LSTM RNN 简介

潘睿

- ▶ 历史 & 基础知识
- ▶ 简介
- ▶ 优化
- ▶应用
- > 实现细节
- ▶ 工具库
- ▶ 展望

▶ 1943年MP模型提出

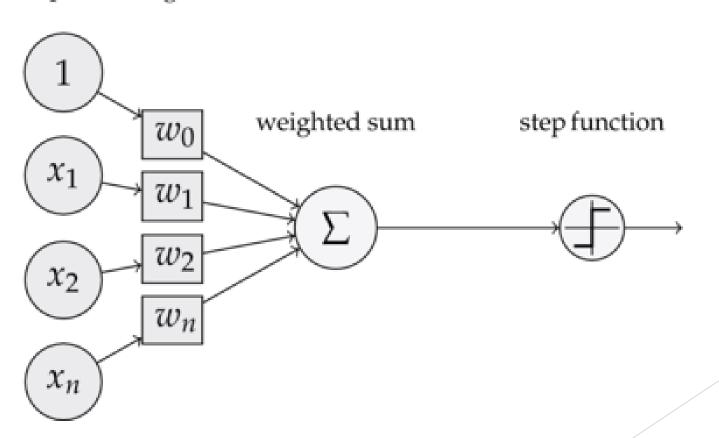
▶标志着神经计算时代的开始

▶1957年提出Perceptron模型(感知器)

▶可以解决分类问题

▶单个神经元

inputs weights

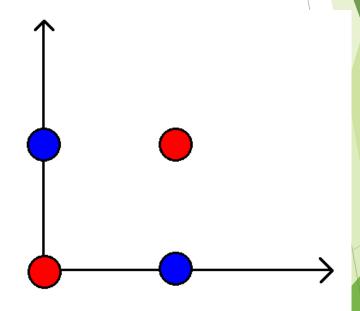


- ► Step function 也叫Activation function
- ▶比较常用的有

Sigmoid	$f(x) = \frac{1}{1 + e^{-x}}$	f'(x) = f(x)(1 - f(x))
TanH	$f(x) = \tanh(x) = \frac{2}{1 + e^{-2x}} - 1$	$f'(x) = 1 - f(x)^2$
Rectified Linear Unit (ReLU)	$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ x & \text{for } x \ge 0 \end{cases}$	$f'(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 & \text{for } x \ge 0 \end{cases}$

▶1969年Perceptron被指出只能做线性划分

▶神经网络进入第一次低潮



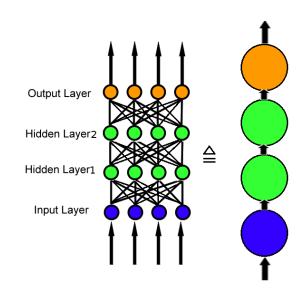
▶ 1982年John J. Hopfield提出一个具有完整 理论基础的神经网络模型

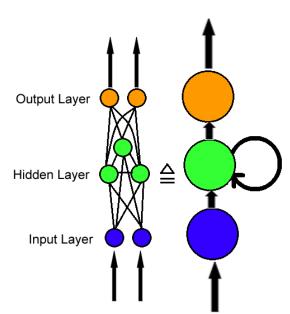
▶神经网络复兴时期开始

▶ 1986年提出Back Propagation (BP) 反向传播学习算法

▶流行至今

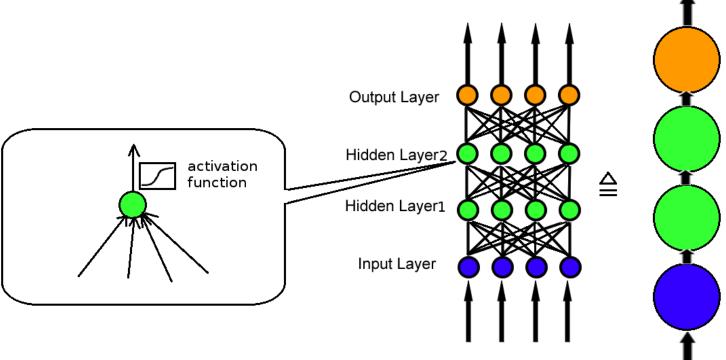
- ▶同一时期
- ► Multilayer perceptron (MLP) 多层感知器
- ► Recurrent Neural Network (RNN) 循环神经网络





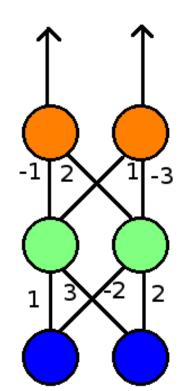
- ► Multilayer perceptron 多层感知器
 - 定义
 - ▶训练
 - ▶理论基础

- ► Multilayer perceptron 多层感知器
- 定义
 - ▶ An MLP consists of multiple layers of nodes in a directed graph, with each layer fully connected to the next one.
 - 多层感知器就是多层神经元,每层有一堆神经元,这一层和下一层的每个神经元全连上



- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Forward Propagation 前向传播
 - ▶ Back Propagation 反向传播

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Forward Propagation 前向传播

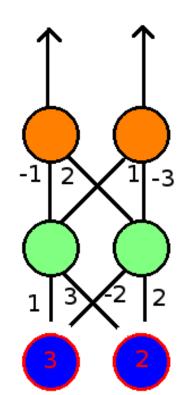


Rectified Linear Unit (ReLU)



$$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ x & \text{for } x \ge 0 \end{cases}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Forward Propagation 前向传播

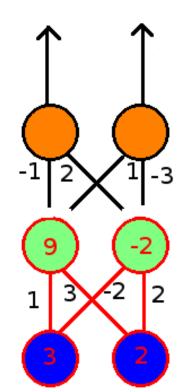


Rectified Linear
Unit (ReLU)



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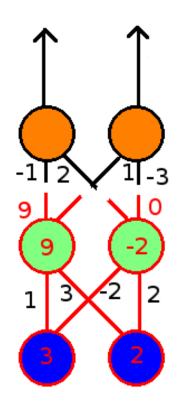
- ► Multilayer perceptron 多层感知器
- ▶训练
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Rectified Linear Unit (ReLU)

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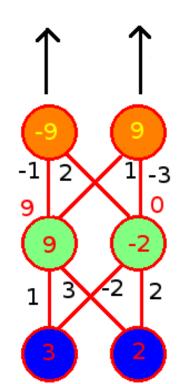
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Activation

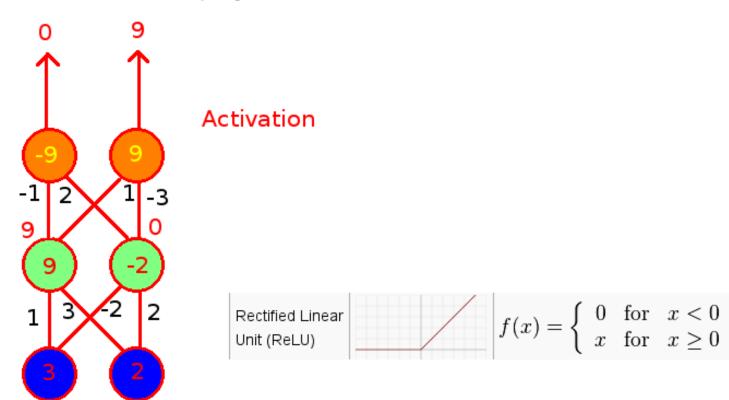


- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Forward Propagation 前向传播



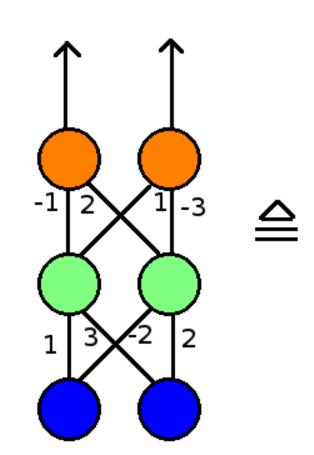
Rectified Linear Unit (ReLU) $f(x) = \left\{ \begin{array}{ll} 0 & \text{for} & x < 0 \\ x & \text{for} & x \geq 0 \end{array} \right.$

