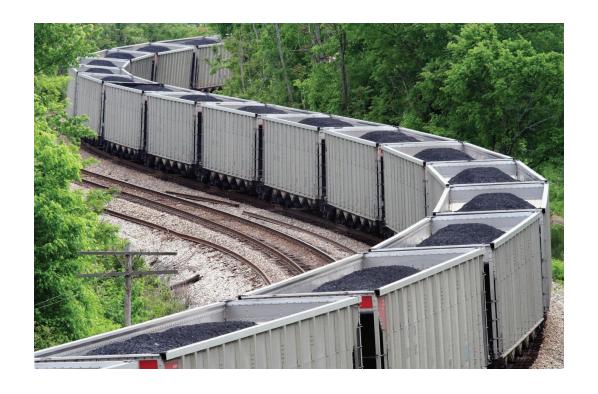
BLG 102E Introduction to Scientific Computing and Engineering

SPRING 2025

WEEK 7





Arrays

- when you need to work with a large number of values all together
- manage collections of data
- stored data is of the same type

Think of a sequence of data:

32 54 67.5 29 35 80 115 44.5 100 65

(all of the same type, of course) (storable as doubles)

32 54 67.5 29 35 80 115 44.5 100 65

Which is the largest in this set?

(You must look at every single value to decide.)

32 54 67.5 29 35 80 115 44.5 100 65

So you would create a variable for each, of course!

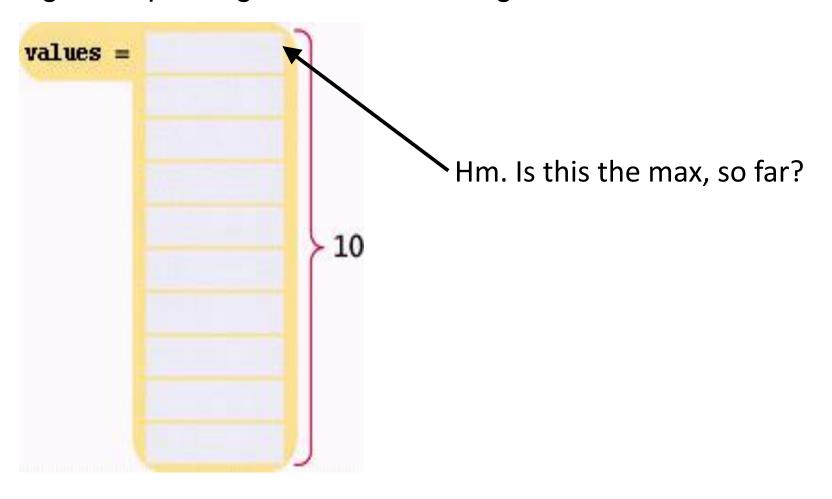
int n1, n2, n3, n4, n5, n6, n7, n8, n9, n10;

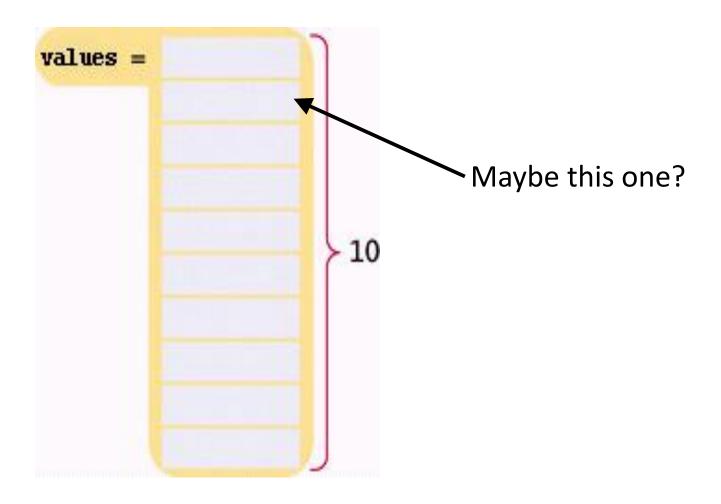
Then what???

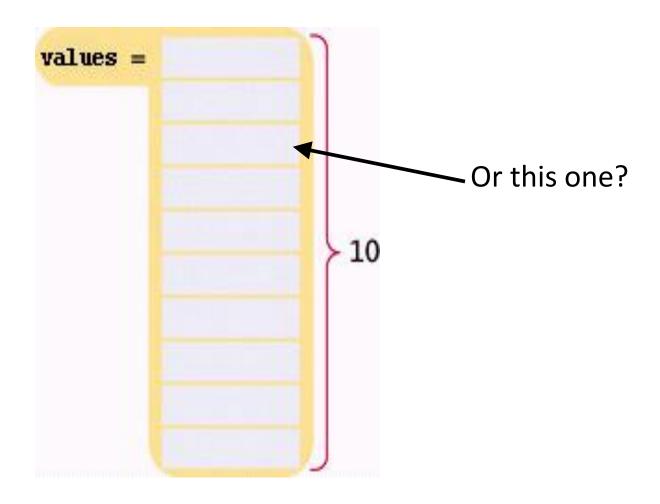
- Arrays
 - Structures of related data items
 - Static entity
 - same size throughout program

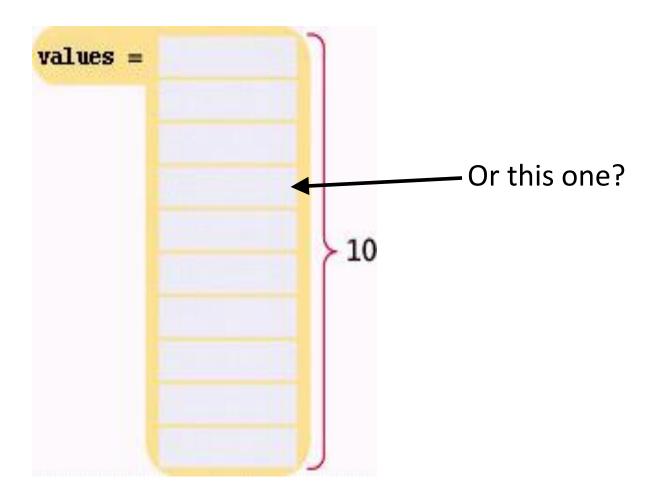
- Array definition
 - Group of consecutive memory locations
 - Same name and data type

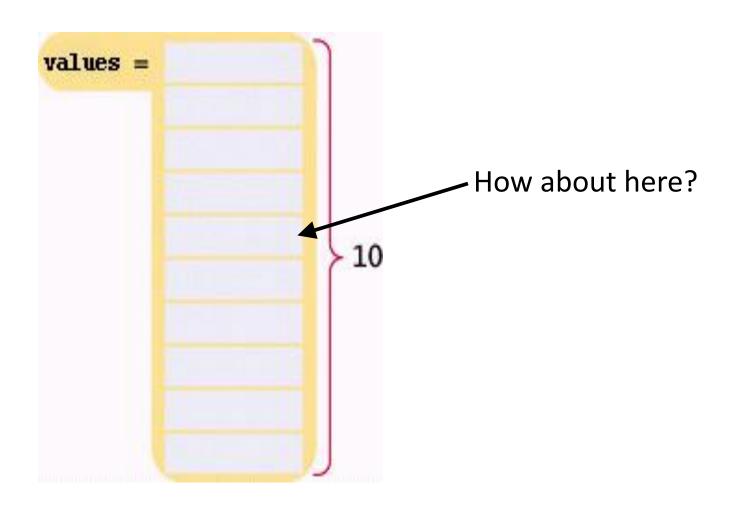
You can easily visit each element in an array, checking and updating a variable holding the current maximum.

