

Fundamentals of Applied Microcontrollers Manual

Seth McNeill

Edition 0.01
2022 March 03

Contents

1	Introduction	4
2	Number Systems	5
2.1	Decimal Numbers	5
2.2	Binary Numbers	6
2.3	Hexadecimal Numbers	6
2.4	Binary Background	7
2.5	Converting Between Bases	8
2.5.1	Binary to Decimal	8
2.5.2	Decimal to Binary	8
2.5.3	Binary and Hexadecimal	9
2.6	Colors	9
2.7	ASCII	9
2.8	Adding and Subtracting Binary Numbers	10
2.8.1	Default method	10
2.8.2	Twos Complement method	10
2.9	Gray Codes	10
2.10	Binary Background	12
2.11	Assignment	12
3	Boolean Logic	14
3.1	Introduction	14
3.2	Methods of Representing Logic	14
3.3	Boolean Algebra	15
3.3.1	Theorems of Boolean Algebra	15
3.4	Logic Gates and Truth Tables	16

4	Arduino Startup	19
4.1	Introduction	19
4.2	Datasheets	19
4.2.1	Arduino Nano Connect RP2040	19
4.2.2	RP2040 Microcontroller	19
4.2.3	IMU - ST LSM6DSOXTR	20
4.2.4	Mic - ST MP34DT06JTR	20
4.2.5	WiFi and Bluetooth - U-blox® Nina W102	20
4.2.6	Cryptographic IC - Microchip® ATECC608A	20
4.3	Installing the IDE	20
5	Buttons and Serial Communications	27
5.1	Introduction	27
5.2	Buttons	27
5.3	Serial Communications	31
5.3.1	Universal Asynchronous Receiver-Transmitter	31
5.3.2	Serial Peripheral Interface	34
5.3.3	Inter-Integrated Circuit	35
5.4	In Case of Upload Lock-up or Failure	36
5.5	Arduino Programming Suggestions	37
5.6	Arduino Button Setup	37
5.7	Arduino Serial Setup	38
5.8	Laboratory Exercises	39
5.8.1	Button to Serial	39
5.8.2	Tones	40
5.8.3	APDS-9960	40
5.8.4	Distance to Tone	40
5.8.5	Color Recognition	40
5.8.6	SHT31	40
5.8.7	Turn In	41
6	Displays	42
6.1	Introduction	42
6.1.1	LCD	42
6.1.2	eInk	42
6.1.3	OLED	43
6.2	Pixel Layout	43
6.3	Using the Display	43

<i>CONTENTS</i>	3
6.4 Lab Exercise	45
6.4.1 To Do	45
6.4.2 Converting Images for Arduino	46
6.4.3 Submit	47
7 Data Collection and Environmental Sensing	48
7.1 Introduction	48
7.2 Laboratory Exercises	48
7.2.1 To Do	48
7.2.2 Suggestions	49
7.2.3 Turn In	50
8 Inertial Measurements	51
8.1 Introduction	51
8.2 Rectilinear Kinematics	51
8.3 Angle Measurement	52
8.3.1 Accelerometer Angles	53
8.3.2 Gyroscope Angles	54
8.3.3 Fusing Accelerometer and Gyroscope Angles	54
8.4 Useful References	55

Chapter 1

Introduction

This book is the accompanying text to a class introducing microcontrollers to upper division, non-electrical engineering undergraduate students who have taken some C programming.

Chapter 2

Number Systems

This chapter introduces the concepts of different numbering systems that are relevant to microcontrollers.

2.1 Decimal Numbers

The standard number system used by humans is based on 10. This logically flows the usual numbers of fingers or toes humans have. When counting in the base 10 (decimal) we start at 0, count up to 9, then run out of numbers to use. When runs out of numbers, we put a number to the left of the column we were counting in, and then start over at zero again which gives us the number 10. A more clear way to count would be to count from 00 to 09, then increment the left digit and start the right digit back at 0. This can be continued until 99 is reached. But now we have a model to follow. If a column gets to 9, we increment a column to the left and start the current column over at 0. This leads to the number 100. This concept can be continued forever.

When given a particular number, 3254, in decimal the value is calculated as

$$3254 = 3 \cdot 1000 + 2 \cdot 100 + 5 \cdot 10 + 4 \quad (2.1)$$

It could also be represented as

$$3254 = 3 \cdot 10^3 + 2 \cdot 10^2 + 5 \cdot 10^1 + 4 \cdot 10^0 \quad (2.2)$$

This is the basis for a positional number system.

2.2 Binary Numbers

Computers run a base 2 system, also known as binary. This means that we only have two options at each position, 1 or 0, instead of the 10 available in the decimal system. However, counting is done in the same way, when you run out of symbols, increment the position to the left and then start over at zero in the current position.

Binary numbers are also positional so a number like 1011 is

$$1011 = 1 \cdot 2^3 + 0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0 = 11_{10} \quad (2.3)$$

where 11_{10} indicates that the number 11 is base 10.

The maximum value a binary number can have is determined by the number of bits it has. The formula is:

$$V_{max} = 2^n - 1 \quad (2.4)$$

where n is the number of bits. For example, an 8 bit number has a maximum value of $2^8 - 1 = 255$.

2.3 Hexadecimal Numbers

The problem for humans is that we have a very difficult time reading binary numbers. Especially once the numbers get long such as 11101101010010110101_2 . The first thing we can do to improve intelligibility is to put a space in every 4 digits so that we aren't completely bowled over by all the digits. This gives us $1110\ 1101\ 0100\ 1011\ 0101_2$. This is better but still leaves some challenges. Someone pointed out that since 4 bits can have 16 different values, what if each 4 bits (also called a nibble) was represented by a single base 16 number. Base 16 is called hexadecimal. It has the problem that it runs out of digits once we get to 10, so it was decided to simply start on the alphabet so 10_{10} is A_{16} , 11_{10} is B_{16} , and so forth. Now the cumbersome binary number we've been playing with can be represented as $ED4B5_{16}$.

A comparison of the different numbering system representations of 0 through 15_{10} are shown in Table [2.1](#).

Decimal	Binary	Hexadecimal
00	0000	0
01	0001	1
02	0010	2
03	0011	3
04	0100	4
05	0101	5
06	0110	6
07	0111	7
08	1000	8
09	1001	9
10	1010	A
11	1011	B
12	1100	C
13	1101	D
14	1110	E
15	1111	F

Table 2.1: Decimal, binary, and hexadecimal numbers align as shown in this table.

2.4 Binary Background

The reasons for this stem from early computers using switches (relays) as their basic computing elements and the fact that telling the difference between a “high” voltage and a “low” voltage is easier to do than to differentiate 10 different voltages. It also allows for a gap between high and low that creates some immunity to noise. (TODO: insert figure or reference figure from logic chapter)

2.5 Converting Between Bases

2.5.1 Binary to Decimal

Converting to decimal is straightforward since we can simply sum each digit multiplied by the power of 2 it represents.

$$V_{10} = \sum_{i=0}^p d_i \cdot 2^i \quad (2.5)$$

In Equation 2.5 the p digits, d_i , of the binary number are summed from right to left while being multiplied by the power of 2 they represent. As an example, convert 1011 0111 to decimal.

$$\begin{aligned} V_{10} &= 1 \cdot 2^0 + 1 \cdot 2^1 + 1 \cdot 2^2 + 0 \cdot 2^3 + 1 \cdot 2^4 + 1 \cdot 2^5 + 0 \cdot 2^6 + 1 \cdot 2^7 \\ &= 1 + 2 + 4 + 0 + 16 + 32 + 0 + 128 \\ &= 183 \end{aligned} \quad (2.6)$$

I usually find it easiest to just remember the powers of two for each place and add them up.

$$\begin{array}{cccccccc} 128 & 64 & 32 & 16 & 8 & 4 & 2 & 1 \\ 1 & 0 & 1 & 1 & 0 & 1 & 1 & 1 \end{array} = 1 + 2 + 4 + 16 + 32 + 128 \quad (2.7)$$

2.5.2 Decimal to Binary

Converting decimal numbers to binary involves dividing by 2 until the remainder is 0 or 1. The process goes as follows:

1. Divide the number by 2. If the remainder is 1 then the least significant bit is 1 otherwise if the remainder is 0 (it was an even number) then the least significant bit is 0.
2. Take the quotient from the previous step and divide by 2. The remainder is the next more significant bit in the binary representation.
3. Repeat Step 2 until the quotient is 0.

As an example, let's convert 11_{10} to binary.

$$\begin{aligned} 11 \nabla \cdot 2 &= 5R1 \rightarrow 1 \text{ (LSB)} \\ 5 \nabla \cdot 2 &= 2R1 \rightarrow 1 \\ 2 \nabla \cdot 2 &= 1R0 \rightarrow 0 \\ 1 \nabla \cdot 2 &= 0R1 \rightarrow 1 \text{ (MSB)} \end{aligned} \quad (2.8)$$

That means that 11_{10} is 1011_2 . As another example let us convert 20_{10} to binary.

$$\begin{aligned}
 20 \nabla \cdot 2 &= 10R0 \rightarrow 0 \text{ (LSB)} \\
 10 \nabla \cdot 2 &= 5R0 \rightarrow 0 \\
 5 \nabla \cdot 2 &= 2R1 \rightarrow 1 \\
 2 \nabla \cdot 2 &= 1R0 \rightarrow 0 \\
 1 \nabla \cdot 2 &= 0R1 \rightarrow 1 \text{ (MSB)}
 \end{aligned} \tag{2.9}$$

This shows that 20_{10} is 10100_2 .

