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Q1) Wild West produced two types of cowboy hats. A type 1 hat req. 3 times as much labour time as a type 2. If the all labour time is ~~deducted~~ allocated to Type 2 alone, company can produce a total 450 Type 2 hats in a day. The market limits are 100 and 300 hats per day respectively. The profit \$8 and \$5 respectively. Determine the number of hats each day that would maximize profit.

- Build the mathematical model of the problem
- Solve the problem graphically.

	<u>Labor</u>	<u>Limit</u>	<u>Profit</u>	
Type 1	3t	100	\$8	450t is total labor
Type 2	t	300	\$5	

i) Math. Model

Decision Variable:

x_1 = Number of hats produced Type 1 per day

x_2 = Number of hats produced Type 2 per day.

Objective Function:

$$\text{maximize } Z = 8x_1 + 5x_2$$

st (constraints) 0

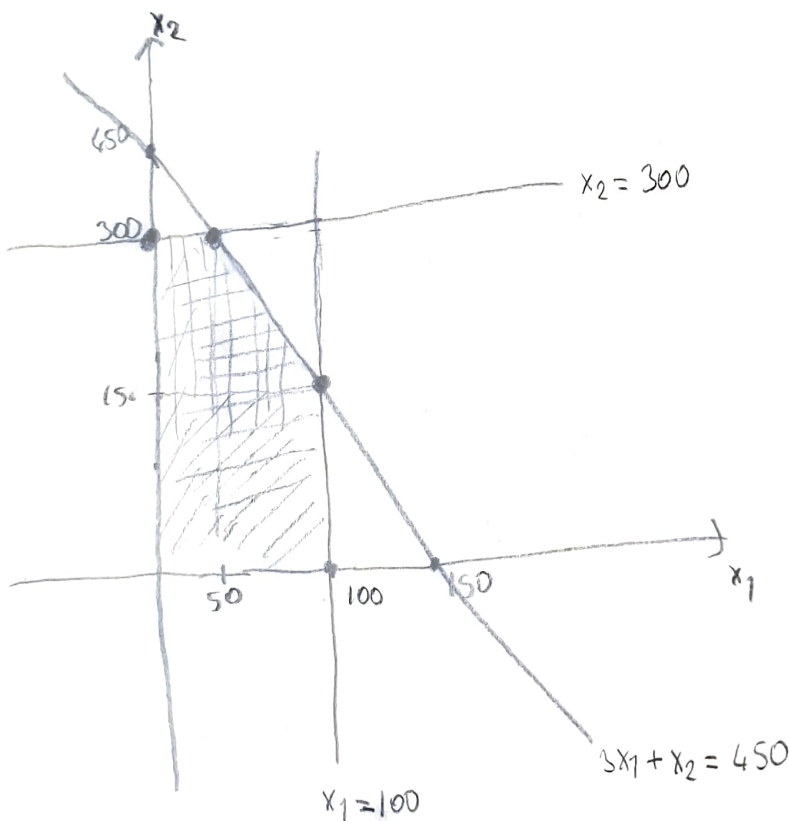
$$x_1 \leq 100$$

$$x_2 \leq 300$$

$$3x_1 + x_2 \leq 450$$

$$x_1, x_2 \in \mathbb{N}$$

ii) Graph



$$Z = 8x_1 + 5x_2$$

Solution 1 $\Rightarrow \underline{x_1 = 50}, \underline{x_2 = 300}, Z = 8 \cdot 50 + 5 \cdot 300 = \boxed{\$1900} \rightarrow \text{optimal}$

Solution 2 $\Rightarrow x_1 = 100, x_2 = 150, Z = 8 \cdot 100 + 5 \cdot 150 = \$1550 \rightarrow \text{feasible but not optimal}$

Solution 3 $\Rightarrow x_1 = 0, x_2 = 300, Z = 8 \cdot 0 + 5 \cdot 300 = \$1500 \rightarrow \text{feasible but not optimal}$