

CSE 321 Homework 5 Report

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EXPLANATIONS OF THE QUESTIONS

Question 1:

I. Algorithm:

Let J be the array of jobs $J = [[t_1, w_1] \dots [t_n, w_n]]$.

If we calculate the w_i / t_i for each job j_i and sort in decreasing order, jobs will be sorted in order to minimizing the weighted sum.

For example;

$J = [[4, 7], [9, 4], [10, 9], [3, 8]]$

$J_1 = [4, 7] \quad T_1 = 4 \quad W_1 = 7$

$J_2 = [9, 4] \quad T_2 = 9 \quad W_2 = 4$

$J_3 = [10, 9] \quad T_3 = 10 \quad W_3 = 9$

$J_4 = [3, 8] \quad T_4 = 3 \quad W_4 = 8$

$$W_1 / T_1 = 7 / 4 = 1.75$$

$$W_2 / T_2 = 4 / 9 = 0.4$$

$$W_3 / T_3 = 9 / 10 = 0.9$$

$$W_4 / T_4 = 8 / 3 = 2.7$$

Job Order = J_4, J_1, J_3, J_2

Lets calculate;

$$C_1 = T_4 * W_4 = 3 * 8 = 24$$

$$C_2 = (T_4 + T_1) * W_1 = 7 * 7 = 49$$

$$C_1 + C_2 = 73$$

If we had chosen opposite:

$$C_1 = T_1 * W_1 = 4 * 7 = 28$$

$$C_2 = (T_4 + T_1) * W_4 = 7 * 8 = 56$$

$$C_1 + C_2 = 84$$

The total sum would be higher.

In conclusion, if we choose the job which has minimum t_i value according to maximum w_i value; we will be choose the minimum t_{i-1} for the next job j_i . In other words we will be increase the multiplier for the next weight with the possible smallest value.

II. Time Complexity:

We're using a bubble sort algorithm here for sorting the values due to a condition; which take $O(n^2)$ time.

$$T(n) \in O(n^2)$$

Question 2-a:

I. Proof:

As I calculated and printed with the code in the .py file :

```
for i= 1 to n
  if Ni < Si then
    Output "NY in Month i" else
    Output "SF in Month i" end
```

The algorithm above does not correctly solve the problem because if the table was:

#	Month1	Month2	Month3	Month4
NY	1	3	2	6
SF	50	20	20	4

$M = 10$

It outputs:

['NY', 'NY', 'NY', 'SF']

The $M = 10$, so according to the algorithm the sum of the costs will be :

Total Cost = $1 + 3 + 2 + 4 + 10 = 20$

But if we would be taken the NY as last city instead of SF, we won't have to be add M value at the end and the correct output would be:

['NY', 'NY', 'NY', 'NY']

And the sum of the costs would be:

Total Cost = $1 + 3 + 2 + 6 = 12$

Question 2-b:

I. Algorithm:

Let $S[s_1 \dots s_n]$ and $N[n_1 \dots n_n]$ be two lists that represents operating costs of 2 cities N for NY and S for SF. n is the # of months and M is the moving cost.

$M = 10$;

ShiftCostBefore = 0;

#	Month1	Month2	Month3	Month4
NY	1	3	20	30
SF	50	20	2	4
Choosen	1	3	2	4
Month	NY	NY	SF	SF

First we take the smallest one of the **first costs**;

$$N[0] = 1 < S[0] = 50$$

$$\text{Choosen}[0] = 1, \text{Month}[0] = \text{NY}$$

Then we compare the second costs with calculating the summation with the moving cost;

$$N[1] = 3 < ((\text{ShiftCostBefore} + M = 10) + (S[1] = 20) = 30)$$

$$\text{Choosen}[1] = 3, \text{Month}[1] = \text{NY}$$

We keep comparing;

$$N[2] = 20 > ((\text{ShiftCostBefore} = 0) + (M = 10) = 10) + (S[2] = 2) = 12)$$

$$\text{Choosen}[2] = 2, \text{Month}[2] = \text{SF}, \text{ShiftCostBefore} += M$$

And last comparison;

$$N[3] = 30 > ((\text{ShiftCostBefore} = 10) + (M = 10) = 20) + (S[3] = 2) = 22)$$

$$\text{Choosen}[3] = 2, \text{Month}[2] = \text{SF}$$

We calculate shifts total so far, cause the next value could be greater than our moving cost.

II. Time Complexity:

For each record, we compare once so the algorithm takes $O(n)$ time.

$$T(n) \in O(n)$$