

Statistics : Study of collecting, describing & draw inferences from data

Types : Descriptive, Inferential Statistics

→ mean, mode median ; → Samp Sampling → P-values → Hypothesis testing

→ Mean : Avg $\frac{\text{Sum of all obs.}}{\text{Total no. of obs.}} = \frac{\sum_{i=1}^n x_i}{n} = \bar{x} \text{ or } \mu_x$

Its univariate analysis, one variable at once (column)
Disadv: outliers affect this majorly.

→ median : middle value i) sort ascending order
ii) pick middle value : odd terms : $\left(\frac{n+1}{2}\right)^{\text{th}}$ term
even terms → $\frac{n^{\text{th}} + \left(\frac{n+1}{2}\right)^{\text{th}}}{2}$

Adv:- outliers few outliers don't affect cent this.

→ Mode : most common, frequent value

If we have only one mode value its unimodal
If we have 2 mode values its Bimodal value
more than 2 mode values: multimodal.

→ Variance (σ^2) : Spread : measure how far a dataset is spread out.

* If all the values are same then no variability (or)
zero variance (or) no spread

* Variance is average squared distance

Note:- Complexity of mean → $O(n)$; median → $O(n \log n)$

• Median is computationally expensive

• Univariate analysis (1D) is analysis of only one variable/column

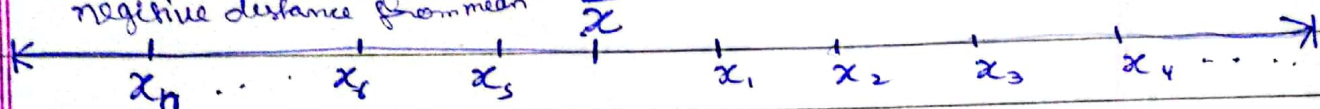
• all mean, median, mode are univariate analysis, even σ^2 & σ

Note:- Mean & median are measure of Central tendency
• Variance, standard deviation, Range, IQR, are measure of Spread

* If spread or variance is small the mean is more accurate compare to large spread

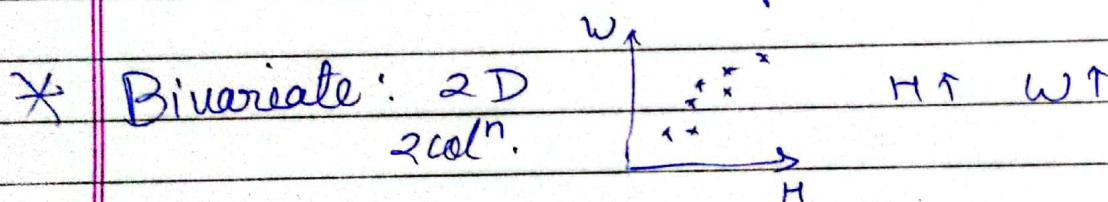
$$\text{Variance} = \sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

→ Variance don't give actual data as square are taken to ^{omit} ~~cancel~~ negative distance from mean \bar{x}



→ Standard deviation = $\sqrt{\text{variance}} = \sqrt{\sigma^2} = \sigma$

* variance, std dev are impacted by Outlier



for Bivariate we use measure of Relationship

→ Co-variance

→ Co-relation

as, variance = $\frac{1}{n} \sum_{i=1}^n (x_i - \mu_x)^2$

co variance = $\frac{1}{n} \sum_{i=1}^n ((x_i - \mu_x)(y_i - \mu_y)) = \text{cov}(x, y)$

value of cov(x, y) can be positive or negative, so if

$\text{cov}(x, y) =$
 $\begin{matrix} +(\text{ve}) & \rightarrow & x \uparrow \Rightarrow y \uparrow \\ -(\text{ve}) & \rightarrow & x \uparrow \Rightarrow y \downarrow \end{matrix}$