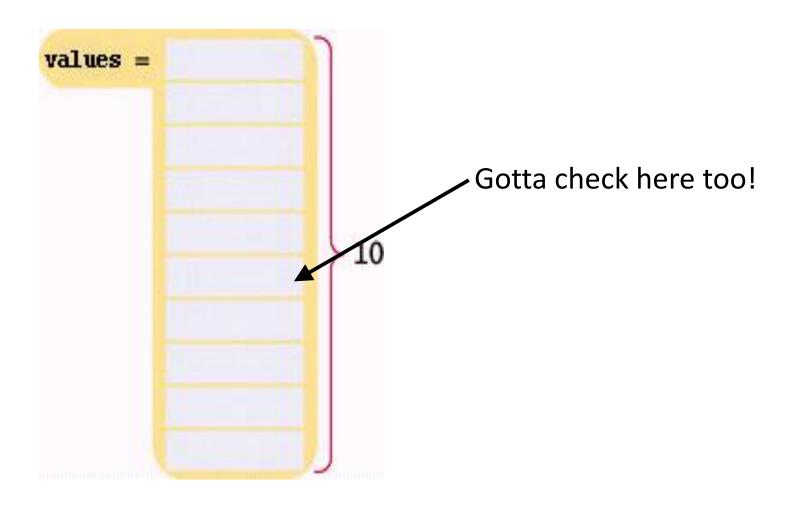


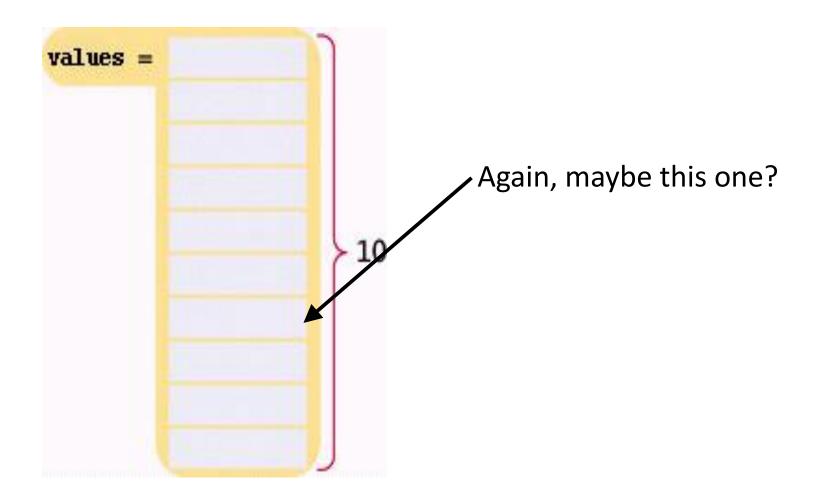


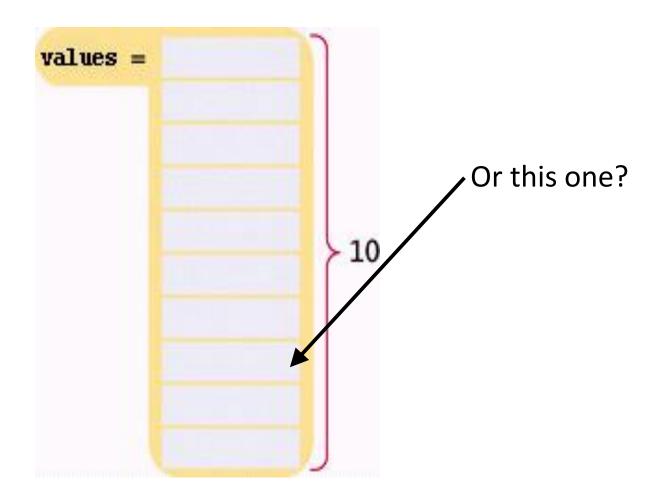


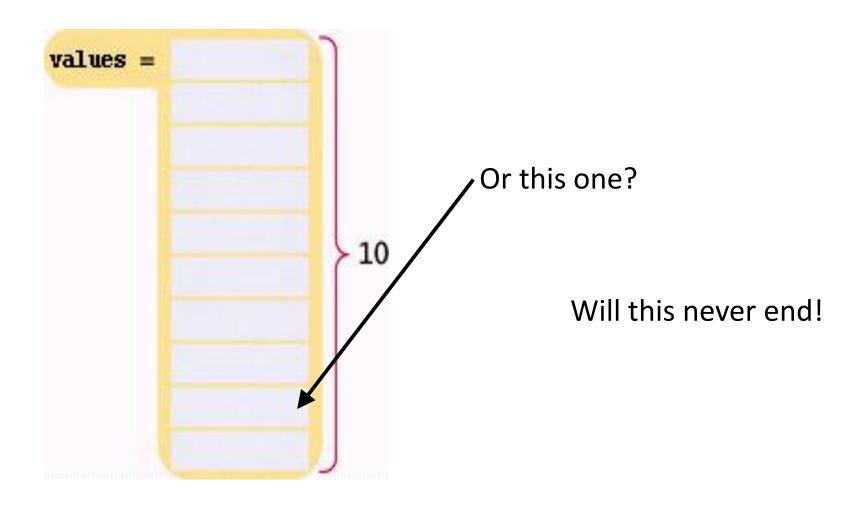


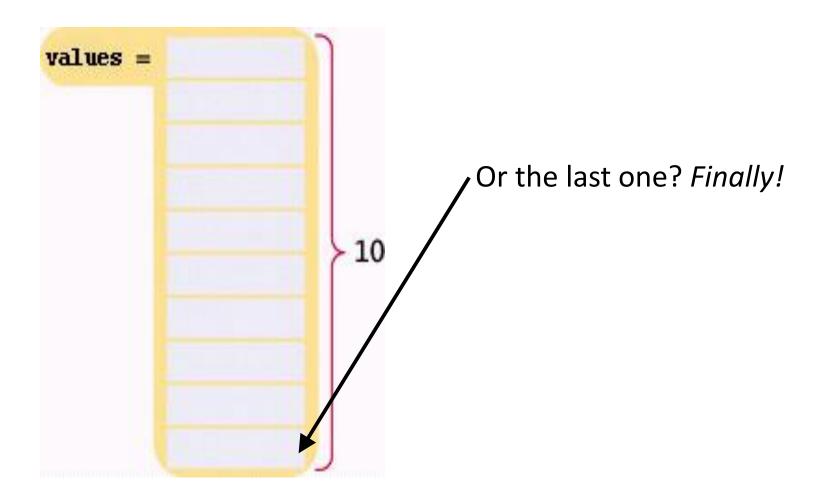










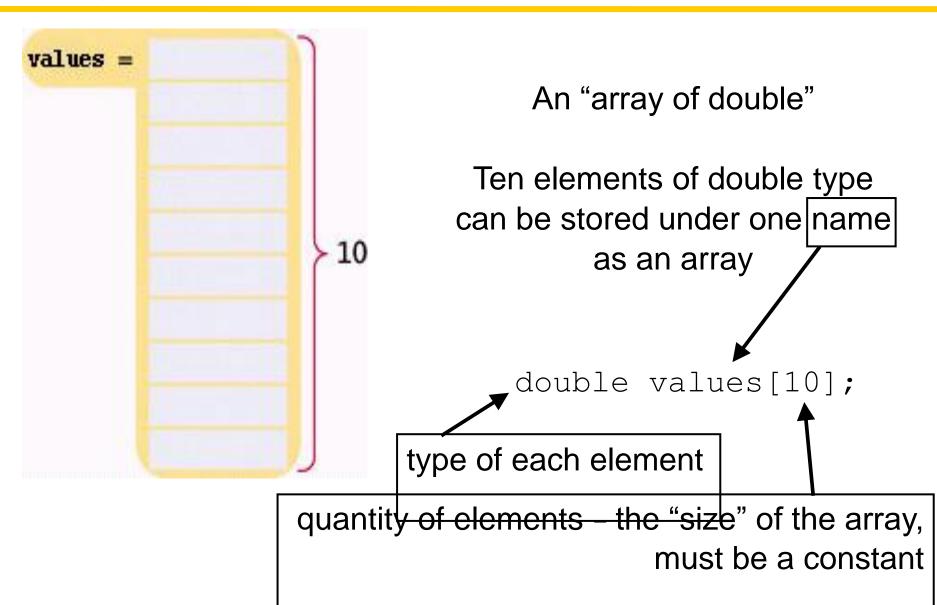


That would have been impossible with ten separate variables!

```
int n1, n2, n3, n4, n5, n6, n7, n8, n9, n10;
```

And what if there needed to be another double in the set?

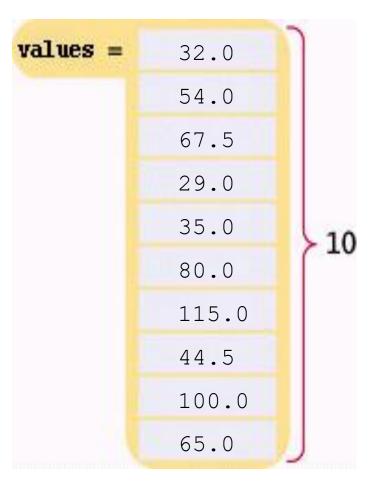
Defining Arrays



Defining Arrays with Initialization

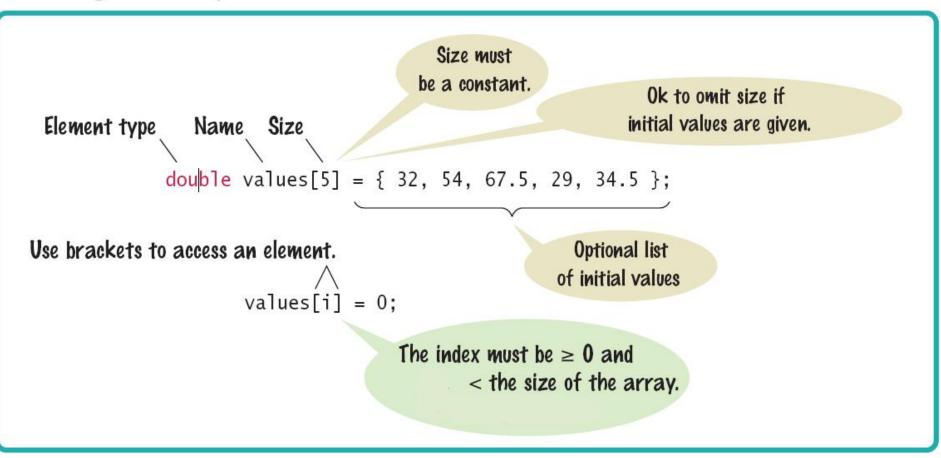
When you define an array, you can specify the initial values:

```
double values[] = { 32, 54, 67.5, 29, 35, 80, 115, 44.5, 100, 65 };
```



Array Syntax

Defining an Array



Array Syntax

Table 1 Defining Arrays		
int numbers[10];	An array of ten integers.	
<pre>const int SIZE = 10; int numbers[SIZE];</pre>	It is a good idea to use a named constant for the size.	
<pre>int size = 10; int numbers[size];</pre>	Caution: In standard C, the size must be a constant. This array definition will not work with all compilers.	
int squares[5] = { 0, 1, 4, 9, 16 };	An array of five integers, with initial values.	
int squares[] = { 0, 1, 4, 9, 16 };	You can omit the array size if you supply initial values. The size is set to the number of initial values.	