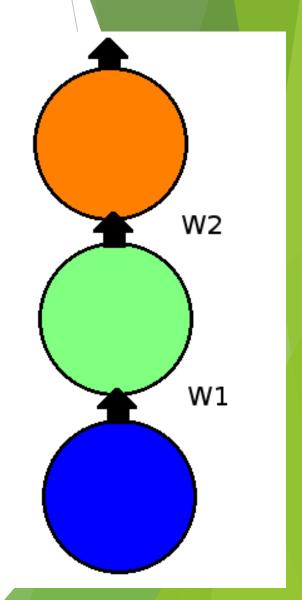
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- ► Multilayer perceptron 多层感知器
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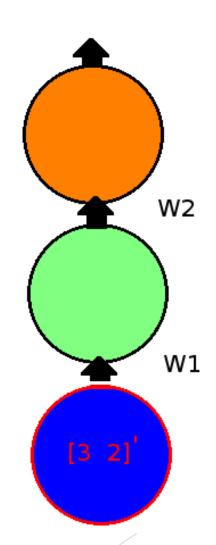
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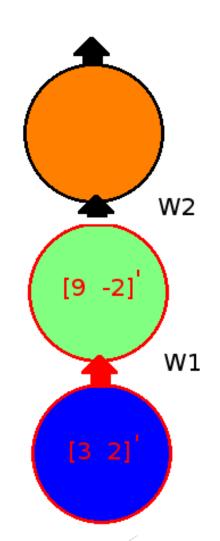
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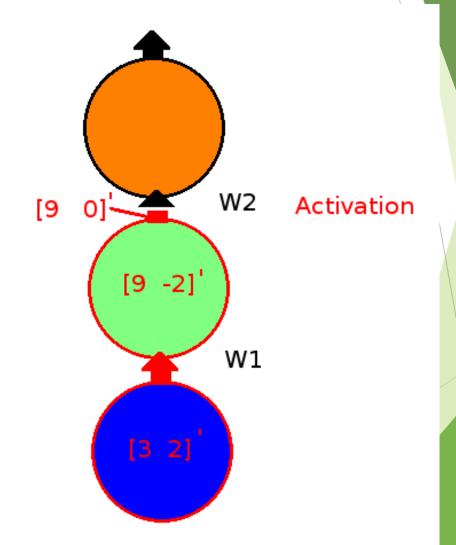
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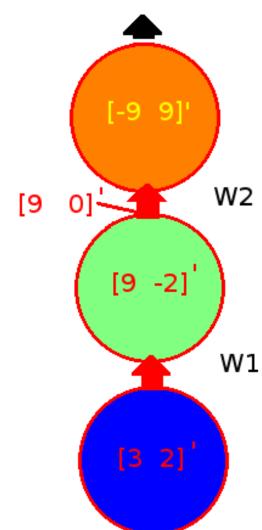
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- ▶训练
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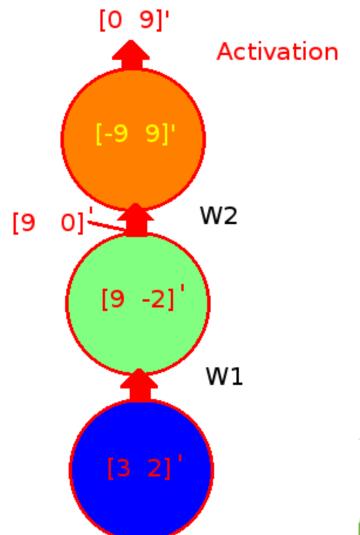
- ► W1 = W2 =
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- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

▶高中题目:如何计算f(g(x))的导函数

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播
- ▶高中题目:如何计算f(g(x))的导函数
- ▶答: f'(g(x)) * g'(x)

- ► Multilayer perceptron 多层感知器
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 - ▶ Back Propagation 反向传播

▶大学题目:如何计算f(g(x))的导函数

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播
- ▶大学题目:如何计算f(g(x))的导函数
- ▶答: $D_{\mathbf{a}}(f \circ g) = D_{g(\mathbf{a})} f \circ D_{\mathbf{a}} g$,

$$D\mathbf{f}(\mathbf{a}) = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & (\mathbf{a}) & \frac{\partial f_1}{\partial x_2} & (\mathbf{a}) & \dots & \frac{\partial f_1}{\partial x_n} & (\mathbf{a}) \\ \frac{\partial f_2}{\partial x_1} & (\mathbf{a}) & \frac{\partial f_2}{\partial x_2} & (\mathbf{a}) & \dots & \frac{\partial f_2}{\partial x_n} & (\mathbf{a}) \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \frac{\partial f_m}{\partial x_1} & (\mathbf{a}) & \frac{\partial f_m}{\partial x_2} & (\mathbf{a}) & \dots & \frac{\partial f_m}{\partial x_n} & (\mathbf{a}) \end{bmatrix}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

▶一个特例:如何计算σ(Wx)的导函数

Sigmoid $f(x) = \frac{1}{1 + e^{-x}} \qquad \qquad f'(x) = f(x)(1 - f(x))$ $Df(\mathbf{a}) = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & (\mathbf{a}) & \frac{\partial f_1}{\partial x_2} & (\mathbf{a}) & \dots & \frac{\partial f_1}{\partial x_n} & (\mathbf{a}) \\ \frac{\partial f_2}{\partial x_1} & (\mathbf{a}) & \frac{\partial f_2}{\partial x_2} & (\mathbf{a}) & \dots & \frac{\partial f_2}{\partial x_n} & (\mathbf{a}) \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial f_m}{\partial x_1} & (\mathbf{a}) & \frac{\partial f_m}{\partial x_2} & (\mathbf{a}) & \dots & \frac{\partial f_m}{\partial x_n} & (\mathbf{a}) \end{bmatrix}.$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

▶一个特例:如何计算σ(Wx)的导函数

$$\frac{\partial \sigma(\mathbf{x})}{\partial \mathbf{x}} = D_{\sigma}(\mathbf{x}) = \begin{bmatrix} \sigma(x_1)(1 - \sigma(x_1)) & 0 & \dots & 0 \\ 0 & \sigma(x_2)(1 - \sigma(x_2)) & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & \sigma(x_m)(1 - \sigma(x_m)) \end{bmatrix}$$

$$\frac{\partial \mathbf{W} \mathbf{x}}{\partial \mathbf{x}} = \mathbf{W}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

▶一个特例:如何计算σ(Wx)的导函数

$$\frac{\partial \sigma(\mathbf{W}\mathbf{x})}{\partial \mathbf{x}} = \frac{\partial \sigma(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}\mathbf{x}} * \frac{\partial \mathbf{W}\mathbf{x}}{\partial \mathbf{x}} = D_{\sigma}(\mathbf{W}\mathbf{x}) * \mathbf{W}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

ightharpoonup 另一个特例:如何计算sum(σ (Wx)) 的导函数

$$\frac{\partial \sum \sigma(\mathbf{W}\mathbf{x})}{\partial \mathbf{x}} = \frac{\partial \sum \sigma(\mathbf{W}\mathbf{x})}{\partial \sigma(\mathbf{W}\mathbf{x})} * \frac{\partial \sigma(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}\mathbf{x}} * \frac{\partial \mathbf{W}\mathbf{x}}{\partial \mathbf{x}} =$$

$$[1, 1, \dots, 1] * D_{\sigma}(\mathbf{W}\mathbf{x}) * \mathbf{W} =$$

$$(\sigma(\mathbf{W}\mathbf{x}))^{T} \odot (1 - \sigma(\mathbf{W}\mathbf{x}))^{T} * \mathbf{W}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

>另一个特例:如何计算sum(σ(Wx)) 的导函数

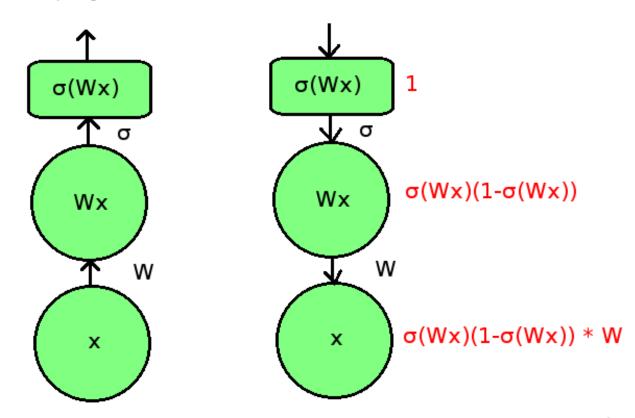
$$(\sigma(\mathbf{W}\mathbf{x}))^T \odot (1 - \sigma(\mathbf{W}\mathbf{x}))^T * \mathbf{W}$$

