



Tensorflow

<https://www.tensorflow.org/>

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- 학습 - 예제들

Tensorflow 2.0 설치하기

<https://www.tensorflow.org/install>

TensorFlow는 다음 64비트 시스템에서 테스트 및 지원됩니다.

- Python 3.5-3.7
- Ubuntu 16.04 이상
- Windows 7 이상
- macOS 10.12.6(Sierra) 이상(GPU 지원 없음)
- Raspbian 9.0 이상

```
# Requires the latest pip
pip install --upgrade pip

# Current stable release for CPU and
# GPU
pip install tensorflow

# Or try the preview build (unstable)
pip install tf-nightly
```



에서 설치된 환경 바로 사용 가능

Tensorflow.org 둘러보기

The screenshot shows the TensorFlow.org website. At the top, there is a navigation bar with the TensorFlow logo, followed by four main categories: 설치 (Installation), 학습 (Learning), API, and 리소스 (Resources). Below this is a secondary navigation bar for 'TensorFlow Core' with links for 개요 (Overview), 튜토리얼 (Tutorial), 가이드 (Guide), and TF 1. The main content area features a large orange graphic on the left and text in Korean. The text reads: 'TensorFlow는 머신러닝을 위한 드 오픈소스 플랫폼입니다.' (TensorFlow is an open-source platform for machine learning). It also states: 'TensorFlow를 사용하면 초보자와 전문가 모두 머신러닝 수 있습니다. 시작하려면 아래의 섹션을 참조하세요.' (With TensorFlow, both beginners and experts can learn machine learning. To get started, refer to the sections below.). There are two '가이드 보기' (View Guide) buttons. Below these buttons, there is explanatory text: '가이드에서는 완벽한 엔드 투 엔드 예제와 함께 TensorFlow를 사용하는 방법을 보여줍니다.' (The guide provides complete end-to-end examples and shows how to use TensorFlow.) and '가이드는 TensorFlow의 개념과 구성요소에 관해 설명합니다.' (The guide explains the concepts and components of TensorFlow).

1. **Tensorflow 설치 방법**
2. **Tensorflow 사용법 학습**
3. **Tensorflow API 문서**
4. **2.의 세부 페이지**
 - a. **개요**
 - b. **튜토리얼**
다양한 예제 및 설정법 포함
 - c. **가이드**
 - d. **TF 1**

TF 2.0 바로 시작하기 (MNIST tutorial)

초보자용

사용자에게 친숙한 Sequential API로 시작하는 것이 가장 좋습니다. 구 성요소를 연결하여 모델을 만들 수 있습니다. 아래의 'Hello World' 예제 를 실행한 다음 [가이드](#)를 방문하여 자세한 내용을 알아보세요.

ML에 관해 배워보려면 [교육 페이지를 확인하세요](#). 엄선된 커리큘럼으로 기본적인 ML 분야의 역량을 키워보세요.

```
import tensorflow as tf
mnist = tf.keras.datasets.mnist

(x_train, y_train), (x_test, y_test) = mnist.load_data()
x_train, x_test = x_train / 255.0, x_test / 255.0

model = tf.keras.models.Sequential([
    tf.keras.layers.Flatten(input_shape=(28, 28)),
    tf.keras.layers.Dense(128, activation='relu'),
    tf.keras.layers.Dropout(0.2),
    tf.keras.layers.Dense(10, activation='softmax')
])

model.compile(optimizer='adam',
              loss='sparse_categorical_crossentropy',
              metrics=['accuracy'])

model.fit(x_train, y_train, epochs=5)
model.evaluate(x_test, y_test)
```

[지금 코드 실행](#)

Google의 대화형 메모장에서 사용해보기

전문가용

Subclassing API는 고급 연구를 위한 define-by-run 인터페이스를 제공합니다. 모델에 대한 클래스를 만든 다음 명령형으로 순방향 패스를 작성합니다. 맞춤형 레이어, 활성화 및 학습 루프를 쉽게 만들 수 있습니다. 아래의 'Hello World' 예제를 실행한 다음 [가이드](#)를 방문하여 자세한 내용을 알아보세요.

```
class MyModel(tf.keras.Model):
    def __init__(self):
        super(MyModel, self).__init__()
        self.conv1 = Conv2D(32, 3, activation='relu')
        self.flatten = Flatten()
        self.d1 = Dense(128, activation='relu')
        self.d2 = Dense(10, activation='softmax')

    def call(self, x):
        x = self.conv1(x)
        x = self.flatten(x)
        x = self.d1(x)
        return self.d2(x)

model = MyModel()

with tf.GradientTape() as tape:
    logits = model(images)
    loss_value = loss(logits, labels)
grads = tape.gradient(loss_value, model.trainable_variables)
optimizer.apply_gradients(zip(grads, model.trainable_variables))
```

[지금 코드 실행](#)

Google의 대화형 메모장에서 사용해보기

필수 문서

TensorFlow 설치

패키지를 설치하거나 소스에서 빌드 합니다. CUDA® 지원 카드에 GPU 지원이 제공됩니다.

TensorFlow 2

코드를 이전하기 위한 TensorFlow 2 권장사항 및 도구입니다.

Keras

Keras는 ML 연구자뿐 아니라 초보자도 쉽게 사용할 수 있는 상위 수준 API입니다.

맞춤설정

연구 및 실험을 위한 TensorFlow입니다. 맞춤 레이어 및 모델, 정방향 전달, 학습 루프를 작성합니다.

데이터 입력 파이프라인

tf.data API를 사용하면 간단하고 재사용 가능한 조각으로 복잡한 입력 파이프라인을 빌드할 수 있습니다.

에스티메이터

확장 및 비동기 학습을 위해 설계된 완전한 모델을 나타내는 상위 수준 API입니다.

모델 저장

체크포인트 또는 저장된 모델 형식을 사용하여 TensorFlow 모델을 저장합니다.

가속기

여러 GPU, 여러 머신 또는 TPU에 학습을 배포합니다.

성능

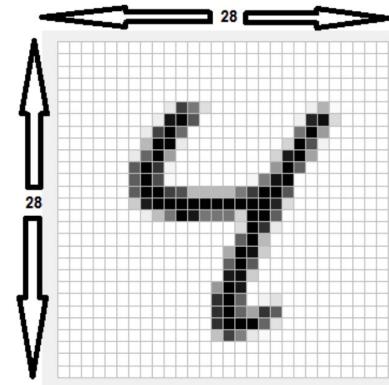
TensorFlow 성능 최적화를 위한 권장사항 및 최적화 기술

MNIST data

MNIST Dataset

000000000000000000
111111111111111111
222222222222222222
333333333333333333
444444444444444444
555555555555555555
666666666666666666
777777777777777777
888888888888888888
999999999999999999

28x28x1 image



train-images-idx3-ubyte.gz: training set images (9912422 bytes)

train-labels-idx1-ubyte.gz: training set labels (28881 bytes)

t10k-images-idx3-ubyte.gz: test set images (1648877 bytes)

t10k-labels-idx1-ubyte.gz: test set labels (4542 bytes)

TF 2.0 바로 시작하기

지난 시간까지 배운것들..

- 퍼셉트론
- 활성화 함수
- 다차원 배열의 계산
- 신경망 구현하기, 출력층 설계하기
- 데이터 추론
- 손실함수
- 미니배치
- 경사 하강법 (수치 미분), 오차역전파법

TF 2.0 바로 시작하기 (MNIST tutorial)

```
1 import tensorflow as tf
2 mnist = tf.keras.datasets.mnist
3
4 (x_train, y_train), (x_test, y_test) = mnist.load_data()
5 x_train, x_test = x_train / 255.0, x_test / 255.0
6
7 model = tf.keras.models.Sequential([
8     tf.keras.layers.Flatten(input_shape=(28, 28)),
9     tf.keras.layers.Dense(128, activation='relu'),
10    tf.keras.layers.Dropout(0.2),
11    tf.keras.layers.Dense(10, activation='softmax')
12])
13
14 model.compile(optimizer='adam',
15                 loss='sparse_categorical_crossentropy',
16                 metrics=['accuracy'])
17
18 model.fit(x_train, y_train, epochs=5)
19 model.evaluate(x_test, y_test)

↳ Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datasets/mnist.npz
11493376/11490434 [=====] - 0s 0us/step
Epoch 1/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.3037 - accuracy: 0.9113
Epoch 2/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.1473 - accuracy: 0.9562
Epoch 3/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.1129 - accuracy: 0.9662
Epoch 4/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.0912 - accuracy: 0.9718
Epoch 5/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.0783 - accuracy: 0.9755
313/313 [=====] - 1s 2ms/step - loss: 0.0822 - accuracy: 0.9763
[0.08216668665409088, 0.9763000011444092]
```

tf.keras.datasets

Modules

`boston_housing` module: Boston housing price regression dataset.

`cifar10` module: CIFAR10 small images classification dataset.

`cifar100` module: CIFAR100 small images classification dataset.

`fashion_mnist` module: Fashion-MNIST dataset.

`imdb` module: IMDB sentiment classification dataset.

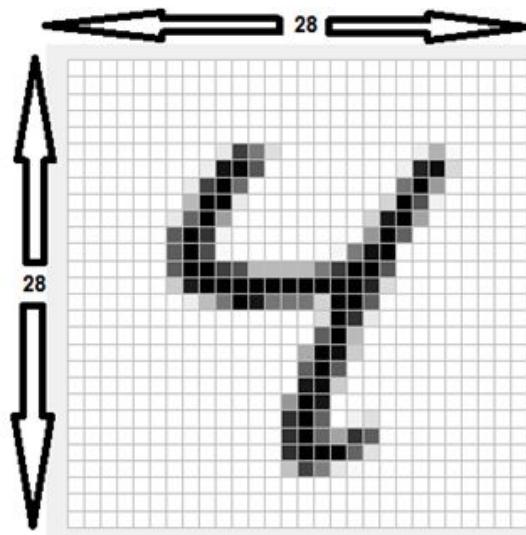
`mnist` module: MNIST handwritten digits dataset.

`reuters` module: Reuters topic classification dataset.