int squares[5] = { 0, 1, 4 };	If you supply fewer initial values than the size, the remaining values are set to 0. This array contains 0, 1, 4, 0, 0.	

Initializing Array Elements

• We can use a list of initializers in declaration statement.

```
int a[ 5 ] = \{ 10, 20, 30, 40, 50 \};
```

If not enough initializers, rightmost elements become 0

```
int a[ 5 ] = { 0 }; // All elements are set to zero
int a[ 5 ] = { 10 }; // First element is 10, other elements are zero
```

- If too many elements, then a syntax error is produced
- C arrays have no bounds checking
 Example: a[200] = 60; The statement will not give compiler error.
- If size omitted, count of initializers will determine the size

```
int a[] = \{ 10, 20, 30, 40, 50 \};
```

5 initializers, therefore compiler knows that array has 5 elements

Example: Initializing an array with a declaration

Program defines and initializes an array.

```
/* Initializing an array with a initializer list */
#include <stdio.h>
int main()
{
  // use initializer list to initialize array n
   int n[10] = \{32, 27, 64, 18, 95, 14, 90, 70, 60, 37\};
   int i; // counter
  printf("Element Value \n" );
  // output contents of array in tabular format
   for (i = 0; i < 10; i++) {
      printf( "%7d %13d \n", i, n[ i ] );
} // end main
```

Program Output

Element	Value	
0	32	
1	27	
2	64	
3	18	
4	95	
5	14	
6	90	
7	70	
8	60	
9	37	

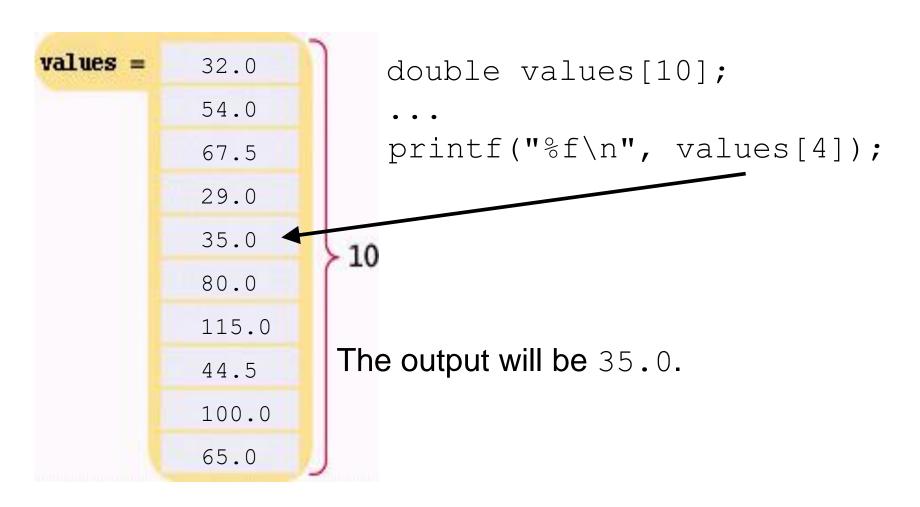
An array element can be used like any variable.