Hadamard product (逐元素相乘)

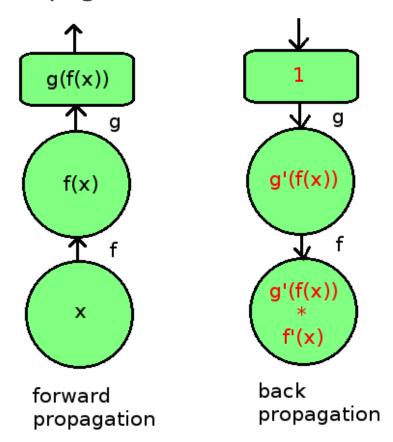
全1向量

矩阵乘法

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播



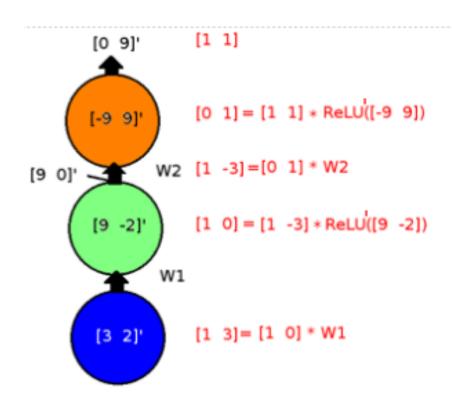
- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播



- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

- **▶** [1 3] [-1 2]

▶ [-2 2]



Rectified Linear Unit (ReLU)

$$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ x & \text{for } x \ge 0 \end{cases}$$

$$f'(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 & \text{for } x \ge 0 \end{cases}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

- ► W1 = W2 =
- **▶** [1 3] [-1 2]
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- ▶ W1, W2的导函数?

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

▶ W1, W2的导函数?

$$\frac{\partial f(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}} = \frac{\partial f(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}\mathbf{x}} * \frac{\partial \mathbf{W}\mathbf{x}}{\partial \mathbf{W}} = \frac{\partial f(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}\mathbf{x}} * \mathbf{T}_{n*n*m}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

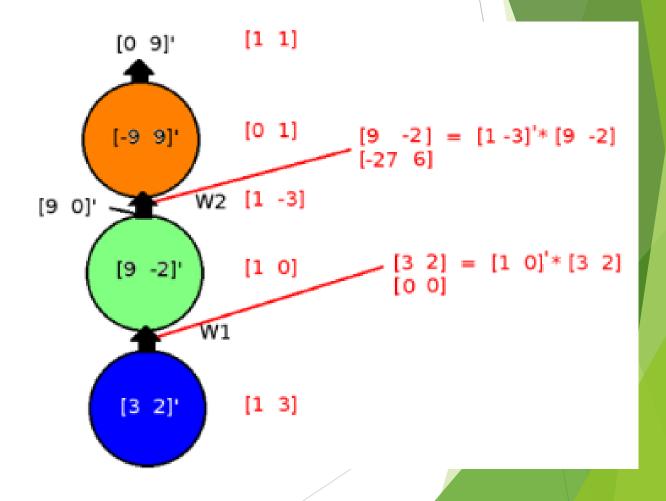
▶ W1, W2的导函数?

$$\frac{\partial \mathbf{W} \mathbf{x}}{\partial \mathbf{W}_{i,j}} = \begin{bmatrix} 0 \\ \vdots \\ 0 \\ x_j(ith\ row) \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

$$let \mathbf{a}^{T} denote \frac{\partial f(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}\mathbf{x}}$$
$$\frac{\partial f(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}_{i,j}} = a_{i}x_{j}$$
$$\frac{\partial f(\mathbf{W}\mathbf{x})}{\partial \mathbf{W}} = \mathbf{a}\mathbf{x}^{T}$$

- ► Multilayer perceptron 多层感知器
- ▶训练
 - ▶ Back Propagation 反向传播

- **▶** [1 3] [-1 2]
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- ► Multilayer perceptron 多层感知器
- ▶理论基础
 - ▶ Universal approximation theorem 通用近似定理
 - ▶ 大意就是三层神经网络只要隐层点够多,就可以近似任何连续函数
 - ▶ 视觉直观解释见 http://neuralnetworksanddeeplearning.com/chap4.html

Let $\varphi(\cdot)$ be a nonconstant, bounded, and monotonically-increasing continuous function. Let I_m denote the m-dimensional unit hypercube $[0,1]^m$. The space of continuous functions on I_m is denoted by $C(I_m)$. Then, given any function $f \in C(I_m)$ and $\varepsilon > 0$, there exists an integer N and real constants $v_i, b_i \in \mathbb{R}$, where $i = 1, \cdots, N$ such that we may define:

$$F(x) = \sum_{i=1}^{N} v_i \varphi\left(w_i^T x + b_i\right)$$

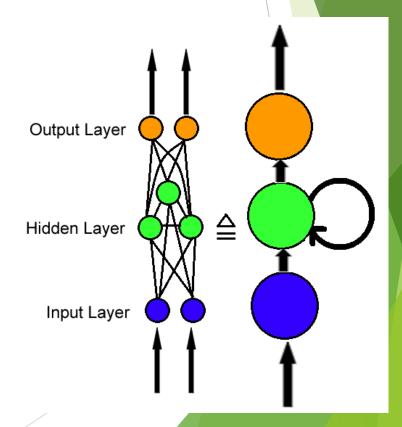
as an approximate realization of the function f where f is independent of arphi; that is,

$$|F(x) - f(x)| < \varepsilon$$

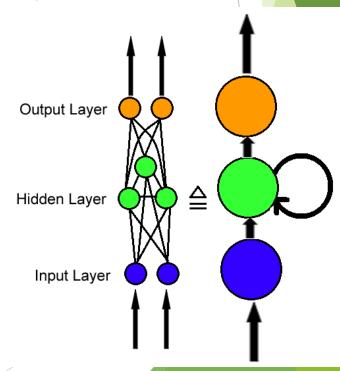
for all $x \in I_m$. In other words, functions of the form F(x) are dense in $C(I_m)$.

- ► Recurrent Neural Network 循环神经网络
 - 定义
 - ▶用法
 - ▶训练
 - ▶理论基础
 - ▶优缺点

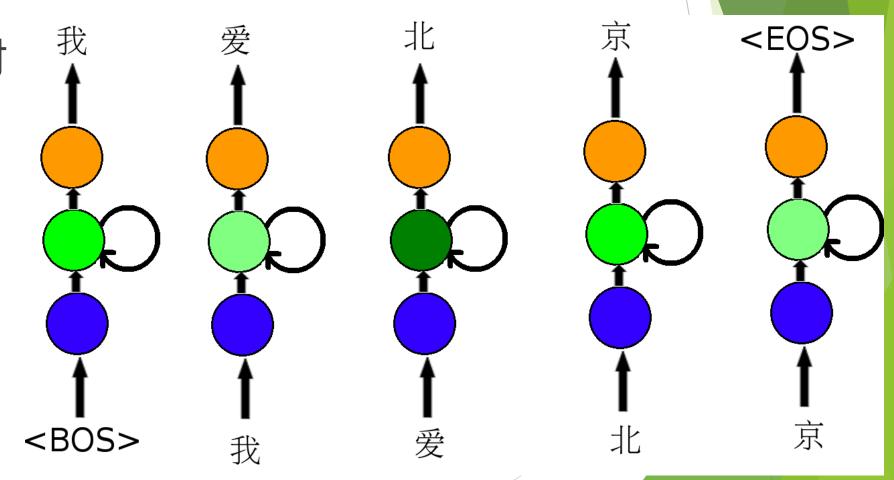
- ▶ Recurrent Neural Network 循环神经网络
- 定义
 - ► A recurrent neural network (RNN) is a class of artificial neural network where connections between units form a directed cycle.
 - ▶ 这个定义更广泛些,下图所示的是当前比较常见的RNN



