

IE Quiz 1

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- 1) Wild west produces two types of cowboy hats. A type 1 hat requires three times as much labor time as a type 2. If the all available labor time is dedicated to Type 2 alone, the company can produce a total of 450 Type 2 hats a day. The market limits for the two types are 100 and 300 hats per day for type 1 and type 2, respectively. The profit is \$8 per type 1 hat and \$5 per type 2 hat. Determine the number of hats of each type that would maximize profit.

- i) Build the mathematical model of the problem.
- ii) Solve the problem graphically.

1) ~~market~~ labor constraint:

$$3x_1 + x_2 \leq 450$$

market constraint:

$$x_1 \leq 100$$

$$x_2 \leq 300$$

non-negativity constraint

$$x_1 \geq 0$$
$$x_2 \geq 0$$

objective function

$$P = 8x_1 + 5x_2$$

maximize: $P = 8x_1 + 5x_2$

Subject to:

$$3x_1 + x_2 \leq 450$$

$$x_1 \geq 0 \quad x_2 \geq 0$$

$$x_1 \leq 100$$

$$x_2 \leq 300$$

$$P = 8x_1 + 5x_2$$

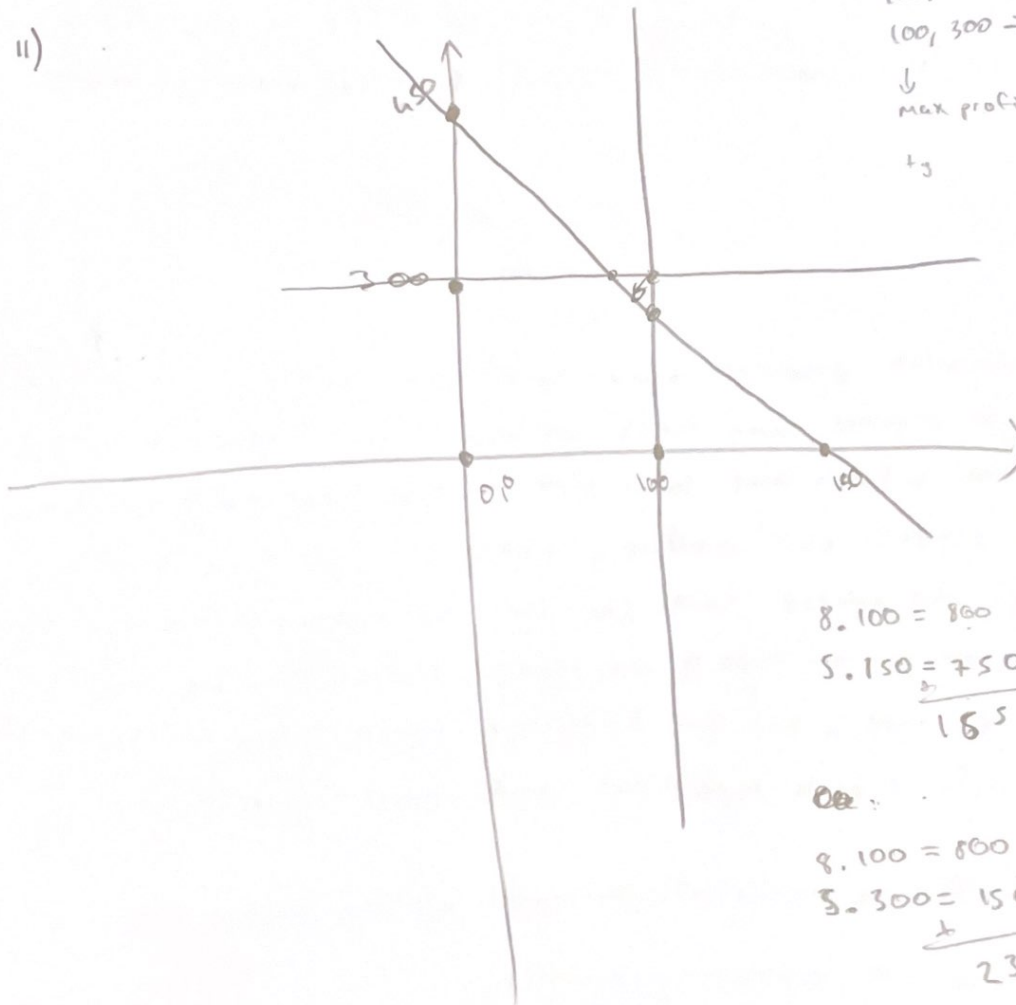
1500

$$\begin{aligned} 0, 0 &\rightarrow 0 \\ 0, 300 &\rightarrow 1500 \\ 100, 150 &\rightarrow 1550 \\ 100, 300 &\rightarrow 2300 \end{aligned}$$

↓
max profit

t_3

ii)



$$8 \cdot 100 = 800$$

$$5 \cdot 150 = 750$$

$$\hline 1550$$

or:

$$8 \cdot 100 = 800$$

$$5 \cdot 300 = 1500$$

$$\hline 2300$$

to maximize the profit

type 1 should be created 100 times

and type 2 should be created

300 times.