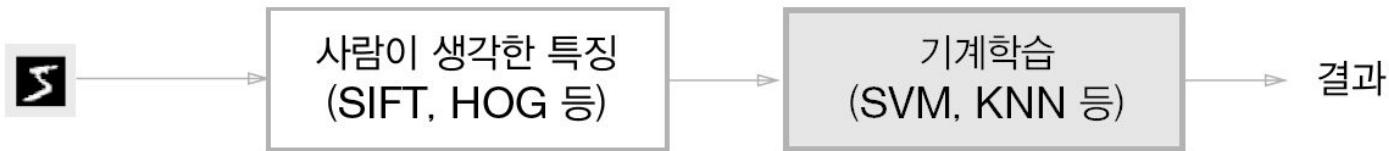
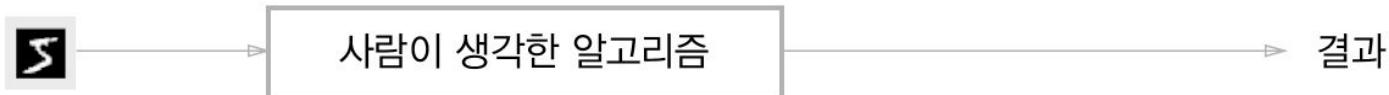
Training Neural Network

MNIST dataset

000000000000000000000000
1111111111111111111111
2222222222222222222222
3333333333333333333333
4444444444444444444444
5555555555555555555555
6666666666666666666666
7777777777777777777777
8888888888888888888888
9999999999999999999999

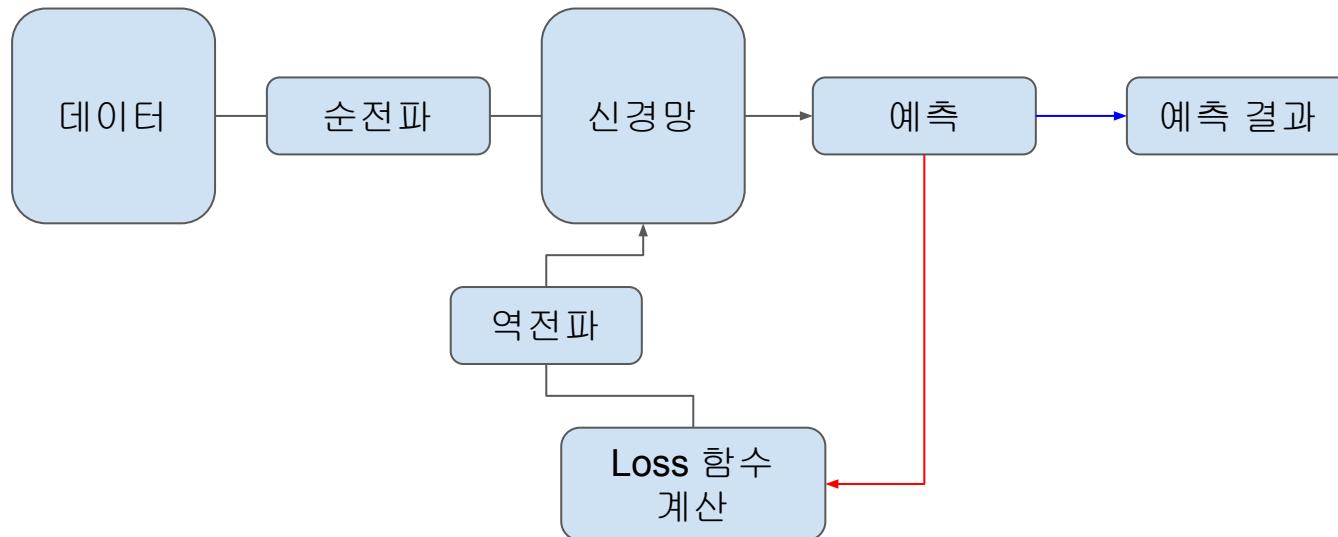


Training MNIST data



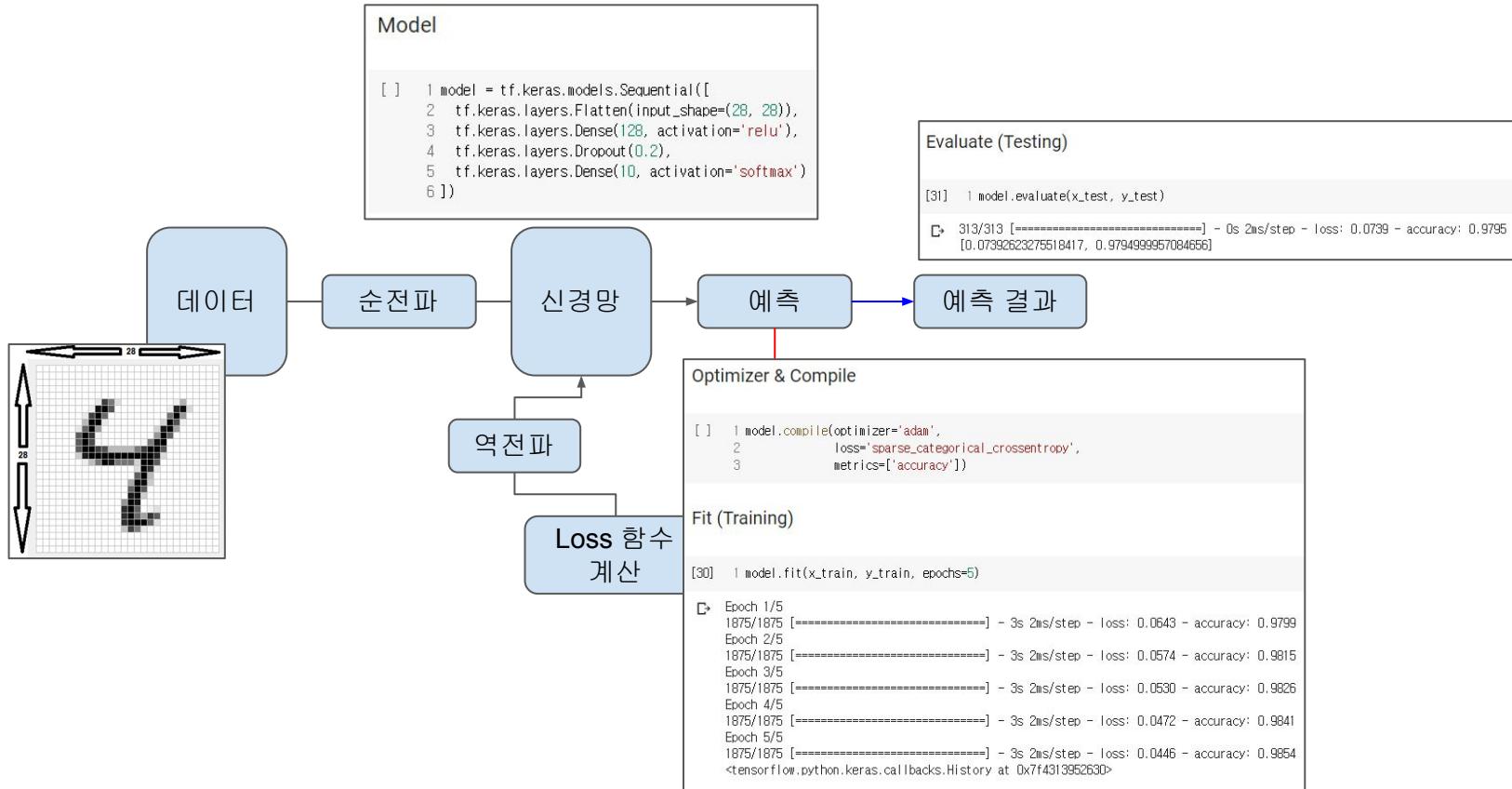
Training MNIST data

[Colab에서 학습해보기](#)



Training MNIST data

[Colab에서 학습해보기](#)



Training MNIST data

Model

```
[ ] 1 model = tf.keras.models.Sequential([
2   tf.keras.layers.Flatten(input_shape=(28, 28)),
3   tf.keras.layers.Dense(128, activation='relu'),
4   tf.keras.layers.Dropout(0.2),
5   tf.keras.layers.Dense(10, activation='softmax')
6 ])
```

```
[32] 1 model.summary()
```

↳ Model: "sequential"

Layer (type)	Output Shape	Param #
flatten (Flatten)	(None, 784)	0
dense (Dense)	(None, 128)	100480
dropout (Dropout)	(None, 128)	0
dense_1 (Dense)	(None, 10)	1290

Total params: 101,770
Trainable params: 101,770
Non-trainable params: 0

Optimizer & Compile

```
[ ] 1 model.compile(optimizer='adam',
2                     loss='sparse_categorical_crossentropy',
3                     metrics=['accuracy'])
```

Fit (Training)

```
[30] 1 model.fit(x_train, y_train, epochs=5)
```

↳ Epoch 1/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.0643 - accuracy: 0.9799
Epoch 2/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.0574 - accuracy: 0.9815
Epoch 3/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.0530 - accuracy: 0.9826
Epoch 4/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.0472 - accuracy: 0.9841
Epoch 5/5
1875/1875 [=====] - 3s 2ms/step - loss: 0.0446 - accuracy: 0.9854
<tensorflow.python.keras.callbacks.History at 0x7f4313952630>

Evaluate (Testing)

```
[31] 1 model.evaluate(x_test, y_test)
```

↳ 313/313 [=====] - 0s 2ms/step - loss: 0.0739 - accuracy: 0.9795
[0.07392623275518417, 0.9794999957084656]

Training MNIST data

Model

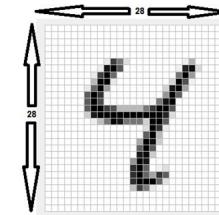
```
[ ] 1 model = tf.keras.models.Sequential([
2   tf.keras.layers.Flatten(input_shape=(28, 28)),
3   tf.keras.layers.Dense(128, activation='relu'),
4   tf.keras.layers.Dropout(0.2),
5   tf.keras.layers.Dense(10, activation='softmax')
6 ])
```

```
[32] 1 model.summary()
```

Model: "sequential"

Layer (type)	Output Shape	Param #
flatten (Flatten)	(None, 784)	0
dense (Dense)	(None, 128)	100480
dropout (Dropout)	(None, 128)	0
dense_1 (Dense)	(None, 10)	1290

Total params: 101,770
Trainable params: 101,770
Non-trainable params: 0



Flatten

input layer

Dense

hidden layer

Dropout



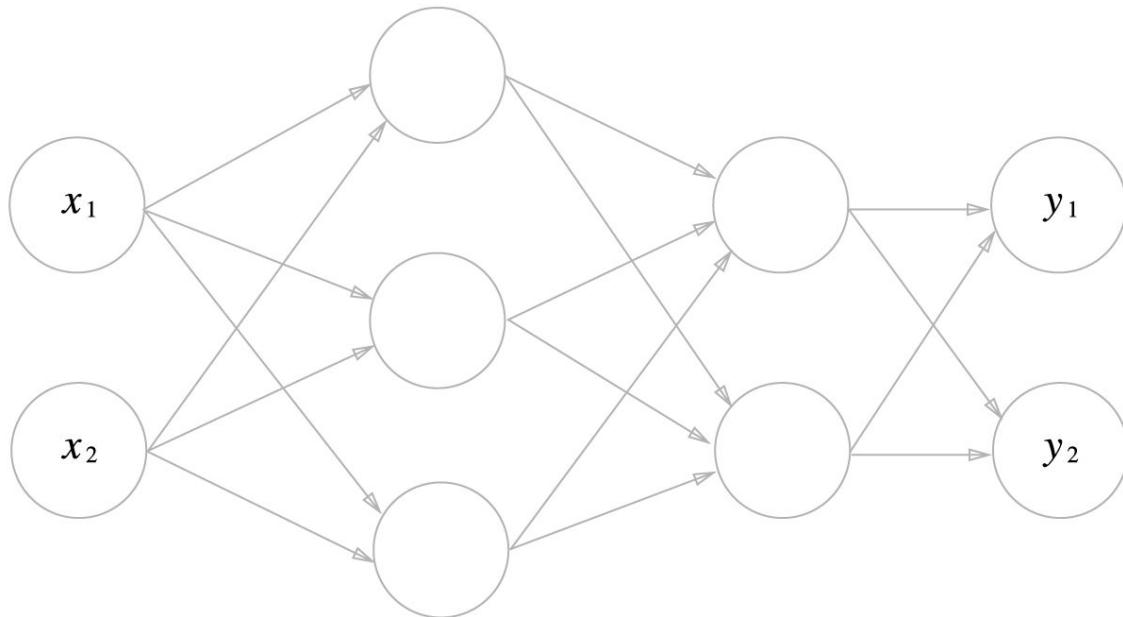
output layer

Training MNIST data

- Dense? Flatten?
- Dropout?
- softmax? relu?
- loss?
- optimizer?
- epochs?