- ▶ Recurrent Neural Network 循环神经网络
- 定义
 - ▶ 注意不要与Recursive Neural Network (递归神经网络)弄混
 - ▶ Recurrent Neural Network是Recursive Neural Network的一个特例
 - ▶ Recursive Neural Network代表了更复杂的结构(树状,图状)
 - ▶ Recurrent Neural Network只代表链状(?) 时序结构

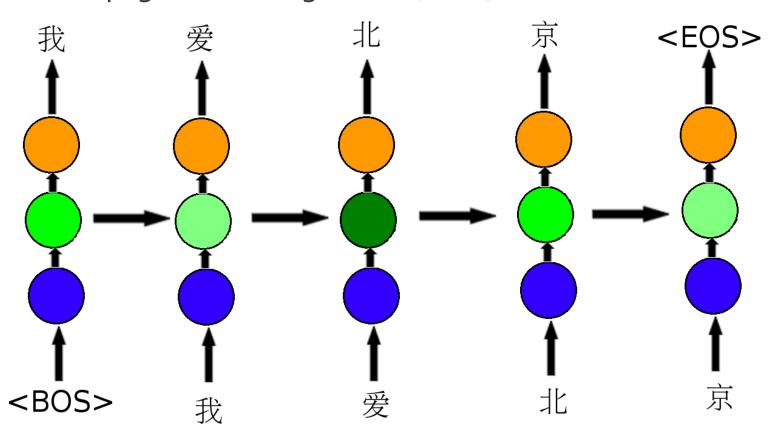


- ▶ Recurrent Neural Network 循环神经网络
- ▶用法
 - ▶序列映射

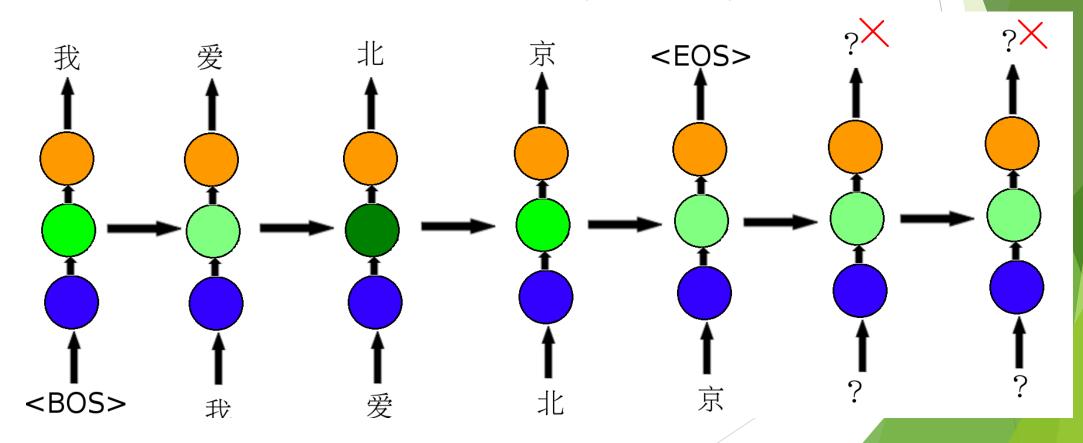


- ▶ Recurrent Neural Network循环神经网络
- ▶训练
 - ▶ Back Propagation Through Time (BPTT)沿时间反向传播
 - ▶ 1987、1988、1995年由多名研究者分别独立提出
 - ▶ BPTT有多种变种,这里只介绍目前最常用的一种

- ▶ Recurrent Neural Network循环神经网络
- ▶训练
 - ▶ Back Propagation Through Time (BPTT)沿时间反向传播



- ▶ Recurrent Neural Network循环神经网络
- ▶训练
 - ▶ 实际情况中往往展开一个最大的固定长度(下图中为7)



- ▶ Recurrent Neural Network循环神经网络
- ▶训练
 - ▶ 对于过长的数据,可以作截断处理
 - ▶ 使用上一截的隐层状态初始化(当然梯度仍无法回传至上一截数据)

▶ Recurrent Neural Network循环神经网络

▶理论基础

- ▶ 输入输出连续的情形下:如果隐藏层神经元足够多,RNN可以一致 逼近任意连续曲线
- ▶ (对于输入输出离散情形也是如此)

Theorem

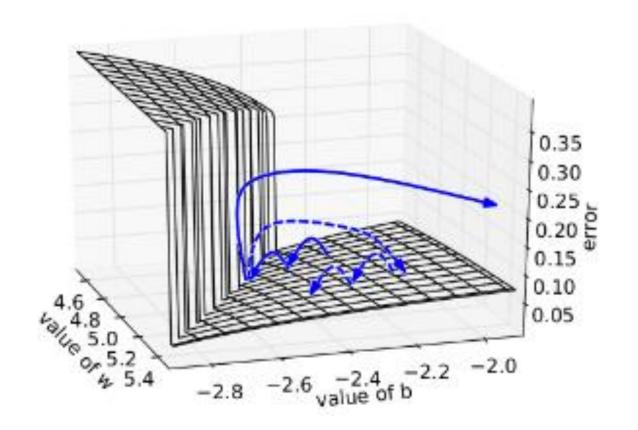
Let be $f: I=[0,T] \rightarrow \mathbb{R}^n$ be a continuous curve, where $0 < T < \infty$. Then, for an arbitrary $\varepsilon > 0$, there exist an integer N and a recurrent networks with n outputs and N hidden units such that

$$\max_{t \in I} |f(t) - u(t)| < \varepsilon,$$

where $u(t)=t(u_1(t),...u_n(t))$ is the internal state of output units of the network.

- ▶ Recurrent Neural Network循环神经网络
- ▶优点
 - ▶ 相比多层感知器,可以处理变长数据
- ▶缺点
 - ▶ Gradient Explosion (梯度爆炸)
 - ► Gradient Vanishing (梯度消失)

- ▶ Recurrent Neural Network循环神经网络
- ▶尝试
 - ▶ [2012] On the difficulty of training recurrent neural networks



▶ 1997年Long Short-Term Memory Recurrent Neural Network (LSTM RNN)提出

▶ 当时神经网络正因为Support Vector Machine (SVM)支撑向量机的火爆而陷入低潮

▶ LSTM最初的提出有几个原因

▶ 为了解决RNN的Gradient Explosion/Vanishing的问题

▶ 为了得到能够学习如何学习的神经网络

- LSTM, 5000 weights, 5 months training:
 metalearns fast online learning algorithm for
 quadratic functions f(x,y)=a₁x²+a₂y²+a₃xy+a₄x+a₅y+a₆
 Huge time lags.
- After metalearning, freeze weights.
- Now use net: Select new f, feed training exemplars
 ...data/target/data/target/data... into input units, one
 at a time. After 30 exemplars the net predicts target
 inputs before it sees them.

No weight changes!

How?

► Metalearner也用RNN应用过,但没有LSTM 如此好的效果

► LSTM的Memory存储了神奇的知识

► 2006年, Deeplearning在ImageNet上取得 巨大突破

> 深度学习开始火爆

- ▶ 2013年 , LSTM在Speech Recognition上取得很好的效果
 - SPEECH RECOGNITION WITH DEEP RECURRENT NEURAL NETWORKS
- ▶ 2014年,LSTM在Machine Translation上取得不错的效果,进入NLP领域
 - ► Sequence-to-sequence-learning-with-neural-networks
- ▶ 只要是和序列映射有关的,LSTM都可以做!
- ► LSTM开始火热