2.5.3 Binary and Hexadecimal

For conversions between binary and hexadecimal I tend to use the table lookup method. After using it enough times you begin to memorize the conversions. In my head I'm usually converting from binary to decimal on each nibble and then converting decimal into hexadecimal. So if I see 0101 I remember it is 5 in decimal which is the same in hex. If I see 1010 I remember that it is $8 + 2 = 10$ which is one more than 9 so it is A in hex.

2.6 Colors

Colors for display on computers are represented as binary numbers. Colors are 24 bit which is broken down into 3 8 bit numbers representing red, green, and blue (RGB). Eight bits give values over the range of 0 to 255 so colors are represented by 3 numbers such as (255, 0, 255) which gives a **color like this**. It is good to note that (255, 255, 255) is white, (0, 0, 0) is black, and (X, X, X) where all three numbers are the same is gray.

Sometimes colors are represented as a 6 digit binary number in hexadecimal form prefixed by 0x such as 0xFF00FF for the color we looked at previously.

2.7 ASCII

Since computers operate using binary numbers, how do we get them to represent human languages? The method caught it is called **American Standard Code for Information Interchange (ASCII)**. Basically, 7 bit numbers were

mapped to letters, numbers, punctuation, symbols, and control characters. Some examples are A is 65, Z is 90, a is 97, z is 122, 0 is 48, 9 is 57. The most used control characters are carriage return (13 or \r) and line feed (10 or \n). Unix based operating systems (Linux, OS X) use line feed to indicate a new line. Windows uses both (\r\n).

Look up an ASCII table online when you need to know the values.

2.8 Adding and Subtracting Binary Numbers

2.8.1 Default method

2.8.1.1 Addition

Calculate the binary sum $0001\ 0011\ 1101 + 0000\ 1011\ 0111$.

$$\begin{array}{r}
 0\ 0\ 0\ 1\ 0\ \overset{1}{0}\ \overset{1}{1}\ \overset{1}{1}\ \overset{1}{1}\ \overset{1}{0}\ 1 \\
 +\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 1\ 0\ 1\ 1\ 1 \\
 \hline
 0\ 0\ 0\ 1\ 1\ 1\ 1\ 1\ 0\ 1\ 0\ 0
 \end{array} \tag{2.10}$$

2.8.1.2 Subtraction

Calculate the binary difference $0001\ 0011\ 1101 - 0000\ 1011\ 0111$.

$$\begin{array}{r}
 0\ 0\ 0\ \overset{0}{\cancel{1}}\ \overset{01}{\cancel{0}}\ 0\ 1\ 1\ \overset{0}{\cancel{1}}\ \overset{01}{\cancel{1}}\ \overset{01}{\cancel{0}}\ 1 \\
 -\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 1\ 0\ 1\ 1\ 1 \\
 \hline
 0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 0
 \end{array} \tag{2.11}$$

2.8.2 Twos Complement method

2.9 Gray Codes

When counting in binary, often times more than one bit changes as the number increments. This works fine in the ideal world, but in the real world, the logic controlling each bit might be slightly different. This will cause

Decimal	Two's Complement
7	0111
6	0110
5	0101
4	0100
3	0011
2	0010
1	0001
0	0000
-1	1111
-2	1110
-3	1101
-4	1100
-5	1011
-6	1010
-7	1001
-8	1000

Table 2.2: This table shows the decimal and two's complement numbers for 4-bits.

one bit to change at a slightly different time than another bit. That causes glitches in the counting that can be disruptive to the overall system.

Take as an example a robot that represents the cardinal directions as binary integers as illustrated in Figure 2.1.

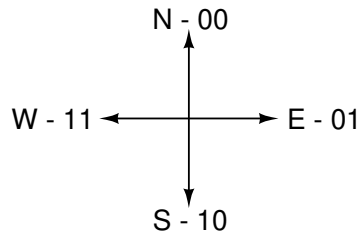


Figure 2.1: This figure shows using regular binary counting to represent the cardinal directions.

Using regular binary counting means that as the direction changes from East to South, two bits have to change. If the bits are driven by real switches

or differing logic they may not change simultaneously leading to possible outputs of E - W - S or E - N - S. If the data is being used in a sequential manner it could lead to erroneous actions by the device (robot, car, etc.). Instead of using regular binary counting, we could use an encoding that only changes one bit at a time as the directions change as shown in Figure 2.2.

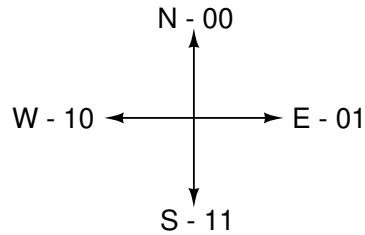


Figure 2.2: This figure shows using Gray codes to represent the cardinal directions.

Counting systems like this are called Gray code after [Frank Gray](#) or reflected binary code. A 4-bit example is shown in Table 2.3.

2.10 Binary Background

Originally, computers were just a bunch of switches, therefore, they only had two positions: on and off. This also has the benefit that there is a large amount of noise immunity. A repeater (buffer) can eliminate by recreating the original signal without noise. These are all great benefits of the binary system.

2.11 Assignment

There is a numbers quiz on Canvas as the assignment for this lab.

Gray Code
0000
0001
0011
0010
0110
0111
0101
0100
1100
1101
1111
1110
1010
1011
1001
1000

Table 2.3: This table shows 4-bit Gray codes with horizontal lines showing the break for 2- and 3-bit Gray codes.

Chapter 3

Boolean Logic

3.1 Introduction

This chapter introduces some basic Boolean logic including gates and Boolean algebra.

When can you drive through an intersection? When the light is NOT red. This is the first and simplest logic operator—the NOT element. It simply changes any TRUE to FALSE or FALSE to TRUE (you can substitute 1 for TRUE and 0 for FALSE, or on/off).

How do you start a car? In most of the cars I have driven I have to press on the brake at the same time as I turn the key. To say it another way, the car starts when I press the break AND turn the key.

$$pressBreak \text{ AND } turnKey = startedCar \quad (3.1)$$

Again on a car, a particular blinker light will turn on if you turn on the turn signal or if you turn on the 4-way blinker.

$$turnSignal \text{ OR } 4wayBlinker = blinking \quad (3.2)$$

The AND and OR in the equation are Boolean operators.

3.2 Methods of Representing Logic

It is important to differentiate between different forms of representation because \overline{EN} means **active low** enable. It does not mean NOT(E AND N). The

understanding of which method is being used is usually derived from context. Using the dot (\cdot) everywhere can become burdensome, so when context makes it obvious (usually examples involving A, B, and C or X and Y) we may drop the dots and just use adjacency to represent the AND function.

3.3 Boolean Algebra

3.3.1 Theorems of Boolean Algebra

Ways to show NOT:

$$NOT(X) = \overline{X} = X' \quad (3.3a)$$

$$\overline{(\overline{X})} = (X')' = X \quad (3.3b)$$

Rules of AND and OR:

AND	OR	
$0 \cdot 0 = 0$	$1 + 1 = 1$	(3.4a)
$1 \cdot 1 = 1$	$0 + 0 = 0$	(3.4b)
$0 \cdot 1 = 1 \cdot 0 = 0$	$1 + 0 = 0 + 1 = 1$	(3.4c)

AND	OR	
$X \cdot 1 = X$	$X + 0 = X$	(3.5a)
$X \cdot 0 = 0$	$X + 1 = 1$	(3.5b)
$X \cdot X = X$	$X + X = X$	(3.5c)
$X \cdot \overline{X} = 0$	$X + \overline{X} = 1$	(3.5d)

For two and three variables you have the following useful equations:

AND	OR	
$X \cdot Y = Y \cdot X$	$X + Y = Y + X$	(3.6a)
$(X \cdot Y) \cdot Z = X \cdot (Y \cdot Z)$	$(X + Y) + Z = X + (Y + Z)$	(3.6b)
$(X + Y) \cdot (X + Z) = X + Y \cdot Z$	$X \cdot Y + X \cdot Z = X \cdot (Y + Z)$	(3.6c)
$X \cdot (X + Y) = X$	$X + X \cdot Y = X$	(3.6d)
$(X + Y) \cdot (X + \overline{Y}) = X$	$X \cdot Y + X \cdot \overline{Y} = X$	(3.6e)
$X \cdot (\overline{X} + Y) = X \cdot Y$	$X + \overline{X} \cdot Y = X + Y$	(3.6f)

$$X \cdot Y + \overline{X} \cdot Z + Y \cdot Z = X \cdot Y + \overline{X} \cdot Z \quad (3.6g)$$

$$(X + Y) \cdot (\overline{X} + Z) \cdot (Y + Z) = (X + Y) \cdot (\overline{X} + Z) \quad (3.6h)$$

A very important pair of equations are DeMorgan's theorems which allow us to switch between sums of products and products of sums.

$$\overline{(X_1 \cdot X_2 \cdot \dots \cdot X_n)} = \overline{X_1} + \overline{X_2} + \dots + \overline{X_n} \quad (3.7a)$$

$$\overline{(X_1 + X_2 + \dots + X_n)} = \overline{X_1} \cdot \overline{X_2} \cdot \dots \cdot \overline{X_n} \quad (3.7b)$$

The following are very important to remember:

$$\overline{A} \cdot \overline{B} \neq \overline{AB} \quad (3.8a)$$

$$\overline{A} + \overline{B} \neq \overline{A + B} \quad (3.8b)$$

3.4 Logic Gates and Truth Tables

It is important to be able to transform between equation, diagrams/circuits, and truth tables.

