Environments

Class outline:

多重环境

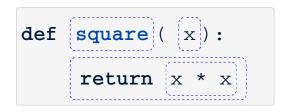
- Multiple environments
- Environments for HOFs
- Local names
- Function composition
- Currying

Multiple Environments

Life cycle of a function

What happens?

Def statement



• A new function is created!

 Name bound to that function in the current frame.

Call expression



- Operator & operands evaluated
- Function (value of operator) called on arguments (values of operands)

Calling/applying



- A new frame is created!
- Parameters bound to arguments
- Body is executed in that new environment

```
1.
```

2.

3.

```
def square(x):
    return x * x
square(square(3))
```

```
1. next
```

3.

```
def square(x):
    return x * x
square(square(3))
```

```
Global frame

square | ● ----> func square(x) [parent=Global]
```

```
Global frame

square | ● ----> func square(x) [parent=Global]
```

```
Global frame

square | ● ----> func square(x) [parent=Global]
```

```
Global frame

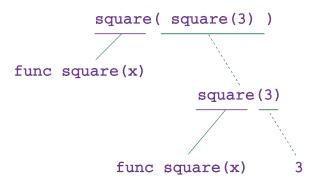
square | ● ----> func square(x) [parent=Global]
```

```
Global frame

square | ● ----> func square(x) [parent=Global]
```

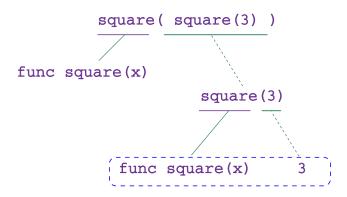
```
Global frame

square | ● ----> func square(x) [parent=Global]
```

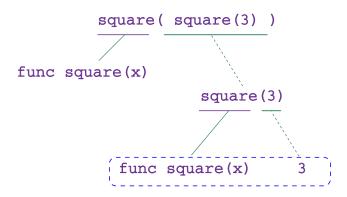


```
Global frame

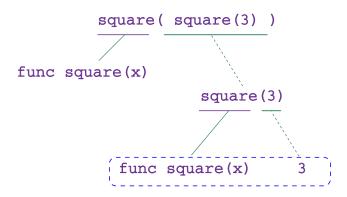
square | ● ----> func square(x) [parent=Global]
```



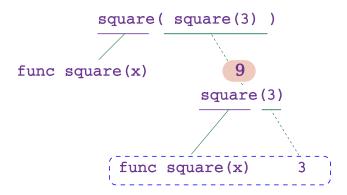
```
next
                                                                                        prev
def square(x):
       return x * x
square(square(3))
Global frame
 square | • ----> func square(x) [parent=Global]
f1: square [parent=Global]
```



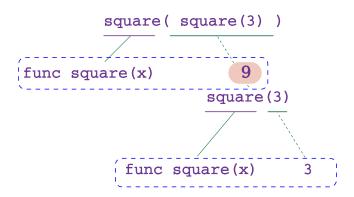
```
prev
                                                                                        next
def square(x):
       return x * x
square(square(3))
Global frame
 square | • ----> func square(x) [parent=Global]
f1: square [parent=Global]
```



```
next
                                                                                             prev
def square(x):
       return x * x
square(square(3))
Global frame
 square | • ----> func square(x) [parent=Global]
f1: square [parent=Global]
           x 3
Return value 9
```



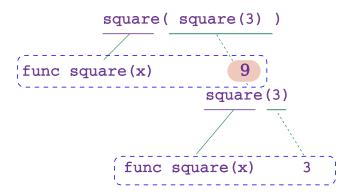
```
next
                                                                                             prev
def square(x):
       return x * x
square(square(3))
Global frame
 square | • ----> func square(x) [parent=Global]
f1: square [parent=Global]
           x 3
Return value 9
```



f2: square [parent=Global]

prev next def square(x): return x * x square(square(3)) Global frame square | • ----> func square(x) [parent=Global] f1: square [parent=Global] x 3 Return value 9

x 9



```
1.
```

3.

```
def square(x):
    return x * x
square(square(3))
```

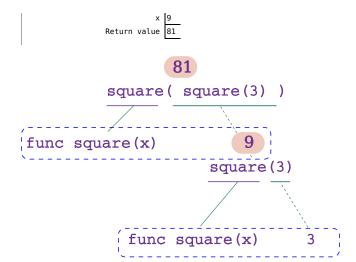
```
Global frame

square | • ----> func square(x) [parent=Global]

fl: square [parent=Global]

x | 3 / 9

f2: square [parent=Global]
```



Multiple environments in one diagram!

```
def square(x):
       return x * x
square(square(3))
Global frame
 square • ----> func square(x) [parent=Global]
f1: square [parent=Global]
f2: square [parent=Global]
           Return value 81
```

An environment is a sequence of frames.