- ► LSTM的结构
- ►LSTM的思想
- ▶用LSTM实现Seq2Seq

Neural Network

Layer

Pointwise

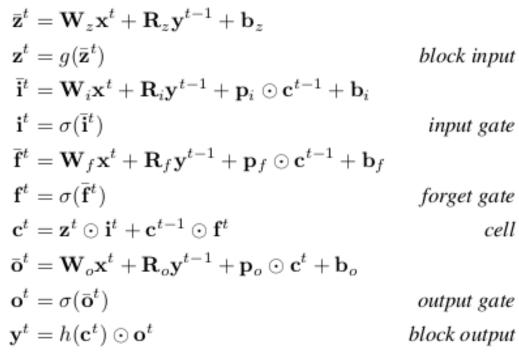
Operation

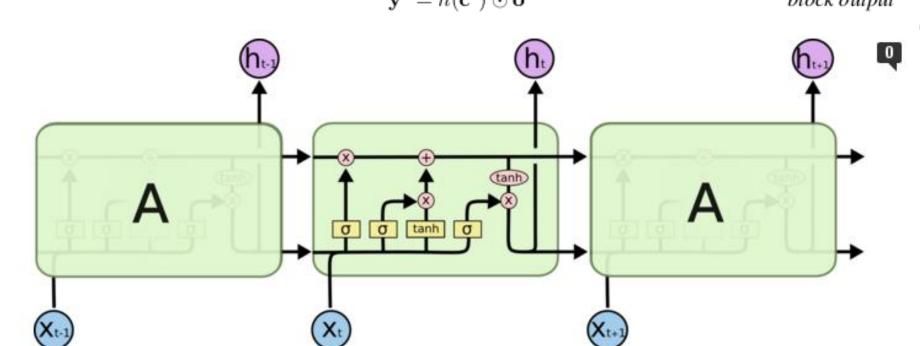
▶通用LSTM的结构

Vector

Transfer

Concatenate

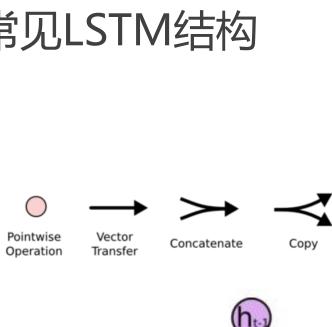


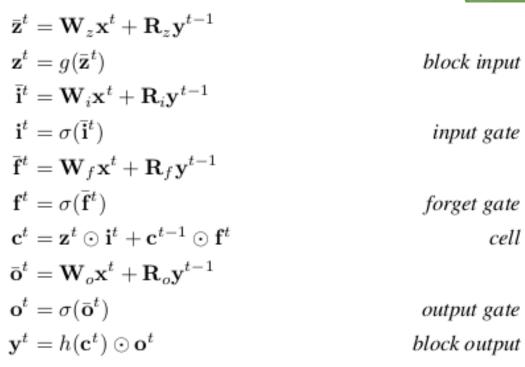


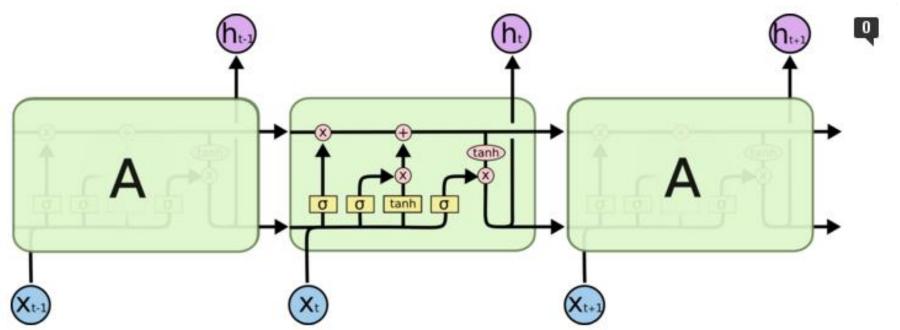
Neural Network

Layer

▶常见LSTM结构







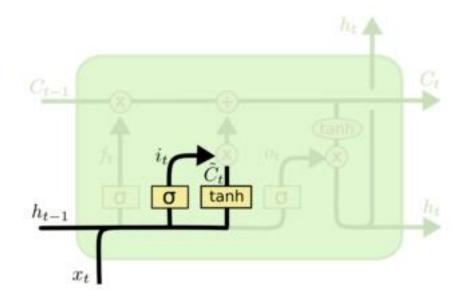
- ▶Gate是一种限制,代表一种选择(0或1)
- ▶不过为了保证可导,所以设置为Sigmoid函数σ(x)

Sigmoid	$f(x) = \frac{1}{1 + e^{-x}}$	f'(x) = f(x)(1 - f(x))
TanH	$f(x) = \tanh(x) = \frac{2}{1 + e^{-2x}} - 1$	$f'(x) = 1 - f(x)^2$

- ▶ Block input
- Input gate
- Forget gate
- Output gate
- ► Block output
- ▶ 输入为3gate , 1input
- ▶ 存储为1memory
- ▶ 输出为1output

$$\begin{split} &\bar{\mathbf{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} \\ &\mathbf{z}^t = g(\bar{\mathbf{z}}^t) & block input \\ &\bar{\mathbf{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} \\ &\mathbf{i}^t = \sigma(\bar{\mathbf{i}}^t) & input gate \\ &\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} \\ &\mathbf{f}^t = \sigma(\bar{\mathbf{f}}^t) & forget gate \\ &\mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ &\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} \\ &\mathbf{o}^t = \sigma(\bar{\mathbf{o}}^t) & output gate \\ &\mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block output \end{split}$$

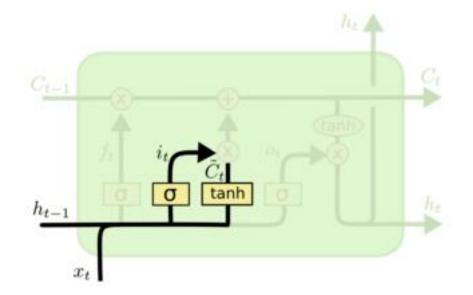
- ▶ Block input
 - ▶ 代表输入信息
 - ▶ 结合上一时间的输出和当前输入
 - ▶ RNN中的原始结构



$$\begin{split} &\bar{\mathbf{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} \\ &\mathbf{z}^t = g(\bar{\mathbf{z}}^t) & block input \\ &\bar{\mathbf{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} \\ &\mathbf{i}^t = \sigma(\bar{\mathbf{i}}^t) & input \ gate \\ &\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} \\ &\mathbf{f}^t = \sigma(\bar{\mathbf{f}}^t) & forget \ gate \\ &\mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ &\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} \\ &\mathbf{o}^t = \sigma(\bar{\mathbf{o}}^t) & output \ gate \\ &\mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block \ output \end{split}$$

$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] \right)$$
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t])$$

- ► Input gate
 - ▶ 是否需要加入新信息?
 - ▶(比如情感分析中的'the'就可以直接无视了)

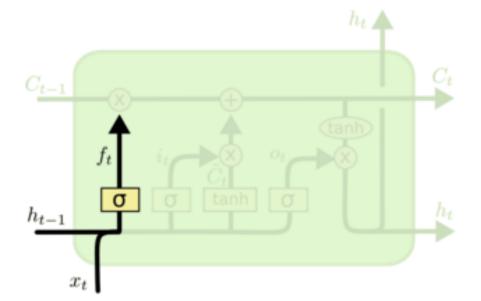


$$\begin{split} &\bar{\mathbf{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} \\ &\mathbf{z}^t = g(\bar{\mathbf{z}}^t) & block input \\ &\bar{\mathbf{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} \\ &\mathbf{i}^t = \sigma(\bar{\mathbf{i}}^t) & input \ gate \\ &\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} \\ &\mathbf{f}^t = \sigma(\bar{\mathbf{f}}^t) & forget \ gate \\ &\mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ &\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} \\ &\mathbf{o}^t = \sigma(\bar{\mathbf{o}}^t) & output \ gate \\ &\mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block \ output \end{split}$$

$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] \right)$$

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t])$$

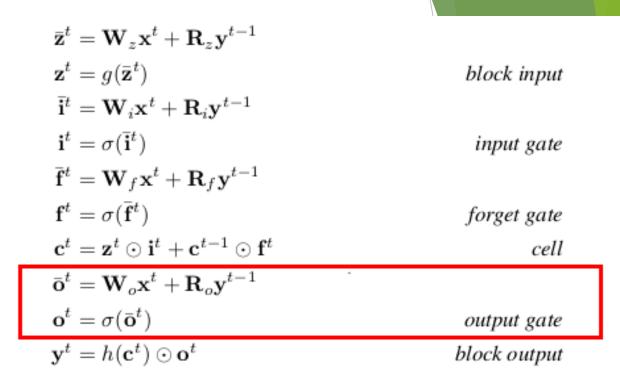
- Forget gate
 - ▶ 是否需要记住/忘记之前的信息?
 - ▶ (比如在情感分析中,看到'but' 这种转折词就忘记之前的内容,看到 'the'这类无关的词就记住)

