

NOTE: ALL ANSWERS TEMPORARY AND NOT CHECKED

**Question 1:** (Section 2.3, #2b)  $B = \{ -\pi^x \mid x \leq 0 \}$ .

**Question 2:** (Section 2.3, #5)

(a)  $S = \{ x \in \mathbf{Z} \mid x \geq 5 \}$ .

(b)  $S = \{ 2x + 1 \mid x \in \mathbf{Z} \}$ .

(c)  $S = \{ x \in \mathbf{Q} \mid x > 0 \}$ .

(d)  $S = \{ x \in \mathbf{R} \mid 1 < x < 7 \}$ .

(e)  $S = \{ x \in \mathbf{R} \mid x^2 > 0 \}$ .

**Question 3:** (Section 5.3, #2)

*Proof.* In order to prove equality, we show that  $A \cup (B \cap C) \subseteq (A \cap B) \cup (A \cap C)$  and  $(A \cap B) \cup (A \cap C) \subseteq A \cup (B \cap C)$ .

( $\rightarrow$ ) Suppose  $x$  is an arbitrary element in  $A \cap (B \cup C)$ . Then,  $x \in A \wedge (x \in B \vee x \in C)$ . By the distributive property of conjunctions and disjunctions,  $(x \in A \wedge x \in B) \vee (x \in A \wedge x \in C)$ . By the definition of

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