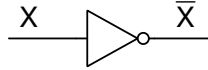


Figure 3.1: The NOT gate, also called an inverter, outputs NOT(A).

A	X
0	1
1	0

Table 3.1: This is the truth table for a NOT gate.

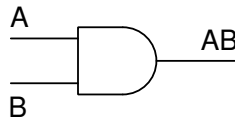


Figure 3.2: The AND gate outputs A AND B.

A	B	X
0	0	0
0	1	0
1	0	0
1	1	1

Table 3.2: This is the truth table for an AND gate.

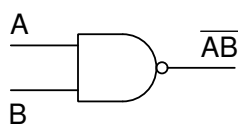


Figure 3.3: The NAND gate outputs NOT(A AND B).

A	B	X
0	0	1
0	1	1
1	0	1
1	1	0

Table 3.3: This is the truth table for an XOR gate.

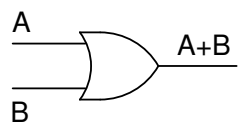


Figure 3.4: The OR gate outputs A OR B.

A	B	X
0	0	0
0	1	1
1	0	1
1	1	1

Table 3.4: This is the truth table for an OR gate.

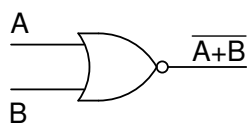


Figure 3.5: The NOR gate outputs NOT(A OR B).

A	B	X
0	0	1
0	1	0
1	0	0
1	1	0

Table 3.5: This is the truth table for an NOR gate.

Chapter 4

Arduino Startup

4.1 Introduction

This chapter gives the students an introduction to the hardware we are using and gets them started with the Arduino IDE.

4.2 Datasheets

4.2.1 Arduino Nano Connect RP2040

The data sheet for the Arduino Nano Connect RP2040 is located at <https://docs.arduino.cc/resources/datasheets/ABX00053-datasheet.pdf>.

The main website for it is at

<https://docs.arduino.cc/hardware/nano-rp2040-connect>

The pinout is at

https://content.arduino.cc/assets/Pinout_NanoRP2040_latest.png.

4.2.2 RP2040 Microcontroller

The RP2040 microcontroller datasheet (all 654 pages) is at <https://datasheets.raspberrypi.com/rp2040/rp2040-datasheet.pdf>.

If you are ever interested in putting the microcontroller onto a circuit board yourself, there is a reference design at

<https://datasheets.raspberrypi.com/rp2040/hardware-design-with-rp2040.pdf>.

4.2.3 IMU - ST LSM6DSOXTR

The IMU datasheet is at

<https://www.st.com/resource/en/datasheet/lsm6dsox.pdf>

4.2.4 Mic - ST MP34DT06JTR

The microphone datasheet is at

<https://www.st.com/resource/en/datasheet/mp34dt06j.pdf>

The [overview page](#) shows that the microphone is still actively being produced.

4.2.5 WiFi and Bluetooth - U-blox® Nina W102

The main page for the wireless unit is at

<https://www.u-blox.com/en/product/nina-w10-series-open-cpu>.

The datasheet is at

https://www.u-blox.com/sites/default/files/NINA-W10_DataSheet_UBX-17065507.pdf.

4.2.6 Cryptographic IC - Microchip® ATECC608A

Note that Microchip [doesn't suggest using this chip in new designs](#) so expect that some future versions of the Nano RP2040 Connect to use the successor ([ATTECC608B](#)).

The datasheet for the A is here:

<https://ww1.microchip.com/downloads/en/DeviceDoc/ATECC608A-CryptoAuthentication-Device-Summary-Data-Sheet-DS40001977B.pdf>.

Note that it says it is a summary datasheet. You have to sign an NDA with Microchip to see the full datasheet.

4.3 Installing the IDE

These directions assume that you are using the lab computers and One Drive.

1. Go to software download page: <https://www.arduino.cc/en/software>
2. Download the Windows ZIP file (not the first link or the app)

3. Open the zip file and copy the folder inside (arduino-1.8.19 as of this writing) into your One Drive folder. This may take a while. If you are on your own computer, you can use any of the programs.
4. Once that transfer finishes, go into the folder and run arduino.exe. Windows will try to save you, but if you click More Info you can click Run Anyway.
5. Windows Defender Firewall will also complain. Uncheck the box that is checked and/or click Cancel.
6. It should load up with a window that looks like Figure 4.1.
7. In order to get it to connect correctly to your board, you need to install the Arduino Nano Connect RP2040 board.
 - (a) Navigate to Tools→Board: “Arduino Uno” (or similar)→Boards Manager
 - (b) It should load as shown in Figure 4.2.
 - (c) In the search bar, type “arduino nano connect” (without the quotes)
 - (d) The first item should be Arduino Mbed OS Nano Boards and should list the Arduino Nano RP2040 Connect.
 - (e) Move your cursor over it and it should show an Install button. Click it to install the board library.
 - (f) Wait for it to finish.
 - (g) While you are waiting, plug your Nano Connect into your computer and let it install it.
 - (h) As it finished, I received a User Account Control warning asking if I wanted to let dpinst-amd64.exe make changes to my device. I said yes.
 - (i) Next it asked me if I wanted to install Arduino Universal Serial Bus devices. Again, click to Install.
 - (j) It popped up again and I clicked Install again. Now it should say that the Arduino Mbed OS Nano Boards has been installed.
 - (k) Close the Boards Manager.

8. Now go to Files→Examples→01.Basics→Blink.
9. This will open another window with the Blink program.
10. Go to Tools→Board→Arduino Mbed OS Nano Boards and select the Arduino Nano RP2040 Connect
11. Go to Tools→Port and select the COM that isn't COM1 (mine showed up as COM5)
12. Click the right arrow under the word edit in the menu to Upload the sketch to the Arduino board.
13. It should say "Compiling sketch..." in the lower left and show a progress bar on the lower right.
14. Then it should switch to Uploading... and finally Done Uploading.
15. An orange light near the USB port on your board should be blinking.
16. Congratulations! You have programmed your board!
17. Now look in the program for the two delay statements. Try changing the values inside the parentheses and re-uploading it. Does the blinking change?
18. In order to save files and have it portable, you need to change the directory where the Arduino IDE stores its sketchbooks
 - (a) Go to File→Preferences
 - (b) Change the Sketchbook location to your OneDrive and a folder named arduino (lowercase is good)
 - (c) My OneDrive was in
C:\Users\mcneils2\OneDrive - Embry-Riddle Aeronautical University\arduino
19. Now try saving the blink sketch with your changed values.
20. Demonstrate your working blink and its storage location to your instructor/TA
21. Here are some other Examples to test:

- (a) Basics → fade: change the variable led to be LED_BUILTIN, watch the red/orange LED pulse
- (b) Analog → AnalogInOutSerial: change analogInPin to A1 and analogOutPin to LED_BUILTIN. Turn the potentiometer (R6) with a screwdriver and watch the LED change accordingly. If you press the magnifying glass button in the top right the actual values will scroll by. You may need to set the baud rate to 9600.
- (c) Digital → DigitalInputPullup: Change the first pinMode call to use 9 instead of 2. The same for the digitalWrite command (2→9). Press the left button and see the LED blink. The right button is pin 10. Note that this program isn't written as well as the others since you have to change a number in two places. Could you rewrite it better?

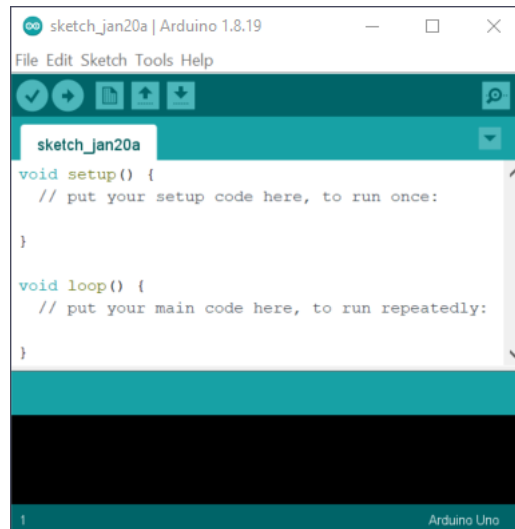


Figure 4.1: This is what the Arduino IDE should load up to.



Figure 4.2: This what the Boards Manager loads up to.

