicious}(\lambda x \text{: Unit. } f \text{. read})) \text{ in} 

let MakeMain =  (\lambda f \text{: } \{\text{File}\} \text{.} \\ \text{plugin } f) \text{ in} 

MakeMain File
```

To get this example to typecheck, the import expression has to select {File.*} as its authority, and plugin.run needs to be annotated with {File.*}. A program would have to be rewritten to explicitly say that plugins can exercise authority over File.

3.4 Resource Leak

This is another example which obfuscates an unsafe effect by invoking it in a higherorder manner. The setup is the same, except the function which plugin passes to malicious now returns File when invoked. malicious uses this function to obtain File and directly invokes read upon it, violating the supposed purity of plugin.

```
module malicious

def log(f: Unit → File):Unit
   f().read

module plugin
import malicious

def run(f: {File}): Unit with ∅
malicious.log(λx:Unit. f)

require File

import plugin

plugin.run(File)
```

The translation is given below. The unannotated code in malicious is given on lines 5-6. The selected authority is \varnothing , to be consistent with the annotation on plugin. Nothing is being imported, so the import binds a name y to unit. This example is rejected by ε -IMPORT because the premise $\varepsilon = \mathsf{effects}(\hat{\tau}) \cup \mathsf{ho\text{-effects}}(\mathsf{annot}(\tau, \varepsilon))$ is not satisfied. In this case, $\varepsilon = \varnothing$ and $\tau = (\mathsf{Unit} \to \{\mathsf{File}\}) \to \mathsf{Unit}$. Then $\mathsf{annot}(\tau, \varepsilon) = (\mathsf{Unit} \to_\varnothing \{\mathsf{File}\}) \to_\varnothing$ Unit and $\mathsf{ho\text{-effects}}(\mathsf{annot}(\tau, \varepsilon)) = \{\mathsf{File.*}\}$. Thus, the premise cannot be satisfied and the example is safely rejected.

```
let malicious =
       (import (∅) y=unit in
2
         \lambda f: Unit \rightarrow \{File\}. f().read) in
   let plugin =
5
      (\lambda f: \{File\}.
         malicious (\lambdax:Unit. f)) in
   let MakeMain =
      (\lambda f: \{File\}.
10
         plugin f) in
11
12
   MakeMain File
13
```

4 Conclusions

We introduced CC, a lambda calculus with primitive capabilities and their effects, which allows unannotated code to be nested inside annotated code with a new import construct. The capability-safe design of CC allows us to safely infer the effects of unannotated code by inspecting what capabilities are passed into it by its annotated surroundings. Such an approach allows code to be incrementally annotated, giving developers a

balance between safety and convenience and alleviating the verbosity that has discouraged widespread adoption of effect systems [18].

More broadly, our results demonstrate that the most basic form of capability-based reasoning—that you can infer what code can do based on what capabilities are passed to it—is not only useful for informal reasoning, but can improve formal reasoning about code by reducing the necessary annotation overhead.

4.1 Related Work

While much related work has already been discussed as part of the presentation, here we cover some additional strands related to capabilities and effects.

Capabilities were introduced by [3] to control which processes in an operating system had permission to access which operating system resources. These early ideas were adapted to the programming language setting as the object capability model, exemplified in the work of Mark [16], which constrains how permissions may proliferate among objects in a distributed system. [14] formalised the notion of a capability-safe language and showed that a subset of Caja (a Javascript implementation) is capability-safe. Miller's model has been applied to more heavyweight systems: [6] combined Hoare logic with capabilities to formalise the notion of trust. Capability-safety parallels have been explored in the operating systems literature, where similar restrictions on dynamic loading and resource access [7] enable static, lightweight analyses to enforce privilege separation [13].

The original effect system by [11] was used to determine what expressions could safely execute in parallel. Subsequent applications include determining what functions a program might invoke [20] and what regions in memory might be accessed or updated during execution [19]. In these systems, "effects" are performed upon "regions"; in ours, "operations" are performed upon "resources". CC also distinguishes between unannotated and annotated code: only the latter will type-and-effect-check. Another capability-based effect system is the one by [4], who use effect polymorphism and possible world semantics to express behavioural invariants on data structures. CC is not as expressive, since it only topographically inspects how capabilities can be passed around a program, but the resulting formalism and theory is much more lightweight.

4.2 Future Work

Our effects model only the use of capabilities which manipulate system resources. This definition could be generalised to track other sorts of effects, such as stateful updates. In our model, resources and operations are fixed throughout runtime; it would be interesting to consider the theory when they can be created and destroyed at runtime.

We hope to extend the ideas in this paper to the point where they might be used in capability-safe languages to help authority-safe design and development. Implementing these ideas in a general-purpose, capability-safe language such as *Wyvern* would do much towards that end. While we have captured the most obvious and basic form of capability-based reasoning about effects, the ideas here could potentially be useful in other kinds of formal reasoning systems.

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