Training MNIST data

- Dense? Flatten?
- Dropout?
- softmax? relu?
- loss?
- optimizer?
- epochs?



epoch / batch / iterations

In the neural network terminology:

one **epoch** = one forward pass and one backward pass of *all* the training examples

batch size = the number of training examples in one forward/backward pass. The higher the batch size, the more memory space you'll need.

number of **iterations** = number of passes, each pass using [batch size] number of examples. To be clear, one pass = one forward pass + one backward pass (we do not count the forward pass and backward pass as two different passes).

Example: if you have *1000 training examples*, and your *batch size is 500*, then it will take 2 iterations to complete 1 epoch.

epoch / batch / iterations

In the neural network terminology:

전체 Training example 단위

one **epoch** - one forward pass and one backward pass of *all* the training examples

한번에 학습 하는 단위

batch size - the number of training examples you'll need.

number of **iterations** - number of passes
one forward pass + one backward pass (with each pass covering $\frac{1}{n}$ of the training examples. To be clear, one pass = one forward pass + one backward pass as two different passes).

Example: if you have 1000 training examples, and your batch size is 500, then it will take 2 iterations to complete 1 epoch.

1000개의 Training Example이 있고, **batch size**가 500이면,
1 epoch을 위해 2의 **iteration**이 필요하다

tf.keras.datasets

https://www.tensorflow.org/api_docs/python/tf/keras/datasets

TensorFlow > API > TensorFlow Core v2.3.0 > Python

Module: tf.keras.datasets



Public API for tf.keras.datasets namespace.

Modules

`boston_housing` module: Boston housing price regression dataset.

`cifar10` module: CIFAR10 small images classification dataset.

`cifar100` module: CIFAR100 small images classification dataset.

`fashion_mnist` module: Fashion-MNIST dataset.

`imdb` module: IMDB sentiment classification dataset.

`mnist` module: MNIST handwritten digits dataset.

`reuters` module: Reuters topic classification dataset.

`dataframe` `boston_housing` module: Boston housing price **regression** dataset.

`image` `cifar10` module: CIFAR10 small **images classification** dataset.

`image` `cifar100` module: CIFAR100 small **images classification** dataset.

`image` `fashion_mnist` module: Fashion-MNIST dataset.

`text` `imdb` module: IMDB **sentiment** classification dataset.

`image` `mnist` module: MNIST handwritten **digits** dataset.

`text` `reuters` module: Reuters **topic** classification dataset.

```
1 boston_data = tf.keras.datasets.module name
2 (x_train, y_train), (x_test, y_test) = boston_data.load_data()
```

dataset 자세히 보기 - boston_housing 예시

The screenshot shows the TensorFlow Core v2.3.0 API documentation for Python. The left sidebar navigation tree is partially highlighted with red boxes around the `tf.keras`, `datasets`, and `boston_housing` sections. The main content area displays the `tf.keras.datasets.boston_housing.load_data` function. The function signature is shown as:

```
tf.keras.datasets.boston_housing.load_data(  
    path='boston_housing.npz', test_split=0.2, seed=113  
)
```

The description below the signature states: "This is a dataset taken from the StatLib library which is maintained at Carnegie Mellon University. Samples contain 13 attributes of houses at different locations around the Boston suburbs in the late 1970s. Targets are the median values of the houses at a location (in k\$).". A note at the bottom says: "The attributes themselves are defined in the [StatLib website](#)".

dataset 자세히 보기 - boston_housing 예시

← → ⌂ ⌂ 안전하지 않음 | lib.stat.cmu.edu/datasets/boston

The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic prices and the demand for clean air', J. Environ. Economics & Management, vol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnostics ... , Wiley, 1980. N.B. Various transformations are used in the table on pages 244-261 of the latter.

Variables in order:

CRIM	per capita crime rate by town
ZN	proportion of residential land zoned for lots over 25,000 sq.ft.
INDUS	proportion of non-retail business acres per town
CHAS	Charles River dummy variable (= 1 if tract bounds river; 0 otherwise)
NOX	nitric oxides concentration (parts per 10 million)
RM	average number of rooms per dwelling
AGE	proportion of owner-occupied units built prior to 1940
DIS	weighted distances to five Boston employment centres
RAD	index of accessibility to radial highways
TAX	full-value property-tax rate per \$10,000
PTRATIO	pupil-teacher ratio by town
B	$1000(Bk - 0.63)^2$ where Bk is the proportion of blacks by town
LSTAT	% lower status of the population
MEDV	Median value of owner-occupied homes in \$1000's

0.00632	18.00	2.310	0	0.5380	6.5750	65.20	4.0900	1	296.0	15.30
396.90	4.98	24.00								
0.02731	0.00	7.070	0	0.4690	6.4210	78.90	4.9671	2	242.0	17.80
396.90	9.14	21.60								

```
1 boston_data = tf.keras.datasets.boston_housing  
2 (x_train, y_train), (x_test, y_test) = boston_data.load_data()  
  
1 x_train[0]  
  
array([ 1.23247,  0.        ,  8.14        ,  0.        ,  0.538        ,  
       6.142        ,  
       91.7        ,  3.9769        ,  4.        ,  307.        ,  21.        ,  396.9        ,  
      18.72       ])
```

Sequential 모델

Sequential 모델은 각 레이어에 정확히 하나의 입력 텐서와 하나의 출력 텐서가 있는 일반 레이어 스택에 적합합니다.

```
# Define Sequential model with 3 layers
model = keras.Sequential(
    [
        layers.Dense(2, activation="relu", name="layer1"),
        layers.Dense(3, activation="relu", name="layer2"),
        layers.Dense(4, name="layer3"),
    ]
)
# Call model on a test input
x = tf.ones((3, 3))
y = model(x)
```

```
# Create 3 layers
layer1 = layers.Dense(2, activation="relu", name="layer1")
layer2 = layers.Dense(3, activation="relu", name="layer2")
layer3 = layers.Dense(4, name="layer3")

# Call layers on a test input
x = tf.ones((3, 3))
y = layer3(layer2(layer1(x)))
```

Sequential 모델

Sequential 모델은 다음의 경우에 적합하지 않습니다.

- 모델에 다중 입력 또는 다중 출력이 있습니다
- 레이어에 **다중 입력** 또는 **다중 출력**이 있습니다
- 레이어 공유를 해야 합니다
- 비선형 토플로지를 원합니다(예: 잔류 연결, 다중 분기 모델)

Sequential 모델

Layer의 추가와 삭제

`add()` 메서드를 통해 Sequential 모델을 점진적으로 작성할 수도 있습니다.

```
model = keras.Sequential()
model.add(layers.Dense(2, activation="relu"))
model.add(layers.Dense(3, activation="relu"))
model.add(layers.Dense(4))
```

레이어를 제거하는 `pop()` 메서드도 있습니다. Sequential 모델은 레이어의 리스트와 매우 유사하게 동작합니다.

```
model.pop()
print(len(model.layers)) # 2
```

Training CIFAR data

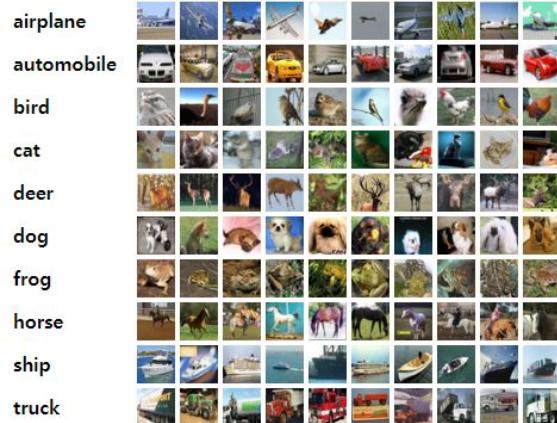
<https://www.cs.toronto.edu/~kriz/cifar.html>

The CIFAR-10 dataset

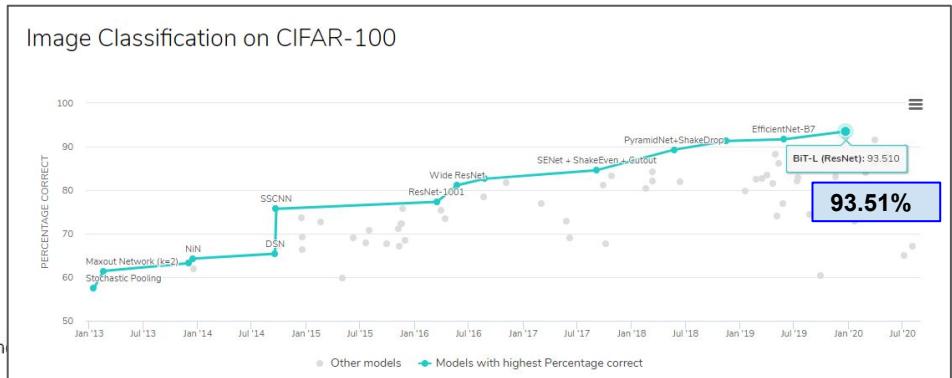
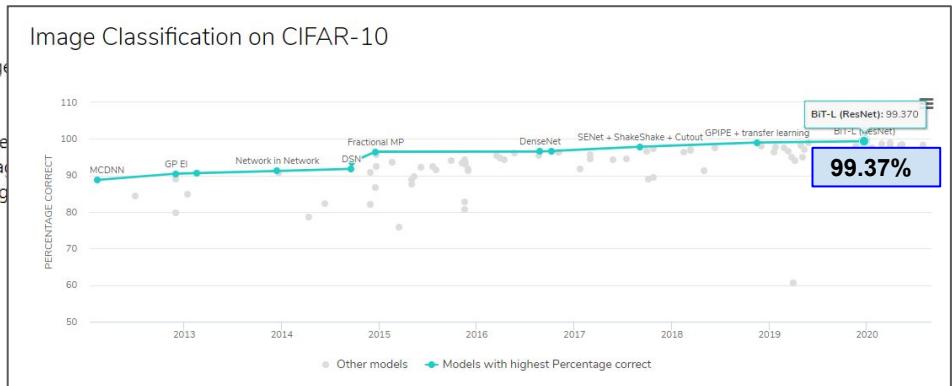
The CIFAR-10 dataset consists of 60000 32x32 colour images in 10 classes, with 6000 image images and 10000 test images.

The dataset is divided into five training batches and one test batch, each with 10000 image randomly-selected images from each class. The training batches contain the remaining images. The batches may contain more images from one class than another. Between them, the training batches from each class.