To access an array element, you use the notation:

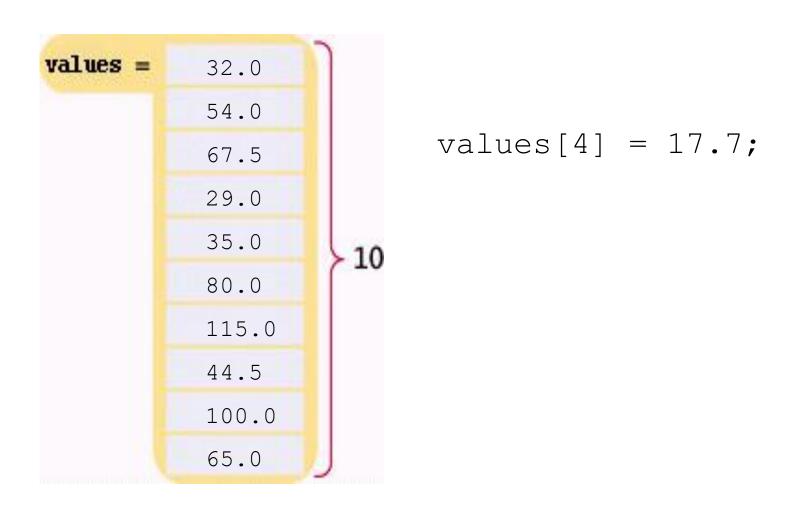
values[i]

where i is the *index*.

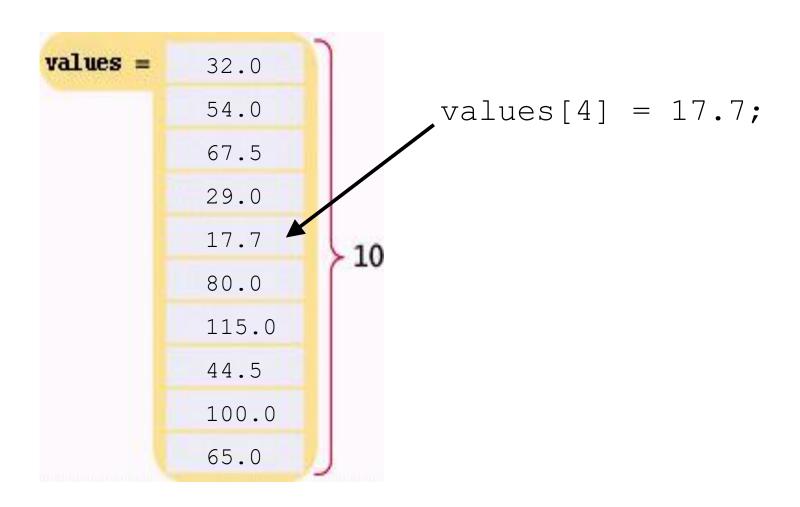
To access the element at index 4 using this notation: values [4] 4 is the index.



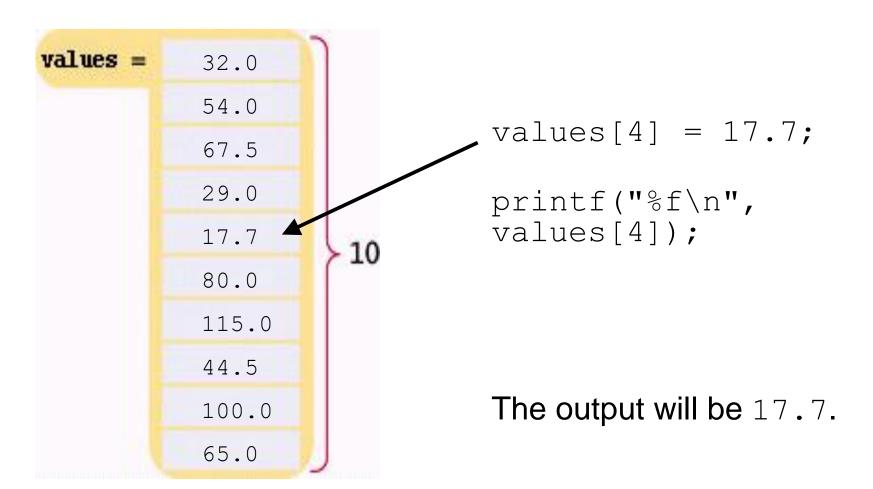
The same notation can be used to change the element.



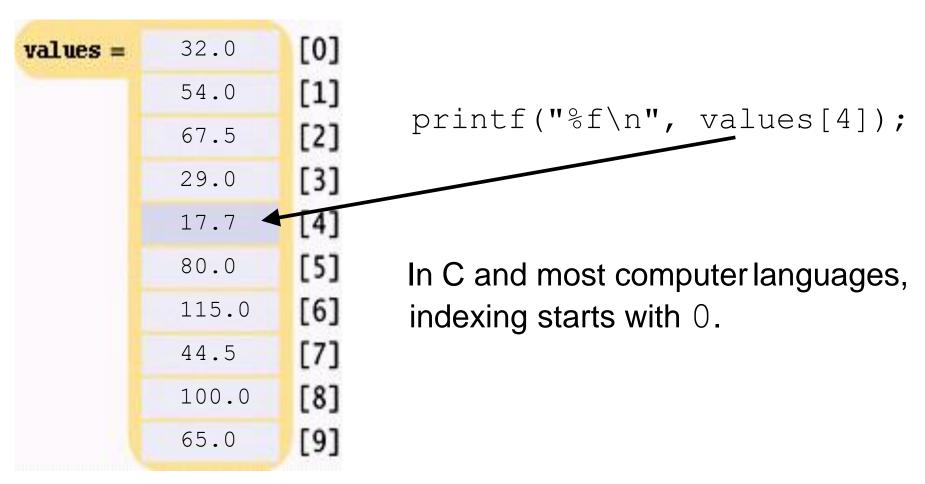
The same notation can be used to change the element.



The same notation can be used to change the element.



You might have thought those last two slides were wrong: values[4] is getting the data from the "fifth" element.



That is, the legal elements for the values array are:

```
values[0], the first element
values[1], the second element
values[2], the third element
values[3], the fourth element
values[4], the fifth element
...
values[9], the tenth and last legal element
recall: double values[10];
```

The index must be >= 0 and <= 9. 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 is 10 numbers.

Partially-Filled Arrays

Suppose an array can hold 10 elements:



Does it always?

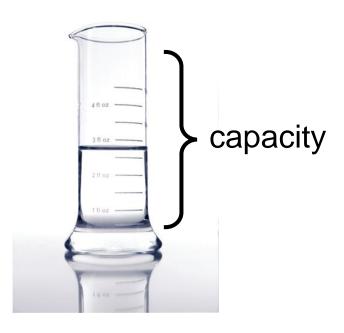
Just look at that beaker.

Guess not!

Partially-Filled Arrays – Capacity

How many elements, at most, can an array hold?

We call this quantity the capacity.



Partially-Filled Arrays – Capacity

For example, we may decide for a particular problem that there are usually ten or 11 values, but never more than 100.

