

Kember C

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Question: Wild West produces two types of cowboy hats. A type 1 requires three times as much labor time as a type 2. If the all available labor time is dedicated to Type 2 alone, the company can produce a total of 450 Type 2 hats a day. The market limits for the two types are 100 and 300 hats per day for Type 1 and Type 2, respectively. The profit is \$8 per Type 1 hat and \$5 per Type 2 hat. Determine the number of hats of each type that would maximize profit.

- Build the mathematical model of the problem.
- Solve the problem graphically.

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i.) Type 1  $\Rightarrow x$  number of hats

Type 2  $\Rightarrow y$  number of hats

Objective function

$$\max z = 8x + 5y$$

Constraints

$$3x + y \leq 450$$

$$x \leq 100$$

$$y \leq 300$$

$$x \geq 0, y \geq 0$$

Type 1  $\Rightarrow$  3 a hours

Type 2  $\Rightarrow$  a hours

max available = 450 a hours

$$3ax + ay \leq 450a$$

Coordinates	$Z = 8x + 5y$
(0, 0)	0
(100, 0)	800
(0, 300)	1500
(50, 300)	2900 max
(100, 150)	1550

Two maximize profit-produce

Type 1  $\Rightarrow$  50

Type 2  $\Rightarrow$  300