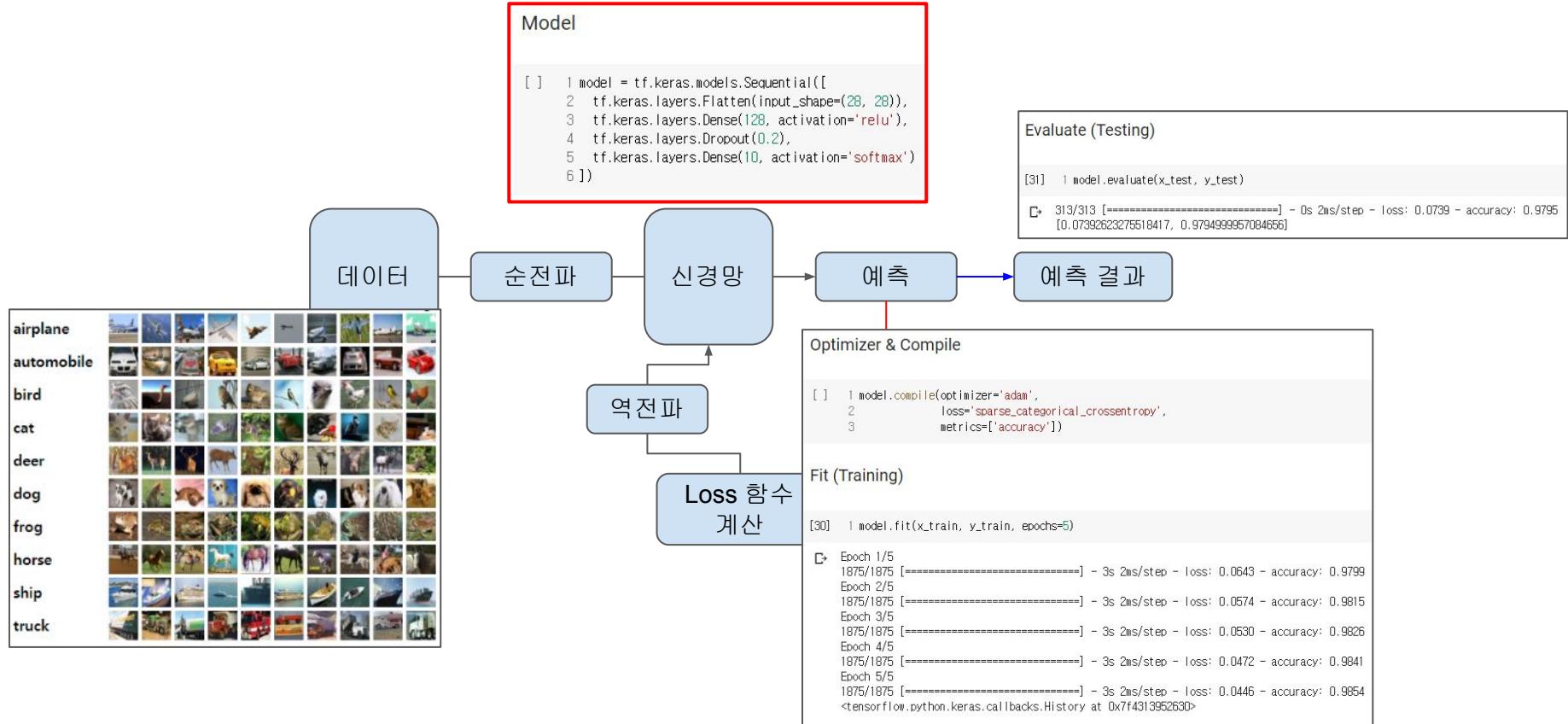
Here are the classes in the dataset, as well as 10 random images from each:



The classes are completely mutually exclusive. There is no overlap between automobiles and SUVs, things of that sort. "Truck" includes only big trucks. Neither includes pickup trucks.



Training CIFAR-10 data



Training CIFAR-10 data

MNIST 학습에 사용했던 모델을 그대로 사용해본다

```
1 model = tf.keras.models.Sequential([
2     tf.keras.layers.Flatten(input_shape=x_shape),
3     tf.keras.layers.Dense(128, activation='relu'),
4     tf.keras.layers.Dropout(0.2),
5     tf.keras.layers.Dense(10, activation='softmax')
6 ])
7
8 model.summary()
9
10 model.compile(optimizer='adam',
11                 loss='sparse_categorical_crossentropy',
12                 metrics=['accuracy'])
13
14 model.fit(x_train, y_train, epochs=5)
15 model.evaluate(x_test, y_test)
```

Model: "sequential_4"

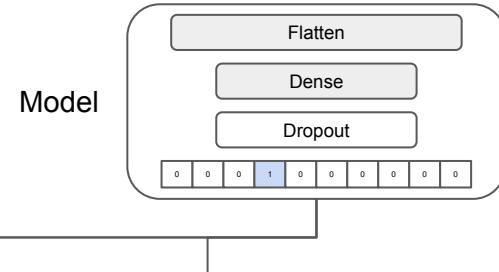
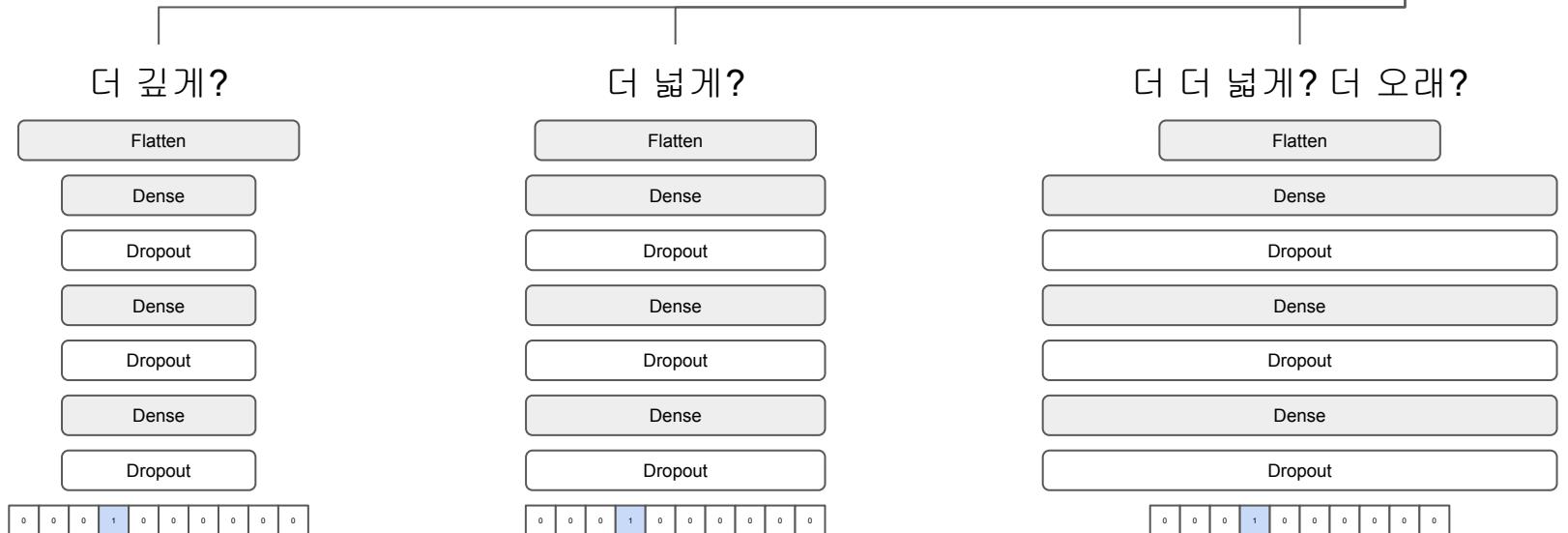
Layer (type)	Output Shape	Param #
flatten_4 (Flatten)	(None, 3072)	0
dense_13 (Dense)	(None, 128)	393344
dropout_9 (Dropout)	(None, 128)	0
dense_14 (Dense)	(None, 10)	1290

Total params: 394,634
Trainable params: 394,634
Non-trainable params: 0

```
Epoch 1/5
1563/1563 [=====] - 3s 2ms/step - loss: 2.0212 - accuracy: 0.2469
Epoch 2/5
1563/1563 [=====] - 3s 2ms/step - loss: 1.9198 - accuracy: 0.2915
Epoch 3/5
1563/1563 [=====] - 4s 2ms/step - loss: 1.8924 - accuracy: 0.3037
Epoch 4/5
1563/1563 [=====] - 3s 2ms/step - loss: 1.8731 - accuracy: 0.3095
Epoch 5/5
1563/1563 [=====] - 3s 2ms/step - loss: 1.8685 - accuracy: 0.3129
313/313 [=====] - 1s 2ms/step - loss: 1.7859 - accuracy: 0.3615
[1.7859476804733276, 0.36149999499320984]
```

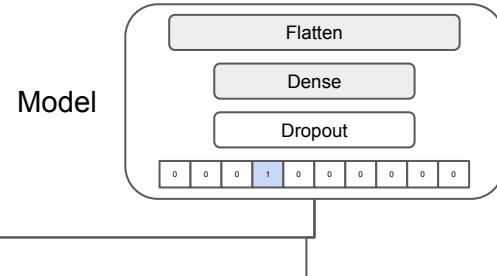
```
1563/1563 [=====] - 3s 2ms/step - loss: 1.8540 - accuracy: 0.3254
Epoch 16/20
1563/1563 [=====] - 3s 2ms/step - loss: 1.8519 - accuracy: 0.3254
Epoch 17/20
1563/1563 [=====] - 4s 2ms/step - loss: 1.8470 - accuracy: 0.3269
Epoch 18/20
1563/1563 [=====] - 3s 2ms/step - loss: 1.8527 - accuracy: 0.3254
Epoch 19/20
1563/1563 [=====] - 3s 2ms/step - loss: 1.8473 - accuracy: 0.3274
Epoch 20/20
1563/1563 [=====] - 4s 2ms/step - loss: 1.8416 - accuracy: 0.3273
313/313 [=====] - 1s 2ms/step - loss: 1.7571 - accuracy: 0.3696
[1.7570570707321167, 0.36959999799728394]
```

Training CIFAR-10 data



[Colab에서 확인하기](#)

Training CIFAR-10 data



더 깊게?

Layer (type)	Output Shape	Param #
flatten_10 (Flatten)	(None, 3072)	0
dense_34 (Dense)	(None, 128)	393344
dropout_21 (Dropout)	(None, 128)	0
dense_35 (Dense)	(None, 128)	16512
dropout_22 (Dropout)	(None, 128)	0
dense_36 (Dense)	(None, 128)	16512
dropout_23 (Dropout)	(None, 128)	0
dense_37 (Dense)	(None, 10)	1290
Total params:	427,658	
Trainable params:	427,658	
Non-trainable params:	0	

427,658

accuracy: 0.3549

더 넓게?

Layer (type)	Output Shape	Param #
flatten_11 (Flatten)	(None, 3072)	0
dense_38 (Dense)	(None, 256)	786688
dropout_24 (Dropout)	(None, 256)	0
dense_39 (Dense)	(None, 256)	65792
dropout_25 (Dropout)	(None, 256)	0
dense_40 (Dense)	(None, 256)	65792
dropout_26 (Dropout)	(None, 256)	0
dense_41 (Dense)	(None, 256)	65792
dropout_27 (Dropout)	(None, 256)	0
dense_42 (Dense)	(None, 10)	2570
Total params:	986,634	
Trainable params:	986,634	
Non-trainable params:	0	

986,634

accuracy: 0.3814

더 더 넓게? & 더 오래?