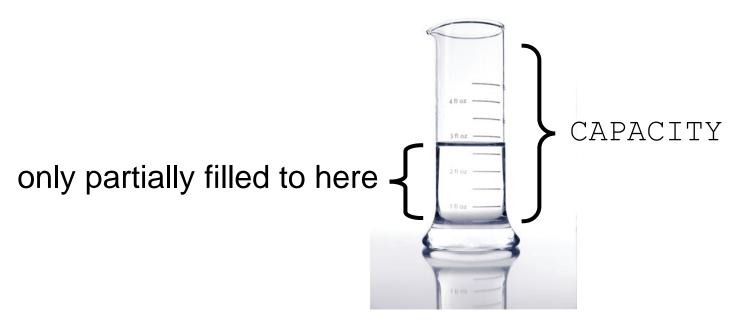
We would set the capacity with a const:

```
const int CAPACITY = 100;
double values[CAPACITY];
```

Partially-Filled Arrays

Arrays will usually hold less than CAPACITY elements.

We call this kind of array a partially filled array:



Partially-Filled Arrays – Companion Variable for Size

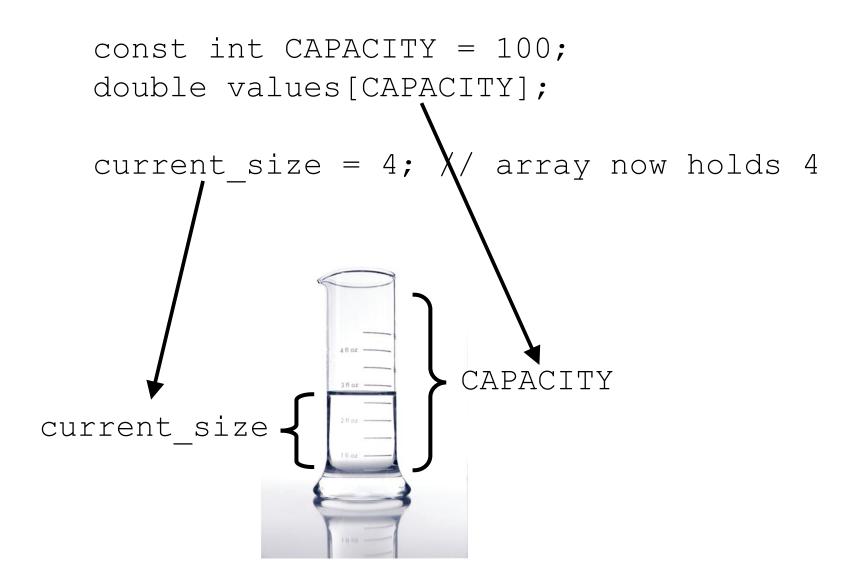
But how many actual elements are there in a partially filled array?

We will use a *companion variable* to hold that amount:

```
const int CAPACITY = 100;
double values[CAPACITY];
int current_size = 0; // array is empty
```

Suppose we add four elements to the array?

Partially-Filled Arrays – Companion Variable for Size



Partially-Filled Arrays – Companion Variable for Size

```
const int CAPACITY = 100;
   double values [CAPACITY];
   current size = 4; // array now holds 4
       values = 32
                  54
                         current_size
                  67
                  24
                                      CAPACITY
Not currently used
```

Partially-Filled Arrays – Capacity

The following loop fills an array with user input. Each time the size of the array changes we update this variable:

```
const int CAPACITY = 100;
double values [CAPACITY];
int current size = 0;
double input;
scanf("%lf", &input);
while (current size < CAPACITY ) {
   if (input > 1) {
      values[current size] = input;
      current size++;
   scanf("%lf", &input);
```

Partially-Filled Arrays – Capacity

The following loop fills an array with user input. Each time the size of the array changes we update this variable:

```
const int CAPACITY = 100;
double values [CAPACITY];
int current size = 0;
double input;
scanf("%lf", &input);
while (current size < CAPACITY ) {
   if (input > \mathscr{D})
      values[gurrent size] = input;
      current size++;
   scanf("%lf", &input);
```

Partially-Filled Arrays – Capacity

When the loop ends, the companion variable current_size has the number of elements in the array.

```
const int CAPACITY = 100;
double values [CAPACITY];
int current size = 0;
double input;
scanf("%lf", &input);
while (current size < CAPACITY ) {
   if (input > 0) {
      values[current size] = input;
      current size++;
   scanf("%lf", &input);
```

Partially-Filled Arrays – Visiting All Elements

How would you print the elements in a partially filled array?

By using the current_size companion variable.

```
for (int i = 0; i < current_size; i++) {
   printf("%f\n", values[i]);
}</pre>
```

```
for (int i = 0; i < current_size; i++) {
    printf("%f\n", values[i]);
}
When i is 0,</pre>
```

To visit all elements of an array, use a variable for the index. A for loop's variable is best:

```
for (int i = 0; i < current_size; i++) {
    printf("%f\n", values[i]);
}</pre>
```

When i is 0, values[i] is values[0], the first element.

```
for (int i = 0; i < current_size; i++) {
    printf("%f\n", values[i]);
}
When i is 0, values[i] is values[0], the first element.
When i is 1,</pre>
```

To visit all elements of an array, use a variable for the index. A for loop's variable is best:

```
for (int i = 0; i < current_size; i++) {
    printf("%f\n", values[i]);
}</pre>
```

When i is 0, values [i] is values [0], the first element.

When i is 1, values[i] is values[1], the second element.

```
for (int i = 0; i < current_size; i++) {
    printf("%f\n", values[i]);
}
When i is 0, values[i] is values[0], the first element.
When i is 1, values[i] is values[1], the second element.
When i is 2,</pre>
```

```
for (int i = 0; i < current size; i++) {
    printf("%f\n", values[i]);
}
When i is 0, values[i] is values[0], the first element.
When i is 1, values[i] is values[1], the second element.
When i is 2, values[i] is values[2], the third element.</pre>
```

```
for (int i = 0; i < current size; i++) {
   printf("%f\n", values[i]);
When i is 0, values[i] is values[0], the first element.
When i is 1, values[i] is values[1], the second element.
When i is 2, values [i] is values [2], the third element.
When i is 9,
```

```
for (int i = 0; i < current size; i++) {
   printf("%f\n", values[i]);
When i is 0, values [i] is values [0], the first element.
When i is 1, values[i] is values[1], the second element.
When i is 2, values [i] is values [2], the third element.
When i is 9, values[i] is values[9],
                          the last legal element.
```

To visit all elements of an array, use a variable for the index.

A for loop's variable is best:

```
for (int i = 0; i < current_size; i++) {
    printf("%f\n", values[i]);
}</pre>
```

Note that the loop ondition is that the index is

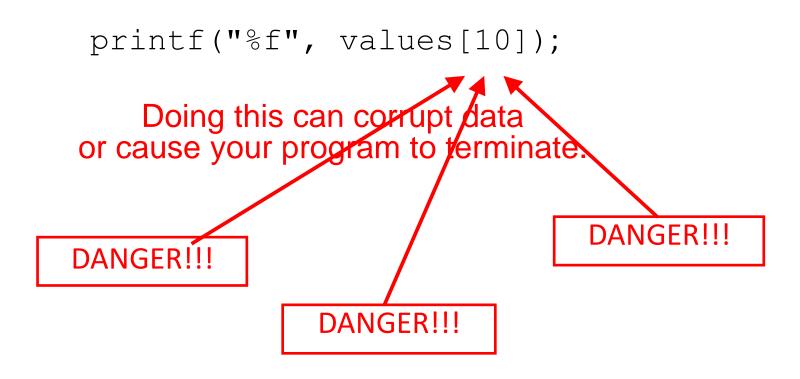
less than current_size

because there is no element corresponding to data[10].