Multiple environments in one diagram!

```
def square(x):
    return x * x
square(square(3))
```

```
Global frame

square • ----> func square(x) [parent=Global]

f1: square [parent=Global]

x 3

Return value 9

f2: square [parent=Global]

x 9

Return value 81
```

An environment is a sequence of frames.

• Environment: Global frame

Multiple environments in one diagram!

```
def square(x):
    return x * x
square(square(3))
```

```
f1: square [parent=Global]

x | 3 | 9 |
Return value | 81
```

An environment is a sequence of frames.

- Environment: Global frame
- Environment: Local frame (f1), then global frame

Multiple environments in one diagram!

```
def square(x):
    return x * x
square(square(3))
```

```
Global frame

2 square • ----> func square(x) [parent=Global]

f1: square [parent=Global]

x | 3 | 9 | |

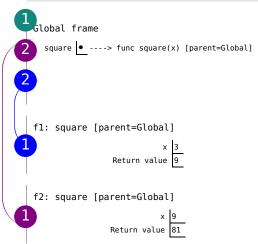
Return value | 9 | 81 |
```

An environment is a sequence of frames.

- Environment: Global frame
- Environment: Local frame (f1), then global frame
- Environment: Local frame (f2), then global frame

Names have no meanings without environments

```
def square(x):
    return x * x
square(square(3))
```



Every expression is evaluated in the context of an environment.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

Names have different meanings in different environments

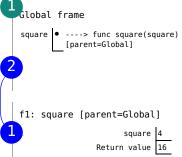
```
def square(square):
    return square * square
square(4)
```

Every expression is evaluated in the context of an environment.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that

Names have different meanings in different environments

```
def square(square):
    return square * square
square(4)
```



Every expression is evaluated in the context of an environment.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that

Environments for higher-order functions

Review: Higher-order functions

A higher-order function is either...

- A function that takes a function as an argument value summation(5, lambda x: x**2)
- A function that returns a function as a return value make_adder(3)(1)

Functions are first class: Functions are values in Python.

Example: Apply twice

```
def apply_twice(f, x):
    return f(f(x))

def square(x):
    return x ** 2

apply_twice(square, 3)
```



View in PythonTutor

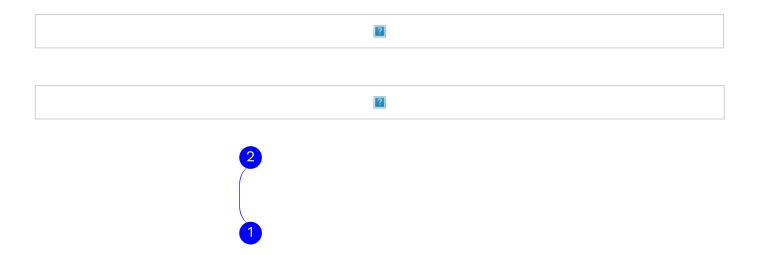
Arguments bound to functions



Arguments bound to functions



Arguments bound to functions



Environments for nested definitions

Example: Make texter

```
def make_texter(emoji):
    def texter(text):
        return emoji + text + emoji
    return texter

happy_text = make_texter("\empsilon")
result = happy_text("lets go to the beach!")
```



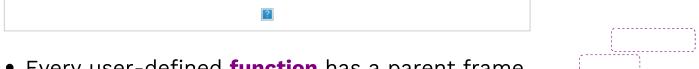
View in PythonTutor

happy_test = text 函数 + emoji 获值 happy_texter("lets go to the beach!") = texter("lets go to the beach!")

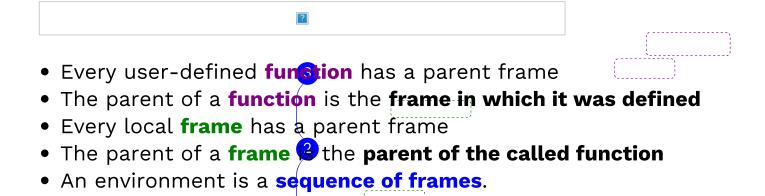




- Livery user-defined runction has a parent frame
- The parent of a function is the frame in which it was defined



- Every user-defined function has a parent frame
- The parent of a function is the frame in which it was defined
- Every local frame has a parent frame
- The parent of a frame is the parent of the called function



How to draw an environment diagram

When a function is defined:

1. Create a function value:

```
func <name>(<formal parameters>) [parent=<label>]
```

- 2. Its parent is the current frame.
- 3. Bind <name> to the function value in the current frame

When a function is called:

- 1. Add a local frame, titled with the <name> of the function being called.
- 2. Copy the parent of the function to the local frame:
 [parent=>label<]</pre>
- 3. Bind the <formal parameters> to the arguments in the local frame.
- 4. Execute the body of the function in the environment that starts with the local frame.