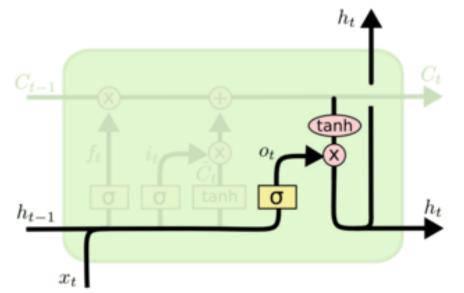


$$\begin{split} &\bar{\mathbf{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} \\ &\mathbf{z}^t = g(\bar{\mathbf{z}}^t) & block input \\ &\bar{\mathbf{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} \\ &\mathbf{i}^t = \sigma(\bar{\mathbf{i}}^t) & input \ gate \\ &\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} \\ &\mathbf{f}^t = \sigma(\bar{\mathbf{f}}^t) & forget \ gate \\ &\mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ &\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} \\ &\mathbf{o}^t = \sigma(\bar{\mathbf{o}}^t) & output \ gate \\ &\mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block \ output \end{split}$$

$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t]\right)$$

- Output gate
 - ► 选取特定记忆影响这次的结果 和控制下次的gate

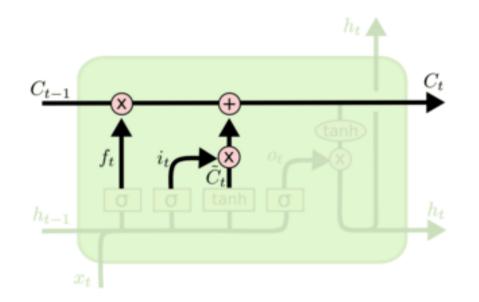




$$o_t = \sigma (W_o [h_{t-1}, x_t])$$
$$h_t = o_t * \tanh (C_t)$$

- Cell
- ▶ 记忆即存储
- ▶ 抹去一些记忆后加入新信息

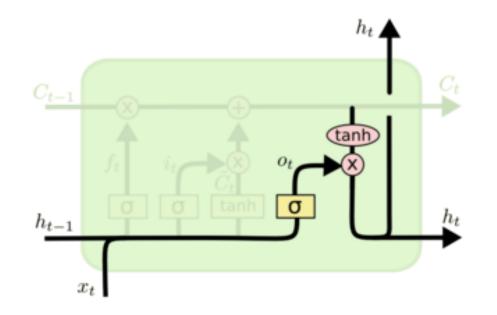
$$\begin{split} &\bar{\mathbf{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} \\ &\mathbf{z}^t = g(\bar{\mathbf{z}}^t) & block input \\ &\bar{\mathbf{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} \\ &\mathbf{i}^t = \sigma(\bar{\mathbf{i}}^t) & input gate \\ &\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} \\ &\mathbf{f}^t = \sigma(\bar{\mathbf{f}}^t) & forget gate \\ &\mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ &\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} \\ &\mathbf{o}^t = \sigma(\bar{\mathbf{o}}^t) & output gate \\ &\mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block output \end{split}$$



$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

- ► Block output
- ▶ 利用记忆产生行为 以及改变下一次的控制

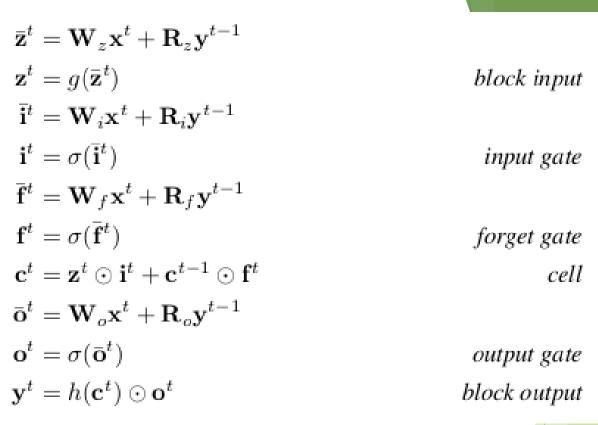
$$\begin{split} &\bar{\mathbf{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} \\ &\mathbf{z}^t = g(\bar{\mathbf{z}}^t) & block input \\ &\bar{\mathbf{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} \\ &\mathbf{i}^t = \sigma(\bar{\mathbf{i}}^t) & input \ gate \\ &\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} \\ &\mathbf{f}^t = \sigma(\bar{\mathbf{f}}^t) & forget \ gate \\ &\mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ &\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} \\ &\mathbf{o}^t = \sigma(\bar{\mathbf{o}}^t) & output \ gate \\ &\mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block \ output \end{split}$$

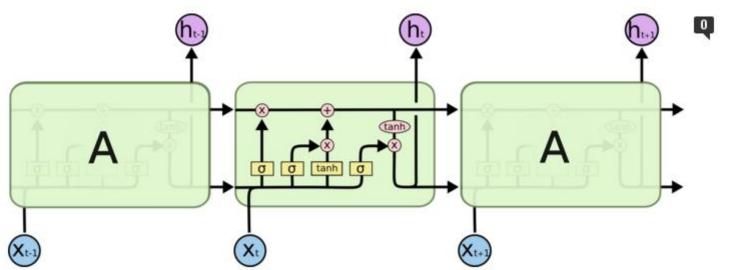


$$o_t = \sigma (W_o [h_{t-1}, x_t])$$
$$h_t = o_t * \tanh (C_t)$$

► LSTM结构总结

- ▶ 选择性输入
- ▶ 选择性记忆
- ▶ 记忆和输入合并
- ▶ 记忆选择性输出





▶LSTM思想

- ▶记忆 Memory
- ▶选择 Gate

简介

- ▶LSTM思想
 - ▶记忆 Memory
 - ▶ RNN不具备很强的记忆性,所以LSTM弥补了这一点
 - ▶ 利用强制的记忆结构

- > 实际上RNN在经过适当的初始化(Recurrent矩阵类似I矩阵)后,也可以达到类似效果
 - ▶ [2015] A Simple Way to Initialize Recurrent Networks of Rectified Linear Units

简介

- ▶LSTM思想
 - ▶选择 Gate

- ▶ LSTM让RNN有了选择信息的能力,更容易排除冗余信息,找到时序依赖关系
- ▶ 实验表明,情感分析中'the', 'an', 'he', 'she'的input gate基本都为0,而强情<mark>感词</mark> 语如'good', 'bad', 'excellent'的input gate基本都为1

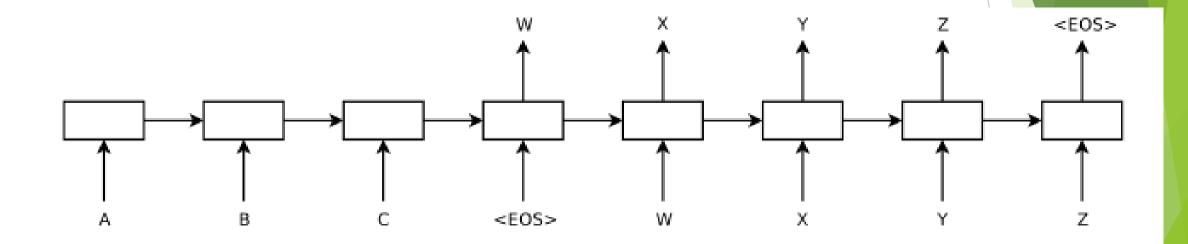
简介

- ▶ LSTM实现Seq2Seq
 - ▶为什么LSTM这么火?
 - ▶处理Sequence序列之间映射关系的强大工具
 - ▶句子
 - ▶语音
 - ▶代码
 - ▶视频
 - ▶轨迹
 - ▶.....(只要是Sequence都能试─试)



► LSTM实现Seq2Seq

▶ [2014] Sequence-to-sequence-learning-with-neural-networks



► Bidirectional LSTM(双向LSTM)

- ▶ 单向LSTM不能很好处理未来信息对当前预测的影响
- ▶ 双向LSTM可以缓解这一问题,实际中效果也确实好
- ▶ 就是暴力把正向和逆向的输出向量拼在一起