Layer (type)	Output Shape	Param #
flatten_12 (Flatten)	(None, 3072)	0
dense_43 (Dense)	(None, 1024)	3146752
dropout_28 (Dropout)	(None, 1024)	0
dense_44 (Dense)	(None, 1024)	1049600
dropout_29 (Dropout)	(None, 1024)	0
dense_45 (Dense)	(None, 1024)	1049600
dropout_30 (Dropout)	(None, 1024)	0
dense_46 (Dense)	(None, 1024)	1049600
dropout_31 (Dropout)	(None, 1024)	0
dense_47 (Dense)	(None, 10)	10250
Total params:	6,305,802	
Trainable params:	6,305,802	
Non-trainable params:	0	

6,305,802

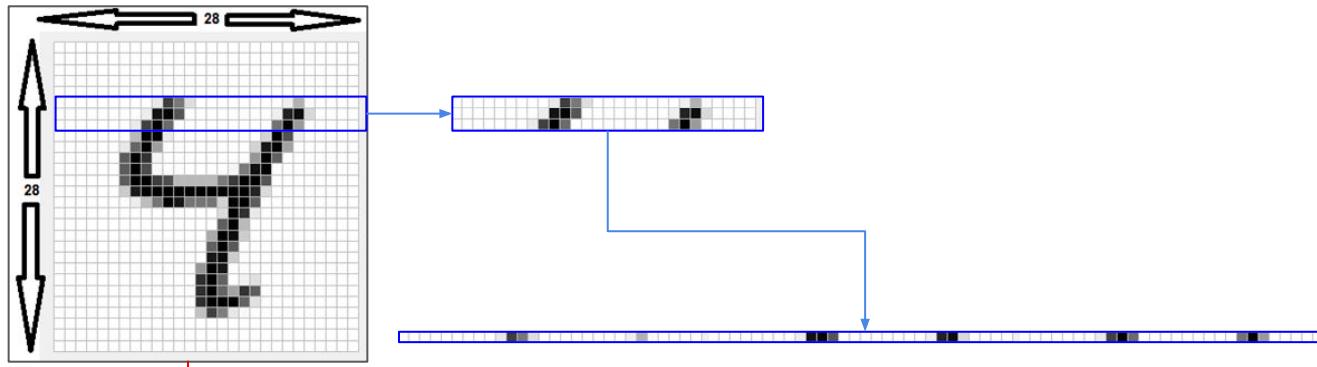
accuracy: 0.4127 / accuracy: 0.4251

20 epoch

100 epoch

성능이 개선되지 않는 이유?

Fully connected layer (Dense layer)의 한계



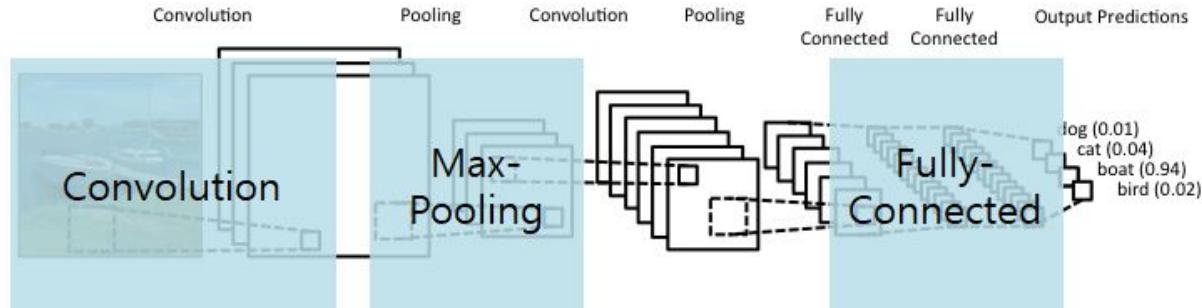
Flatten data

데이터의 형상이 무시되는 문제점이 있음

```
model = tf.keras.models.Sequential([
    tf.keras.layers.Flatten(input_shape=(28, 28)),
    tf.keras.layers.Dense(128, activation='relu'),
    tf.keras.layers.Dropout(0.2),
    tf.keras.layers.Dense(10, activation='softmax')
])
```

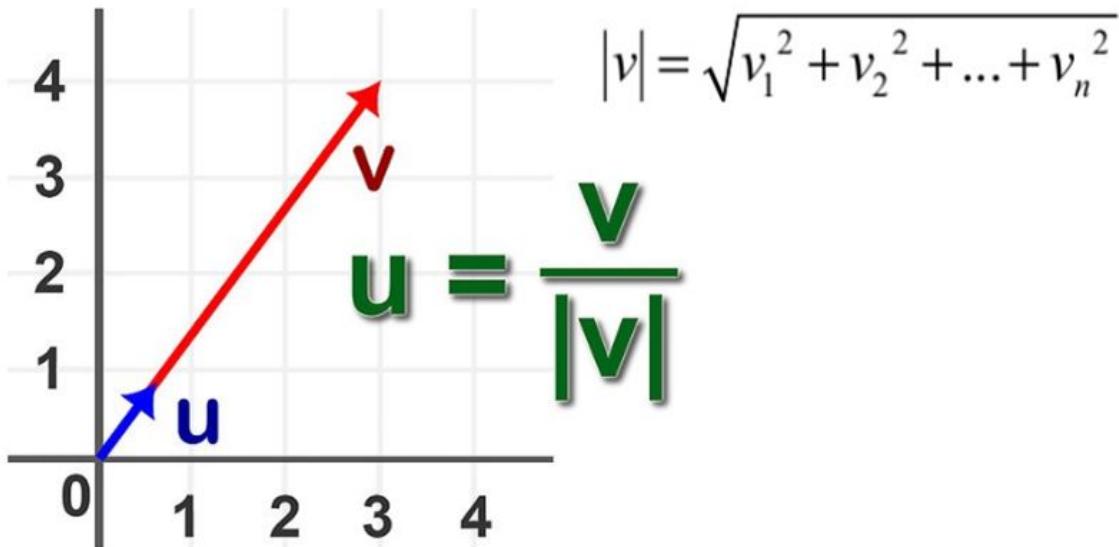
Convolutional Neural Network (합성곱 신경망)

- Layer의 구성
 - Convolution Layer – Feature 추출
 - Max-Pooling Layer – Local Search
 - Fully-Connected Layer – 최종 분류



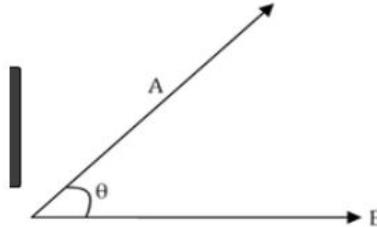
Convolution Layer

- 정규화 (Normalization)
- 벡터를 자신의 길이로 나누어 주면 길이가 1이고 방향만 남은 단위벡터가 됨
- 벡터의 길이는 벡터의 norm 이라고도 함



Convolution Layer

- 벡터의 내적 (Inner Product)
- 내적의 기하학적 의미는 A를 B로 사영시킨 선분의 길이와 B의 길이의 곱



$$\vec{A} \cdot \vec{B} = \|\vec{A}\| \|\vec{B}\| \cos \theta$$
$$\cos \theta = \frac{\vec{A} \cdot \vec{B}}{\|\vec{A}\| \|\vec{B}\|}$$
$$\theta = \cos^{-1} \left(\frac{\vec{A} \cdot \vec{B}}{\|\vec{A}\| \|\vec{B}\|} \right)$$

- 식으로 나타내면 다음과 같다

$$= x_1y_1 + x_2y_2 + \cdots + x_ny_n = \sum_{i=1}^n x_iy_i$$

$$= \mathbf{x}^T \mathbf{y} = \mathbf{y}^T \mathbf{x}$$

Convolution Layer

- 정규화 + 내적 = $\cos(\theta)$
- 앞선 내적 공식에서 $\cos(\theta)$ 값은 다음과 같이 구할 수 있다

$$\cos \theta = \frac{\overrightarrow{A} \cdot \overrightarrow{B}}{\|\overrightarrow{A}\| \|\overrightarrow{B}\|}$$

- 정규화를 시키면 분모의 A,B벡터의 길이가 1이므로 A,B의 내적이 $\cos(\theta)$ 값이 됨
- 두 벡터의 $\cos(\theta)$ 값은 두 벡터의 유사성을 비교하는 척도로 사용 가능 (높을수록 유사, 낮을수록 이질)

Convolution Layer

- **Concatenate**
- 2개의 열벡터 A,B가 있다면

A	B
1	2
2	4
3	6

- concat(A,B) by x 축
- concat(A,B) by y축
- concat(A,B) by z축

A,B	
A	B
1	2
2	4
3	6

1
2
3
2
4
6

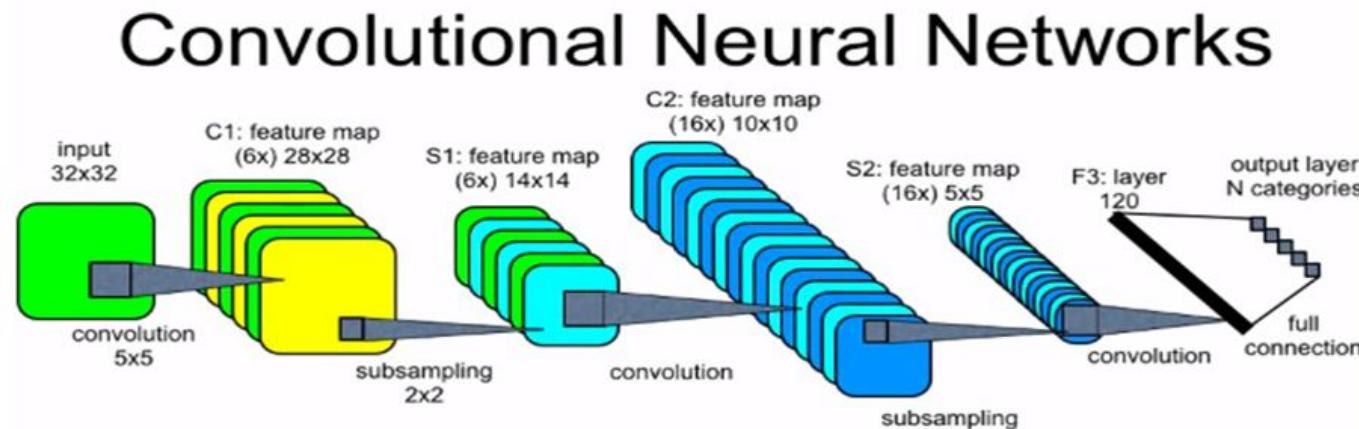
A
1
2
3

벡터가 아닌 행렬 또는 n차원 tensor에도 동일하게 적용

Convolutional Neural Network (합성곱 신경망)

