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a) let x be the number of Type 1 hats produced and y be the Type 2

Type 1 hats: $3y = x$

$x \leq 100$ and $y \leq 100$

Total profit is $P = 8x + 5y$

We want to maximize the profit so the constraints are:

Total labor time available is

$$3x + y = 450$$

$$\begin{aligned} x &\leq 100 \\ y &\leq 300 \\ x &\geq 0 \\ y &\geq 0 \\ 3x + y &= 450 \end{aligned}$$

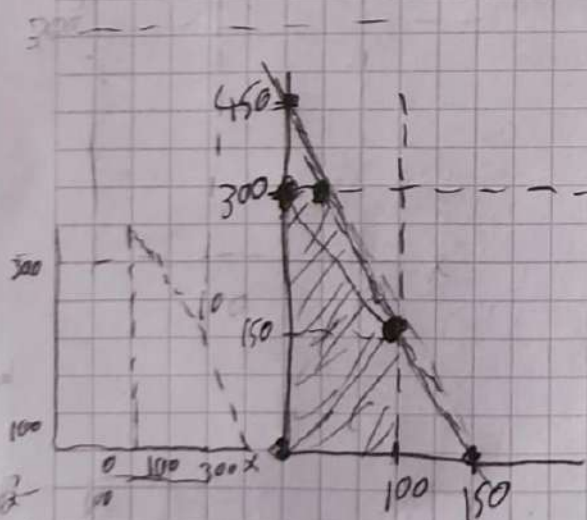
① The graphical solution

$3x + y \leq 450$ represents a straight line with a slope of -3 and intercept on the y axis of 450

$x \leq 100$ vertical line at $x = 100$

$y \leq 300$ horizontal line at $y = 300$

$3x + y = 450$ represent a straight line passing through $(0, 450)$ and $(150, 0)$



To maximize profit we check corners

Corner points of the feasible section:

$(0, 300)$, $(0, 450)$, $(100, 150)$, $(50, 300)$

$(0, 300)$ Profit = $5(300) = 1500$ \$

$(0, 450)$ Profit = $5(450)$

$(100, 150)$ Profit = $8(100) + 5(150) = 1300$ \$

$(50, 300)$ Profit = $8(50) + 5(300) = 1700$ \$

We conclude that $(50, 300)$ gives the highest profit of 1700 \$

Therefore the number of Type 1 hats should be produced per day is 50 and Type 2 hats per day is 300

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- ① Will west produces two types of cowboy hats. A type 1 hat requires three times as much labour time as type 2. If all available labor time is dedicated to type 2 alone, the company can produce a total of 450 type 2 hats a day. The market limits for the two types are 100 and 300 hats per day for Type 1 and Type 2 respectively. The profit is \$8 per Type 1 hat and \$5 per Type 2 hat. Determine the number of hats each type that would maximize profit.
- ② Build mathematical model of the problem.
- ③ Solve the problem graphically.

Solutions are on the next page: