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Signature: 

Question

1. Wild West produces two types of cowboy hats. A type 1 hat requires 3 times as much labor time as a type 2. If the all available labor time is dedicated to type 2 alone, the company can produce a total of 450 type 2 hats a day. The market limits for the two types are 100 and 300 hats per day for type 1 and type 2 respectively. The profit is \$8 per day type 1 hat and \$5 per Type 2 hat. Determine the num of hats that would max profit.

- (i). Build the mat. model of prob.
- (ii). Solve the problem graphically.

Solution.

$x_1 \rightarrow$ type 1 hat

$x_2 \rightarrow$ type 2 hats

Objectives gives function:

maximize: $8x_1 + 5x_2$

Constraints:

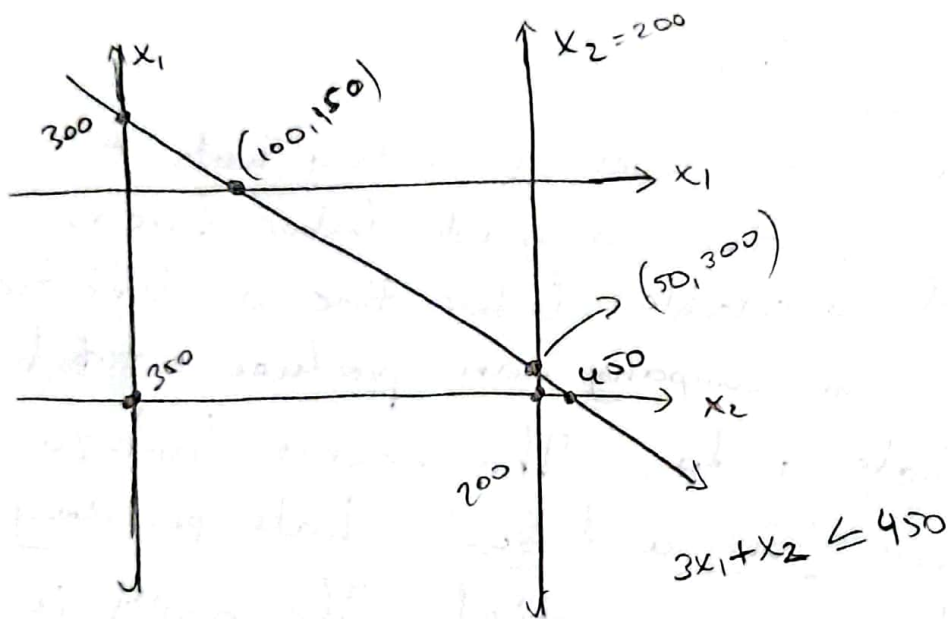
$$3x_1 + x_2 \leq 450$$

$$x_1 \leq 100$$

$$x_2 \leq 300$$

Type 2 need T hours
available hours: $450T$

$$3Tx_1 + Tx_2 \leq 450T$$



$$\begin{array}{r} 400 + 1500 \\ 2400 \end{array}$$
$$\begin{array}{r} 50 \\ 300 \\ 350 \end{array}$$
$$\begin{array}{r} 100 \\ 150 \\ 250 \end{array}$$
$$\begin{array}{r} 400 \\ 120 \\ 520 \end{array}$$
$$\begin{array}{r} 320 \\ 280 \\ 600 \end{array}$$

Optimal point is

$$x_1 = 50$$

$$x_2 = 300$$

Optimal value

$$\boxed{1900 \$}$$

$$150 + 300 \leq 450$$

$$3.50$$

$$8x_1 + 5x_2$$

$$8 \cdot 50 + 5 \cdot 300$$

$$400 + 1500 = 1900 \$$$