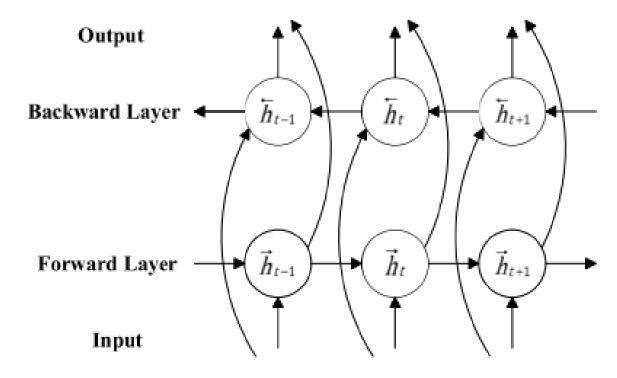


Fig.2. Bidirectional RNN

► Gated Recurrent Unit(GRU)

- ▶ LSTM训练非常慢, GRU对此做了优化
- ▶ 减少一个Gate,速度快25%,

效果没有明显下降

$$\tilde{h}_t^j = \tanh \left(W \mathbf{x}_t + U \left(\mathbf{r}_t \odot \mathbf{h}_{t-1} \right) \right)^j,$$

$$z_t^j = \sigma \left(W_z \mathbf{x}_t + U_z \mathbf{h}_{t-1} \right)^j.$$

$$r_t^j = \sigma \left(W_r \mathbf{x}_t + U_r \mathbf{h}_{t-1} \right)^j.$$

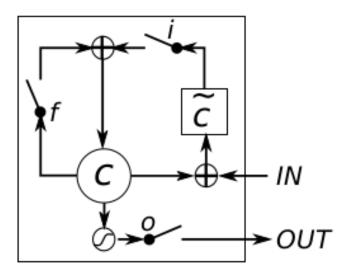
$$h_t^j = (1 - z_t^j)h_{t-1}^j + z_t^j \tilde{h}_t^j,$$

block input

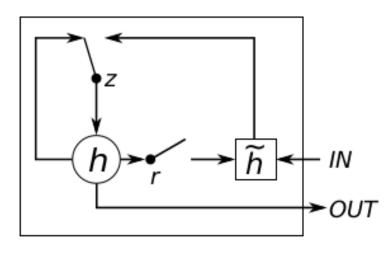
update gate

reset gate

output/memory



(a) Long Short-Term Memory



(b) Gated Recurrent Unit

► Gated Recurrent Unit(GRU)

- ▶ 主要合并了input gate和forget gate
- ▶ 另外还合并了隐层和记忆

$$\tilde{h}_t^j = \tanh \left(W \mathbf{x}_t + U \left(\mathbf{r}_t \odot \mathbf{h}_{t-1} \right) \right)^j,$$

$$z_t^j = \sigma \left(W_z \mathbf{x}_t + U_z \mathbf{h}_{t-1} \right)^j.$$

$$r_t^j = \sigma \left(W_r \mathbf{x}_t + U_r \mathbf{h}_{t-1} \right)^j.$$

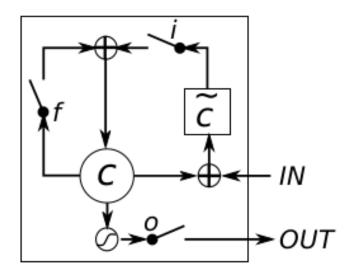
$$h_t^j = (1 - z_t^j)h_{t-1}^j + z_t^j \tilde{h}_t^j,$$

block input

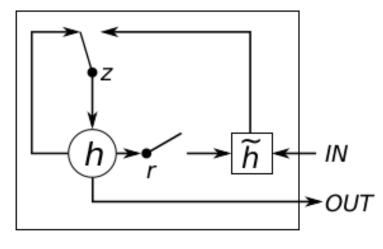
update gate

reset gate

output/memory



(a) Long Short-Term Memory



(b) Gated Recurrent Unit

- ► Multilayer LSTM(多层次LSTM)
 - ▶ 对深度的无限追求(RNN本身横着就够深了,现在竖着也要变深)
 - ▶ 正常2~3层都会有提升,4层以上就不好说了

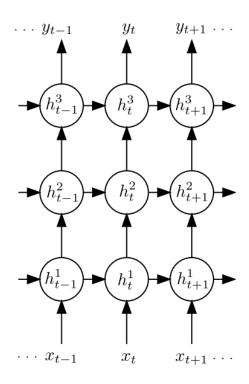
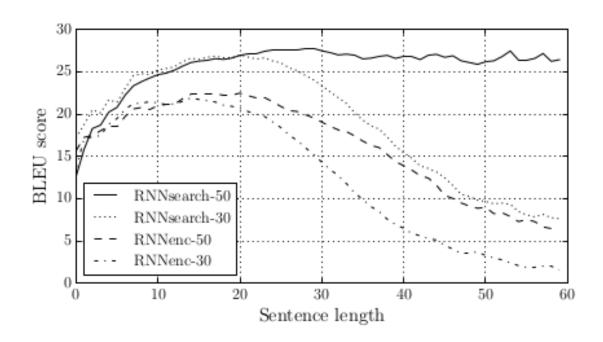
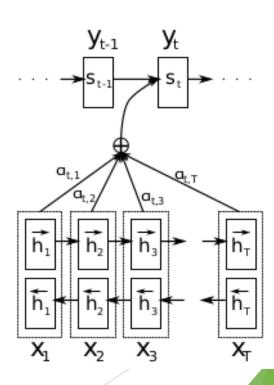


Fig. 3. Deep Recurrent Neural Network

► Attention-based LSTM (基于注意力的LSTM)

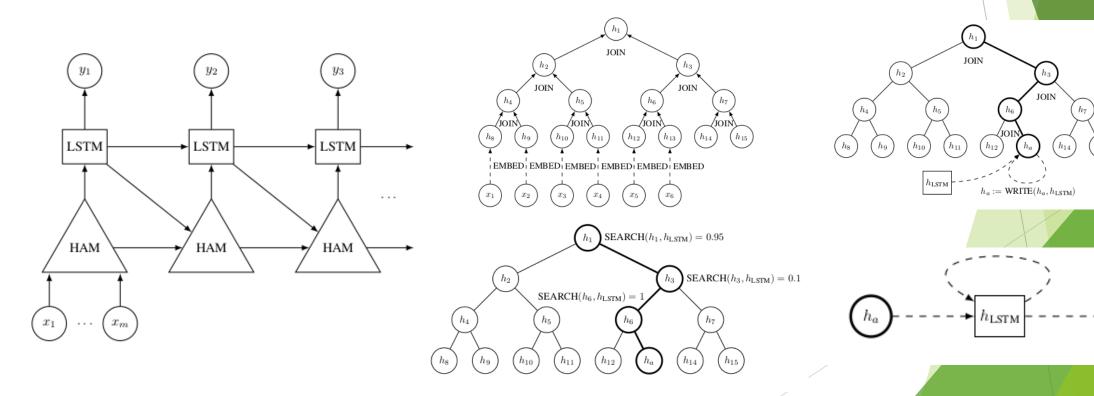
- ▶ LSTM记忆力不好
- ▶ 训练用30长度的句子,测试用50长度的,效果就不行
- ▶ Attention-based把句子全给LSTM连上,让他挑看着顺眼的最匹配的





Hierarchical Attentive Memory

- ▶ Attention机制的升级版,将输入组织成二叉树,有效提高了效率
- ▶ 泛化能力增强:在训练数据为长度32的序列时,给长度在64-128的序列排序取得 0.24%的错误率(同样情况下使用纯attention机制错误率为100%)



- ▶ Sentiment classification情感分析
 - ► [2015] Improved semantic representations from tree-structured long short-term memory networks
- ▶ Language Modeling语言模型
 - ▶ [2015] Character-Aware Neural Language Models
- ▶ Sequence Generation 序列生成
 - http://karpathy.github.io/2015/05/21/rnn-effectiveness/
- ▶ Speech Recognition 语音识别
 - ▶ [2013] SPEECH RECOGNITION WITH DEEP RECURRENT NEURAL NETWORKS
- ► Machine Translation 机器翻译
 - ▶ [2014] Neural machine translation by jointly learning
- ▶ Question Answering 问答系统
 - ▶ [2015] Neural Responding Machine for Short-Text Conversation

▶ 我说这是LSTM生成的你信吗?

