$$\eta^{\ell}(a) \xrightarrow{1} \eta^{\ell-1}(a) \xrightarrow{1} \eta(a) = aba \xrightarrow{1} \eta^{0}(a) = a \xrightarrow{1} e$$