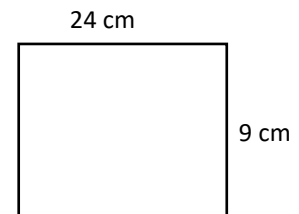


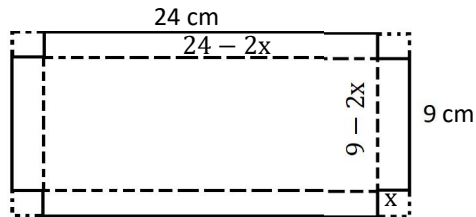
1. Berapa potongan agar volume maxs? Dengan menggunakan turunan



2. Ada kawat panjangnya 36 m kawat itu akan memagari sesuatu daerah persegi, berapa luas maksimal daerah yang bisa dipagari?

Jawaban

1.



$$V = \rho \cdot \ell \cdot \tau$$

$$V = (24 - 2x) \cdot (9 - 2x) \cdot x$$

$$V = (216 - 48x - 18x + 4x^2) \cdot x$$

$$V = (216 - 66x + 4x^2) \cdot x$$

$$V = 216x - 66x^2 + 4x^3$$

$$\frac{dy}{dx} = a \cdot nx^{n-1}$$

$$V' = 216 \cdot 1x^{1-1} - 66 \cdot 2x^{2-1} + 4 \cdot 3x^{3-1}$$

$$V' = 216x^0 - 132x^1 + 12x^2$$

Turunan 1

$$V' = 216 - 132x + 12x^2$$

$$V' = 216 - 132x + 12x^2 : 12$$

Turunan 2

$$V' = 18 - 11x + x^2 = 0$$

$$V' = x^2 - 11x + 18 = 0$$

$$V' = (x - 9)(x - 2) = 0$$

$$x = 9 \quad x = 2$$

Untuk menghitung volume diambil

$x=2$

Jika $x=9$ lebarnya akan habis dipotong

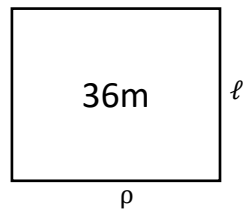
Volume maxs

$$V = 216x - 66x^2 + 4x^3$$

$$V = 216 \cdot 2 - 66 \cdot 2^2 + 4 \cdot 2^3$$

$$V = 432 - 264 + 32$$

2.



$$\text{keliling} = 36\text{m}$$

$$2(\rho + \ell) = 36$$

$$\rho + \ell = \frac{36}{2}$$

$$\rho + \ell = 18\text{m}$$

$$\ell = 18 - \rho$$

Cari panjang

$$\text{luas} = \rho \cdot \ell$$

$$\text{luas} = \rho \cdot (18 - \rho)$$

$$L(\rho) = 18\rho - \rho^2$$

$$\frac{dy}{dx} = a \cdot nx^{n-1}$$

$$L' = 18 \cdot 1\rho^{1-1} - 1 \cdot 2\rho^{2-1}$$

$$= 18\rho^0 - 2\rho^1$$

Turunan 1

$$L' = 18 - 2\rho$$

$$L' = 18 - 2\rho : 2$$

Turunan 2

$$L' = 9 - \rho$$

$$0 = 9 - \rho$$

$$\rho = 9$$

Cari lebar

$$\ell = 18 - \rho$$

$$\ell = 18 - 9$$

$$\ell = 9$$

Luas maxs

$$\text{Luas} = \ell \times \rho$$

$$\text{Luas} = 9 \times 9$$

$$\text{Luas} = 81\text{m}^2$$