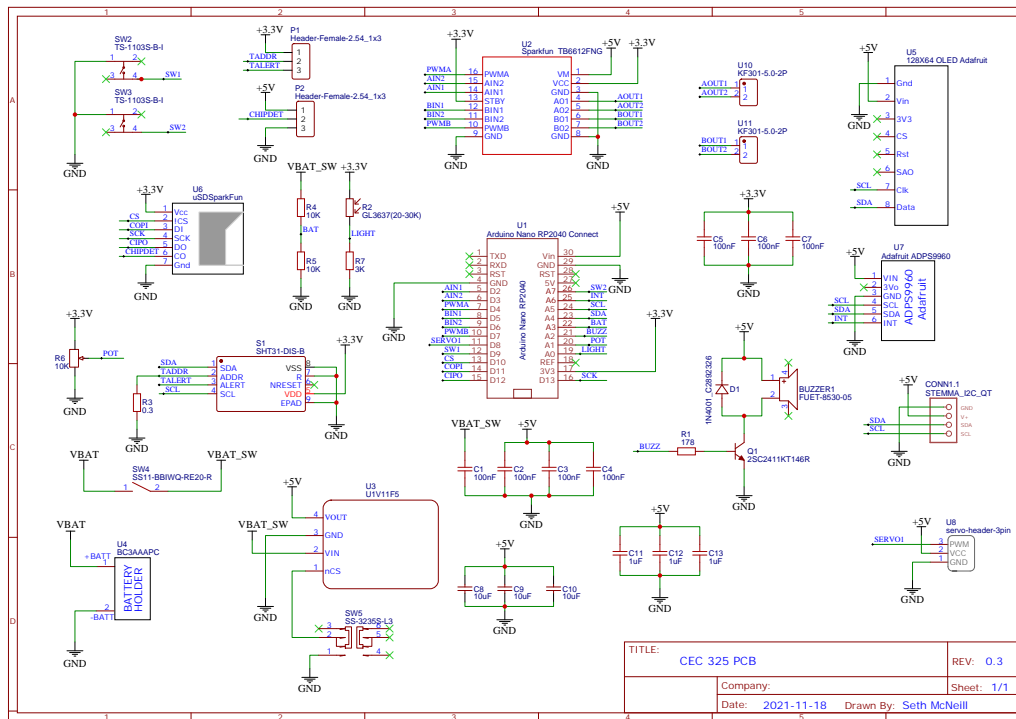


Figure 4.3: This is the schematic of version 0.3 of the board. This is the board used in Spring 2022.

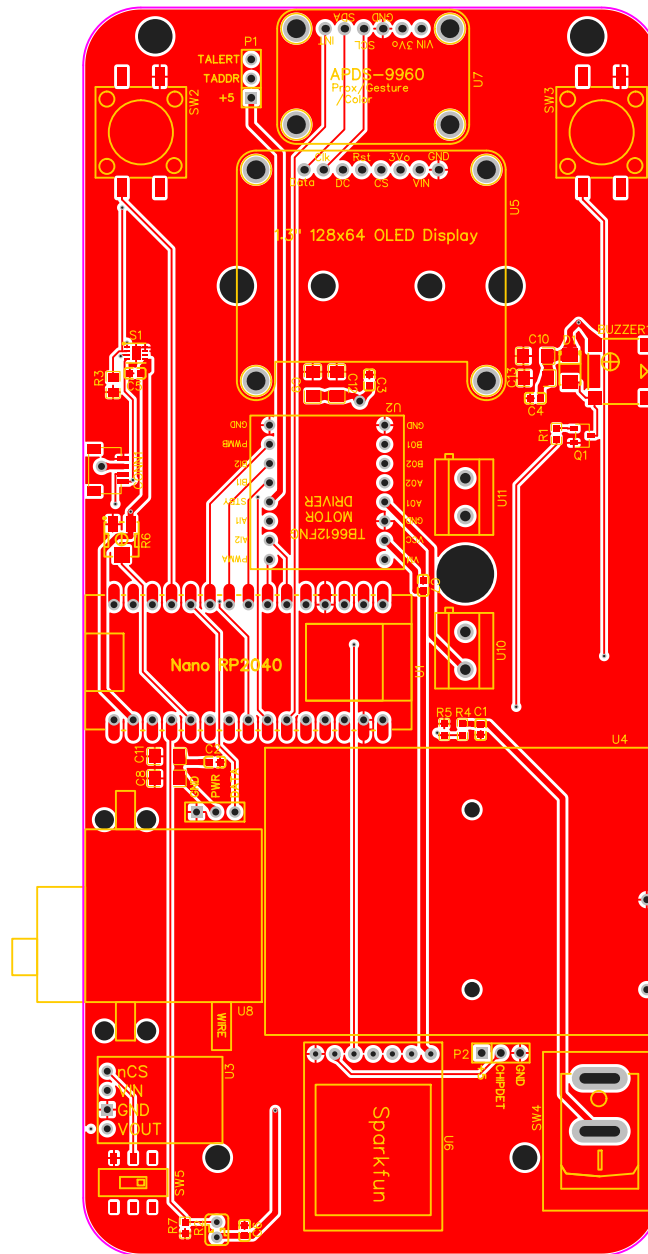


Figure 4.4: This shows the top of version 0.3 of the board for this class to help locate components.

Chapter 5

Buttons and Serial Communications

5.1 Introduction

This chapter introduces students to using buttons and serial communications.

5.2 Buttons

A typical button circuit is shown in Figure 5.1. The input is high until the button is pressed. Unfortunately, being mechanical, buttons do not always create nice, clean switched inputs as is shown in Figure 5.2. Maxim Integrated has a [nice paper](#) on the topic advertizing their devices to solve the problem. However, if we don't have the option of adding their hardware, some work can be done in software to debounce an input. As Maxim mentions, software debouncing is not free. It does incur some overhead so you probably do not want to do it for many inputs. An example of software debouncing is in Listing 5.1.

```
/*
```

```
Debounce
```

```
Each time the input pin goes from LOW to HIGH (e.g.  
because of a push-button  
press), the output pin is toggled from LOW to HIGH  
or HIGH to LOW. There's a
```

minimum delay between toggles to debounce the circuit (i.e. to ignore noise).

The circuit:

- LED attached from pin 13 to ground through 220 ohm resistor*
- pushbutton attached from pin 2 to +5V*
- 10 kilohm resistor attached from pin 2 to ground*
- Note: On most Arduino boards, there is already an LED on the board connected to pin 13, so you don't need any extra components for this example.*

*created 21 Nov 2006
by David A. Mellis
modified 30 Aug 2011
by Limor Fried
modified 28 Dec 2012
by Mike Walters
modified 30 Aug 2016
by Arturo Guadalupi*

This example code is in the public domain.

*<https://www.arduino.cc/en/Tutorial/BuiltInExamples/Debounce>
/

*// constants won't change. They're used here to set
pin numbers:
const int buttonPin = 9; // the number of the
pushbutton pin
const int ledPin = 13; // the number of the LED
pin

// Variables will change:*

```
int ledState = LOW;           // the current state of
    the output pin
int buttonState;              // the current reading
    from the input pin
int lastButtonState = LOW;    // the previous reading
    from the input pin

// the following variables are unsigned longs
// because the time, measured in
// milliseconds, will quickly become a bigger number
// than can be stored in an int.
unsigned long lastDebounceTime = 0; // the last
    time the output pin was toggled
unsigned long debounceDelay = 50;    // the debounce
    time; increase if the output flickers

void setup() {
  Serial.begin(115200);
  while(!Serial) delay(10);
  Serial.println("Starting...");

  pinMode(buttonPin, INPUT);
  pinMode(ledPin, OUTPUT);

  // set initial LED state
  digitalWrite(ledPin, ledState);
}

void loop() {
  // read the state of the switch into a local
  // variable:
  int reading = digitalRead(buttonPin);

  // check to see if you just pressed the button
  // (i.e. the input went from LOW to HIGH), and you'
  // ve waited long enough
  // since the last press to ignore any noise:
```

```
// If the switch changed, due to noise or pressing:
if (reading != lastButtonState) {
    // reset the debouncing timer
    lastDebounceTime = millis();
}

if ((millis() - lastDebounceTime) > debounceDelay) {
    // whatever the reading is at, it's been there for
longer than the debounce
    // delay, so take it as the actual current state:

    // if the button state has changed:
    if (reading != buttonState) {
        buttonState = reading;

        // only toggle the LED if the new button state is
        HIGH
        if (buttonState == HIGH) {
            ledState = !ledState;
        }
    }
}

// set the LED:
digitalWrite(ledPin, ledState);

// save the reading. Next time through the loop, it'
ll be the lastButtonState:
lastButtonState = reading;
}
```

Listing 5.1: This is the Arduino example of software debouncing.

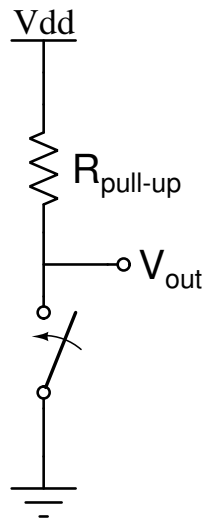


Figure 5.1: This is a typical button input circuit. It is active low in that the output signal will be high until the button is pressed.