Local names

Example: Thingy Bobber

```
def thingy(x, y):
    return bobber(y)

def bobber(a):
    return a + y

result = thingy("ma", "jig")
```

What do you think will happen?

Example: Thingy Bobber

```
def thingy(x, y):
    return bobber(y)

def bobber(a):
    return a + y

result = thingy("ma", "jig")
```

What do you think will happen?



Local name visibility

Local names are not visible to other (non-nested) functions.



- An environment is a squence of frames.
- The environment created by calling a top-level function consists of one local frame followed by the global frame.



Function Composition

Example: Composer

```
def happy(text):
    return "** + text + "**"

def sad(text):
    return "** + text + "**

def composer(f, g):
    def composed(x):
        return f(g(x))
    return composed

msg1 = composer(sad, happy) ("cs61a!")
msg2 = composer(happy, sad) ("eecs16a!")
```

What do you think will happen?

Example: Composer (Part 2)

One of the composed functions could itself be an HOF...

```
def happy(text):
    return "0" + text + "0"
def sad(text):
    return "8" + text + "8"
def make texter(emoji):
    def texter(text):
        return emoji + text + emoji
    return texter
def composer(f, q):
    def composed(x):
        return f(g(x))
    return composed
composer(happy, make_texter("""))('snow day!')
```



composer(happy, make_texter(""")) ("snow day!")

```
composer(happy, make_texter("%")) ("snow day!")

composer(happy, make_texter("%"))
```

```
composer(happy, make_texter("%")) ("snow day!")

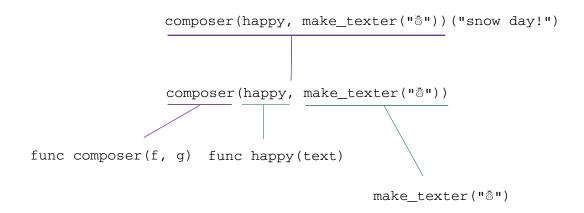
composer(happy, make_texter("%"))

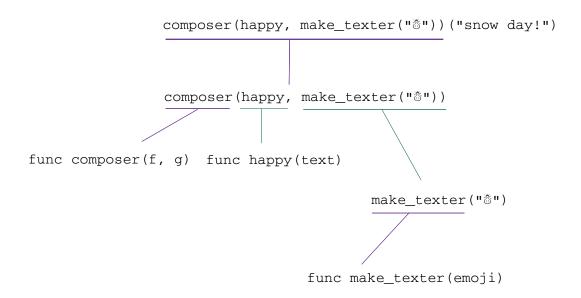
func composer(f, g)
```

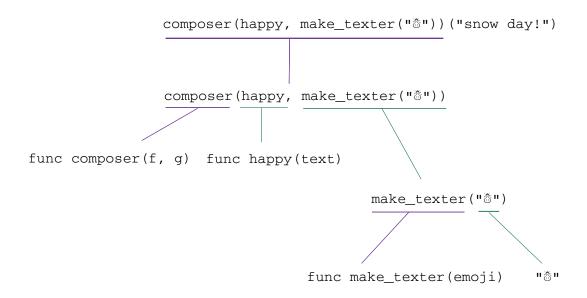
```
composer(happy, make_texter("%")) ("snow day!")

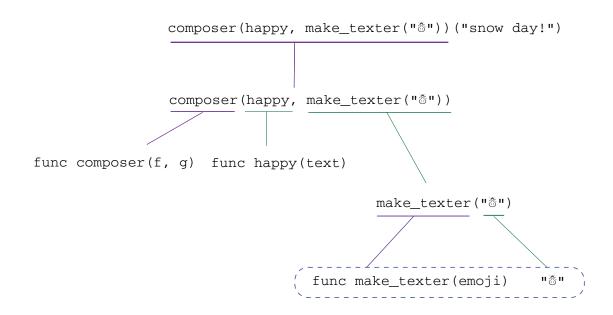
composer(happy, make_texter("%"))

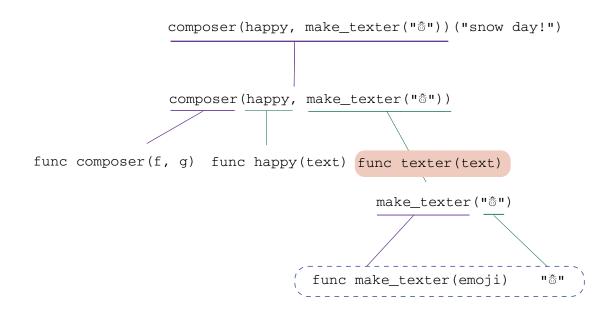
func composer(f, g) func happy(text)
```