But current_size (10) is the number of elements we want to visit.

Illegally Accessing an Array Element – Bounds Error

A *bounds* error occurs when you access an element outside the legal set of indices:



Recall that the type of every element must be the same. That implies that the "meaning" of each stored value is the same.

```
int scores[NUMBER_OF_SCORES];
```

Clearly the meaning of each element is a score.

But an array could be used improperly:

```
double personal_data[3];
personal_data[0] = age;
personal_data[1] = bank_account;
personal_data[2] = shoe_size;
```

Clearly these doubles do not have the same meaning!

But worse:

```
personal_data[ ] = new_shoe_size;
```

But worse:

Oh dear!

Which position was I using for the shoe size?

Arrays should be used when the meaning of each element is the same.

Common Array Algorithms

There are many typical things that are done with sequences of values.

There many common algorithms for processing values stored in arrays.

Common Algorithms – Filling

This loop fills an array with zeros:

```
for (int i = 0; i < size of values; i++) {
   values[i] = 0;
}</pre>
```

Common Algorithms – Filling

Here, we fill the array with squares (0, 1, 4, 9, 16, ...).

Note that the element with index 0 will contain 0², the element with index 1 will contain 1², and so on.

```
for (int i = 0; i < size of squares; i++) {
    squares[i] = i * i;
}</pre>
```

Consider these two arrays:

```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];
```

How can we copy the values from squares to lucky numbers?

Let's try what seems right and easy...

```
squares = lucky numbers;
```

...and wrong!

You cannot assign arrays!

You will have to do your own work.

```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 0</pre>
```

```
      squares =
      0
      [0]
      lucky_numbers =
      [0]

      1
      [1]
      [1]
      [1]

      4
      [2]
      [2]
      [2]

      9
      [3]
      [3]
      [4]
```

```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 0</pre>
```

```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 1</pre>
```

```
squares = 0 ....[0] lucky_numbers = 0 [0]
```

```
1 [1]
```

```
int squares[5] = \{ 0, 1, 4, 9, 16 \};
int lucky numbers[5];
for (int i = 0; i < 5; i++) {
   lucky numbers[i] = squares[i];
```

when i is 1

```
lucky_numbers = ___
squares =
                          [0]
                                                                      [0]
                          [1]
                                                                      [1]
                           [2]
                                                                      [2]
                  9
                           [3]
                                                                      [3]
                  16
                          [4]
                                                                      [4]
```

```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 2</pre>
```

```
    squares =
    0
    [0]
    lucky_numbers =
    0
    [0]

    1
    [1]
    1
    [1]

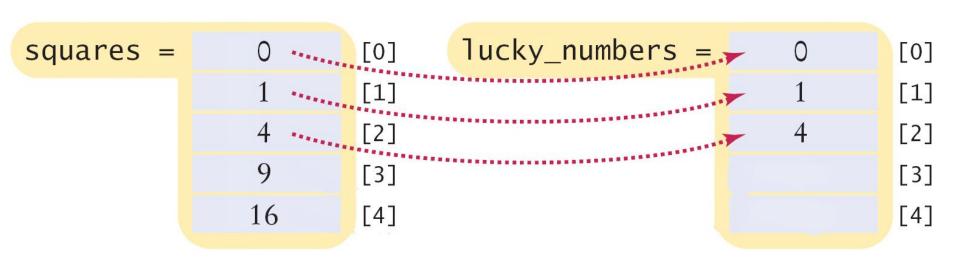
    4
    [2]
    [2]
    [2]

    9
    [3]
    [3]

    16
    [4]
    [4]
```

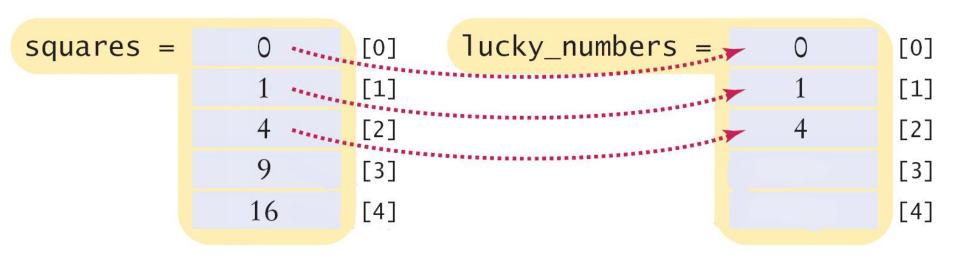
```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 2</pre>
```



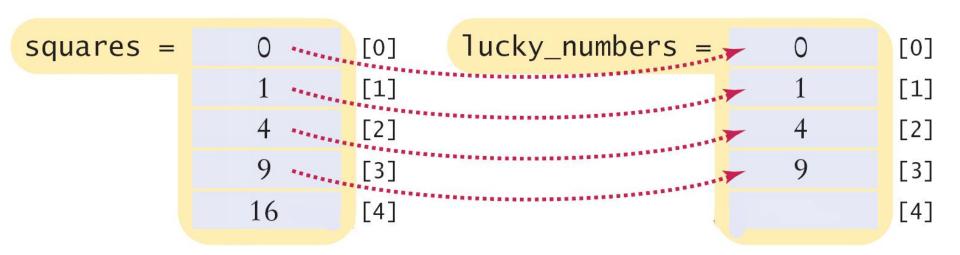
```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 3</pre>
```



```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 3</pre>
```



```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 4</pre>
```

```
      squares =
      0
      [0]
      lucky_numbers =
      0
      [0]

      1
      [1]
      1
      [1]

      4
      [2]
      4
      [2]

      9
      [3]
      9
      [3]

      16
      [4]
      [4]
```

Common Algorithms – Copying

```
int squares[5] = { 0, 1, 4, 9, 16 };
int lucky_numbers[5];

for (int i = 0; i < 5; i++) {
   lucky_numbers[i] = squares[i];
}
   when i is 4</pre>
```

 squares =
 0
 [0]
 lucky_numbers =
 0
 [0]

 1
 [1]
 1
 [1]

 4
 [2]
 4
 [2]

 9
 [3]
 9
 [3]

 16
 [4]
 [4]

Common Algorithms – Sum and Average Value

You have already seen the algorithm for computing the sum and average of set of data. The algorithm is the same when the data is stored in an array.

```
double total = 0;
for (int i = 0; i < size of values; i++) {
   total = total + values[i];
}</pre>
```

The average is just arithmetic:

```
double average = total / size of values;
```

Common Algorithms – Who Is the Tallest?

If everyone's height is stored in an array, determining the largest value (what's the tallest person's height?) is just another algorithm...



Common Algorithms – Maximum and Minimum

To compute the largest value in an array, keep a variable that stores the largest element that you have encountered, and update it when you find a larger one.

```
double largest = values[0];
for (int i = 1; i < SiZE Of values; i++) {
   if (values[i] > largest) {
     largest = values[i];
   }
}
```

Common Algorithms – Maximum and Minimum

To compute the largest value in an array, keep a variable that stores the largest element that you have encountered, and update it when you find a larger one.

```
double largest = values[0];
for (int i = 1; i < SiZe Of values; i++) {
   if (values[f] > largest) {
      largest = values[i];
   }
}
Note that the loop starts at 1
because we initialize largest with data[0].
```

Common Algorithms – Who Is the Shortest?