5.3 Serial Communications

Serial communications sends data one bit at a time from one device to another as shown in Figure 5.3. This is in contrast to parallel communications where multiple bits (8 in the example) are transferred simultaneously between devices as shown in Figure 5.4. As can be seen parallel communications is much faster than serial since you can send so many bits simultaneously. However, parallel requires many more pins on each device to communicate. This is challenging in the embedded systems world since most microcontrollers don't have many pins. Also, connectors with many pins tend to fail more often than connectors with fewer pins. Because of these reasons, the embedded world communicates primarily with serial protocols.

A table of serial protocols is listed in Table 5.1.

5.3.1 Universal Asynchronous Receiver-Transmitter

The Universal Asynchronous Receiver-Transmitter (UART) protocol has been around quite a while. Older computers used to ship with serial ports that used this protocol, usually implemented as the RS-232 protocol. UARTs are used to communicate between two devices. It does not allow for more than

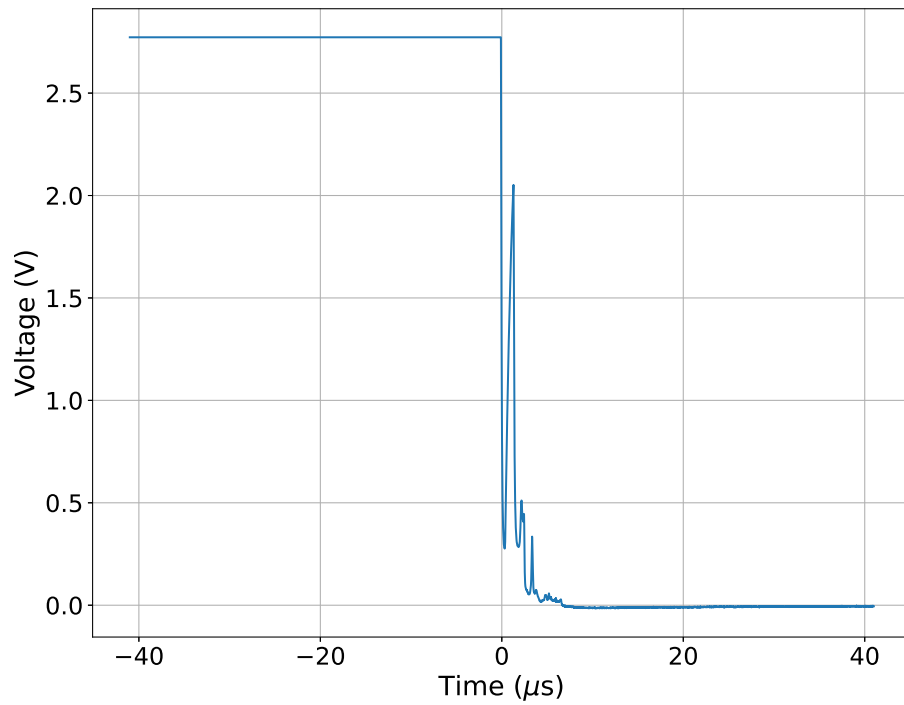


Figure 5.2: This is an example of what the output signal from a button with the circuit in Figure 5.1 could look like.

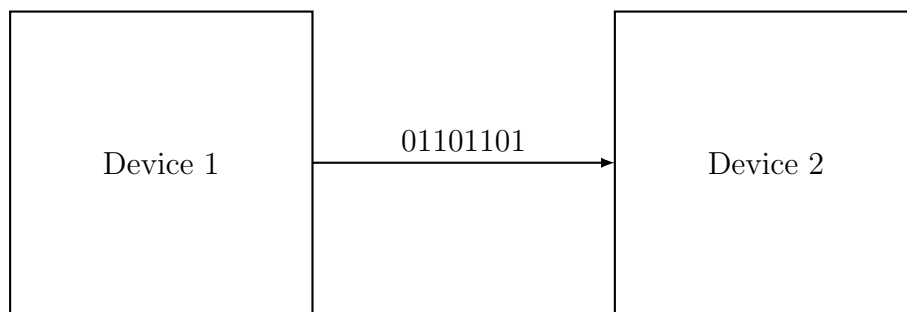


Figure 5.3: Serial transfers one bit at a time.

two devices. It is full duplex and communicates over 2 wires (plus a ground for reference). One wire transmits data from Device 1 to Device 2 and is

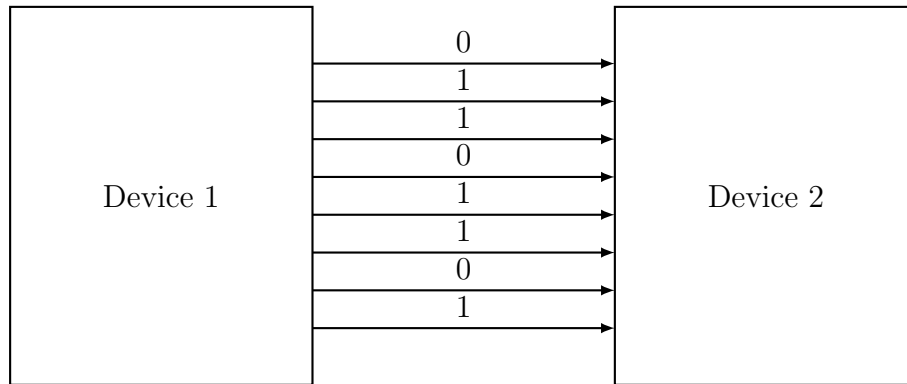


Figure 5.4: Parallel transfers multiple bits at a time.

Protocol	Description
UART	Used to communicate between computers and Arduino boards
SPI	Used for higher speed communications between devices on circuit boards
I ² C	Only uses two wires and allows for multiple controllers and peripherals
<i>CAN</i>	<i>Often used in the automotive industry</i>
<i>RS-485</i>	<i>Differential signaling for robustness (noisy and long wires)</i>
<i>1-Wire</i>	<i>Only requires 1 wire and ground (no power) to communicate</i>
<i>USB</i>	<i>Ubiquitous on computers now</i>

Table 5.1: This is a list of some of the more common serial protocols. The grayed out protocols will not be discussed further.

connected to Device 1's TX pin and Device 2's RX pin. The second wire transmits data from Device 2 to Device 1 and is connected to Device 1's RX pin and Device 2's TX pin. This is illustrated in Figure 5.5. This protocol does require both devices to use the same specified transmission speed. Some common speeds are 9600, 14,400, 57,600, and 115,200. It can go faster. Nowadays, it is generally best to go as fast as possible so that the communications takes less of the processor's time. The most common speed used now seems to be 115,200. The asynchronous part of the name comes from the fact that there is no clock line for UARTs. It typically has a maximum speed of 1.5 megabits per second (Mbps).

UART is the protocol used to communicate between the computer and your Arduino board. You can see this in the code in the setup function where `Serial.begin(115200)` or `Serial.begin(9600)` shows up often.

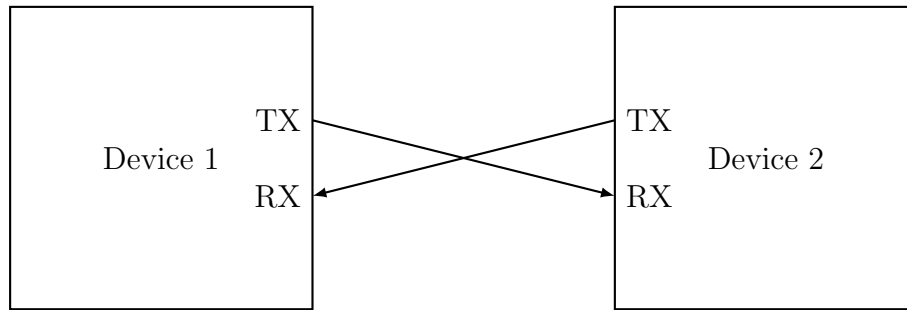


Figure 5.5: A UART has full duplex between two entities.

5.3.2 Serial Peripheral Interface

The Serial Peripheral Interface (SPI) is a full-duplex serial interface shown in Figure 5.6. It is setup in a controller-peripheral (previously known as master-slave) architecture with only one controller on the bus. It does allow for multiple peripherals by giving each peripheral its own chip select (CS) line. Since it is synchronous, it does require a clock line. This means that it takes a minimum of 4 wires as listed in Table 5.2. The SCLK signal is the clock signal used by both the controller and peripheral. There is one CS line per peripheral. The CS line lets the controller specify which peripheral it is communicating with. The COPI line is the data going from the controller to the peripheral. The CIPO line is the data going from the peripheral to the controller.

SPI has a maximum data rate of 60 Mbps, which is the fastest of the 3 protocols commonly used in the embedded world. Because of this, it is used in more data intense situations like SD Cards (where we will be using it) and displays.

Signal	Description
SCLK	Clock signal to keep everything synchronized
CS	Chip select—tells a peripheral that the controller is communicating with it
COPI	Controller Out, Peripheral In (used to be MOSI)
CIPO	Controller In, Peripheral Out (used to be MISO)

Table 5.2: The SPI protocol uses these signals to connect.