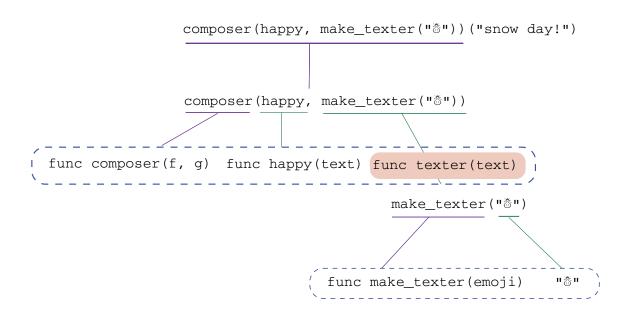


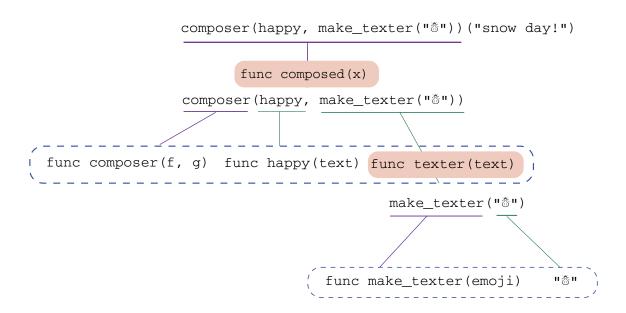


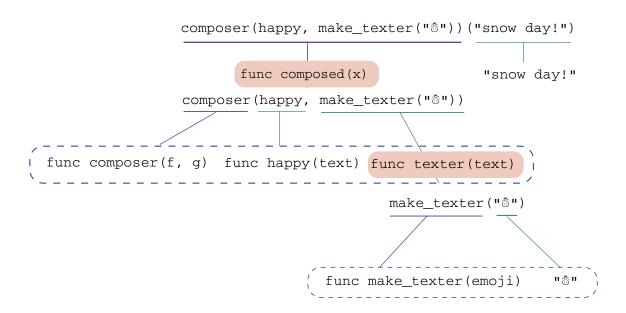


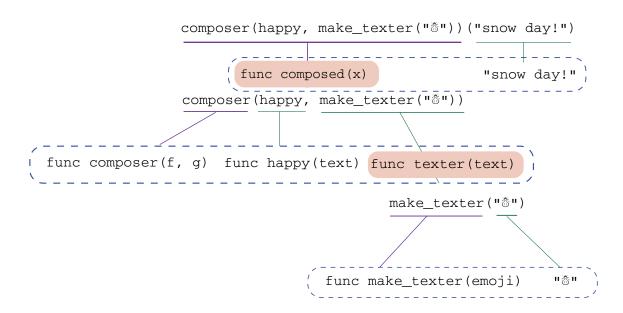


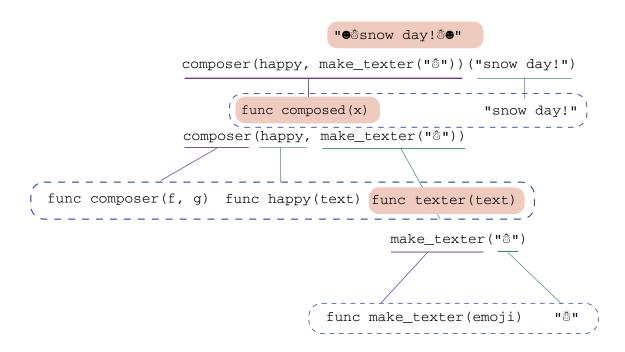












Currying

add vs. make_adder

Compare...

```
from operator import add
add(2, 3)
```

```
def make_adder(n):
    return lambda x: n + x

make_adder(2)(3)
```

What's the relationship between add(2, 3) and make_adder(2)(3)?

Function currying

Currying: Converting a function that takes multiple arguments into a single-argument higher-order function.

柯里化把一个多元函数转换为多个一元函数的链式调用

A function that currys any two-argument function:

```
def curry2(f):
    def g(x):
        def h(y):
          return f(x, y)
        return h
    return g
```

Function currying

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```
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```

```
make_adder = curry2(add)
make_adder(2)(3)
```

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A function that currys any two-argument function:

```
def curry2(f):
    def g(x):
        def h(y):
            return f(x, y)
        return h
    return g
make_adder = curry2(add)
make_adder(2)(3)
```

Why "currying"?

It's not food! X X

Named after American logician Haskell Curry, but actually published first by Russian Moses Schönfinkel, based on principles by German Gottlob Frege.

See also: Stigler's law of eponymy