음성인식, 이미지 인식과 같은 2차원 데이터를 처리하기 좋은 딥 러닝 알고리즘

1. Feature 추출 (Convolution Stage, Cn)
2. Subsampling, Sn
3. 위 두 stage를 1차원 벡터 (그림에서는 F3)가 나올 때까지 반복
4. Classification

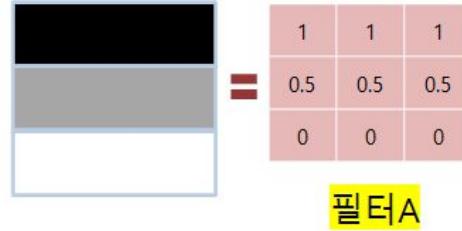


Convolution Layer

흰색을 0, 회색을 0.5, 검정을 1이라고 했을 때 아래 이미지에서 오른쪽과 같은 특징을 찾고 싶다고 한다면



원래 이미지



필터 A

||

0	0	0	0	0	0	0	0	0
0	1	1	1	0	0.5	0	0	0
0	0.5	0.5	0	0.5	0	0	0	0
0	0	0	1	1	1	1	0	0
0	1	0.5	0.5	0.5	0.5	0	0	0
0	0	1	0	1	0	0	0	0
0	0	0	0	0	0	0	0	0



정규화 + Convolution!! (합성곱)

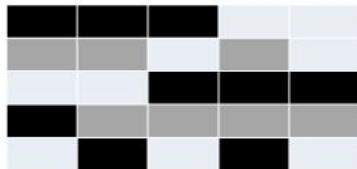
$$\begin{matrix} 1 & 2 \\ 3 & 4 \end{matrix} * \begin{matrix} 5 & 6 \\ 7 & 8 \end{matrix} = 1 \times 5 + 2 \times 6 + 3 \times 7 + 4 \times 8 = 70$$

중앙 파란색은 원래 이미지,
주변의 옅은 색은 차원을 유지하고 경
계를 구분하는 역할 (선택)

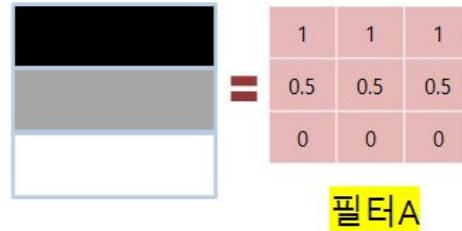
Convolution은 지정된 범위에서의 벡터
내적이며 정규화가 되어 있으므로
코사인유사도와 의미가 정확히 같음

Convolution Layer

흰색을 0, 회색을 0.5, 검정을 1이라고 했을 때 아래 이미지에서 오른쪽과 같은 특징을 찾고 싶다고 한다면



원래 이미지



필터 A

II

0	0	0	0	0	0	0	0
0	1	1	1	0	0.5	0	0
0	0.5	0.5	0	0.5	0	0	0
0	0	0	1	1	1	0	0
0	1	0.5	0.5	0.5	0.5	0	0
0	0	1	0	1	0	0	0
0	0	0	0	0	0	0	0

중앙 파란색은 원래 이미지,
주변의 옅은 색은 차원을 유지하고 경
계를 구분하는 역할 (선택)



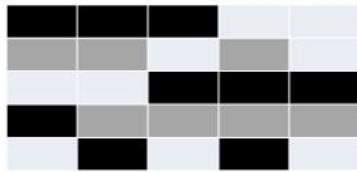
정규화 + Convolution!! (합성곱)

$$\begin{matrix} 1 & 2 \\ 3 & 4 \end{matrix} * \begin{matrix} 5 & 6 \\ 7 & 8 \end{matrix} = 1 \times 5 + 2 \times 6 + 3 \times 7 + 4 \times 8 = 70$$

Convolution은 지정된 범위에서의 벡터
내적이며 정규화가 되어 있으므로
코사인유사도와 의미가 정확히 같음

Convolution Layer

흰색을 0, 회색을 0.5, 검정을 1이라고 했을 때 아래 이미지에서 오른쪽과 같은 특징을 찾고 싶다고 한다면



원래 이미지



필터 A

II

0	0	0	0	0	0	0	0
0	1	1	1	0	0.5	0	0
0	0.5	0.5	0	0.5	0	0	0
0	0	0	1	1	1	1	0
0	1	0.5	0.5	0.5	0.5	0	0
0	0	1	0	1	0	0	0
0	0	0	0	0	0	0	0

중앙 파란색은 원래 이미지,
주변의 옅은 색은 차원을 유지하고 경
계를 구분하는 역할 (선택)



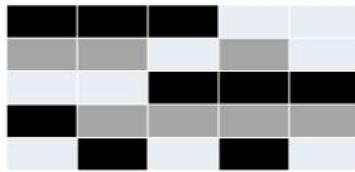
정규화 + Convolution!! (합성곱)

$$\begin{matrix} 1 & 2 \\ 3 & 4 \end{matrix} * \begin{matrix} 5 & 6 \\ 7 & 8 \end{matrix} = 1 \times 5 + 2 \times 6 + 3 \times 7 + 4 \times 8 = 70$$

Convolution은 지정된 범위에서의 벡터
내적이며 정규화가 되어 있으므로
코사인유사도와 의미가 정확히 같음

Convolution Layer

흰색을 0, 회색을 0.5, 검정을 1이라고 했을 때 아래 이미지에서 오른쪽과 같은 특징을 찾고 싶다고 한다면



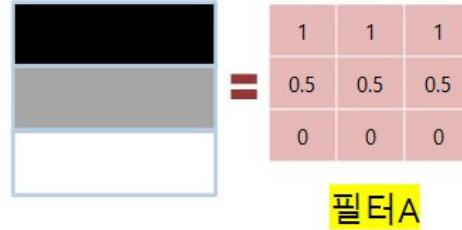
원래 이미지

||

0	0	0	0	0	0	0	0
0	1	1	1	0	0.5	0	0
0	0.5	0.5	0	0.5	0	0	0
0	0	0	1	1	1	1	0
0	1	0.5	0.5	0.5	0.5	0.5	0
0	0	1	0	1	0	0	0
0	0	0	0	0	0	0	0

필터A

중앙 파란색은 원래 이미지,
주변의 옅은 색은 차원을 유지하고 경
계를 구분하는 역할 (선택)



정규화 + Convolution!! (합성곱)

$$\begin{matrix} 1 & 2 \\ 3 & 4 \end{matrix} * \begin{matrix} 5 & 6 \\ 7 & 8 \end{matrix} = 1 \times 5 + 2 \times 6 + 3 \times 7 + 4 \times 8 = 70$$

Convolution은 지정된 범위에서의 벡터
내적이며 정규화가 되어 있으므로
코사인유사도와 의미가 정확히 같음

Convolution Layer

- Filter의 연산을 직접 해 봅시다!

0	0	0	0	0	0	0	0
0	1	1	1	0	0.5	0	*
0	0.5	0.5	0	0.5	0	0	필터A
0	0	0	1	1	1	0	
0	1	0.5	0.5	0.5	0.5	0	
0	0	1	0	1	0	0	
0	0	0	0	0	0	0	

- 1. 정규화를 거쳐

0.471	0.471	0.471
0.236	0.236	0
0	0	0.471

*

0.516	0.516	0.516
0.258	0.258	0.258
0	0	0

- 2. Convolution을 하면

$$0.471 * 0.516 + 0.471 * 0.516 + \dots + 0.471 * 0 = \underline{\underline{0.852}}$$

- 수학적 의미를 염밀하게 따지지 않는다면 해당 영역이 필터와 85.2% 유사하다고 생각하여도 무방

Convolution Layer

- 이 과정을 모든 영역에 적용하면?

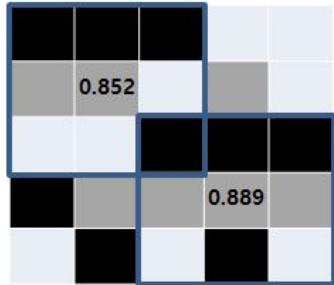
0	0	0	0	0	0	0	0
0	1	1	1	0	0.5	0	0
0	0.5	0.5	0	0.5	0	0	0
0	0	0	1	1	1	0	0
0	1	0.5	0.5	0.5	0.5	0	0
0	0	1	0	1	0	0	0
0	0	0	0	0	0	0	0

*

1	1	1
0.5	0.5	0.5
0	0	0

=

0.327	0.414	0.327	0.316	0.183
0.816	0.852	0.609	0.426	0.245
0.390	0.447	0.573	0.516	0.467
0.258	0.552	0.652	0.889	0.690
0.689	0.816	0.778	0.781	0.632



원래 이미지



필터A

원래 이미지에서 필터A와 가장
유사한 부분은 파란 테두리 부분!

이런 필터를 여러개 사용하여
Concatenate

Convolution Layer

- Convolution filter의 예시

- Sharpen

0	0	0	0	0
0	0	-1	0	0
0	-1	5	-1	0
0	0	-1	0	0
0	0	0	0	0



- Edge Detect

0	1	0
1	-4	1
0	1	0



- Blur

0	0	0	0	0
0	1	1	1	0
0	1	1	1	0
0	1	1	1	0
0	0	0	0	0



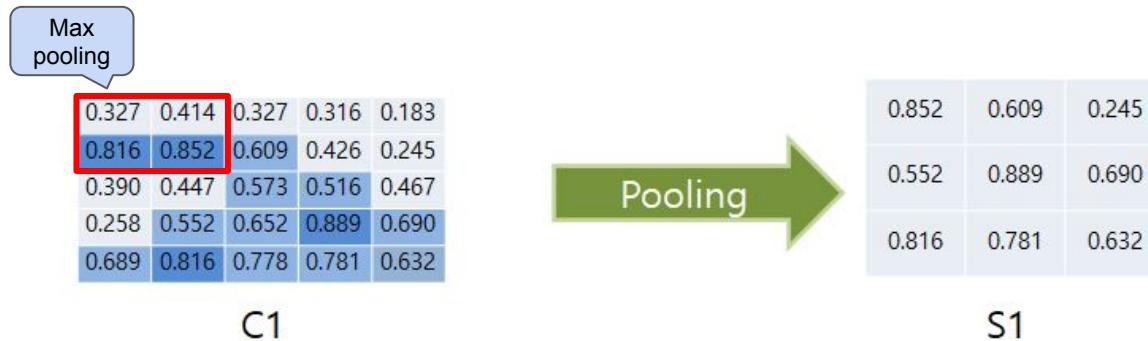
- Emboss

-2	-1	0
-1	1	1
0	1	2



Pooling Layer

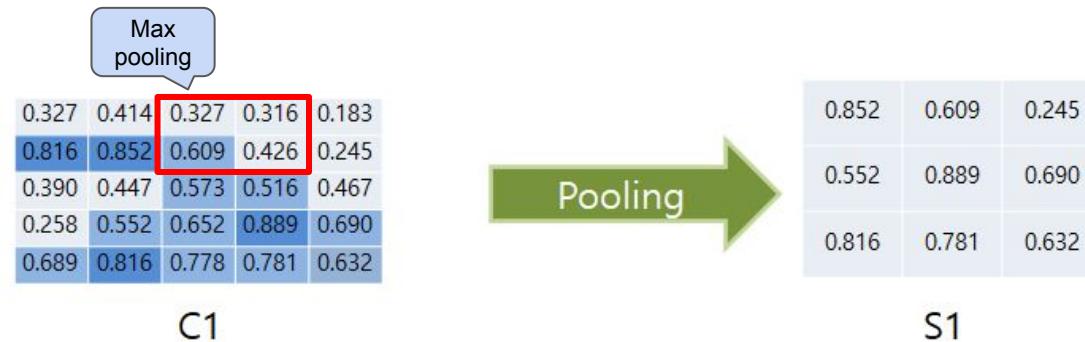
- Convolution을 실행한 C1에서 특징 (통상적으로 2x2 4칸 중 가장 큰 값을 고르는 Max Pooling을 사용)을 추려 냄