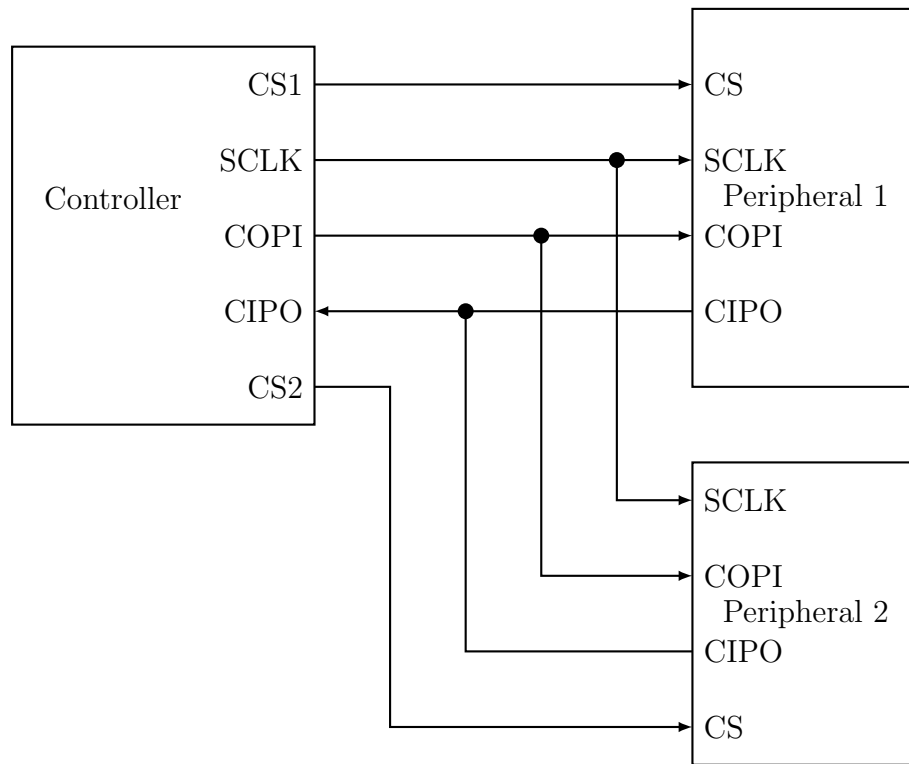


Figure 5.6: SPI allows for one (sometime more) controller and multiple peripherals.

5.3.3 Inter-Integrated Circuit

The Inter-Integrated Circuit (I²C, IIC, or I2C) protocol is multi-controller and multi-peripheral. Basically, any device connected to the bus can drive the communication. It is single ended so data only flows one way at a time. It only requires 3 wires, SCL - clock, SDA - Data, and a ground reference. SCL and SDA do require pull-up resistors so that devices only have to pull the lines to ground to communicate as shown in Figure 5.7. Instead of using chip select lines like SPI, I2C requires each peripheral to have a unique address. I2C addresses for modules that are on the board or may be used with the board can be seen in Table 5.3. I2C has a max speed of 3.4 Mbps but is only 100 kbps in standard mode.

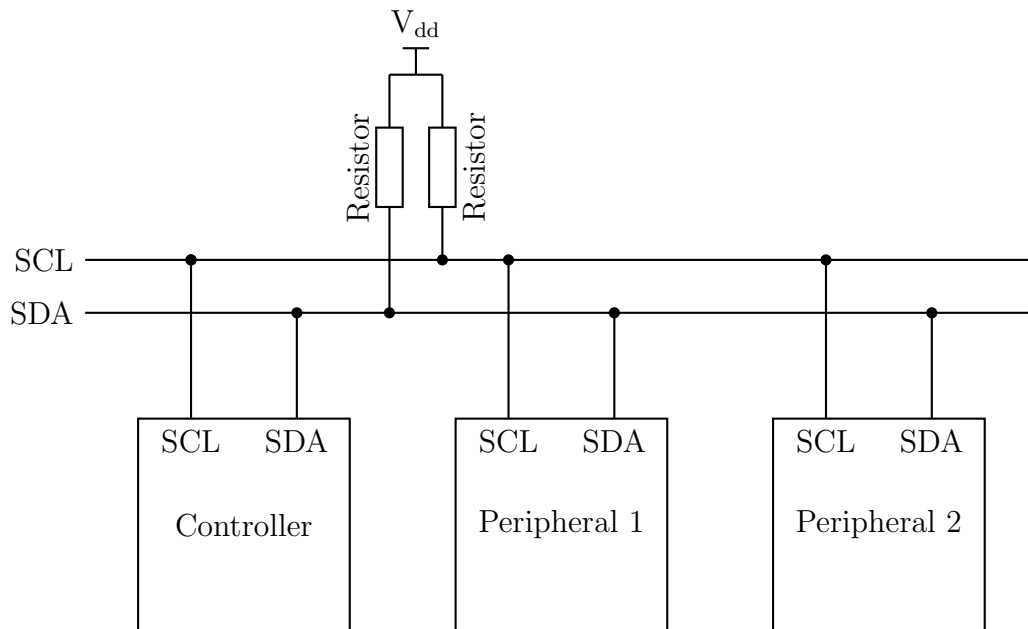


Figure 5.7: I²C allows for multiple controllers and peripherals on the same bus.

Address (HEX)	Module
0x44 or 0x45	SHT31-DIS Temperature/Humidity
0x3D	1.3" 128x64 OLED Display
0x39	APDS-9960 Light, Color, Proximity, Gesture
0x77	BME688 Temperature, Humidity, Gas
0x2D, 0x53, and 0x57	ST25DV16 Dynamic NFC/RFID Tag IC
0x30 or other	NeoKey 1x4 QT breakout board
0x10	STEMMA MiniGPS
0x6A or 0x6B	LSM6DSOX IMU on the Nano Connect
0x60	ATECC608A Cryptographic on the Nano Connect

Table 5.3: I2C addresses for relevant modules.

5.4 In Case of Upload Lock-up or Failure

If the Arduino IDE is having trouble uploading to the Arduino Nano RP2040 Connect, try double pressing (not too fast) the reset button on the Nano once the IDE starts trying to upload.

5.5 Arduino Programming Suggestions

In general, try to start from an existing set of code (an example for instance) when working on something. For example, if you need to use the APDS-9960, load one of the examples from the library, then modify it until it does what you want. Once you have written a few sketches, you might write a generic starting point for your subsequent sketches.

5.6 Arduino Button Setup

An example of how to setup the buttons on the CEC 325 board. Some important details to note is that the left button is attached to pin D9 (referred to as 9 in the Arduino infrastructure) which is attached to the RP2040 on the Arduino Nano RP2040 Connect module. The RP2040 has internal pull-up resistors that are tied correctly to the Arduino IDE so that the pins can be setup using `pinMode(LEFT_BUTTON_PIN, INPUT_PULLUP);` and do not require an external pull-up resistor. The right button is attached to pin A7 on the module which is routed to the Wi-FiNINA module. This module's internal pull-up is not implemented in the Arduino IDE (as of 2022 February 03). Therefore, it needs an external pull-up AND requires the sketch to include "Wi-FiNINA.h" AND the pin variable HAS to be declared using `#define` rather than a `const int`.

```
/* button_demo.ino
 *
 * Gives an example of how to use the buttons on
 * the CEC 325 board.
 *
 * Seth McNeill
 * 2022 February 03
 */

#include "Wi-FiNINA.h" // for A4-A7 and wifi/bluetooth

#define LEFT_BUTTON_PIN 9 // This input is on the
    RP2040 and has builtin pullup that works
#define RIGHT_BUTTON_PIN A7 // This input is on the
    Wi-FiNINA and doesn't have working internal pullup
```

```
void setup() {
  Serial.begin(115200);
  //while(!Serial) delay(10);
  delay(2000);

  Serial.println("Starting...");

  pinMode(LEFT_BUTTON_PIN, INPUT_PULLUP);
  pinMode(RIGHT_BUTTON_PIN, INPUT);
  pinMode(LED_BUILTIN, OUTPUT);
}

void loop() {
  // note that the buttons read 1 (HIGH or true) when
  not pressed
  if(!digitalRead(LEFT_BUTTON_PIN)) {
    Serial.println("Left button pushed");
  }
  if(!digitalRead(RIGHT_BUTTON_PIN)) {
    Serial.println("Right button pushed");
  }
  delay(100); // keeps the loop from running too fast
             with nothing pushed
}
```

Listing 5.2: This is an example of how to setup the buttons on the CEC 325 board.

5.7 Arduino Serial Setup

The serial port has to be setup in the `setup()` function in the Arduino IDE. An example of setting it up is shown in Listing 5.3.

```
void setup() {
  Serial.begin(115200); // starts the serial
                      connection at 115200 data (baud) rate
}
```

```
// If you are attached to a computer (not a robot on  
battery power  
while(!Serial) delay(10); // wait for serial to  
start  
// delay(2000); // if might be on battery, just  
wait a bit for it to start  
Serial.println("Starting...");  
  
}  
  
void loop() {  
  Serial.println("This has a new line character at the  
    end");  
  Serial.print("This does not have a new line at the  
    end: ");  
  Serial.println(millis());  
  delay(5000);  
}
```

Listing 5.3: This is an example of how to start the serial port at 112,500 in the Arduino system.