Who's the shortest in the line? (What'is the shortest person's height?)

Common Algorithms – Maximum and Minimum

For the minimum, we just reverse the comparison.

```
double smallest = values[0];
for (int i = 1; i < size of values; i++) {
   if (values[i] < smallest) {
      smallest = values[i];
   }
}</pre>
```

These algorithms require that the array contain at least one element.

Common Algorithms – Element Separators

When you display the elements of an array, you usually want to separate them, often with commas or vertical lines, like this:

Note that there is one fewer separator than there are numbers.

To print five elements, you need *four* separators.

Common Algorithms – Element Separators

Print the separator before each element except the initial one (with index 0):

```
1 | 4 | 9 | 16 | 25

for (int i = 0; i < size of values; i++) {
   if (i > 0) {
      printf(" | ");
   }
   printf("%d", values[i]);
}
```

Common Algorithms – Linear Search

Find the position of a certain value, say 100, in an array:

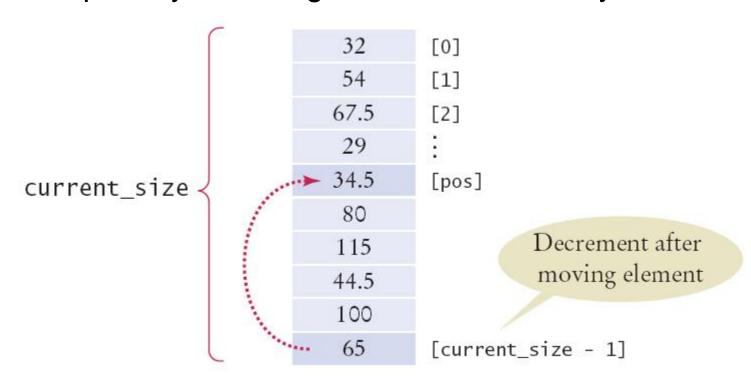
```
int pos = 0;
bool found = false;
while (pos < SiZe Of values && !found) {
   if (values[pos] == 100) {
      found = true;
   } else {
      pos++;
   }
}</pre>
```

Common Algorithms – Removing an Element, Unordered

Suppose you want to remove the element at index i.

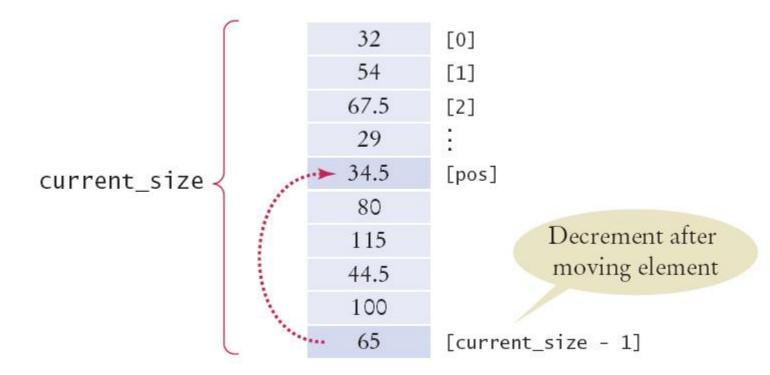
If the elements in the array are not in any particular order, that task is easy to accomplish.

Simply overwrite the element to be removed with the *last* element of the array, then remove the value that was copied by shrinking the size of the array.



Common Algorithms – Removing an Element, Unordered

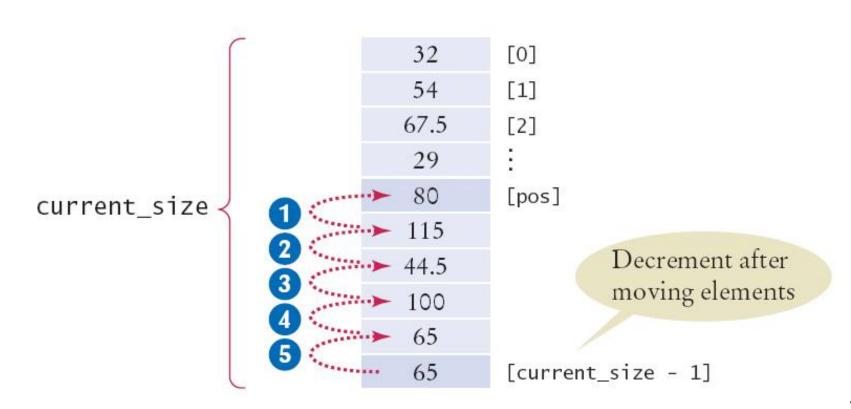
```
values[pos] = values[current_size - 1];
current_size--;
```



Common Algorithms - Removing an Element, Ordered

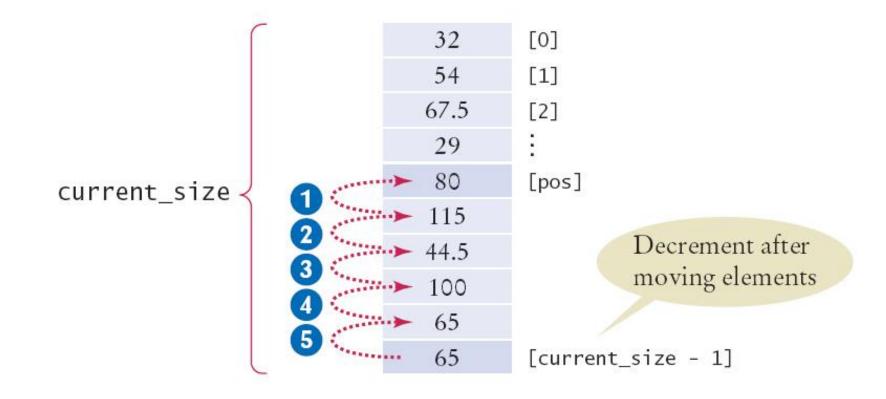
The situation is more complex if the order of the elements matters.

Then you must move all elements following the element to be removed "down" (to a lower index), and then remove the last element by shrinking the size.



Common Algorithms – Removing an Element, Ordered

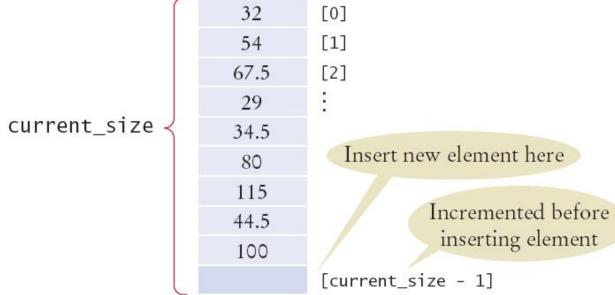
```
for (int i = pos + 1; i < current_size; i++) {
   values[i - 1] = values[i];
}
current_size--;</pre>
```



Common Algorithms – Inserting an Element Unordered

If the order of the elements does not matter, in a partially filled array (which is the only kind you can insert into), you can simply insert a new element at the end.

```
if (current_size < CAPACITY) {
   current_size++;
   values[current_size - 1] = new_element;
}</pre>
```

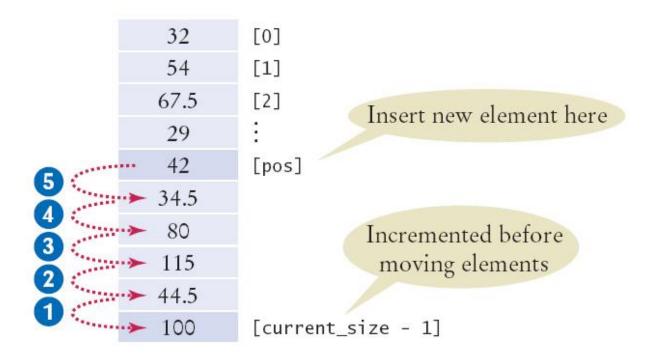


Common Algorithms – Inserting an Element Ordered

If the order of the elements does matter, it is a bit harder.