- S1을 새로운 Input처럼 생각하며 Convolution과 Subsampling을 반복

Pooling Layer

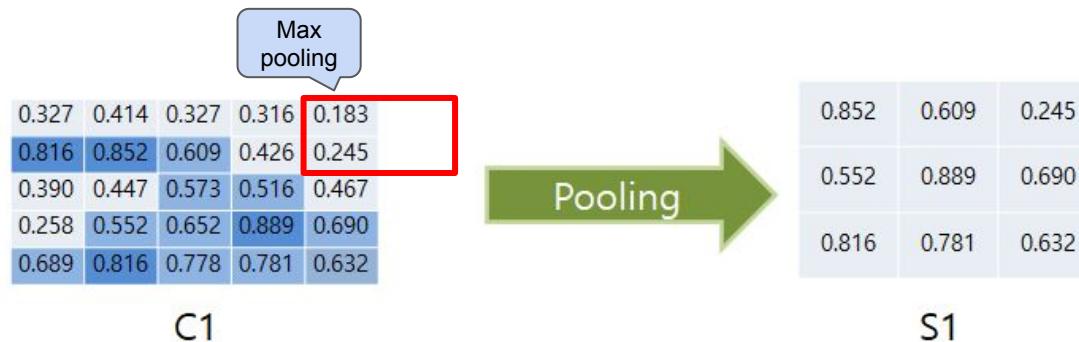
- Convolution을 실행한 C1에서 특징 (통상적으로 2x2 4칸 중 가장 큰 값을 고르는 Max Pooling을 사용)을 추려 냄



- S1을 새로운 Input처럼 생각하며 Convolution과 Subsampling을 반복

Pooling Layer

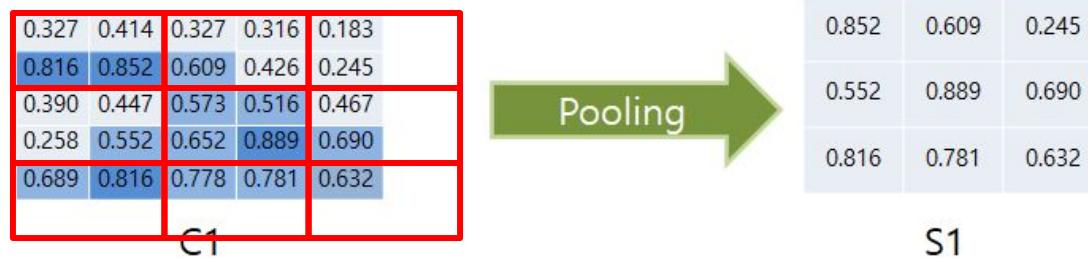
- Convolution을 실행한 C1에서 특징 (통상적으로 2x2 4칸 중 가장 큰 값을 고르는 Max Pooling을 사용)을 추려 냄



- S1을 새로운 Input처럼 생각하며 Convolution과 Subsampling을 반복

Pooling Layer

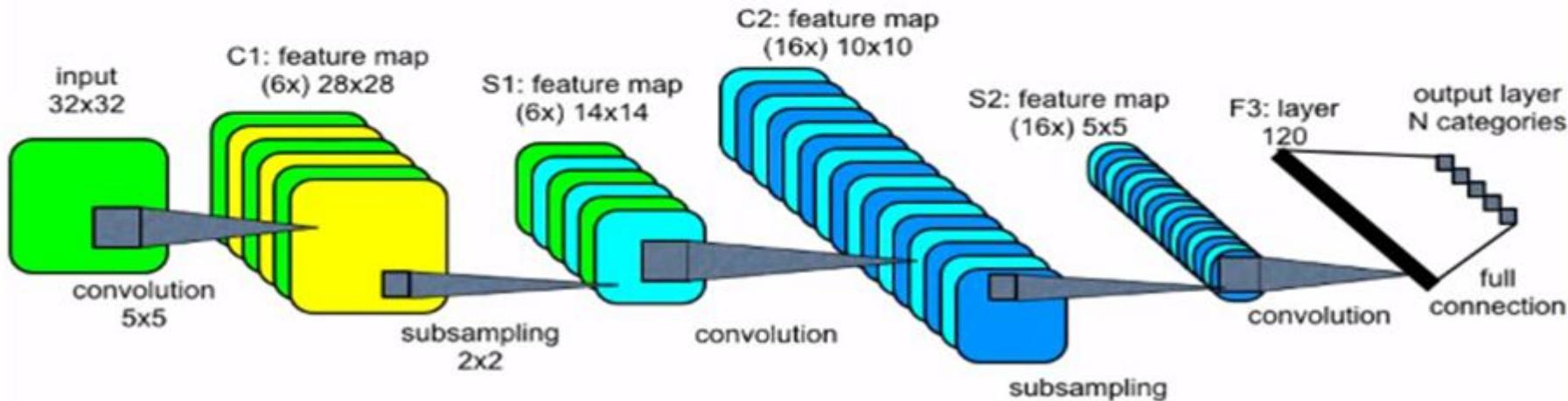
- Convolution을 실행한 C1에서 특징 (통상적으로 2x2 4칸 중 가장 큰 값을 고르는 Max Pooling을 사용)을 추려 냄



- S1을 새로운 Input처럼 생각하며 Convolution과 Subsampling을 반복

Fully Connected Layer

Convolutional Neural Networks



- MLP (Multi Layer Perceptron)에서 사용된 구조와 동일함
- 일반적으로 여러 필터를 통과한 특징들을 flatten 시켜
하나의 벡터로 만든 후 최종 output 예측 직전단계에 활용함

Some Techniques

Data Augmentation

- Random cropping to 224 X 224 images
- Altering RGB/Grayscale
- Flipping
- ...



Some Techniques

- Input 데이터에 이미지 변형 과정을 거쳐 데이터 자체의 특징은 유지하면서 데이터의 양은 늘려 학습의 효율을 크게 증가시킬 수 있는 기법. 데이터의 수가 적을 때 효과가 좋음.

Rotation



Zoom



Flip (Horizontal, Vertical)



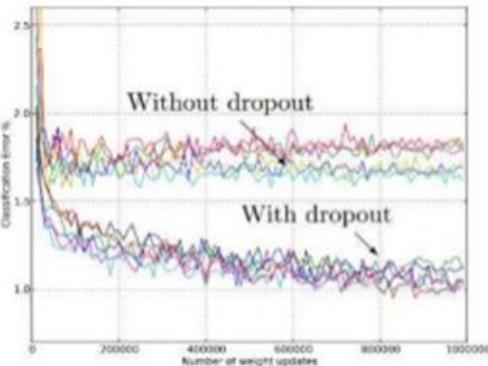
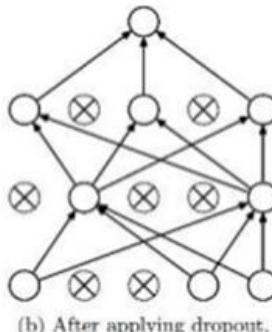
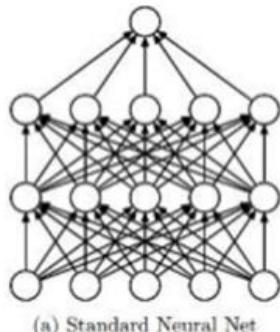
Shift (Width, Height)



Some Techniques

Dropout – Avoiding overfitting

- Fully-connected layers Node의 0.0~0.5를 데이터에 따라 off함
- Mini-batch마다 사용하는 neuron의 종류가 달라짐
- 여러 개의 architecture를 ensemble하는 효과가 생김
- Better generalization



Training CIFAR-10 data

합성곱 신경망 (Convolutional Neural Network)

Layer (type)	Output Shape	Param #
conv2d_6 (Conv2D)	(None, 30, 30, 32)	896
max_pooling2d_4 (MaxPooling2D)	(None, 15, 15, 32)	0
conv2d_7 (Conv2D)	(None, 13, 13, 64)	18496
max_pooling2d_5 (MaxPooling2D)	(None, 6, 6, 64)	0
conv2d_8 (Conv2D)	(None, 4, 4, 64)	36928
flatten_8 (Flatten)	(None, 1024)	0
dense_30 (Dense)	(None, 64)	65600
dense_31 (Dense)	(None, 10)	650
<hr/>		
Total params: 122,570		
Trainable params: 122,570		
Non-trainable params: 0		

```
Epoch 1/5  
1563/1563 [=====] - 5s 3ms/step - loss: 1.4835 - accuracy: 0.4626  
Epoch 2/5  
1563/1563 [=====] - 4s 3ms/step - loss: 1.1241 - accuracy: 0.6044  
Epoch 3/5  
1563/1563 [=====] - 4s 3ms/step - loss: 0.9768 - accuracy: 0.6571  
Epoch 4/5  
1563/1563 [=====] - 4s 3ms/step - loss: 0.8794 - accuracy: 0.6931  
Epoch 5/5  
1563/1563 [=====] - 4s 3ms/step - loss: 0.8053 - accuracy: 0.7190  
313/313 [=====] - 1s 2ms/step - loss: 0.8871 [accuracy: 0.6957  
[0.887057900428772, 0.6956999897956848]]
```

훨씬 적은 파라미터 수로 좋은 결과를 얻었음

Training CIFAR-10 data

epoch 5 -> 50

```
Epoch 45/50
1563/1563 [=====] - 4s 3ms/step - loss: 0.1037 - accuracy: 0.9643
Epoch 46/50
1563/1563 [=====] - 5s 3ms/step - loss: 0.1198 - accuracy: 0.9587
Epoch 47/50
1563/1563 [=====] - 4s 3ms/step - loss: 0.1102 - accuracy: 0.9617
Epoch 48/50
1563/1563 [=====] - 4s 3ms/step - loss: 0.1116 - accuracy: 0.9626
Epoch 49/50
1563/1563 [=====] - 4s 3ms/step - loss: 0.1026 - accuracy: 0.9651
Epoch 50/50
1563/1563 [=====] - 5s 3ms/step - loss: 0.1105 - accuracy: 0.9628
313/313 [=====] - 1s 2ms/step - loss: 2.5728 - accuracy: 0.6903
[2.5728492736816406, 0.6902999877929688]
```

학습 epoch를 50으로 늘렸지만 test accuracy에서 개선이 없었음

Training CIFAR-10 data

Model: "sequential_3"