I strongly suggest having the `setup()` function output to the serial port right after the serial port is started so that you can know that your board has booted. Note that if you do not have a serial port (your robot is running off of batteries so that it is not plugged into a computer) you need to remove the `while(!Serial) delay(10)` line and replace it with some sort of timeout function. A `delay(2000)` is usually sufficient to allow the serial to start if it exists but not hang if it doesn't. There are more complicated ways to do this, but that will be left as an exercise for the reader.

5.8 Laboratory Exercises

5.8.1 Button to Serial

Create a sketch that prints to the serial port at 115,200 each time a button is pressed. The message should indicate which button is pressed. Both buttons should work on your board. Don't forget that the right button (A7) requires

WiFiNINA.h to be included and the pin designation to be a `#define` not a `const int`. The error messages are pretty helpful on this.

5.8.2 Tones

Create a sketch that plays a short tune when one of the buttons is pressed. There are examples of using the `tone` function in Examples → 02.Digital. The buzzer is attached to pin A2 on the Arduino Nano RP2040 Connect.

5.8.3 APDS-9960

Create a sketch that prints the distance and color to the serial port once a second. In order to get the APDS-9960 working, you will need to install a library for it. Arduino, Adafruit, and Sparkfun all have libraries available in the library manager. I have been using the Arduino one. Once you install the library, a new folder on the Examples menu should show up. Look through the examples to get an idea how to do this.

5.8.4 Distance to Tone

Create a sketch that plays an increasing tone as the APDS-9960's distance measurement decreases. It should play no tone if there is nothing nearby (sensor reading 255 from the Arduino library).

5.8.5 Color Recognition

Create a sketch that plays a tone or turns on a light (LED) when a specific color is seen by the APDS-9960. My playing with the color readings is that it is not very precise. It is probably best to choose colors and just react to redder colors or something down that line.

5.8.6 SHT31

Install the Adafruit SHT31 library and run it to see the temperature and humidity.

5.8.7 Turn In

After demonstrating each sketch to the instructor, submit a copy of all the sketches compiled into a single PDF to Canvas. Also, submit the sketch files. Be sure that each sketch has the following header:

```
/* sketch_name.ino
 *
 * A description of what the sketch does
 * and the inputs/outputs it needs.
 *
 * All authors' names (if working with a
 * partner be sure to include both your names)
 * CEC 326 (or other class name)
 * Today's date in the format YYYY mmmmm dd
 * as in 2022 February 03
 */
```

Chapter 6

Displays

6.1 Introduction

Adding a display to a device allows much more information to be shared from the device to the user than just using LEDs or buzzers. There are several types of displays that are commonly used in the embedded systems world.

6.1.1 LCD

The most common is a Liquid Crystal Display (LCD). Most of the computer monitors and computers are LCD. This technology gives good contrast, fast response (which gamers like), and minimal burn in. Old CRT displays had to have screensavers so that whatever was usually showing on the display wouldn't be there permanently. Thankfully modern displays don't typically have this problem. LCDs do require a backlight. This determines how bright the colors are. The pixels in the display just modulate how much of the backlight is showing.

At times you will find TFT displays. This stands for thin-film-transistor liquid-crystal display. They are a better version of LCD.

6.1.2 eInk

eInk displays are also available for embedded systems. Kindles are probably the most popular commercial product using eInk type displays. These displays are of particular interest because they keep their display even when the

power is turned off. This allows for very low power operations. The downsides are that they work off of reflected light so require special backlighting to be viewed at night and that they are very slow. A small display may take a second to refresh and some recommend not to update them more than once every few minutes if possible.

6.1.3 OLED

The display in this class is based on Organic Light Emitting Diodes (OLED). The cool part about this technology is that instead of each pixel blocking the backlight to make the display like in LCDs, in OLED displays each pixel is an LED that emits light. This makes OLED displays very bright with very good contrast ratios. They also have fast response times. The particular OLED display we are using in the class will get dimmer with time. [Adafruit notes](#) that it becomes noticeable after about 1000 hours of being on. This is 41.7 days, so after a year of continuous use, an OLED display might not be very bright.

6.2 Pixel Layout

The layout of pixels on a display can be thought of as a cartesian coordinate system with a couple minor differences. First, pixels take up space, so the indexing is between the lines rather than on the lines. Second, the +Y axis points downward as shown in [Figure 6.1](#). The units for the coordinates is always pixels and the coordinates are always integers.

Pixels can vary in size. This is important to keep in mind if you are trying to display something with a specific size. Pixel size varies from display to display so read carefully if you want something to display a specific size.

6.3 Using the Display

The display on the lab board is a 1.3" monochrome display 128 pixels wide and 64 pixels high. Since it is monochrome 1 represents white and 0 black for a pixel colors. Two libraries are required to use it:

1. `Adafruit_GFX.h` - this is the generic graphics library

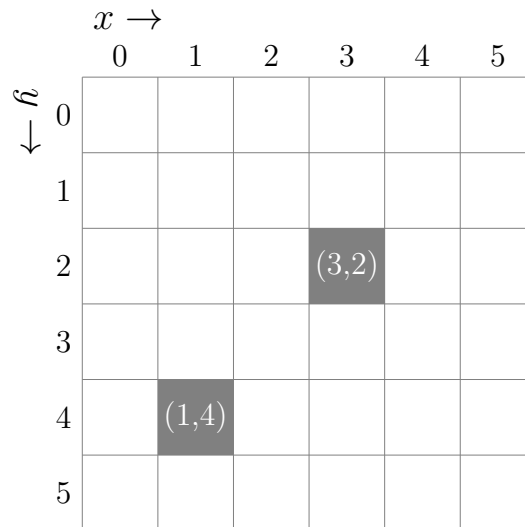


Figure 6.1: Pixels in a display occupy space and are referenced to the top left corner with the positive Y axis going down.

2. `Adafruit_SSD1306.h` - this is specific to our display

An example that shows much of the available functionality can be found (once the libraries are installed) at Examples \rightarrow Adafruit SSD1306 \rightarrow 128x64 I2C. The following have to be defined to use a display:

1. Width - how many pixels wide the display is
2. Height - how many pixels high the display is
3. I2C address - what address the I2C display is accessed at
4. Reset pin - not attached to anything on our board so use -1
5. I2C interface - which I2C interface to communicate over. In our case we only use one, but there are situations where you use more than one I2C interface.

An example of creating a display instance is as follows:

```
Adafruit_SSD1306 display(SCREEN_WIDTH, SCREEN_HEIGHT, &Wire
, OLED_RESET);
```

Some useful methods that can be called on the display object are:

1. `clearDisplay` - clears everything to black
2. `display` - show whatever has been queued up in the buffer
3. `setTextSize` - sets the size of the text (usually 1 or 2)
4. `setTextColor` - set what color the text should
5. `print/println` - these act the same as they do when using `Serial`
6. `drawBitmap` - draws a bitmap stored using `PROGMEM`. It requires the following arguments
 - (a) `xpos` - the x position for the image
 - (b) `ypos` - the y position for the image
 - (c) `bitmap variable` - the variables with the actual image
 - (d) `width` - image width in pixels
 - (e) `height` - image height in pixels
 - (f) `color` - color for the nonzero pixels in the image
7. more can be [found here](#).
8. Functions specific to our display can be [found here](#).

The colors for our display are `SSD1306_WHITE` and `SSD1306_BLACK`. Note that text normally wraps if it is too long for the current line.

6.4 Lab Exercise

6.4.1 To Do

This is an implementation of the display homework. Below is the modified version for lab with some additions so read carefully.

Based on the Example `ssd1306_128x64_i2c` and the button programs you have already written, write a program for the CEC 326 board that does the following:

1. Displays a custom (written by you) set of text for 2 seconds indicating the start of the program

2. Moves a custom BMP left with the left button and right with the right button. You can base this off of the `testanimate` function.
3. Once you have that working, switch your custom message on boot from [1](#) to display the current temperature and humidity from the SHT31. I based my SHT31 code on the Adafruit SHT31 library.

Some thoughts about the process:

1. The example code has `testanimate` called inside `setup()`. Your function should be called from the loop function.
2. Note that the `testanimate` function has an infinite loop inside it. Your function should not have an infinite loop inside it.
3. Your code should have a proper header at the top
4. Don't forget to call `display.display()` to actually display something on the screen.
5. Have your bitmap start at the location `(display.width()/2, display.height()/2)`
6. Check to see if the bitmap has hit the edges of the screen using the `display.width()` and `display.height()` functions.
7. Approach this one step at a time.
8. Go back through and double check all your logic.
9. Ask if you have questions, but be sure to include a copy of the code you have so far.

6.4.2 Converting Images for Arduino

A website for converting images to a format that the Arduino system can use is at <http://javl.github.io/image2cpp/>. I used the following settings:

1. Canvas size: 16x16
2. Background color: Black
3. Invert image color: checked

4. Center horizontal and vertical
5. Arduino code, single bitmap
6. Horizontal - 1 bit per pixel
7. Change the name in the code from NaN to something useful.
8. reformatted it by adding new lines to make it fit nicely

6.4.3 Submit

1. Demonstrate your program running to the instructor.
2. Submit a PDF of your code on Canvas.

Chapter 7

Data Collection and Environmental Sensing

7.1 Introduction

This chapter introduces students to the concepts of collecting data in general and environmental data in particular.