"The surprised in investors weren't going to raise money. I'm not the company with the time there are all interesting quickly, don't have to get off the same programmers. There's a super-angel round fundraising, why do you can do. If you have a different physical investment are become in people who reduced in a startup with the way to argument the acquirer could see them just that you're also the founders will part of users' affords that and an alternation to the idea. [2] Don't work at first member to see the way kids will seem in advance of a bad successful startup. And if you have to act the big company too."

▶ 我说这是LSTM生成的你信吗?

For $\bigoplus_{n=1,...,m}$ where $\mathcal{L}_{m_{\bullet}} = 0$, hence we can find a closed subset \mathcal{H} in \mathcal{H} and any sets \mathcal{F} on X, U is a closed immersion of S, then $U \to T$ is a separated algebraic space.

Proof. Proof of (1). It also start we get

$$S = \operatorname{Spec}(R) = U \times_X U \times_X U$$

and the comparison in the fibre product covering we have to prove the lemma generated by $\coprod Z \times_U U \to V$. Consider the maps M along the set of points Sch_{fppf} and $U \to U$ is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset $W \subset U$ in Sh(G) such that $Spec(R') \to S$ is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that f_i is of finite presentation over S. We claim that $\mathcal{O}_{X,x}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X,x'} \to \mathcal{O}'_{X',x'}$ is separated. By Algebra, Lemma ?? we can define a map of complexes $GL_{S'}(x'/S'')$ and we win.

To prove study we see that $\mathcal{F}|_U$ is a covering of \mathcal{X}' , and \mathcal{T}_i is an object of $\mathcal{F}_{X/S}$ for i > 0 and \mathcal{F}_p exists and let \mathcal{F}_i be a presheaf of \mathcal{O}_X -modules on \mathcal{C} as a \mathcal{F} -module. In particular $\mathcal{F} = U/\mathcal{F}$ we have to show that

$$\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\operatorname{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$$

is a unique morphism of algebraic stacks. Note that

Arrows =
$$(Sch/S)_{fppf}^{opp}$$
, $(Sch/S)_{fppf}$

and

$$V = \Gamma(S, \mathcal{O}) \longrightarrow (U, \operatorname{Spec}(A))$$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by $X_{spaces,\acute{e}tale}$ which gives an open subspace of X and T equal to S_{Zar} , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S. Lemma 0.1. Assume (3) and (3) by the construction in the description.

Suppose $X = \lim |X|$ (by the formal open covering X and a single map $\underline{Proj}_X(A) = \operatorname{Spec}(B)$ over U compatible with the complex

$$Set(A) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_{Y}}).$$

When in this case of to show that $Q \to C_{Z/X}$ is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S. Moreover there exists a closed subspace $Z \subset X$ of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

f is locally of finite type. Since S = Spec(R) and Y = Spec(R).

Proof. This is form all sheaves of sheaves on X. But given a scheme U and a surjective étale morphism $U \to X$. Let $U \cap U = \coprod_{i=1,...,n} U_i$ be the scheme X over S at the schemes $X_i \to X$ and $U = \lim_i X_i$.

The following lemma surjective restrocomposes of this implies that $\mathcal{F}_{x_0} = \mathcal{F}_{x_0} = \mathcal{F}_{x_0,\dots,0}$.

Lemma 0.2. Let X be a locally Noetherian scheme over S, $E = \mathcal{F}_{X/S}$. Set $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$. Since $\mathcal{I}^n \subset \mathcal{I}^n$ are nonzero over $i_0 \leq p$ is a subset of $\mathcal{J}_{n,0} \circ \overline{A}_2$ works.

Lemma 0.3. In Situation ??. Hence we may assume q' = 0.

Proof. We will use the property we see that $\mathfrak p$ is the mext functor (??). On the other hand, by Lemma ?? we see that

$$D(O_{X'}) = O_X(D)$$

where K is an F-algebra where δ_{n+1} is a scheme over S.

▶ 我说这是LSTM生成的你信吗?

```
* Increment the size file of the new incorrect UI FILTER group information
* of the size generatively.
static int indicate policy(void)
 int error;
 if (fd == MARN_EPT) {
    * The kernel blank will coeld it to userspace.
   if (ss->segment < mem total)</pre>
     unblock_graph_and_set_blocked();
    else
     ret = 1;
   goto bail;
 segaddr = in_SB(in.addr);
 selector = seg / 16;
 setup works = true;
 for (i = 0; i < blocks; i++) {
   seq = buf[i++];
   bpf = bd->bd.next + i * search;
   if (fd) {
     current = blocked;
 rw->name = "Getjbbregs";
 bprm_self_clearl(&iv->version);
 regs->new = blocks[(BPF_STATS << info->historidac)] | PFMR_CLOBATHINC_SECONDS << 1
 return segtable;
```

▶ 但这还远远没有结束.....

- ▶ Sorting 排序!?
 - ▶ [2014] Neural Turing Machine
- ▶ Taxi Destination Prediction的士目的预测!?
 - ▶ [2015] Artificial Neural Networks Applied to Taxi Destination Prediction
- ▶ Python Interpreter Python解释器!?
 - ▶ [2014] Learn to execute
- ▶ 写简单的程序!?
 - ► [2015] Neural Programmer-Interpreters

实现细节

实现细节

- ▶ 一些小Trick
 - ▶ 初始化矩阵都在[-0.01, 0.01]比较好,均匀分布
 - ▶ Peephole和bias不要比较好(常用版本LSTM)
 - ▶ GRU很好用
 - ▶ 用GPU训练,多GPU更好
 - ▶ Learning rate学习率开始可以比较大,之后可以变小
 - ▶ 用Gradient Clipping防止梯度爆炸
 - ▶ 在适当的地方放Dropout防止Overfitting
 - ▶ Mini-batch,不然GPU没法加速,batch大小很讲究
 - ▶ 使用Momentum加速收敛
 - ► 在训练时往Gradient里加高斯noise

实现细节

- ▶ 梯度更新方法
 - ▶ 不同task不同,大概有以下几种
 - ▶裸的SGD
 - ▶前期learning rate很大,过一段时间后逐渐减少
 - ► AdaGrad
 - **►**Rmsprop
 - ► AdaDelta
 - ► AdaM

► Theano

- ▶ Python前端 , C++实现
- ▶自动求导
- ▶ 将图结构编译成GPU流,存储时间都有优化

► Torch7

- ► Lua前端, C/CUDA实现
- ▶ 嵌入式支持得很好

▶ TensorFlow

▶ Google第二代深度学习系统

MXNet

- ▶ 结合命令式语言(如Caffe)和符号式语言(如Theano)
- ▶ 对多GPU有一定支持

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- ▶ 后端库(想自己实现的请看这里)
- ► CUDA
 - ▶ 非常容易上手的GPU编程语言
 - ▶ 然而Parallel programming is easy as long as you don't care about performance
- ► CUBLAS
 - ▶ 支持大部分矩阵/向量操作,已经做过大量底层优化
- **CUDNN**
 - ▶ 支持神经网络的常用操作,已经做过大量底层优化
- ► CUSPARSE
 - ▶ 支持一部分稀疏矩阵/向量操作,已经做过大量底层优化

- ▶ LSTM已经有大量现成实现
 - ► C++
 - Python
 - Matlab

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▶ 所以没事千万别自己实现

▶ (用Theano只要5行我会乱说?)

- ▶当前工具库的评价
 - ▶ [2015] Comparative Study of Caffe, Neon, Theano, and Torch for Deep Learning
 - ▶目前还没有通用的支持多机多GPU的框架出现

展望

展望

▶ LSTM存在的问题

- ▶记忆力不足
- ▶只能处理序列映射
- ▶ 理论基础仍缺乏,调参手段一大堆
- ▶结合更多类型数据

展望

▶ 继LSTM之后又一火爆话题

- ▶ Attention-based mechanism 注意力机制
 - ▶ [2014] Neural machine translation by jointly learning
 - ▶ 论如何用一个模型达到Google Translation的效果

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Q&A