Layer (type)	Output Shape	Param #
conv2d_11 (Conv2D)	(None, 30, 30, 64)	1792
max_pooling2d_8 (MaxPooling2)	(None, 15, 15, 64)	0
conv2d_12 (Conv2D)	(None, 13, 13, 128)	73856
max_pooling2d_9 (MaxPooling2)	(None, 6, 6, 128)	0
conv2d_13 (Conv2D)	(None, 4, 4, 128)	147584
flatten_1 (Flatten)	(None, 2048)	0
dense_2 (Dense)	(None, 128)	262272
dense_3 (Dense)	(None, 10)	1290
Total params: 486,794		
Trainable params: 486,794		
Non-trainable params: 0		

```
Epoch 47/50
1563/1563 [=====] - 12s 7ms/step - loss: 0.0700 - accuracy: 0.9794
Epoch 48/50
1563/1563 [=====] - 11s 7ms/step - loss: 0.0782 - accuracy: 0.9768
Epoch 49/50
1563/1563 [=====] - 12s 7ms/step - loss: 0.0722 - accuracy: 0.9784
Epoch 50/50
1563/1563 [=====] - 12s 7ms/step - loss: 0.0712 - accuracy: 0.9786
313/313 [=====] - 1s 4ms/step - loss: 3.1726 - accuracy: 0.6930
[3.172563076019287, 0.6930000185966492]
```

accuracy: 0.6930

layer를 추가했으나 비슷한 성능

Layer (type)	Output Shape	Param #
conv2d_14 (Conv2D)	(None, 30, 30, 64)	1792
max_pooling2d_10 (MaxPooling2)	(None, 15, 15, 64)	0
conv2d_15 (Conv2D)	(None, 13, 13, 128)	73856
max_pooling2d_11 (MaxPooling2)	(None, 6, 6, 128)	0
conv2d_16 (Conv2D)	(None, 4, 4, 128)	147584
flatten_2 (Flatten)	(None, 2048)	0
dropout (Dropout)	(None, 2048)	0
dense_4 (Dense)	(None, 128)	262272
dense_5 (Dense)	(None, 10)	1290
Total params: 486,794		
Trainable params: 486,794		
Non-trainable params: 0		

```
Epoch 47/50
1563/1563 [=====] - 12s 7ms/step - loss: 0.1414 - accuracy: 0.9532
Epoch 48/50
1563/1563 [=====] - 12s 7ms/step - loss: 0.1410 - accuracy: 0.9519
Epoch 49/50
1563/1563 [=====] - 12s 7ms/step - loss: 0.1336 - accuracy: 0.9546
Epoch 50/50
1563/1563 [=====] - 12s 7ms/step - loss: 0.1382 - accuracy: 0.9543
313/313 [=====] - 1s 4ms/step - loss: 1.5392 - accuracy: 0.7249
[1.539198875427246, 0.7249000072479248]
```

accuracy: 0.7249

Dropout을 적용한 결과 약간의 개선

Fashion-MNIST data



레이블	클래스
0	T-shirt/top
1	Trouser
2	Pullover
3	Dress
4	Coat
5	Sandal
6	Shirt
7	Sneaker
8	Bag
9	Ankle boot

Fashion-MNIST data

데이터 불러오기 & 정규화

```
1 import tensorflow as tf
2 fashion_mnist = tf.keras.datasets.fashion_mnist
3 (x_train, y_train), (x_test, y_test) = fashion_mnist.load_data()
4
5 x_train = x_train.reshape((60000, 28, 28, 1))
6 x_test = x_test.reshape((10000, 28, 28, 1))
7
8 # 픽셀 값을 0~1 사이로 정규화합니다.
9 x_train, x_test = x_train / 255.0, x_test / 255.0
```

Fashion-MNIST data

모델 정의하기

CNN?

```
1 from tensorflow.keras import datasets, layers, models
2
3 model = models.Sequential()
4 model.add(layers.Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1)))
5 model.add(layers.MaxPooling2D((2, 2)))
6 model.add(layers.Conv2D(64, (3, 3), activation='relu'))
7 model.add(layers.MaxPooling2D((2, 2)))
8 model.add(layers.Conv2D(64, (3, 3), activation='relu'))
9 model.add(layers.Flatten())
10 model.add(layers.Dense(64, activation='relu'))
11 model.add(layers.Dense(10, activation='softmax'))
```

MLP?

```
1 from tensorflow import keras
2 # layer를 하나씩 추가하는 방식
3 model = keras.models.Sequential()
4 model.add(keras.layers.Flatten(input_shape=[28,28]))
5 model.add(keras.layers.Dense(300, activation="relu"))
6 model.add(keras.layers.Dense(100, activation="relu"))
7 model.add(keras.layers.Dense(10, activation="softmax"))
8
9 # 층 리스트로 전달하는 방식
10 model = keras.models.Sequential([
11     keras.layers.Flatten(input_shape=[28,28]),
12     keras.layers.Dense(300, activation="relu"),
13     keras.layers.Dense(100, activation="relu"),
14     keras.layers.Dense(10, activation="softmax"),
15 ])
```

Fashion-MNIST data

모델 컴파일 & 모델 학습 및 평가

```
model.compile(loss="sparse_categorical_crossentropy", optimizer="sgd", metrics=["accuracy"])
history = model.fit(x_train, y_train, epochs=30, validation_data=(x_test, y_test))
```

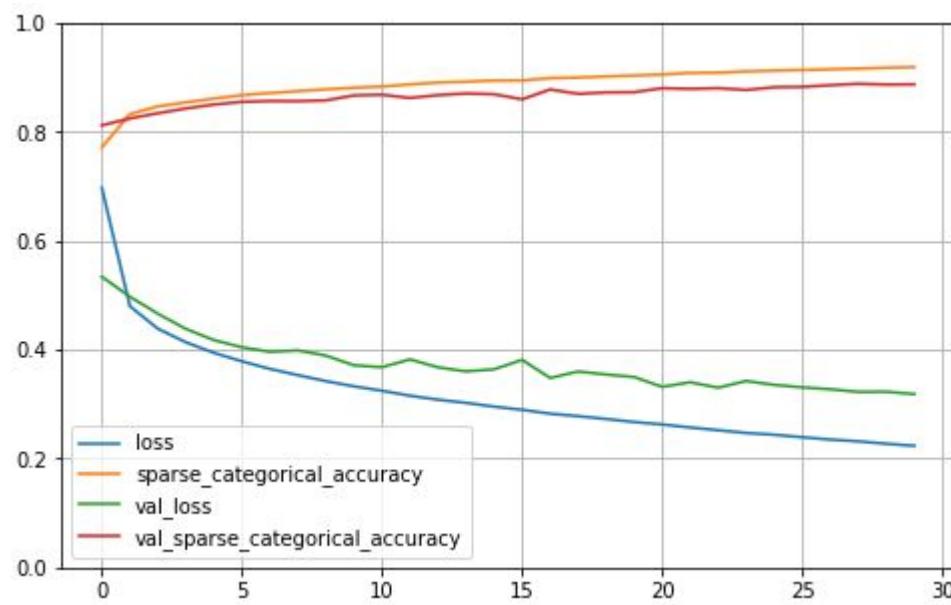
```
1875/1875 [=====] - 6s 3ms/step - loss: 0.2521 - sparse_categorical_accuracy: 0.9088 - val_loss: 0.3303 - val_sparse_categorical_accuracy: 0.8804
Epoch 24/30
1875/1875 [=====] - 6s 3ms/step - loss: 0.2471 - sparse_categorical_accuracy: 0.9111 - val_loss: 0.3425 - val_sparse_categorical_accuracy: 0.8771
Epoch 25/30
1875/1875 [=====] - 6s 3ms/step - loss: 0.2438 - sparse_categorical_accuracy: 0.9126 - val_loss: 0.3354 - val_sparse_categorical_accuracy: 0.8821
Epoch 26/30
1875/1875 [=====] - 6s 3ms/step - loss: 0.2392 - sparse_categorical_accuracy: 0.9137 - val_loss: 0.3308 - val_sparse_categorical_accuracy: 0.8827
Epoch 27/30
1875/1875 [=====] - 6s 3ms/step - loss: 0.2350 - sparse_categorical_accuracy: 0.9150 - val_loss: 0.3274 - val_sparse_categorical_accuracy: 0.8858
Epoch 28/30
1875/1875 [=====] - 6s 3ms/step - loss: 0.2317 - sparse_categorical_accuracy: 0.9164 - val_loss: 0.3225 - val_sparse_categorical_accuracy: 0.8885
Epoch 29/30
1875/1875 [=====] - 6s 3ms/step - loss: 0.2273 - sparse_categorical_accuracy: 0.9179 - val_loss: 0.3228 - val_sparse_categorical_accuracy: 0.8870
Epoch 30/30
1875/1875 [=====] - 6s 3ms/step - loss: 0.2234 - sparse_categorical_accuracy: 0.9190 - val_loss: 0.3186 - val_sparse_categorical_accuracy: 0.8873
```

Fashion-MNIST data

학습 곡선 확인하기

```
import pandas as pd
import matplotlib.pyplot as plt

pd.DataFrame(history.history).plot(figsize=(8,5))
plt.grid(True)
plt.gca().set_ylim(0, 1)
plt.show()
```



Fashion-MNIST data

모델 평가

```
1 model.evaluate(x_test, y_test)

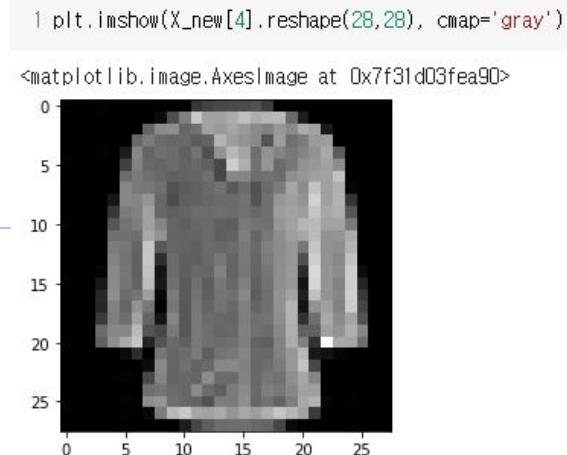
313/313 [=====] - 1s 2ms/step - loss: 0.3247 - sparse_categorical_accuracy: 0.8860
[0.32465073466300964, 0.8859999775886536]
```

데이터 예측하기

```
1 X_new = x_test[:5]
2 y_proba = model.predict(X_new)
3 y_proba.round(2)
```

array([[0. , 0. , 0. , 0. , 0. , 0. , 0. , 0.01, 0. , 0.98],
 [0. , 0. , 0.98, 0. , 0.02, 0. , 0. , 0. , 0. , 0.],
 [0. , 1. , 0. , 0. , 0. , 0. , 0. , 0. , 0. , 0.],
 [0. , 1. , 0. , 0. , 0. , 0. , 0. , 0. , 0. , 0.],
 [0.49, 0. , 0.02, 0. , 0.01, 0. , 0.48, 0. , 0. , 0.]],

T-shirt/top Shirt



Fashion-MNIST data

모델 저장 & 복원

```
1 model.save('fashion_mnist_mlp_model.h5')
```

```
1 model_loaded = keras.models.load_model('fashion_mnist_mlp_model.h5')
```

```
1 y_proba = model_loaded.predict(X_new)  
2 y_proba.round(2)
```

```
array([[0. , 0. , 0. , 0. , 0. , 0. , 0. , 0.01, 0. , 0.98],  
       [0. , 0. , 0.98, 0. , 0.02, 0. , 0. , 0. , 0. , 0. ],  
       [0. , 1. , 0. , 0. , 0. , 0. , 0. , 0. , 0. , 0. ],  
       [0. , 1. , 0. , 0. , 0. , 0. , 0. , 0. , 0. , 0. ],  
       [0.49, 0. , 0.02, 0. , 0.01, 0. , 0.48, 0. , 0. , 0. ]],
```

복원된 모델의 예측결과가
저장한 모델과 같은 것을 확인함