7.2 Laboratory Exercises

7.2.1 To Do

For the lab, collect the following data and display it once a second on the display with the appropriate units if you can make them fit.

1. The output from `millis()` (ms)
2. Light intensity as a number between 0 and 1023 (unitless)
3. Potentiometer value as a voltage between 0 and 3.3 V
4. Battery voltage as a voltage between 0 and 6.6 V
5. Temperature in Fahrenheit
6. Relative humidity in %
7. Distance as a number (unitless)

8. Color as integers between 0 and 255 in the form (R,G,B) (unitless)
9. Accelerometer readings in g's (ax, ay, az) (g)
10. Gyroscope readings in degrees per second (gx, gy, gz) (dps)

7.2.2 Suggestions

Do the temperature and humidity last since the SHT31 sensor sometimes requires power cycling to get working after uploading code to the Nano Connect.

Use a `String` object to accumulate your display string and then call `display.println(yourString)` to display it. Note a few things:

1. The `String` type starts with a capital S.
2. You can add to the `String` object using `+=` or just `+`, but with only the plus operator, all arguments have to be of the same type.
3. The `String` object also allows you to limit the number of decimal places for `float` types.

An example is shown in Listing 7.1.

```
String dispStr;
dispStr = "T(F),H(%): ";
dispStr += String(tF,1);
dispStr += ",";
dispStr += String(humidity,1);
dispStr += "\n";
// Control the display
display.clearDisplay();
display.setTextSize(1); // Normal 1:1 pixel scale
display.setCursor(0,0); // Start at top-left corner
display.println(dispStr);
display.display();
```

Listing 7.1: This is an example of using a `String` object to display text and float variables. The floats are limited to 1 decimal place such that 7.123 would be displayed as 7.1.

7.2.3 Turn In

Submit a copy of your code and a video (or link to a video) of your board running your code. The video should include both lab partners faces.

Chapter 8

Inertial Measurements

8.1 Introduction

This chapter introduces students to using collecting inertial data such as linear and angular acceleration.

8.2 Rectilinear Kinematics

Rectilinear kinematics is about motion along a straight line. This provides a good starting point for discussing the mathematics of inertial measurements.

Time, position, velocity, and acceleration have the following differential relationships:

$$a = \frac{dv}{dt} \quad (8.1a)$$

$$v = \frac{ds}{dt} \quad (8.1b)$$

$$a \, ds = v \, dv \quad (8.1c)$$

If the acceleration is known (or can be assumed to be) constant, Equations [8.1](#) can be integrated to give Equations [8.2](#).

$$v = v_0 + a_c t \quad (8.2a)$$

$$s = s_0 + v_0 t + 0.5 a_c t^2 \quad (8.2b)$$

$$v^2 = v_0^2 + 2 a_c (s - s_0) \quad (8.2c)$$

Constant acceleration is usually applied to the kinematics of projectiles where the constant acceleration is due to gravity. In the case of a digital IMU, the acceleration measurement is reported periodically (at 104 Hz in the default case of the LSM6DSOXTR on the Nano RP2040 Connect). Since it is a sampled system, we cannot just integrate Equations 8.1 to get velocity and position. What we do instead is to assume constant acceleration between samples and run a cumulative sum to calculate the velocity and position.

Integrating also assumes the knowledge of initial conditions. Usually we start with an initial condition of being at rest. This simplifies our starting point. At each subsequent calculation, the output of the previous sample is taken as the initial condition. This is shown in Equations 8.3.

$$v[k] = v[k - 1] + a[k - 1]\Delta t \quad (8.3a)$$

$$s[k] = s[k - 1] + v[k - 1]\Delta t + 0.5a[k - 1](\Delta t)^2 \quad (8.3b)$$

As will become quite clear, this provides a noisy output with drift due to the two numeric integrations. There are several options for cleaning it up. One is to use trapezoidal rather than rectangular numeric integration. Another is to add some form of filtering to reduce the drift. Some options are a high pass filter on the acceleration and/or the velocity, Kalman filtering, or particle filtering.

8.3 Angle Measurement

Since earth's gravity provides a constant acceleration, detecting that constant allows a measurement of the angle between a device and it to determine the angle between. That is the basis for measuring the angle of a device using accelerometers. Since gyroscopes measure the rate of rotation, summing this angular speed over time will also give an estimate of angle. First, we will go over the basics of accelerometer angle measurement, then gyroscope angle measurement, and lastly, how to combine both measurements to correct the error each is prone to. A paper showing several of these techniques is [Using Inertial Sensors for Position and Orientation Estimation](#).

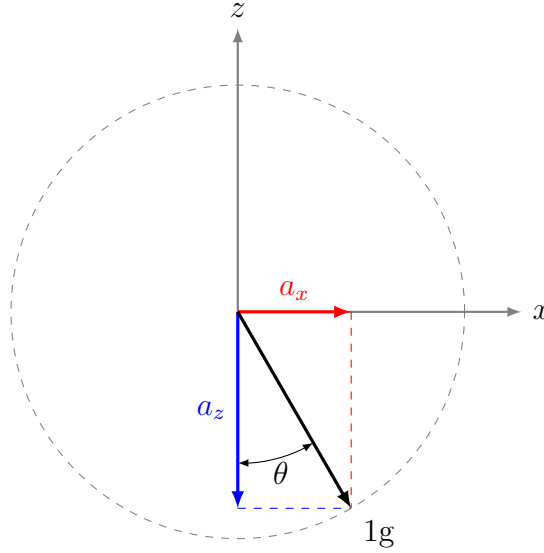


Figure 8.1: This shows the relative intensities of the accelerometer x and z (a_x and a_z respectively) measurements to the earth's gravity from the sensor frame of reference.

8.3.1 Accelerometer Angles

The problem is illustrated in Figure 8.1. In this case, we will take the x-axis as the horizontal axis and the z-axis is the vertical. We will assume that there are no external forces applied besides the force of gravity. This is faulty if the device is translating or otherwise not rotating about the IMU. However, we can still get some useful information even with this assumption. The vector sum of a_x and a_z add to a point on the unit (1 g) circle. Therefore, the angle can be calculated as shown in Equation 8.4.

$$\theta_a = \tan^{-1} \left(\frac{a_x}{a_z} \right) = \text{atan2}(a_x, a_z) \quad (8.4)$$

The atan2 function is provided in most languages. It is a “safe” version of \tan^{-1} that deals with zeros and signs of a_x and a_z correctly and cleanly. If the language you are use has it (which it does) then use it to prevent calculation problems. Note that Equation 8.4 is not time dependant and does not have any numerical integration. It provides a ground truth of the angle based on the assumptions at the beginning: no forces other than gravity and no noise.

Unfortunately, the output tends to have high frequency noise so you usually want to run the output through a low-pass filter.

8.3.2 Gyroscope Angles

Gyroscopes output angular velocity, ω , which when integrated can give the current angle relative to the starting angle. Since this system is sampled, instead of integration use a cumulative sum where each data point is based on the previous one. Equation 8.5 shows the mathematical approximation of the current angle based on the derivative of the angle θ with respect to time. This derivative is ω that is output by the gyroscope.

$$\theta(t + \Delta t) \approx \theta(t) + \frac{\partial}{\partial t}\theta(t)\Delta t \quad (8.5)$$

The actual implementation of Equation 8.5 is shown in Equation 8.6.

$$\theta_g[t] = \theta_g[t - 1] + \omega\Delta t \quad (8.6)$$

Since this calculation is based on integration it is susceptible to drift. The error in the output will increase over time. A way to fix this is to run the output through a high pass filter to block the low frequency drift.

8.3.3 Fusing Accelerometer and Gyroscope Angles

The errors in accelerometer angle measurement are complementary to those in the gyroscope angle estimates since the acceleration estimates need a low pass filter and the gyroscope estimates need a high pass filter. If the values are combined carefully we can take advantage of the best properties of both measurements and use them to correct the errors in the other measurements. A complementary filter as shown in Equation 8.7 works well for this.

$$\theta_{mixed}[t] = \alpha (\theta_{mixed}[t - 1] + \omega_{gyro}\Delta t) + (1 - \alpha) \text{atan2}(a_x, a_z) \quad (8.7)$$

As can be seen, if $\alpha = 0$, Equation 8.7 reduces to the accelerometer angle measurement and if $\alpha = 1$ it reduces to the gyroscope angle measurement. Choosing an α value between 0 and 1 gives a mixture of both results. Also, remember that the θ on the right side of Equation 8.7 is the previously calculated mixed θ , not the output from a separately calculated gyroscope

angle as one might be tempted to do. Choose α through tuning (guided trial and error) based on the specific system that is being implemented and problem needing to be solved. In one example, I found a value of $\alpha = 0.95$ worked well.

It is very important to keep the units from each function correct. The gyroscopes on the Arduino Nano Connect RP2040 output in degrees per second. The inverse tangent functions typically return values in radians.

8.4 Useful References

1. <https://stanford.edu/class/ee267/lectures/lecture9.pdf>
2. <https://stanford.edu/class/ee267/lectures/lecture10.pdf>
3. https://stanford.edu/class/ee267/notes/ee267_notes_imu.pdf