To insert an element at position i, all elements from that location to the end of the array must be moved "up".

After that, insert the new element at the now vacant position [i].



Common Algorithms – Inserting an Element Ordered

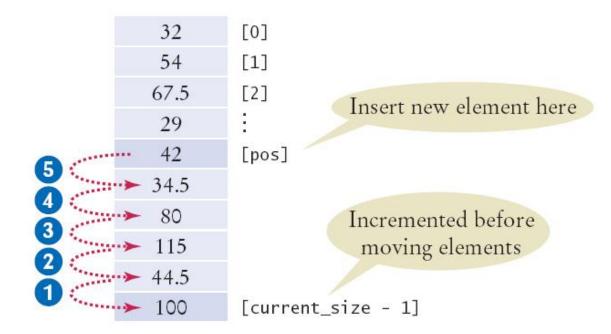
First, you must make the array one larger by incrementing current_size.

Next, move all elements above the insertion location to a higher index.

Finally, insert the new element in the place you made for it.

Common Algorithms – Inserting an Element Ordered

```
if (current_size < CAPACITY) {
    current_size++;
    for (int i = current_size - 1; i > pos; i--) {
       values[i] = values[i - 1];
    }
    values[pos] = new_element;
}
```



Common Algorithms – Swapping Elements

Swapping two elements in an array is an important part of sorting an array.

To do a swap of two things, you need *three* things.

Common Algorithms – Swapping Elements

Suppose we need to swap the values at positions i and j in the array. Will this work?

```
values[i] = values[j];
values[j] = values[i];
```

Look closely!

In the first line you lost – forever! – the value at i, replacing it with the value at j.

Then what?

Put' j's value back in j in the second line?

Common Algorithms – Swapping Elements

```
double temp = values[i];
values[i] = values[j];
values[j] = temp;
```

STEP One

save the value at i

STEP Two

replace the value at i

STEP Three

now you can change the value at j because you saved from i

Common Algorithms – Reading Input

If the know how many input values the user will supply, you can store them directly into the array:

```
double values[NUMBER_OF_INPUTS];
for (i = 0; i < NUMBER_OF_INPUTS; i++) {
   scanf("%lf", &values[i]);
}</pre>
```

Common Algorithms – Reading Input

When there will be an arbitrary number of inputs, things get more complicated.

Add values to the end of the array until all inputs have been made. Again, the companion variable will have the number of inputs.

```
double values[CAPACITY];
int current_size = 0;
double input;
scanf("%lf", &input);
while (input > 0 && current_size < CAPACITY) {
   values[current_size] = input;
   current_size++;
   scanf("%lf", &input);
}</pre>
```

Common Algorithms – Reading Input

Unfortunately it's even more complicated:

Once the array is full, we allow the user to keep entering!

Because we can't change the size of an array after it has been created, we'll just have to give up for now.

Common Algorithms

Now back to where we started:

How do we determine the largest in a set of data?

```
#include <stdio.h>
#include <stdlib.h>

int main()
{
    const int CAPACITY = 1000;
    double values[CAPACITY];
    int current_size = 0;
```

```
printf("Please enter values, 0 to quit:\n");
double input;
scanf("%lf", &input);
while (input > 0 && current_size < CAPACITY) {
  values[current_size] = input;
  current_size++;
  scanf("%lf", &input);</pre>
```

```
double largest = values[0];
for (int i = 1; i < current_size; i++) {
   if (values[i] > largest) {
      largest = values[i];
   }
}
```

```
for (int i = 0; i < current_size; i++) {
    printf(" %f ", values[i]);
    if (values[i] == largest) {
        printf(" (largest value) ");
    }
    printf("\n");
}
return EXIT_SUCCESS;</pre>
```

Example: Printing a Histogram

```
/* fig06_08.c
  Histogram printing program */
#include <stdio.h>
#define SIZE 10
int main() {
  // use initializer list to initialize array n
   int n[SIZE] = { 19, 3, 15, 7, 11, 9, 13, 5, 17, 1 };
  int i; // outer for counter for array elements
  int j; // inner for counter counts stars in each histogram bar
  printf( "Element Value Histogram \n" );
  // for each element of array n, output a bar of the histogram
  for ( i = 0; i < SIZE; i++ ) {</pre>
     for (j = 1; j \le n[i]; j++) \{ // print one bar \}
        printf( "*" );
     } // end inner for
     printf( "\n" ); // end a histogram bar
  } // end outer for
} // end main
```

Program Output

Element	Value	Histogram
0	19	*****
1	3	***
2	15	********
3	7	****
4	11	*****
5	9	*****
6	13	******
7	5	****
8	17	********
9	1	*

Histograms are printed horizontally.

Example: Statistical Calculations

- Read student scores entered by user, and store into an array X.
- Calculate the followings.

$$\sum_{i=1}^{N} X_{i}$$

$$Average(\bar{x}) = \frac{\sum_{i=1}^{N} (x_{i} - \bar{x})^{2}}{N}$$

$$Variance = \frac{\sum_{i=1}^{N} (x_{i} - \bar{x})^{2}}{N}$$

Standard deviation = $\sqrt{Variance}$

Absolute deviation =
$$\frac{\sum_{i=1}^{N} |x_i - \overline{x}|}{N}$$

Example: Statistical Calculations

Part 1 of 2

```
#include <stdio.h>
#include <math.h> // pow,fabs,sqrt functions
#define MAXSTUDENTS 100
int main()
{
    int score[MAXSTUDENTS]; // Array
    int N = 0; // Number of students
    float avg, variance, std_dev, abs_dev;
    float total = 0, sqr total = 0, abs total = 0;
    int i = 0;
    printf("How many students are there?");
    scanf("%d", &N);
    for (i = 0; i < N; i++)
        printf("Enter grade of student # %d : ", i + 1);
        scanf("%d", &score[i]);
        total += score[i];
```

Example: Statistical Calculations

Part 2 of 2

```
avg = total / N;
   for (i = 0; i < N; i++)
       sqr_total += pow( score[i] - avg , 2);
       abs total += fabs(score[i] - avg);
   variance = sqr total / N;
   std dev = sqrt(variance);
   abs dev = abs total / N;
   printf("Average = %f\n", avg);
   printf("Variance = %f\n", variance);
   printf("Standard deviation = %f\n", std_dev);
   printf("Absolute deviation = %f\n", abs dev);
} // end main
```

Program Output

```
How many students are there ? 4
Enter grade of student # 1 : 92
Enter grade of student # 2 : 62
Enter grade of student # 3 : 70
Enter grade of student # 4 : 51
                  = 68.750000
Average
Variance = 300.916656
Standard deviation = 17.346949
Absolute deviation = 12.250000
```